

Scalable Distributed Reasoning using MapReduce

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Abstract. We address the problem of scalable distributed reasoning, proposing a technique for materialising the closure of an RDF graph (under the RDFS and OWL Horst semantics) based on MapReduce. We have implemented our approach on top of Hadoop and deployed it on a compute cluster of up to 64 commodity machines. We show that a naive implementation on top of MapReduce is straightforward but performs badly and we present several non-trivial optimisations. Our algorithm is scalable and allows us to compute the RDFS closure of 865M triples from the Web (producing 30B triples) in less than two hours, faster than any other published approach.

1 Introduction

In this paper, we address the problem of *scalable distributed reasoning*. Most existing reasoning approaches are centralised, exploiting recent hardware improvements and dedicated data structures to reason over large-scale data [? ? ?]. However, centralised approaches typically scale in only one dimension: they become faster with more powerful hardware.

Therefore, we are interested in parallel, distributed solutions that partition the problem across many compute nodes. Parallel implementations can scale in two dimensions, namely hardware performance of each node and the number of nodes in the system. Some techniques have been proposed for distributed reasoning, but, as far as we are aware, they do not scale to orders of 10^8 triples.

We present a technique for materialising the closure of an RDF graph in a distributed manner, on a cluster of commodity machines. Our approach is based on MapReduce [3] and can be used to compute the closure under both the RDFS rules [?] and the OWL Horst semantics [?]. This paper can be seen as a response to the challenge posed in [10] to exploit the MapReduce framework for efficient large-scale Semantic Web reasoning.

This paper is structured as follows: we start, in Section 2, with a discussion of the current state-of-the-art, and position ourselves in relation to these approaches. We summarise the basics of MapReduce with some examples in Section 3. In Section 4 we provide an initial implementation of forward-chaining RDFS materialisation with MapReduce. We call this implementation “naive” because it directly translates known distributed reasoning approaches into MapReduce. This implementation is easy to understand but performs poorly because of

load-balancing problems and because of the need for fixpoint iteration. Therefore, in Section 5, an improved implementation is presented using several intermediate MapReduce functions. Finally, we evaluate our approach in Section 6, showing runtime and scalability over various datasets of increasing size, and speedup over increasing amounts of compute nodes.

2 Related work

[7] compute the closure of an RDF graph using two passes over the data on a single machine. They implement only a fragment of the OWL Horst semantics, to allow efficient materialisation, and to prevent “ontology hijacking”. Our approach borrows from their ideas, but by using well-defined MapReduce functions our approach allows straightforward distribution over many nodes, leading to improved results.

[10] use MapReduce to answer SPARQL queries over large RDF graphs, and mention closure computation, but do not provide any details or results. In comparison, we provide algorithm details, make the code available open-source, and report on experiments of up to 865M triples.

[9] show that graph-partitioning techniques improve reasoning over first-order logic knowledge bases, but do not apply this in a distributed or large-scale context. [13] present a technique for parallel OWL inferencing through data partitioning. Experimental results show good speedup but on relatively small datasets (1M triples) and runtime is not reported. In contrast, our approach needs no explicit partitioning phase and we show that it is scalable over increasing dataset size.

In previous work [11] we have presented a technique based on data-partitioning in a self-organising P2P network. A load-balanced auto-partitioning approach was used without upfront partitioning cost. Experimental results were however only reported for relatively small datasets of up to 15M triples.

Several techniques have been proposed based on deterministic rendezvous-peers on top of distributed hashables [1, 2, 4, 8]. However, because of load-balancing problems due to the data distributions, these approaches do not scale [11].

3 What is the MapReduce framework?

MapReduce is a framework for parallel and distributed processing of batch jobs [3]. Each job consists of two phases: a map and a reduce. The mapping phase partitions the input data by associating each element with a key. The reduce phase processes each partition independently. All data is processed based on key/value pairs: the map function processes a key/value pair and produces a set of new key/value pairs; the reduce merges all intermediate values with the same key into final results.

