# An Accurate, Continuous, and Lossless Self-Learning CMOS Current-Sensing Scheme for Inductor-Based DC-DC Converters

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Abstract—Sensing current is a fundamental function in power supply circuits, especially as it generally applies to protection and feedback control. Emerging state-of-the-art switching supplies, in fact, are now exploring ways to use this sensed-current information to improve transient response, power efficiency, and compensation performance by appropriately self-adjusting, on the fly, frequency, inductor ripple current, switching configuration (e.g., synchronous to/from asynchronous), and other operating parameters. The discontinuous, non-integrated, and inaccurate nature of existing lossless current-sensing schemes, however, impedes their widespread adoption, and lossy solutions are not acceptable. Lossless, filter-based techniques are continuous, but inaccurate when integrated on-chip because of the inherent mismatches between the filter and the power inductor. The proposed G<sub>M</sub>-C filter-based, fully integrated current-sensing CMOS scheme circumvents this accuracy limitation by introducing a self-learning sequence to start-up and power-on-reset. During these seldom-occurring events, the gain and bandwidth of the internal filter are matched to the response of the power inductor and its equivalent series resistance (ESR), effectively measuring their values. A 0.5  $\mu$ m CMOS realization of the proposed scheme was fabricated and applied to a current-mode buck switching supply, achieving overall DC and AC current-gain errors of 8% and 9%, respectively, at 0.8 A DC load and 0.2 A ripple currents for 3.5  $\mu$ H–14  $\mu$ H inductors with ESRs ranging from 48 m $\Omega$  to 384 m $\Omega$  (other lossless, state-of-the-art solutions achieve 20%-40% error, and only when the nominal specifications of the power MOSFET and/or inductor are known). Since the self-learning sequence is non-recurring, the power losses associated with the foregoing solution are minimal, translating to a 2.6% power efficiency savings when compared to the more traditional but accurate series-sense resistor (e.g., 50 m $\Omega$ ) technique.

Index Terms—Current-mode, current sensing, DC-DC converters,  $G_{\rm M}$ -C filter, inductance measurement, lossless, power management, self-learning, switching regulators.

### I. INTRODUCTION

SWITCHING DC-DC converters are an indispensable component of every battery-operated device, efficiently supplying power to all vital and supplementary blocks of the system. While it is possible to design these switching supplies without sensing current, with only output voltage information [1], [2], short-circuit protection and increasingly stringent performance requirements force designers to include a current-sensing function to almost all practical solutions.

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Boost and buck-boost DC-DC converters, for instance, are optimally stable under the guise of a current-mode topology, in which case sensing current eases feedback control requirements [3]. Additionally, modern state-of-the-art designs use sensed-current information to optimally set the operating mode of the system for highest power efficiency [4]; balance the various phase loads of multiphase converters [5]; control and regulate single-inductor, multiple-output topologies [6]; and even multiply the inductance of micro-scale power inductors [7]. The over-riding requirements for all these applications are losslessness for increased battery life, integration for small footprint solutions, accuracy for high performance, and in many cases, continuous operation for maximum flexibility and optimum performance.

Achieving both losslessness and accuracy is difficult. Adding a series sense-resistor, for instance, and sensing the voltage across it can be accurate, but necessarily lossy because it carries all of the sensed current, which can be on the order of Amperes, reducing the overall power efficiency of a switching supply by 2%–10%. The only way to completely eliminate the losses is by not introducing any additional series devices in the power-carrying paths of the system, in other words, by using the components that already exist in the power stage, like the power inductor, output capacitor, and the surrounding power switches [8]. Unfortunately, however, the impedances of these devices vary significantly with process, temperature, vendor, and design, and this variation translates to poor current-sensing tolerance. Nevertheless, given the sensitive nature of battery life in portable electronics to power losses, accuracy is often sacrificed for lifetime.

Series MOSFET's Ron [9] and parallel current-sensing FET (sense-FET) [9]–[15] schemes are among the most popular lossless sensing techniques today. In the MOSFET's Ron case, the voltage across a power switch is measured and divided by its estimated turn-on resistance to extrapolate the value of the current flowing through it, when it is conducting. This resistance, unfortunately, typically varies with temperature, process, and supply voltages by 50%-200% [9]. In the sense-FET scheme, a mirror transistor is used to source a fraction of the switch current, and its accuracy is determined by the matching performance of the current mirror in triode (Ohmic/non-saturated region), whose mirroring ratio is on the order of 1000 or higher. Although accuracies of ±4% are reported [15], channel-length modulation and process-induced mismatch errors between sense- and power-FETs, whose device ratio is considerably large with minimum channel lengths, can cause  $3\sigma$  errors as large as  $\pm 20\%$ [16]. Ultimately, sensing the switch current is discontinuous because of the very nature of the switch, conducting current

only a fraction of the period. The noisy sensed current must therefore be synchronized and/or averaged via a sample-and-hold network. Sensing the inductor current continuously may be achieved with complementary sense-FETs, but the complexity and noise necessarily increase. The sense-FET, which enjoys better matching performance, is further limited to fully integrated solutions, where the switches are on-chip, because well-matched sense-FETs are not otherwise available.

The only means of sensing the current continuously is by altogether avoiding the switches, which is the basic feature of the filter approach. These schemes indirectly measure the inductor current, which is inherently continuous, by applying the inductor voltage across a tuned low-pass filter and sensing the filter current. Since there is no switching noise, the filter is better suited for current-mode feedback control applications [9], [17]. The accuracy, however, much like the switch-based schemes, is dependent on the tolerance of the inductance and equivalent series resistance (ESR) of the power inductor and the tuning accuracy of the filter, whose overall tolerance can be  $\pm 28\%$  (inductance, ESR, and temperature variation of  $\pm 15\%$ ,  $\pm 11\%$ , and 70 °C, respectively) and worse for extended temperature-range applications [17].

For any lossless technique to be accurate, the circuit must sense the voltage across an existing power device whose impedance is well-known, exploiting Ohm's law. Unfortunately, accuracy degrades as the sensing circuit is fully integrated on-chip, as power device tolerance and characteristics, be it from a power switch, inductor, or capacitor, become even more unknown (i.e., dependent on vendor and application in addition to temperature and process technology). A self-learning scheme is therefore proposed, wherein the power inductor is measured and characterized during start-up and/or power-on-reset events, as will be described in Section II. The design of a 0.5  $\mu$ m CMOS prototype is presented in Section III and its application to a current-mode buck converter discussed in Section IV. Experimental results are subsequently presented in Section V and conclusions drawn in Section VI.

# II. PROPOSED SELF-LEARNING SCHEME

As just alluded, the driving force behind the proposed current-sensing scheme is to automatically and indirectly measure the inductance and equivalent series resistance (ESR) of an off-chip power inductor during start-up. Tuning the sensing circuit during start-up and measuring inductor current during normal operating conditions assure both accuracy and continuous operation. These general concepts are applied to the filter technique because of its losslessness (i.e., no additional series sense power device is necessary), low switching noise, and high bandwidth, assuming the tuning values are stored and the tuning circuitry disengaged during normal operating conditions.

In the proposed solution, which is illustrated in Fig. 1, the inductor current is measured by applying the voltage across L and  $R_{\rm ESR}$  to a  $G_{\rm M}$ -C filter whose voltage frequency response matches the current response of the inductor. The output voltage of the filter is therefore proportional to inductor current  $I_{\rm L}$  [17], [18]:

$$V_{\rm Sense}(\mathrm{s}) = (\mathrm{g_{m1}R})\mathrm{R_{ESR}}\left(\frac{1+\mathrm{sL/R_{ESR}}}{1+\mathrm{sRC}}\right)I_{\mathrm{L}}(\mathrm{s})$$
 (1)

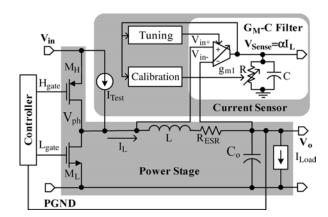


Fig. 1. Block diagram of the proposed self-learning current-sensing scheme.

where  $g_{m1}$  is the transconductance of the  $G_{\rm M}$  cell, R the filter resistor, and C the filter capacitor. If the product of R and C is tuned to the ratio of L and  $R_{\rm ESR}$ 

$$\frac{L}{R_{FSR}} = RC \tag{2}$$

 $V_{
m Sense}$  is independent of frequency and linearly and directly proportional to  $I_{
m L}$ 

$$V_{\text{sense}} = (g_{\text{m1}}R)R_{\text{ESR}}I_{\text{L}}$$
 (3)

where product  $(g_{m1}R)R_{\rm ESR}$  is the current-sensing gain, which can be calibrated to any value (e.g., 0.5 V/A) by properly adjusting  $g_{m1}$  and/or R. During normal operation,  $R_{\rm ESR}$  can change with frequency because of skin effect but its effects are most prevalent at frequencies higher than the switching frequency and minimal at frequencies of interest.