Algorithm 1 Counting term occurrences in RDF NTriples files

```
map(key, value):  
  // key: line number  
  // value: triple  
  emit(value.subject, blank); // emit a blank value, since  
  emit(value.predicate, blank); // only amount of terms matters  
  emit(value.object, blank);  
  
reduce(key, iterator values):  
  // key: triple term (URI or literal)  
  // values: list of irrelevant values for each term  
  int count=0;  
  for (value in values)  
    count++; // count number of values, equalling occurrences  
  emit(key, count);
```

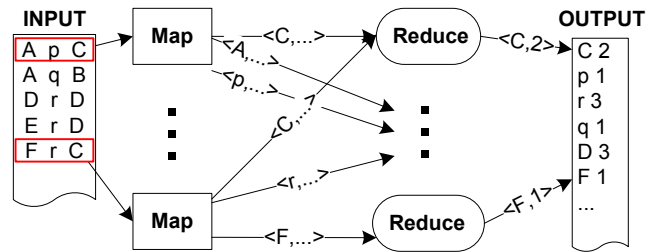


Fig. 1. MapReduce processing

3.1 A simple MapReduce example: term count

We illustrate the use of MapReduce through an example application that counts the occurrences of each term in a collection of triples. As shown in Algorithm 1, the *map* function partitions these triples based on each term. Thus, it emits intermediate key/value pairs, using the triple terms (s,p,o) as keys and blank, irrelevant, value. The framework will group all intermediate pairs with the same key, and invoke the *reduce* function with the corresponding list of values, summing these the number of values into an aggregate term count (one value was emitted for each term occurrence).

This job could be executed as shown in Figure 1. The input data is split in several blocks. Each computation node operates on one or more blocks, and performs the map function on that block. All intermediate values with the same key are sent to one node, where the reduce is applied.

3.2 Characteristics of MapReduce

This simple example illustrates some important elements of the MapReduce programming model:

- since the *map* operates on single pieces of data without dependencies, partitions can be created arbitrarily and can be scheduled in parallel across many

nodes. In this example, the input triples can be split across nodes arbitrarily, since the computations on these triples (emitting the key/value pairs), are independent of each other.

- the *reduce* operates on an iterator of values because the set of values is typically far too large to fit in memory. This means that the reducer can only partially use correlations between these items while processing: it receives them as a stream instead of a set. In this example, operating on the stream is trivial, since the reducer simply increments the counter for each item.
- the *reduce* operates on all pieces of data that share some key. By assigning proper keys to data items during the *map*, the data is partitioned for the *reduce* phase. A skewed partitioning (i.e. skewed key distribution) will lead to imbalances in the load of the compute nodes. If term x is relatively popular the node performing the *reduce* for term x will be slower than others. To use MapReduce efficiently, we must find balanced partitions of the data.

4 Naive RDFS reasoning with MapReduce

The closure of an RDF input graph under the RDFS semantics [?] can be computed by applying all RDFS rules iteratively on the input until no new data is derived (fixpoint). The RDFS rules, shown in Table 1, have one or two antecedents. For brevity, we ignore rules with one antecedent (the rules 1, 4a, 4b, 6, 8, 10, 12 and 13) since these can be evaluated at any point in time without a join. Rules with two antecedents are more challenging to implement since they require a join over two parts of the data: if the join is successful, we derive a consequence.

1: $s p o$ (if o is a literal)		\Rightarrow $!n$ $rdf:type$ $rdfs:Literal$
2: p $rdfs:domain$ x	$\&$ $s p o$	\Rightarrow s $rdf:type$ x
3: p $rdfs:range$ x	$\&$ $s p o$	\Rightarrow o $rdf:type$ x
4a: $s p o$		\Rightarrow s $rdf:type$ $rdfs:Resource$
4b: $s p o$		\Rightarrow o $rdf:type$ $rdfs:Resource$
5: p $rdfs:subPropertyOf$ q $\&$ q $rdfs:subPropertyOf$ r		\Rightarrow p $rdfs:subPropertyOf$ r
6: p $rdf:type$ $rdf:Property$		\Rightarrow p $rdfs:subPropertyOf$ p
7: $s p o$	$\&$ p $rdfs:subPropertyOf$ q	\Rightarrow $s q o$
8: s $rdf:type$ $rdfs:Class$		\Rightarrow s $rdfs:subClassOf$ $rdfs:Resource$
9: s $rdf:type$ x	$\&$ x $rdfs:subClassOf$ y	\Rightarrow s $rdf:type$ y
10: s $rdf:type$ $rdfs:Class$		\Rightarrow s $rdfs:subClassOf$ s
11: x $rdfs:subClassOf$ y	$\&$ y $rdfs:subClassOf$ z	\Rightarrow x $rdfs:subClassOf$ z
12: p $rdf:type$ $rdfs:ContainerMembershipProperty$		\Rightarrow p $rdfs:subPropertyOf$ $rdfs:member$
13: o $rdf:type$ $rdfs:Datatype$		\Rightarrow o $rdfs:subClassOf$ $rdfs:Literal$

Table 1. RDFS rules [?]

4.1 Encoding an example RDFS rule in MapReduce

Applying the RDFS rules means performing a join over some terms in the input triples. Let us consider for example rule 9 from Table 1, which derives `rdf:type` based on the sub-class hierarchy. We can implement this join with a *map* and *reduce* function, as shown in Figure ?? and Algorithm 2:

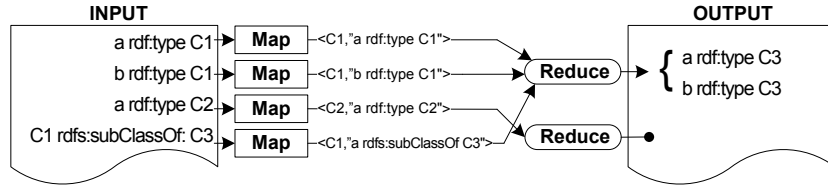


Fig. 2. Encoding RDFS rule 9 in MapReduce.

Algorithm 2 Naive sub-class reasoning (RDFS rule 9)

```

map(key, value):
  // key: lineNumber (irrelevant)
  // value: triple
  switch triple.predicate
  case "rdf:type":
    emit(triple.object, triple); // group (s rdf:type x) on x
  case "rdfs:subClassOf":
    emit(triple.subject, triple); // group (x rdfs:subClassOf y) on x

reduce(key, iterator values):
  // key: triple term, eg x
  // values: triples, eg (s type x), (x subClassOf y)
  superclasses=empty;
  types=empty;

  // we iterate over triples
  // if we find subClass statement, we remember the super-classes
  // if we find a type statement, we remember the type
  for (triple in values):
    switch triple.predicate
    case "rdfs:subClassOf":
      superclasses.add(triple.object) // store y
    case "rdf:type":
      types.add(triple.subject) // store s

  for (s in types):
    for (y in classes):
      emit(null, triple(s, "rdf:type", y));

```

In the *map*, we process each triple and output a key/value pair, using as value the original triple, and as key the triple's term (`s,p,o`) on which the join should be performed. To perform the sub-class join, triples with `rdf:type` should be

grouped on their object (eg. “x”), while triples with `rdfs:subClassOf` should be grouped on their subject (also “x”). When all emitted tuples are grouped for the reduce phase, these two will group on “x” and the reducer will be able to perform the join.

4.2 Complete RDFS reasoning: the need for fixpoint iteration

If we perform this *map* once (over all input data), and then the *reduce* once, we will not find *all* corresponding conclusions. For example, to compute the transitive closure of a chain of n `rdfs:subClassOf`-inclusions, we would need to iterative the above *map/reduce* steps n times.

Obviously, the above *map* and *reduce* functions encode only rule 9 of the RDFS rules. We would need to add other, similar, *map* and *reduce* functions to implement each of the other rules. These other rules are interrelated: one rule can derive triples that can serve as input for another rule. For example, rule 2 derives `rdf:type` information from `rdfs:domain` statements. After applying that rule, we would need to re-apply our earlier rule 9 to derive possible superclasses.

Thus, to produce the complete RDFS closure of the input data using this technique we need to add more *map/reduce* functions, chain these functions to each other, and iterate these until we reach some fixpoint.

5 Efficient RDFS reasoning with MapReduce

The previously presented implementation is straightforward, but is inefficient because it produces duplicate triples (several rules generate the same conclusions) and because it requires fixpoint iteration. We encoded, as example, only rule 9 and we launched a simulation over the Falcon dataset, which contains 35 million triples. After 40 minutes the program had not yet terminated, but had already generated more than 50 billion triples. Considering that the unique derived triples from Falcon are no more than 1 billion, the ratio of unique derived triples to duplicates is at least 1:50.