During each start-up and power-on-reset event, after biasing currents and voltages are properly set, but before the switching supply is allowed to start, the tuning and calibration circuits are engaged, properly adjusting and setting current-sensing filter parameters  $\rm g_{m1}$  and  $\rm R$ . During this process, power switches  $\rm M_H$  and  $\rm M_L$  are both off and test current  $\rm \it I_{Test}$  is forced into inductor L at switching node  $\rm \it V_{ph}$ . Once  $\rm g_{m1}$  and R are set, they are stored and the DC-DC converter is then allowed to start and operate normally. Since the tuning and calibration circuits are only active during start-up, they incur no power losses during regular operation.

#### A. Tuning and Calibration

The purpose of the self-learning sequence is to satisfy the condition specified in (2), where time-constants RC and  $L/R_{ESR}$  match, and to set the current sensing gain to a known value (i.e.,  $(g_{m1}R)R_{ESR} = \alpha$ ). These conditions are satisfied during a two-step process: tuning and calibration. The tuning process sets the gain-bandwidth product of the filter and calibration adjusts the filter DC gain. Tuning, in particular, is performed by injecting a triangular test current into the power inductor, as shown in Fig. 2, and gradually adjusting transconductance  $g_{m1}$  until the peak of the AC portion of sense voltage  $V_{Sense}$  matches a pre-determined value. The frequency of the injected signal, which is not necessarily equal to the switching frequency, is sufficiently high to ensure the AC portion of the voltage across the inductor is dominated by inductance L and

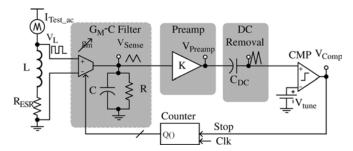


Fig. 2. Block diagram of the tuning phase.

not resistance  $R_{\rm ESR}$ , since impedance Ls at high frequencies is much larger than  $R_{\rm ESR}$ . The resulting AC voltage across the inductor is therefore a square signal (inductor voltage is linearly proportional to the rising/falling rate of its current), which after applying it to a  $G_{\rm M}$ -C integrator filter, translates to a triangular voltage, as seen at  $V_{\rm Sense}$ , since again, impedance 1/Cs is significantly smaller than R at high frequencies. The signal is then buffered, its DC component removed via coupling capacitor  $C_{\rm DC}$ , and  $g_{\rm m}$  gradually stepped up from its lowest point with a counter until the peak-to-peak voltage of the amplified  $V_{\rm Sense}$  signal (i.e.,  $KV_{\rm Sense}$ ) equals  $V_{\rm Tune}$ :

$$KV_{Sense} = KV_{L} \left(\frac{g_{m}}{C_{S}}\right) \approx K(I_{Test\_ac}L_{S}) \left(\frac{g_{m}}{C_{S}}\right)$$
$$= I_{Test\_ac} \left(\frac{KLg_{m}}{C}\right) \equiv V_{Tune}, \tag{4}$$

at which point comparator CMP stops the clock and stores the value. The buffer introduces gain K to increase the tuning resolution of CMP because the peak-to-peak current ripple of  $I_{\rm Test}$  is low and subsequently so is the AC amplitude of  $V_{\rm Sense}$ .

As a side note, R is kept at its minimum value during this part of the process to reduce DC offsets in the system and consequently relax the DC-blocking performance requirements of  $C_{\rm DC}$  (i.e., reduce the order of the high-pass filter). Ideally, the test frequency should be close to the switching frequency of the regulator to ensure L is measured close to the operating frequency because inductance may be different at two frequencies. However, experiments only showed a 1% per decade decrease in inductance, which for a tuning frequency of 100 kHz and a converter operating frequency of 1 MHz amounts to 1% error.

In the calibration phase, which immediately follows the tuning cycle, a DC current is fed into the inductor, DC-blocking capacitor  $C_{\rm DC}$  is removed, and R is gradually increased from its minimum point with a counter until the output of the pre-amplifier reaches  $V_{\rm Cal}$ , as shown in Fig. 3. Since the voltage across  $R_{\rm ESR}$  overwhelms that of L because impedance Ls is much lower than  $R_{\rm ESR}$  and only DC values exist, the amplified version of  $V_{\rm Sense}$  (i.e.,  $KV_{\rm Sense}$ ) is adjusted until it equals calibration voltage  $V_{\rm Cal}$ :

$$KV_{Sense} = V_{L}(g_{m}R)K \approx (R_{ESR}I_{Test\_DC})(g_{m}R)K \equiv V_{Cal}.$$
(5)

If tuning and calibration reference impedances  $V_{\rm Tune}/I_{\rm Test\_ac}$  and  $V_{\rm Cal}/I_{\rm Test\_DC}$  match

$$\frac{V_{\mathrm{Tune}}}{I_{\mathrm{Test\_ac}}} \approx \frac{\mathrm{KLg_m}}{\mathrm{C}} \equiv \frac{V_{\mathrm{Cal}}}{I_{\mathrm{Test\_DC}}} \approx \mathrm{R_{ESR}g_mRK}$$
 (6)

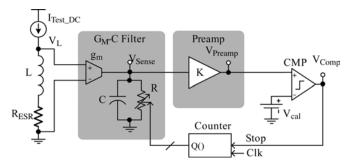


Fig. 3. Block diagram of the calibration phase.

 $G_{\rm M}$ -C filter time-constant RC equals inductor time-constant  $L/R_{\rm ESR}$ , which corresponds to the targeted condition prescribed by (2), and current sensing is possible:

$$V_{\text{sense}} = (\text{Rg}_{\text{m}} \text{R}_{\text{ESR}}) I_{\text{L}} \approx \left(\frac{V_{\text{Cal}}}{\text{KI}_{\text{Test\_DC}}}\right) I_{\text{L}} \equiv \alpha I_{\text{L}}$$
 (7)

where (3) and (6) are recombined and  $\alpha$  is the overall currentsensing gain of the circuit.

#### B. Error Sources

The accuracy of the foregoing technique is dependent on tuning and calibration accuracy. Consequently, the AC and DC sensing errors are the result of the tuning and calibration loops, respectively, which are in turn affected by the input-referred offsets of the G<sub>M</sub> cell, comparator CMP, and the pre-amplifier; the tolerance of  $V_{\text{Cal}}$ ,  $V_{\text{Tune}}$ ,  $I_{\text{Test\_DC}}$ , and  $I_{\text{Test\_ac}}$  and the resolution or quantization error of sensing parameters g<sub>m</sub> and R (minimum five bits of resolution were used, which translates to maximum of 3.2% quantization error). Because test currents cannot exceed reasonable levels and the resulting test voltage across the power inductor is low (on the order of 1–5 mV), overall sensing accuracy is particularly sensitive to the input-referred offset of the G<sub>M</sub> cell. Currents over 50 mA, for example, which would increase the magnitude of the signal, require significant die area overhead and result in parasitic hot spots that not only affect the self-learning results but also unnecessarily push the thermal limits of the package. The end result is that the G<sub>M</sub> cell must incorporate a dynamic offset-canceling feature [19].

Another source of error is drift, when inductance and/or ESR change from their self-learned values. This variation may be the result of temperature, power level, and/or wear and tear. Of these, the temperature coefficient (TC) of the ESR, which is approximately 3900 ppm/°C (TC of copper), has the worse effect [17], on the order of  $\pm 20\%$  for every 100 °C. Fortunately, this error is systematic and linear, and can therefore be compensated by including it in the system. A simple way to compensate for temperature errors is to use a proportional to absolute temperature (PTAT)  $V_{\rm Cal}$  voltage source in the calibration loop with its temperature coefficient equal to the of the ESR. Similarly, when processing the DC output voltage of the current-sensing filter,  $V_{\rm Sense}$  should also be compared against a PTAT voltage source, not a temperature-independent voltage. The errors caused by variations in other operating point conditions, such as inductance changes with temperature, are negligibly small [17] and can be compensated during each startup and/or power-on-reset event.