In the following subsections, we introduce three optimisations to greatly decrease the number of jobs and time required for closure computation:

5.1 Loading schema triples in memory

Typically, schema triples are far less numerous than instance triples [7]; As also shown in Table 2, our experimental data¹ indeed exhibit a low ratio between schema and instance triples. In combination with the fact that RDFS rules with two antecedents include at least one schema triple, we can infer that joins are made between a large set of instance triples and a small set of schema triples. For example, in rule 9 of Table 1 the set of `rdf:type` triples is typically far larger than the set of `rdfs:subClassOf` triples. As our first optimisation, we

¹ from the Billion Triple challenge 2008, <http://www.cs.vu.nl/~pmika/swc/btc.html>

schema type	amount	fraction
domain, range (p rdfs:domain D, p rdfs:range R)	30.000	0.004%
sub-property (a rdfs:subPropertyOf b)	70.000	0.009%
sub-class (a rdfs:subClassOf b)	2.000.000	0.2%

Table 2. Schema triples (amount and fraction of total triples) in datasets

can therefore locally load the small set of `rdfs:subClassOf` triples in memory and launch a MapReduce job that joins the instance triples it receives as input with the in-memory schema triples on-the-fly.

5.2 Data preprocessing to avoid duplicates

The join with the schema triples can be physically executed either during the map or during the reduce phase of the job. After initial experiments, as our second optimisation we have concluded that it is faster to perform the join in the reduce, since doing so in the map results in producing large numbers of duplicate triples.

Let us illustrate our case with an example based on rule 2 (`rdfs:domain`). Assume an input with ten different triples that share the same subject and predicate but have a different object. If the predicate has a domain associated with it and we execute the join in the mappers, the framework will output a copy of the new triple for each of the ten triples in the input. These triples can be correctly filtered out by the reducer, but they will cause significant overhead since they will need to be stored locally and be transferred over the network.

We can avoid the generation of duplicates if we first group the triples by subject and then we execute the join over the single group. We can do it by designing a mapper that outputs an intermediate tuple that has as key the triple’s subject and as value the predicate. In this way the triples will be grouped together and we will execute the join only once, avoiding generating duplicates.

In general, we set as key those parts of the input triples that are also used in the derived triple. The parts depend on the applied rule. In the example above, the only part of the input that is also used in the output is the subject. Since the key is used to partition the data, for a given rule, all triples that produce some new triple will be sent to the same reducer. It is then trivial to output that triple only once in the reducer. As value, we emit those elements of the triple that will be matched against the schema.

5.3 Ordering the application of the RDFS rules

We analyse the RDFS ruleset with regard to input and output of each rule, to understand which rule may be triggered by which other rule. By ordering the execution of rules we can limit the number of iterations needed for full closure. As explained before, we ignore some of the rules with a single antecedent (1, 4, 6, 8, 10) without loss of generality: these can be implemented at any point in

time without a join, using a single pass over the data. We first categorise the rules based on their output:

- rules 5 and 12 produce schema triples with *rdfs:subPropertyOf* as predicate,
- rules 11 and 13 produce schema triples with *rdfs:subClassOf* as predicate,
- rules 2, 3, and 9 produce instance triples with *rdf:type* as predicate,
- rule 7 may produce arbitrary triples.

We also categorise the rules based on the predicates in their antecedents:

- rules 5 and 10 operate only on triples with sub-class or sub-property triples,
- rules 9, 12 and 13 operate on triples with type, sub-class, and sub-property,
- rule 2, 3 and 7 can operate on arbitrary triples.

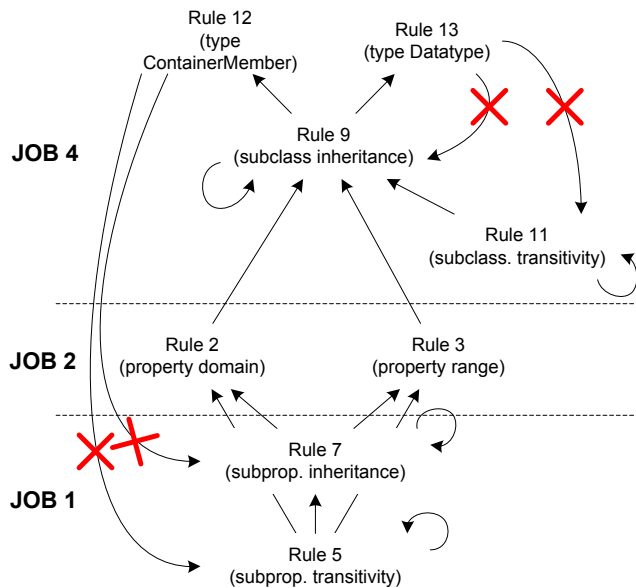


Fig. 3. Relation between the various RDFS rules

Figure 2 displays the relation between the RDFS rules, connecting rules based on their input and output (antecedents and consequents). An ideal execution should proceed from the bottom of the picture to the top: first apply the transitivity rules (rule 5 and 11), then apply rule 7, then rule 2 and 3, then rule 9 and finally rules 12 and 13.

It may seem that rule 12 and 13 could produce triples that would serve as input to rules 5 and 11; however, looking carefully we see that this is not the case: Rule 12 outputs (*?s rdfs:subPropertyOf rdfs:member*), rule 13 outputs (*?s rdfs:subClassOf rdfs:Literal*). For rules 5 and 11 to fire on these,

Algorithm 3 RDFS sub-property reasoning

```
map(key, value):
  // key: null
  // value: triple
  if (subproperties.contains(value.predicate)) // for rule 7
    key = "1" + value.subject + "-" + value.object
    emit(key, value.predicate)
  if (subproperties.contains(value.object) &&
      value.predicate == "rdfs:subPropertyOf") // for rule 5
    key = "2" + value.subject
    emit(key, value.object)

reduce(key, iterator values):
  // key: flag + some triples terms (depends on the flag)
  // values: triples to be matched with the schema
  values = values.unique // filter duplicate values

switch (key[0])
case 1: // we are doing rule 7: subproperty inheritance
  for (predicate in values)
    // iterate over the predicates emitted in the map and collect superproperties
    superproperties.add(subproperties.recursive_get(value))
  for (superproperty in superproperties)
    // iterate over superproperties and emit instance triples
    emit(null, triple(key.subject, superproperty, key.object))
case 2: // we are doing rule 5: subproperty transitivity
  for (predicate in values)
    // iterate over the predicates emitted in the map, and collect superproperties
    superproperties.add(subproperties.recursive_get(value))
  for (superproperty in superproperties)
    // emit transitive subproperties
    emit(null, triple(key.subject, "rdfs:subPropertyOf", superproperty))
```

rdfs:member and *rdfs:Literal* must have been defined as sub-classes or sub-properties of something else. However, in RDFS none of these is a sub-class or sub-property of anything. They could of course be super-classed by arbitrary users on the Web. However, we ignore such “unauthorised” statements following the advice against “ontology hijacking” from [7]. Hence, the output of rules 12 and 13 cannot serve as input to rules 5 and 11. Similarly, rules 2 and 3 cannot fire.

Furthermore, rule 9 cannot fire after rule 13, since this would require using literals as subjects, which we ignore as being non-standard RDF. The only rules that could fire after rule 12 are rules 5 and 7. For complete RDFS inferencing, we would need to evaluate these rules for each container-membership property found in the data, but as we will show, in typical datasets these properties occur very rarely.

As our third optimisation, we conclude that instead of having to iterate over all RDFS rules until fixpoint, it is instead sufficient to process them only once, in the order indicated in Figure 2.

5.4 The complete picture

In this section, we present an updated algorithm implementing the above optimisations. The complete algorithm consists of five sequential MapReduce jobs,

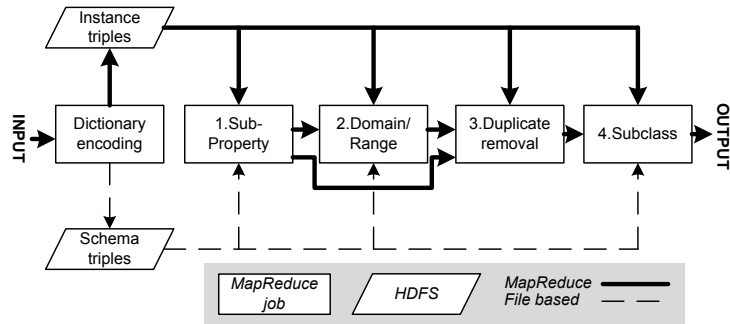


Fig. 4. Data flow. The solid lines refer to data split partitioned using MapReduce while the dashed lines refer to shared data. Note that the data transferred using MapReduce is orders of magnitude larger than the shared data.

as shown in Figure 3. First, we perform dictionary encoding and extract the schema triples to a shared distributed file system. Then, we launch the RDFS reasoner: a sequence of four jobs that implement the presented rule ordering.

The first RDFS job applies the rules that involve the sub-property relations. The second applies the rules concerning domain and range. The third cleans up the duplicated statements produced in the first step and the last applies the rules that use the sub-class relations. In the following subsections, each of these jobs is explained in detail.