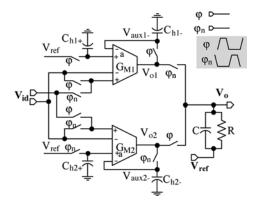


Fig. 4. Auto-zeroed, ping-ponging  $G_{\rm M}\text{-}C$  filter circuit.

# III. CURRENT-SENSING CIRCUIT

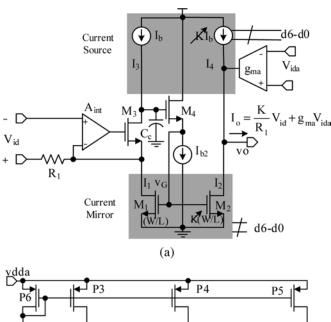
# A. $G_{\mathrm{M}}$ -C Filter

The  $G_M$ -C filter is a first-order, low-pass filter (Fig. 1) with a programmable gain and bandwidth feature (variable  $g_m$  and filter resistor R) [20]. As discussed earlier, because of low ESR values, the voltage across the inductor is small and on the order of tens of millivolts (i.e., 1 A load current transient into an ESR of  $50~\text{m}\Omega$  produces a 50~mV drop). The situation is even worse during startup, when relatively small test currents (i.e., 50~mA) are used, resulting in test signals at the input of the filter on the order of 1–5~mV, thereby requiring low offset performance. Since the goal is continuous operation, which is useful in current-mode controllers and other high performance applications, the offset-cancellation technique must also be continuous.

The proposed continuous low offset  $G_M$ -C filter is illustrated in Fig. 4 and is comprised of two well-matched, auto-zeroed, ping-ponging [19] dual-input summing transconductors (i.e.,  $G_{M1}$  and  $G_{M2}$ ); two offset-programming capacitors for each transconductor (i.e.,  $C_{h1-}$ ,  $C_{h1+}$ ,  $C_{h2-}$ , and  $C_{h2+}$ ); a single bandwidth-setting capacitor C; gain-setting resistor R; and non-overlapping clock signals  $\varphi$  and  $\varphi_n$ . The non-overlapping feature is implemented to prevent various cross-wiring events. Input voltage  $V_{\rm ref}$ , against which filter output voltage  $V_{\rm o}$  is referenced, is used as a virtual ground (AC ground). Finally, as in all ping-pong schemes, while one transconductor processes the input signal, the other one auto-zeroes.

The difference in the proposed offset-cancellation scheme with state-of-the-art is that a summing amplifier is used to program and cancel the offset by dedicating an input differential pair to the input signal and another to subtract (i.e., cancel) the offset. The key advantage to this configuration is that the large holding capacitor is de-coupled from the high bandwidth path, that is to say, not connected to the input ac-signal path and therefore not bandwidth-limiting the signal. A large holding capacitor is desirable because it reduces clock feed-through and charge injection, consequently improving offset cancellation performance, all without adversely affecting bandwidth.

In the switching supply circuit shown in Fig. 1, the G<sub>M</sub>-C filter must be programmable and highly linear across the rail-to-rail input voltage range. Since the non-inverting input periodically swings from the positive to the negative supply, a varia-



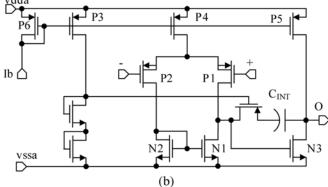


Fig. 5. (a) Linear dual-input transconductor cell and (b)  $A_{\rm int}$  implementation.

tion in transconductance  $(\Delta g_m)$  in these two states translates to a systematic input-referred offset error voltage  $(V_{os\_gm})$ :

$$V_{\text{os-gm}} = \frac{\Delta V_{\text{o}}}{g_{\text{m}}R} = \frac{V_{\text{id}}\Delta g_{\text{m}}R}{g_{\text{m}}R} = \left(\frac{\Delta g_{\text{m}}}{g_{\text{m}}}\right)V_{\text{id}}$$
 (8)

where  $V_{\rm id}$  is the differential voltage applied to the transconductor [8], [20]. Parasitic voltage artifacts present in the non-inverting input signal like inductive ringing are filtered by the low frequency  $G_{\rm M}$ -C filter (just as L filters these same non-idealities from affecting the inductor current) and therefore have little to no effects on offset or circuit operation. Similarly, since dead time introduces short-lived parasitic diode voltage drops to this signal, its effects are also filtered and therefore relatively inconsequential. In fact, since this signal is applied to both inductor (current filter) and  $G_{\rm M}$ -C circuit (voltage filter), its parasitic effects on inductor current are reproduced by the current-sensing block, further validating the sensing capability of the circuit.

Because polysilicon resistors are many times more linear than transistors and the non-inverting input of the transconductor is connected to a low impedance node (i.e., connected to a source capable of supplying current), a wide input voltage range resistor-dependent current conveyor [21]–[23], as shown in Fig. 5, can be used in place of a traditional differential pair transconductor. The input terminals of amplifier  $A_{\rm int}$  are virtually short-circuited because of negative feedback and the resulting current

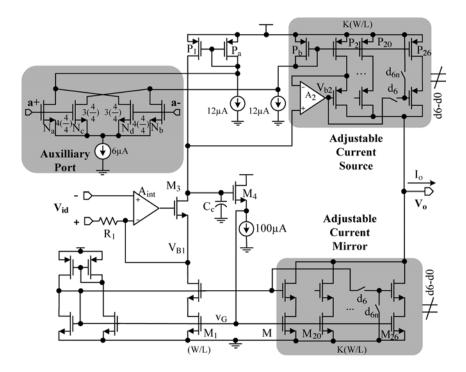


Fig. 6. G<sub>M</sub> cell.

flowing through series resistor  $R_1$  ( $I_{R1}$ ) is proportional to the differential input voltage applied to the  $G_M$ -C cell ( $V_{id}$ ):

$$I_{\rm R1} = \frac{V_{\rm id}}{R_1}.\tag{9}$$

The current conveyor converts the large voltage variations across the inductor into current, thereby not affecting the voltage biasing point of differential amplifier  $A_{\rm int}$ , whose input terminals remain biased at the regulated output voltage of the converter ( $A_{\rm int}$ 's non-inverting input). The wide voltage swing is only applied across a polysilicon resistor, which has a relatively low voltage coefficient (e.g., 50 ppm/V) and therefore negligible adverse effects on the circuit. This current is then mirrored to the output by current mirror  $M_1-M_2$ , ultimately defining the transconductance to

$$g_{\rm m} \equiv \frac{I_{\rm o}}{V_{\rm id}} = \frac{1}{V_{\rm id}} \left( \frac{V_{\rm id} K}{R_1} \right) = \frac{K}{R_1}$$
 (10)

where K is a digitally programmable current-mirror gain.

The gate of  $M_4$  is high impedance and is therefore the gain- and bandwidth-setting node of the current-mirror's controlling feedback loop. Compensation capacitor  $C_c$  ensures the bandwidth-setting pole is at sufficiently low frequencies to prevent parasitic high frequency poles from compromising stability. This  $M_4-M_1-M_3$  feedback loop, however, adds a parasitic high frequency pole to the signal-flowing path ( $V_{id}$  to  $I_o$ ) approximately at its gain-bandwidth product ( $g_{m1}/C_c$ ), and  $C_c$  is therefore selected to balance stability against high bandwidth. Because of the current-conveyor configuration (i.e., amplifier  $A_{int}$ 's inverting input is approximately equal to  $A_{int}$ 's non-inverting input),  $A_{int}$ 's input common-mode range need only include the regulated output voltage range of the converter (non-inverting input voltage range), which superimposes relatively relaxed input common-mode range requirements

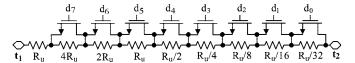


Fig. 7. Programmable and binarily weighted polysilicon resistor R.

on  $A_{\rm int}$ .  $A_{\rm int}$ , as shown in Fig. 5(b), is therefore a standard ground-sensing two-stage pMOS input differential amplifier with a Miller-compensating ( $C_{\rm INT}$ ) capacitor that produces a gain-bandwidth product of 10 MHz, which constitutes another parasitic pole in the signal-flowing path from  $V_{\rm id}$  to  $I_{\rm o}$ .