Distributed dictionary encoding in MapReduce To reduce the physical size of the input data, we perform a dictionary encoding, in which each triple term is rewritten into a unique and small identifier. We have developed a novel technique for distributed dictionary encoding using MapReduce, rewriting each term into an 8-byte identifier; the encoding scales linearly with the input data. Due to space limitations, we refer the reader to [?]. Encoding all 865M triples takes about 1 hour on 32 nodes. Note that schema triples are extracted during dictionary encoding.

First job: apply rules on sub-properties The first job applies rules 5 and 7, which concern sub-properties, as shown in Algorithm 3. Since the schema triples are loaded in memory, these rules can be applied simultaneously.

To avoid generation of duplicates, we follow the principle of setting as the tuple’s key the triple’s parts that are used in the derivation. This is possible because all inferences are drawn on an instance triple and a schema triple and we load all schema triples in memory. That means that for rule 5 we output as key the triple’s subject while for rule 7 we output a key consisting of subject and object. We add an initial flag to keep the groups separated since later we have to apply a different logic that depends on the rule. In case we apply rule 5, we output the triple’s object as value, otherwise we output the predicate.

Algorithm 4 RDFS domain and range reasoning

```
map(key, value):
  // key: null
  // value: triple
  if (domains.contains(value.predicate)) then // for rule 2
    key = value.subject
    emit(key, value.predicate + "d")
  if (ranges.contains(value.predicate)) then // for rule 3
    key = value.object
    emit(key, value.predicate + 'r')
```

```
reduce(key, iterator values):
  // key: subject of the input triples
  // values: predicates to be matched with the schema
  values = values.unique // filter duplicate values
  for (predicate in values)
    switch (predicate.flag)
      case "r": // rule 3: find the range for this predicate
        types.add(ranges.get(predicate))
      case "d": // rule 2: find the domain for this predicate
        types.add(domains.get(predicate))
  for (type in types)
    emit(null, triple(key, "rdf:type", type))
```

The reducer reads the flag of the group's key and applies to corresponding rule. In both cases, it first filters out duplicates in the values. Then it recursively matches the tuple's values against the schema and saves the output in a set. Once the reducer has finished with this operation, it outputs the new triples using the information in the key and in the derivation output set.

This algorithm will not derive a triple more than once, but duplicates may still occur between the derived triples and the input triples. Thus, at a later stage, we will perform a separate duplicate removal job.

Second job: apply rules on domain and range The second job applies rules 2 and 3, as shown in Algorithm 4. Again, we use a similar technique to avoid generating duplicates. In this case, we emit as key the triple's subject and as value the predicate. We also add a flag so that the reducers know if they have to match it against the domain or against the range schema. Tuples about domain and range will be grouped together if they share the same subject since the two rules might derive the same triple.

Third job: delete duplicate triples The third job eliminates duplicates between the previous two jobs and the input data. It iterates over the all triples and emits only those that were derived but not part of the input dataset: the *map* outputs each triple, with a flag to indicate whether this triple was original or derived; the *reduce* simply filters the derived triples. Due to space limitations, we refer the reader to [?].

Fourth job: apply rules on sub-classes The last job applies rules 9, 11, 12, and 13, which are concerned with sub-class relations. The procedure, shown in

Algorithm 5 RDFS sub-class reasoning

```
map(key, value):
  // key: source of the triple (irrelevant)
  // value: triple
  if (value.predicate = "rdf:type")
    key = "0" + value.predicate
    emit(key, value.object)
  if (value.predicate = "rdfs:subClassOf")
    key = "1" + value.predicate
    emit(key, value.object)

reduce(key, iterator values):
  //key: flag + triple.subject
  //iterator: list of classes
  values = values.unique // filter duplicate values

  for (class in values)
    superclasses.add(subclasses.get_recursively(class))

  switch (key[0])
  case 0: // we're doing rdf:type
    for (class in superclasses)
      if !values.contains(class)
        emit(null, triple(key.subject, "rdf:type", class))
  case 1: // we're doing subClassOf
    for (class in superclasses)
      if !values.contains(class)
        emit(null, triple(key.subject, "rdfs:subClassOf", class))
```

Algorithm 5, is similar to the previous job with the following difference: during the map phase we do not filter the triples but forward everything to the reducers instead. In doing so, we are able to also eliminate the duplicates against the input.

6 Experimental results

We use the Hadoop² framework, an open-source Java implementation of MapReduce. Hadoop is designed for clusters of commodity machines. It uses a distributed file system built from the local disks of the participating machines, and manages execution details such as data transfer, job scheduling, and error management.

Our experiments were performed on the DAS-3 distributed supercomputer³ using up to 64 compute nodes. Each node was equipped with two dual-core 2.4GHz Opteron processors, 4GB of main memory and 250GB hard disk. Nodes were interconnected through Gigabit Ethernet. We have experimented on real-world data from the Billion Triple Challenge 2008⁴. An overview of these datasets is shown in Table 2(a), where dataset *all* refers to all the challenge datasets combined except for Webscope, whose access is limited under a license. All the code used for our experiments is publicly available⁵.

² <http://hadoop.apache.org>

³ <http://www.cs.vu.nl/das3>

⁴ <http://www.cs.vu.nl/~pmika/swc/btc.html>

⁵ <https://code.launchpad.net/~jrnb/+junk/reasoning-hadoop>

6.1 Results for RDFS reasoning

We evaluate our system by the time required to calculate the full closure. We have repeated each run three times, we report the average and the relative deviation σ (the standard deviation divided by the average). The runtime results, along with the number of output triples are presented in Table 2(a). Figure 5 shows the time needed for each reasoning phase. Our implementation shows very high performance: for the combined dataset of 865M triples, it produced 30B triples in less than one hour. This amounts to a total throughput of 8.77 million triples/sec. for the output and 252.000 triples/sec. for the input. These results do not include dictionary encoding, which took, as mentioned, one hour for all datasets combined. Including this time, the throughput becomes 4.27 million triples/sec. and 123.000 triples/sec. respectively, which to the best of our knowledge, still outperforms any results reported both in the literature [?] and on the Web⁶.

Besides absolute performance, an important metric in parallel algorithms is how performance scales with additional compute nodes. Table 4 shows the speedup gained with increasing number of nodes and the resulting efficiency, on the Falcon and DBpedia datasets. Similar results hold for the other datasets. To the best of our knowledge, the only published speedup results for distributed reasoning on a dataset of this size can be found in [11]; for both datasets, and all numbers of nodes, our implementation outperforms this approach.

The speedup results are also shown in Figure 4. They show that our high throughput rates are already obtained when utilising only 16 compute nodes. We attribute the decreasing efficiency on larger numbers of nodes to the fixed Hadoop overhead for starting jobs on nodes: on 64 nodes, our computation per node is not big enough to compensate platform overhead.

Figure 5 shows the division of runtime over the computation phase from Figure 3, and confirms the widely-held intuition that subclass-reasoning is the most expensive part of RDFS inference on real-world datasets.

We have verified the correctness of our implementation on the (small) Wordnet dataset. We have not stored the output of our algorithm: 30B triples (each of them occupying 25 bytes using our dictionary encoding) produce 750GB of data. Mapping these triples back to the original terms would require approx. 500 bytes per triple, amounting to some 15TB of disk space.

6.2 Results for OWL reasoning

We have also encoded the OWL Horst rules [?] to investigate whether our approach can be extended for efficient OWL reasoning. The OWL Horst rules are more complex than the RDFS rules, and we need to launch more jobs to compute the full closure. Due to space restrictions, we refer to [?], for the algorithms and the implementation.

On the LUBM(50) benchmark dataset [?], containing 7M triples, we compute the OWL Horst closure on 32 nodes in about 3 hours, resulting in about

⁶ e.g. at esw.w3.org/topic/LargeTripleStores

dataset	input	output	time	σ
Wordnet	1.9M	4.9M	3'39"	9.1%
Falcon	32.5M	863.7M	4'19"	3.8%
Swoogle	78.8M	1.50B	7'15"	8.2%
DBpedia	150.1M	172.0M	5'20"	8.6%
others	601.5M			
<i>all</i>	864.8M	30.0B	56'57"	1.2%

Table 3. Closure computation using datasets of increasing size on 32 nodes

(a) Falcon				(b) DBpedia			
nodes	runtime (s)	speedup	efficiency	nodes	runtime (s)	speedup	efficiency
1	3120	1	1	1	1639	1	1
2	1704	1.83	0.92	2	772	2.12	1.06
4	873	3.57	0.89	4	420	3.9	0.98
8	510	6.12	0.76	8	285	5.76	0.72
16	323	9.65	0.60	16	203	8.07	0.5
32	229	13.61	0.43	32	189	8.69	0.27
64	216	14.45	0.23	64	156	10.53	0.16