The programmable K-gain current mirror implemented with  $M_1 - M_2$  and its slave current source  $KI_b$  are shown in Fig. 6, where a digital word determines the connectivity of the binarily weighted array of current mirrors. Cascoding devices are added to the current mirrors and sources to increase their respective output impedances and consequently increase the transconductor's overall output impedance. For functional and therefore power and real-estate efficiency, the bias current generator and the auxiliary transconductor are combined into a single circuit via transistor current-mirror pairs  $P_a - P_1$  and  $P_b - P_2$ , where amplifier A<sub>2</sub> equates the drain voltages of P<sub>1</sub> and P<sub>2</sub> to minimize channel-length modulation errors and at the same time properly set the biasing voltage of the gates of the upper cascoding devices. The auxiliary pair consists of current-canceling differential pairs  $N_{\rm a}-N_{\rm b}$  and  $N_{\rm c}-N_{\rm d}$ , whose net result is a low transconductance value (g<sub>ma\_d</sub>) [19] that is then multiplied by current gain K with  $P_b - P_{2\times}$  mirror:

$$g_{ma} = Kg_{ma,d}. \tag{11}$$

Transconductance  $g_{\text{ma\_d}}$  was designed to be roughly equal to  $1/R_1$  (i.e., 4  $\mu A/V$  ).

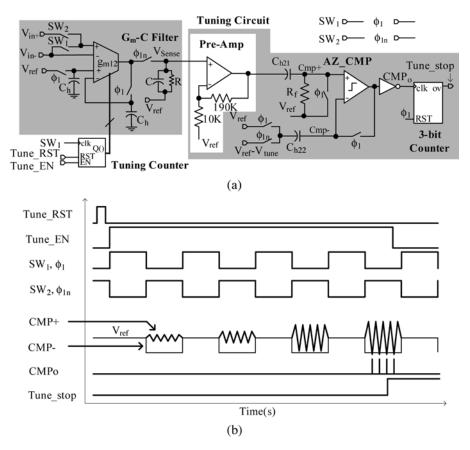


Fig. 8. (a) Tuning circuit and (b) its relevant waveforms.

The bandwidth of the  $G_M$ -C filter is tuned by adjusting its shunting load resistance (R in Fig. 1). A 1 k $\Omega/\square$  binarily weighted polysilicon resistor is used for this (Fig. 7). Programmability is achieved by decoding a digital word and deciphering the connectivity of controlling nMOS switches  $d_7-d_0$  from it. When bits  $d_7-d_0$  are all one, all switches are closed, short-circuiting the large resistor and resulting in an overall resistance of  $R_u$ , the minimum resistance value. As the bit word  $d_7-d_0$  progresses from all ones to all zeros, the switch resistance increases to  $9R_u$  in  $R_u/32$  increments.

# B. Tuning Circuit

For ease, only one of the two ping-ponging  $G_{\rm M}$  cells is used during the tuning and calibration process, as illustrated in Fig. 8(a). The subsequent pre-amplifier is a two-stage, Miller-compensated opamp in a non-inverting feedback configuration with a closed-loop gain of 26 dB (less than 0.1 dB of gain error) and a bandwidth of 1 MHz (five times higher than the frequency of the triangular test signal). It drives the high-pass, DC-blocking filter, which has a 3 dB bandwidth of 20 kHz ( $R_f$  is 1 M $\Omega$  and  $C_{h21}$  is 8 pF). The output of the filter is then fed to an auto-zeroed comparator with a propagation delay of 40 ns for an overdrive input signal of 10 mV. The comparator is also a standard two-stage Miller-compensated amplifier to ensure it is stable during its auto-zeroing phase.

Functionally, once the tuning process is engaged by Tune\_RST and Tune\_EN, the tuning counter is reset and allowed to count, gradually increasing  $g_{m1}$  and therefore

increasing the triangular ripple voltage seen at the input of auto-zeroed comparator AZ\_CMP Fig. 8(b). This process continues until the peak ripple voltage reaches tuning voltage  $V_{\rm Tune}$ , at which point the tuning counter stops (Tune\_stop transitions to a high state) and  $g_{\rm m1}$  is set. In the tuning sequence, auto-zeroing clock signals  $\varphi_1$  and  $SW_1$  are in phase, and so are  $\varphi_{\rm 1n}$  and  $SW_2$ , but not so in calibration, which is why they are separated here. When  $SW_1$  is high, both the  $G_{\rm M}$  cell and AZ\_CMP are auto-zeroed (i.e., connected in a unity-gain configuration to measure their respective offset voltages and store them in holding capacitors); the triangular test signal is then processed when  $S_{\rm W1}$  is low.

A 3-bit counter is placed at the output of the buffered comparator for deglitching purposes, to avoid noise glitches from inadvertently stopping the tuning sequence. The output of the comparator is continually low when the peak-to-peak voltage of the triangular signal is not sufficiently amplified. When  $g_{\rm m1}$  and consequently the peak voltage of the triangular signal are high enough, the output of the comparator starts toggling back and forth from low to high states, and only when eight consecutive transitions occur does the 3-bit counter disengage the tuning process via Tune\_stop.

# C. Calibration Circuit

More so than in the tuning process, low offset operation is critical for calibration, on the order of tens of microvolts, because the input test signal is only a few millivolts. Best offset cancellation is achieved when the offset voltage is stored at the

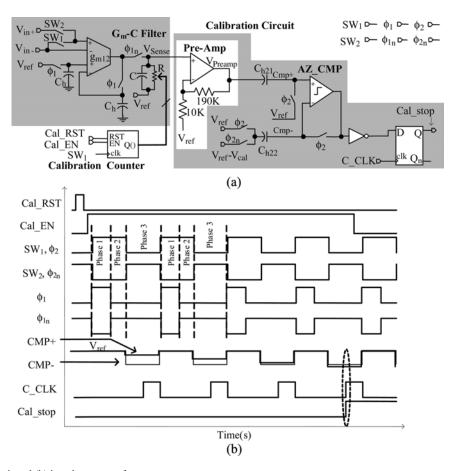


Fig. 9. (a) Calibration circuit and (b) its relevant waveforms.

output because the errors are attenuated by the gain of the amplifier, when referred back to the input signals. However, this can only be done when the gain of the amplifier is low enough (e.g., less than 40) to prevent its output from saturating to the rails during the measurement phase, or by means of an auto-zeroing technique called residual successive memorization (RSM) [24]. The main idea behind RSM is to divide a high gain stage into several low gain stages, each of which provides an auto-zeroing point. Generally, an amplifier chain with N gain stages consists of N + 1 phases, and in the first phase, all stages are connected in unity-gain configuration and their offsets stored in holding capacitors at their respective outputs. During each subsequent intermediate phase (phases 2 to N), while the inputs of the first stage are kept intact, the output of each subsequent stage is connected to the input of the following stage, one at a time, sequentially from the second to the last stage, gradually driving the accumulated offset voltage to the last stage. Finally, during the last phase (phase N + 1), all gain stages are connected serially and the input signal is injected into the first stage. The intermediate phases are necessary to locally cancel the offset of each stage and prevent each stage from saturating to the rails because of large initial offsets. At this point, the overall performance of the circuit is limited by charge injection and clock feed-through errors [19].

The proposed calibration circuit uses the  $G_M$  cell and the comparator to incorporate the RSM scheme, as illustrated in Fig. 9(a), which is why auto-zeroing clock signals  $SW_1$ ,  $\varphi_1$ ,

 $\varphi_2$ , and their inverted counterparts (SW<sub>2</sub>,  $\varphi_{1n}$ , and  $\varphi_{2n}$ ) and control signal C\_CLK are used. First, both the G<sub>M</sub> cell and the comparator are auto-zeroed and their offsets stored at their respective outputs (i.e., SW<sub>1</sub>,  $\varphi_1$ , and  $\varphi_2$  are high), as shown in Fig. 9(b). In the second phase, auto-zeroing is disengaged only for the  $G_{\mathrm{M}}$  cell, but keeping its inputs intact (i.e.,  $\mathrm{SW}_1$  stays high and  $\varphi_1$  transitions low). In doing so, the clock feed-through and charge injection errors caused by toggling  $\varphi_1$  are measured and stored by holding capacitor Ch21. In the third and final phase, the test signal is injected into the  $G_{\rm M}$  cell, the comparator is brought out of its auto-zeroing phase, and the circuit is connected serially to allow the comparator to process and compare the amplified test signal against calibration target voltage  $V_{\rm Cal}$ . As in tuning, the calibration counter increments, increasing filter resistor R and the amplitude of the signal fed into comparator AZ\_CMP, until the amplified signal surpasses  $V_{\text{Cal}}$  (i.e., there is just enough DC gain), at which point C\_CLK, which samples the inverted output of the comparator in the middle of the third phase, activates Cal\_stop and consequently stops the counter and the calibration process.

#### D. Triangular Wave Generator

The triangle signal generator is a modified version of typical sawtooth and clock generator circuits used in pulse-width modulated (PWM) switching supplies [15], [25]. The circuit sources and sinks current into and from a capacitor (Fig. 10).

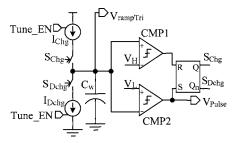


Fig. 10. Triangle and clock generator circuit.

When the capacitor voltage exceeds upper threshold  $V_{\rm H}$ , comparator CMP1 disconnects charge current  $I_{\rm Chg}$  from capacitor  ${\rm C_W}$  and connects discharge current  $I_{\rm Dchg}$  in its place, forcing the capacitor voltage to reverse direction. When the voltage then reaches lower limit  $V_{\rm L}$ , comparator CMP2 effectively reverses the process by connecting charge current  $I_{\rm Chg}$  back to  ${\rm C_W}$ , starting another cycle. The end result is a triangular voltage on  ${\rm C_W}$  with upper and lower peak limits of  $V_{\rm H}$  and  $V_{\rm L}$ , respectively. Finally, since the output of comparator CMP2 is a periodic digital signal, it is used as the master clock for the tuning and calibration process as well as the switching clock for the PWM buck regulator circuit.

The values of the charge and discharge currents during the tuning and calibration process are different. In tuning, a 50% duty-cycle triangular signal is generated with equal charge and discharge currents. In calibration and during normal operating conditions, however, no longer is a triangular waveform required. As a result, and since normal operating conditions requires a sawtooth ramp signal, the discharge current is set to a value that is approximately 10 times larger than the charge current. Similarly, since the peak-to-peak voltages of the triangular signal and the sawtooth ramp are different, their respective upper and lower limits ( $V_{\rm H}$  and  $V_{\rm L}$ ) are also set to different values.

# E. Test-Current Circuit

The basic function of the test-current circuit shown in Fig. 11 is to drive triangular and DC currents through the power inductor back to ground during the tuning and calibration process, when PWM switches  $\rm M_L$  and  $\rm M_H$  are both off. It does this by converting ripple and DC voltage signals into currents, sourcing them into inductor L, and sinking them back to ground via switch  $\rm M_b$ . Opamp  $\rm A_{TCG}$  and  $\rm M_a$  are connected in negative feedback configuration with a gain-bandwidth product of 10 MHz, forcing test voltage  $V_{Test}$ , which is referenced to the supply voltage, to the bottom terminal of test resistor  $\rm R_T$ . The current flowing through  $\rm R_T$  and  $\rm M_a$  is therefore set to  $(V_{DD}-V_{Test})/\rm R_T$ . During tuning,  $V_{Test}$  is derived from the triangular waveform generator; otherwise, it is set to a DC reference voltage during calibration or  $V_{DD}$  during normal operating conditions.

The high frequency components of the triangular current sourced into the inductor causes oscillations at  $V_{\rm Ph}$  because of the LC tank that results from power inductor L, output capacitor  $C_{\rm o}$ , and the parasitic capacitors surrounding the inductor. To damp these oscillations, damping resistor  $R_{\rm Damp}$  (200  $\Omega$ ) is connected across the inductor, but only during start-up. Its

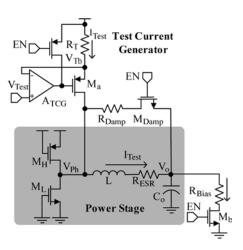


Fig. 11. Test-current circuit.

resistance is large enough to allow most of the test current (more than 99%) to flow into the inductor. The purpose of resistor  $R_{\rm Bias}$  is to bring the regulator's output voltage  $V_{\rm o}$  within common-mode voltage range of the  $G_{\rm M}$  cell. Finally, when tuning and calibration are finished, transistors  $M_{\rm a}$ ,  $M_{\rm b}$ , and  $M_{\rm Damp}$  are off.

# IV. CURRENT-MODE DC-DC BUCK CONVERTER

To verify the operation of the proposed current-sensing circuit, a PWM current-mode buck converter is designed, fabricated, and tested. The switching regulator is supplied from a 2.6–3.5 V DC supply and loaded with up to 0.8 A while regulating an output voltage of 1.5 V, which constitutes a typical portable CMOS application. The overall system is composed of a power stage, a feedback controller, and an inductor current-sensing block (Fig. 12). The output stage is switched at a constant frequency and the regulating feedback loop is consequently designed with a unity-gain frequency that is well below the switching frequency (e.g., 100 kHz for 1 MHz switching frequency). In all, the current-sensing block sends inductor current information back to the controller so that it may, in turn, along with output voltage information, regulate how the power stage transfers power from the input supply to the load.

# A. Controller

The feedback controller consists of an error amplifier with a frequency-compensating filter, a summing comparator, a ramp and pulse generator, a latch, a driver and dead-time control circuit, a reference and bias generator, and "house-keeping" start-up functions regulating and monitoring how the converter starts. Functionally, power switches M<sub>L</sub> and M<sub>H</sub> constitute an inverting driver whose supply is connected to the input supply voltage and its output generates a PWM signal, the average of which is set by the amount of time it is at  $V_{in}$  (i.e.,  $DV_{in}$ , where D is its duty cycle percentage of the time M<sub>H</sub> is conducting in a given switching cycle). The LC tank then filters this PWM signal so that its output is simply the average, i.e., DV<sub>in</sub>. The error amplifier closes a shunt negative feedback loop and, in the process, drives whatever signal is required to set output voltage  $V_0$  to reference voltage  $V_{ref}$ , virtually short-circuiting the inputs of the error amplifier [1], [2].

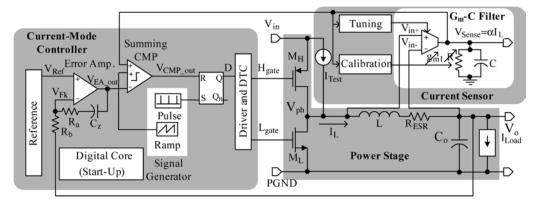


Fig. 12. Current-mode buck converter with the proposed self-learning current-sensing feature.

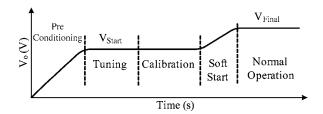


Fig. 13. Start-up sequence of the switching supply circuit.

The error signal generated by the amplifier is a slowly moving voltage against which a sawtooth overlapped by the sensed inductor current information and fed to summing comparator CMP generates the PWM signal driving the power stage. In essence, whenever the peak of the inductor current, which is triangular in nature and emulated by  $V_{\rm Sense}$ , surpasses slow-moving signal  $V_{\rm EA_{-}out}$ , the latch is reset with  $V_{\rm CMP_{-}out}$  and  $M_{\rm L}$  is therefore turned on (and  $M_{\rm H}$  off). This is reversed whenever a pulse, which defines the switching frequency of the converter, sets the latch, starting yet another cycle. A ramp signal is subtracted from the slow-moving error amplifier output via the summing comparator to reduce noise sensitivity and prevent large signal instability (i.e., sub-harmonic oscillations) at duty cycles exceeding 50%, which is otherwise known in literature as slope compensation [2].