Table 4. Speedup with increasing number of nodes

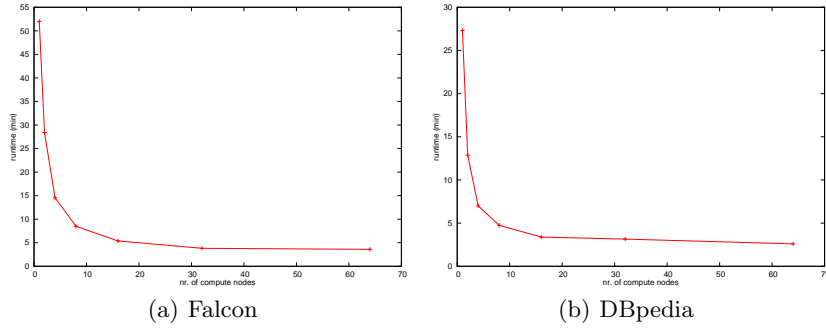


Fig. 5. Speedup with increasing number of nodes

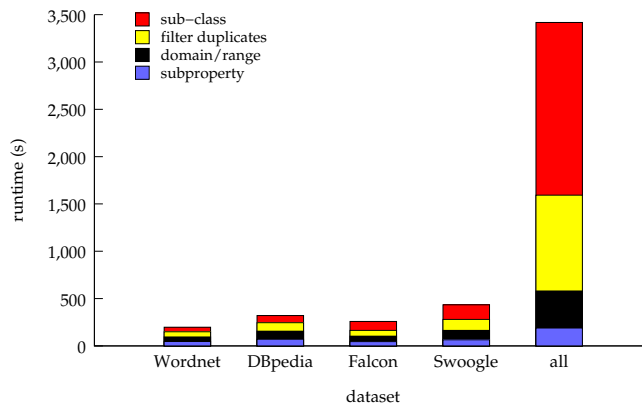


Fig. 6. Detailed reasoning time (per phase) for various datasets (32 nodes)

13M triples. In comparison, the RDFS closure on the same dataset is computed in about 10 minutes, resulting in about 8.6M triples. On a real-world dataset (Falcon, 35M triples) we stopped OWL Horst inference after 12 hours, at which point more than 130 MapReduce jobs had been launched, and some 3.8B triples had been derived. Clearly, our implementation on OWL Horst has room for optimisation; on RDFS, our optimisations drastically reduced computation time.

6.3 Discussion

Some datasets produce very large amounts of output. For example, the closure of the Swoogle and Falcon datasets is around $20\times$ the original data. We attribute these differences to the content and quality of these datasets: data on the Web contains cycles, override definitions of standard vocabularies, etc. Instead of applying the standard RDFS and OWL rules, [7] propose to only consider “authoritative” statements to prevent this data explosion during reasoning. In this paper, we did not focus on data quality. To avoid the observed inference explosion, the approach from [7] can be added to our algorithms.

As explained, the presented algorithm performs incomplete RDFS reasoning. We omit the rules with one antecedent as these can be parallelised efficiently and are commonly ignored by reasoners as being uninteresting. If standard compliance is sought, these rules can be implemented with a single *map* over the final data, which is very easy to parallelise and should not take more than some minutes. Similarly, we have ignored the rule concerning container-membership properties since these occur very rarely: in all 865M triples, there are only 10 container-membership properties, of which one is in the `example.org` namespace, and two override standard RDFS. If needed, membership properties can be implemented in the same way as the subproperty-phase (albeit on much less data), which takes approximately 3 minutes to execute on the complete dataset, as seen in Figure 5.

7 Conclusion

We have shown a scalable distributed implementation of RDFS reasoning based on MapReduce which can infer 30 billion triples from a real-world dataset in less than two hours, yielding an input and output throughput of 123.000 triples/second and 4.27 million triples/second respectively. To the best of our knowledge, our system outperforms any other published approach. To achieve this, we have presented some non-trivial optimisations for encoding the RDFS ruleset in MapReduce. We have evaluated the scalability of our implementation on a cluster of 64 compute nodes using several real-world datasets.

A remaining challenge is to apply the same techniques successfully to OWL-Horst reasoning. Our first experiments have shown this to be more challenging.

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