The appealing feature of a current-mode topology is ease of frequency compensation because it transforms a complex-conjugate LC pole pair into what amounts a single pole [1], [2], [26]. It does this by adding an internal high frequency series feedback loop inside the outer voltage-regulating loop. Basically, the inductor current is sensed and regulated within the inner loop, thereby effectively turning the inductor into a current source, the output of which simply introduces a single pole when confronted with output capacitor Co. No compensation filter is required in this case; however, filter capacitor Cz and resistors R<sub>a</sub> and R<sub>b</sub> are introduced to improve the regulating performance of the regulator by increasing the DC open-loop gain. They basically add a pole at the origin and a zero within the bandwidth of the voltage loop (another pole is also added outside the bandwidth but that has little effect on the circuit) [26]. The gain at low frequencies is therefore high (set by the open-loop differential gain of the error amplifier) and attenuated

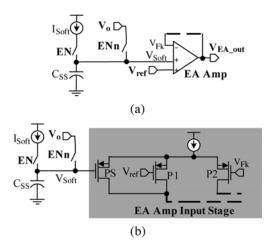


Fig. 14. Soft-start circuit.

as  $C_Z$ 's impedance decreases with frequency, until flattening the gain across the error amplifier to the ratio of  $R_a$  to  $R_b$ .

The summing comparator is designed with multiple low gain stages to gradually amplify the input overdrive and therefore achieve highest bandwidth [27], [28]. For the foregoing design, the comparator is designed to exhibit a 50 ns delay when confronted with an input overdrive of 10 mV. The purpose of the driver and dead-time control (DDTC) circuit is to build up enough drive to quickly charge and discharge the highly capacitive gates of switches  $M_L$  and  $M_H$ , and prevent them from conducting at the same time, which would otherwise constitute a short-circuit condition (shoot-through current) [1], [2], [15]. Drive is built by cascading gradually increasing inverters, where each inverter is a factor larger in size than the previous one.

#### B. Start-Up

The start-up block is responsible for governing not only the tuning and calibration phases but also the gradual and well-controlled ramp-up of the DC-DC converter. Once the input supply voltage is high enough, a pre-conditioning phase is asserted to ensure all biasing blocks are working properly and within operating limits, including allowing the regulator's output voltage to reach and stay within its input common-mode range (in this case, 0.6 V). The load is disabled during this time and a 50 mA

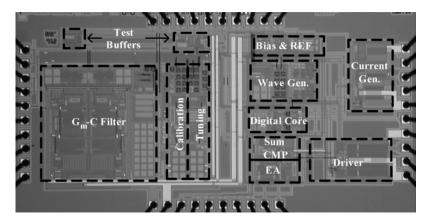


Fig. 15. Chip photograph of the prototyped self-learning converter.

peak-to-peak triangular current is sourced into the inductor in the latter stages of this phase. Only when the output capacitor is charged to approximately 0.9 V (well above 0.6 V), which is determined by a comparator within the start-up block, is tuning allowed to start, marking the end of the pre-conditioning phase (Fig. 13) and the onset of the tuning cycle.

As discussed earlier, when the targeted tuning transconductance  $(g_{\rm m1})$  is reached, Tune\_stop is asserted, disabling the tuning block and engaging the calibration sequence. Similarly, when the targeted resistance (R) is reached, Cal\_stop is asserted, disabling the calibration block and allowing a soft-start circuit to ramp-up the supply circuit to its targeted value (in this case, 1.5 V). The function of the soft-start block is to reliably ramp up the supply without damaging the components in the power stage with excessive inductor current, which is achieved by slowing down the ramp-up process.

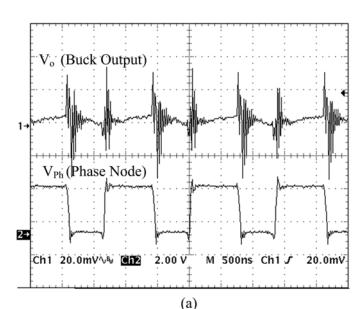
The core of the soft-start circuit is a slowly charging capacitor whose voltage is used to ramp the effective reference of the circuit until the output reaches its target. Since the output voltage in the foregoing start-up sequence is already at approximately 0.9 V when soft-start begins, the soft-start capacitor must be initialized to this level. This is done by connecting it in parallel with the output during the previous phases (i.e., pre-conditioning, tuning, and calibration). Once calibration ends, the soft-start capacitor is disconnected from the output and connected to a charging current (Fig. 14). Amplifier EA regulates the converter output to this slowly rising voltage ( $V_{\rm Soft}$ ) until it reaches  $V_{\rm ref}$ , at which point EA regulates against  $V_{\rm ref}$ .

A transistor is added to the input differential stage of amplifier EA to transition the regulation from  $V_{\rm Soft}$  to  $V_{\rm ref}$  Fig. 14(b) [1]. At first, when  $V_{\rm Soft}$  and output voltage  $V_{\rm o}$  are 0.9 V and  $V_{\rm ref}$  is 1.5 V, transistor P1 is off and transistors PS and P2 comprise the differential input pair, regulating  $V_{\rm o}$  to  $V_{\rm Soft}$ . When  $V_{\rm Soft}$  reaches within the vicinity of  $V_{\rm ref}$ , P1 starts to conduct, but soon thereafter, PS is turned off because  $V_{\rm Soft}$  surpasses  $V_{\rm ref}$ . Once  $V_{\rm Soft}$  is high enough, PS is completely off and P1 and P2 then regulate  $V_{\rm o}$  to  $V_{\rm ref}$ , linearly and softly transitioning from  $V_{\rm Soft}$  to  $V_{\rm ref}$ . Soft-start capacitor  $C_{\rm SS}$  and current  $I_{\rm Soft}$  are designed to ramp-up the supply in 2 ms. Capacitor  $C_{\rm SS}$  is external to the IC, as are the passive devices in the compensation network.

# V. EXPERIMENTAL RESULTS

The proposed 0.5  $\mu$ m CMOS (AMI) current-sensing and current-mode DC-DC buck converter circuit was fabricated, tested, and evaluated. The power stage, the passive components of the frequency compensation circuit, and the soft-start capacitor were off-chip (Fig. 12). The power stage consisted of a 3.9  $\mu$ H power inductor with a 48 m $\Omega$  ESR, 47  $\mu$ F output capacitor, and IRF7317 power switches having typical turn-on resistances of 65 m $\Omega$  and 27 m $\Omega$  for the pMOS and nMOS switches, respectively. The frequency-compensating passives consisted of 15 k $\Omega$ , 1 k $\Omega$ , and 2 k $\Omega$  resistors for  $R_a$ ,  $R_b$ , and  $R_c$ and 20 nF for C<sub>z</sub>. A 2 nF capacitor was used for the soft-start function  $(C_{SS})$ . The rest of the circuit, as pictured in Fig. 15, was fully integrated into a 3 mm  $\times$  1.5 mm silicon die. To accelerate the calibration phase, the digital core was designed to disconnect G<sub>M</sub>-C filter capacitor C only during this period, but this turned out to have adverse effects because noise degraded the calibration accuracy. An external RC low-pass filter was consequently added to the output of the G<sub>M</sub>-C filter, which was pinned out and accessible. Over all, the switching regulator circuit was fully functional, as shown in Fig. 16(a), where the circuit was loaded with a DC current of 0.8 A. The output ripple voltage, excluding noise, was less than 10 mV. Table I summarizes the experimental parametric performance of the overall switching current-mode buck converter. The response of the loop to a load transient event is shown in Fig. 16(b).

To evaluate the ac-gain accuracy of the current-sensing circuit, a sense resistor of 50 m $\Omega$  and a differential sense amplifier with a gain of ten was added to the printed-circuit board (PCB) to generate a reference signal (ideal) against which the output of the proposed circuit could be evaluated, matching the current-to-voltage gain of the circuit at 0.5 V/A. The DC accuracy was tested against the load current to which the supply circuit was exposed. In the end, after allowing the circuit to properly start, the measured output of the G<sub>M</sub>-C filter (i.e., sensed inductor current) was evaluated against its ideal AC and DC counterparts (Figs. 17 and 18). The experimental continuous inductor ripple current response of the proposed circuit matched the AC reference with an AC error of less than 9%. The experimental DC accuracy was better than 8%, and this resulted because the  $G_{\mathrm{M}}$  cell's gain was not perfectly linear throughout the load-current range.



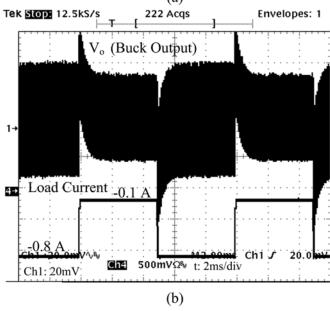


Fig. 16. Switching converter output voltage  $V_{\rm o}$  and switching node  $V_{\rm Ph}$  waveforms under a (a) DC load of 0.8 A and (b) output voltage under a series of transient load steps.

As the circuit enters the tuning phase, the external LC network is first charged with a constant current until the output voltage is raised above 1 V, at which point the test current circuit starts sourcing a triangular current into L, as shown in Fig. 19(a) and (b), where the ringing effects of rectangular waveform  $V_{\rm ph}$  (phase node) are the result of the parasitic inductances and capacitances present at that node. The amplitude of the ripple is then slowly increased from its lowest ac-gain setting (low amplitude ripple in Fig. 19(c)) until its target value is reached (higher amplitude ripple in Fig. 19(d)), when the circuit is tuned. At this point, signal Tune\_stop is asserted eight times to alert the digital core that tuning is completed.

To test the tuning range of the proposed circuit, a 200 kHz, 50% duty-cycle pulse was injected into the  $G_{\rm M}$ -C filter with a magnitude varying from 60 mV to 340 mV, emulating the

TABLE I
EXPERIMENTAL PARAMETRIC PERFORMANCE
OF THE CURRENT-MODE BUCK CONVERTER

Parameter	Value
Feedback Control	Current-Mode Synchronous PWM
Input Voltage (Vin)	2.6 - 3.5 V
Output Voltage (targeted for 1.5 V)	1.496 V
Output Current	0 - 0.8 A
Switching Frequency	780 kHz
Steady-State Output Voltage Ripple	<± 10 mV
Efficiency at $I_{Load}$ =0.8 A & $V_{in}$ =2.7 V with Lossless Current Sensing with $R_{Sense}$ Current Sensing	85.67 % 83.05 %
Load Regulation (LDR) (I <sub>Load</sub> =0-0.8 A)	-0.34 %
Line Regulation (LNR) (V <sub>in</sub> =2.7-3.5 V)	0.85 %
Soft-Start Delay	2.2 ms

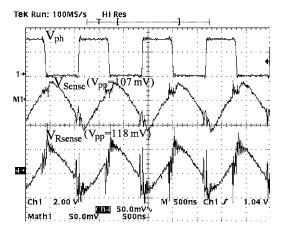


Fig. 17. Experimental sensed and reference AC inductor currents.

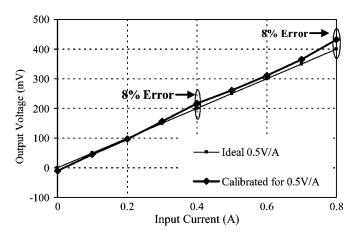


Fig. 18. Experimental sensed and ideal DC inductor currents.

effects of inductors in the range of 3  $\mu$ H and 17  $\mu$ H (L =  $V_{\rm Mag}\Delta T/\Delta I_{\rm Test}$ , where  $\Delta T=2.5~\mu s$  and  $\Delta I_{\rm Test}=50~{\rm mA}$ ), while monitoring the outputs of the  $G_{\rm M}$ -C filter and the tuning comparator. When the tuning circuit locked in place, the output of the  $G_{\rm M}$ -C filter was compared to the targeted 25 mV value ( $V_{\rm Tune}$ ) and errors were calculated accordingly. For inductors ranging from 3.5  $\mu$ H to 14  $\mu$ H, the tuning circuit locked within approximately 4% of its target (Fig. 20). This inductance range corresponds to the range for which  $g_{\rm m1}$  can be adjusted.

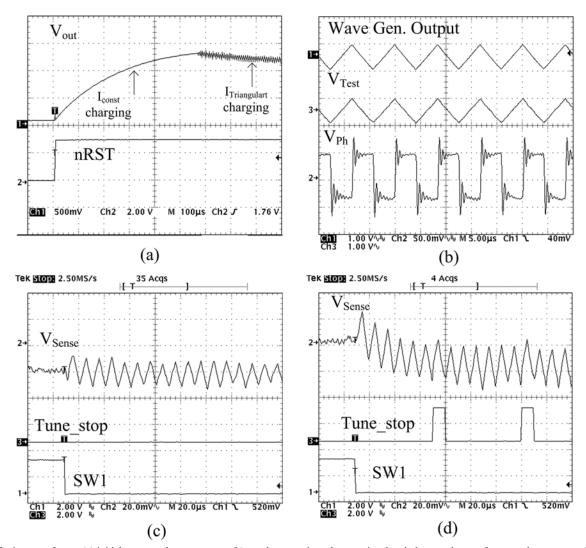


Fig. 19. Tuning waveforms: (a) initial output voltage ramp-up, (b) steady-state triangular test-signal and phase-node waveforms, and current-sensing filter and tuning circuit outputs (c) as ripple gain is increased (before reaching its target value) and (d) after target gain is reached and circuit is locked (tuned).

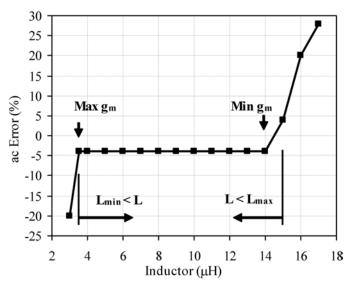


Fig. 20. Tuning inductance range and corresponding AC gain error.

The tuning range gain error was lower than the previously measured AC accuracy (-4% versus -9%) because their re-

spective frequencies were different (200 kHz versus 780 kHz). The error is greater at higher frequencies because the presence of parasitic poles present at higher frequencies further attenuate the gain, corresponding to a gain drop larger than 20 dB per decade. This was corroborated by another measurement whereby an 800 kHz test signal was tested. The gain of the circuit was further attenuated by 5%, when compared to the 200 kHz measurement, matching the 5% discrepancy between the AC and tuning loop measurements. Using a tuning switching frequency closer to the switching frequency would mitigate this error, but also increase the magnitude of the oscillations at  $V_{\rm ph}$  during the tuning process (when a triangular current is sourced into the inductor). The higher oscillations can be damped with a smaller  $\ensuremath{R_{\mathrm{Damp}}},$  but in that case, more test current would flow through  $R_{\ensuremath{\mathrm{Damp}}}$  , instead of the inductor, reducing the sensing accuracy of the system. Alternatively, the G<sub>M</sub> cell could be designed such that its parasitic poles are well above the switching frequency of the converter.

As described in Section III, the calibration process is comprised of three phases, the first two of which are for auto-zeroing offsets and the last is to sample the output and calibrate it against a target value in a sequential search fashion. Fig. 21

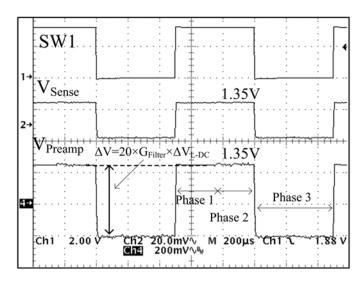


Fig. 21.  $V_{\rm Preamp}$  and  $V_{\rm Sense}$  during calibration, where DC filter gain  $G_{\rm Filter}$  is 6.38, inductor-ESR voltage  $V_{\rm L-DC}$  is 3.6 mV, and supply voltage  $V_{\rm DD}$  is 3.2 V.

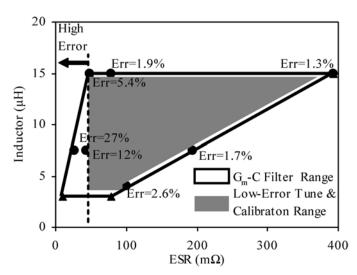


Fig. 22. Calibration range and DC errors for increasing ESR and inductance values.

illustrates the relevant calibration waveforms where Phase 3 is used to process the calibration procedure, which is to stop the calibration counter from incrementing R and the DC gain of the filter in each successive cycle when pre-amplifier voltage  $V_{\rm Preamp}$  reaches its target value of 0.5 V below 1.35 V, which corresponds to a current-sensing gain of 0.5 V/A. In testing the calibration range, the inductor's ESR must be considered and, for this test, a DC voltage was superimposed across the inputs of the G<sub>M</sub> cell to emulate the DC voltage across the inductor and its ESR during start-up ( $V_L = R_{ESR}I_{Test}$ ). Higher ESR values correspond to higher test voltages across the inductor during calibration, which eases the input-offset requirements of the G<sub>M</sub> cell and therefore improves calibration accuracy. Calibration accuracy consequently improves with higher ESR values, as also experimentally verified (Fig. 22). The area enclosed by the solid dark lines in Fig. 22 denotes the programmability range of the G<sub>M</sub>-C filter and the gray area the region for which there is less than 5.5% error. The end result was that ESR values below

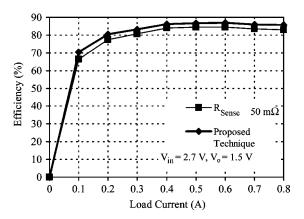


Fig. 23. Overall power efficiency of the switching power supply with the proposed current-sensing circuit and without it (with  $R_{\rm Sense}$ ).

 $48~\text{m}\Omega$  ( $V_L$  is 2.4 mV) rapidly degraded the calibration accuracy (DC error) beyond 5.4% (e.g., 12% and 27% for ESRs of  $44~\text{m}\Omega$  and  $26~\text{m}\Omega$ , respectively). Ultimately, the total gain error of the sensing circuit (AC and DC) is the linear sum of the AC and DC errors, which amount to 8.5% for an inductance and ESR combination of 3.9  $\mu\text{H}$  and  $48~\text{m}\Omega$  at a DC load current of 0.8 A and ripple peak-to-peak current of 0.2 A.

The overall efficiency performance of the current-mode DC-DC converter with and without the current-sensing circuit for loads ranging from 0 to 0.8 A is shown in Fig. 23. In the latter case, where a 50 m $\Omega$  series resistor is used in place of the proposed sensing circuit, the tuning and calibration circuits and the  $G_{\rm M}$ -C filter were disabled and the voltage across the series sense resistor was buffered and applied to the summing comparator, in place of  $V_{\rm Sense}$ . Ultimately, the sense resistor essentially incurred an efficiency loss of 2.3% at 0.8 A, which corresponds to the gain in efficiency of the proposed scheme, when considering the accuracies both of these schemes can achieve. As is normally the case, efficiency decreases slightly when load currents increase beyond their midrange level (0.5 A in this case) because of increasing conduction losses across the power MOSFET switches.

The efficiency is low during light loading conditions because the switching frequency is constant (i.e., converter is always in PWM mode) and no power-saving scheme, such as pulse frequency modulation (PFM), is used to decrease the frequency and therefore decrease its associated switching power losses. In fact, a meaningful efficiency comparison cannot really be ascertained at lighter loads (less than 0.2 A) because the design of the differential amplifier used to amplify the voltage across the sense resistor is not optimized and its quiescent power losses are higher than those of the G<sub>M</sub>-C filter prototyped. The efficiency at these lighter loads is expected to be on the same order because, just as the amplifier amplifies the voltage across the sense resistor, the G<sub>M</sub>-C filter processes the voltage across the inductor, both of which constitute constant loads to the system. Table II summarizes the experimental parametric performance of the proposed self-learning current-sensing CMOS circuit prototype and its G<sub>M</sub>-C filter.

The tuning and calibration functions of the proposed current-sensing  $G_M$ -C filter can be viably implemented with a digital-signal processor (DSP), but only if a high quality analog reference is used to calibrate the current-sensing device, or

TABLE II
EXPERIMENTAL PARAMETRIC PERFORMANCE OF THE PROPOSED
SELF-LEARNING CURRENT-SENSING CMOS CIRCUIT PROTOTYPE

Parameter	Value	
Technology	AMI's CMOS 0.5 μm	
Die Area (including pads)	3 mm x 1.5 mm	
Quiescent Current for Entire System	1.6 - 2.1 mA	
(during normal operation)	(for various values of g <sub>m1</sub> )	
Input Supply Voltage	2.6 - 3.5 V	
Self-Learning Current-Sensing Circuit		
Load Current (Inductor DC Current)	0 - 0.8 A	
Sensing Gain (Rgain=VSense/IL)	0.5 V/A	
Errors ( $I_{Load}$ =0.8 A, $\Delta I_{L}$ =0.2 A)		
ac	-9%	
DC (including offsets)	+8%	
Random Offset	$\pm 0.4\%$	
Non Linearity (Systematic Offset)	-2%	
Total (weighted DC + ac errors)	8.51%	
Tunable Inductor Range	3.5 μΗ -14 μΗ	
Inductor's ESR Range	$48~\text{m}\Omega - 384~\text{m}\Omega$	
Worst-Case Start-Up Time	484 ms	
G <sub>M</sub> -C Filter		
BW (1/RC) Programmability	1.1 kHz to 6.4 kHz	
(worst-case resolution by design)	(3.2%)	
Gain (g <sub>m</sub> R) Programmability	1.27 - 29.16 (V/V)	
(worst-case resolution by design)	(3.2%)	
Input-Referred Offset for 3 Samples at Gain=9.92, Max. R, V <sub>DD</sub> =3-4.2V, and ICMR=1-1.5 V	<±210 μV	
Transient Glitches	< 40 mV	
Input-Referred Total Noise (C=60 pF, Gain=9.92, & Max. R)	93 μV	
Filter Nonlinearity ( $\Delta g_m/g_m$ ) For a Rail-to-Rail Input (3 V)	-57 dB	
Second (Parasitic) Pole	4 MHz	
Auto-Zeroing Clock Frequency	1 kHz	

if the analog test-signal and tuning and calibration method proposed here are used. Digital controllers for high speed applications, however, are often less appealing than their analog counterparts because of their relatively higher silicon real-estate demands, longer response times (lower speed), and higher processing costs [29], and a DSP is therefore not always available. State-of-the-art analog current-sensing solutions, on the other hand, such as a Sense-FET, may be less accurate and only applicable to on-chip switches but often less complex and less area-intensive, and they should consequently be used in crude on-chip current-sensing applications. The proposed technique is accurate and lossless but relatively complex, so its market space tends to be in high performance applications where current-based mode-hopping schemes are used to increase efficiency and improve regulating performance.

The relatively long calibration and tuning cycles can be considerably reduced if the sequential search (i.e., linear search with a sequential up counter) were replaced with a binary search (i.e., successive range divisions) or any other more sophisticated convergent search algorithm. For instance, while a linear search requires an average of  $2^{N-1}$  counts, where N is the number of programmability bits, the binary search only requires N, thereby potentially decreasing the 500 ms calibration process down to

approximately 16 ms. Alternatively, if time overhead is still an issue, the long calibration cycles can be altogether avoided during *soft* re-start events by deglitching the events and storing the calibration settings in on-chip memory modules; the settings could then be refreshed and reprogrammed during *hard* re-set conditions.

For considerably higher switching frequency applications (e.g., 100 MHz), the bandwidths of the G<sub>M</sub>-C cell, controller, and all signal-processing blocks must be scaled accordingly, and the switching noise that is injected as a result is similarly filtered. The underlying idea behind the proposed current-sensing scheme is to build a voltage-mode G<sub>M</sub>-C filter that reproduces the filtering effects the inductor has on its current, so its respective bandwidths are equal to  $R_{ESR}/2\pi L$ , which is relatively low compared to the switching frequency (e.g., a few kHz of bandwidth compared to a few MHz of switching frequency). Consequently, the switching noise injected into the analog filter is well attenuated (e.g., by about 60 dB), making the foregoing solution relatively robust to switching noise. Although switching frequencies on the order of hundreds of mega-Hertz are attractive from the perspective of LC integration, practical designs generally conform to lower switching frequencies (e.g., less than 10 MHz) to keep switching power losses low and therefore maintain high efficiency performance. The 200 MHz converter reported in [30] achieved 80% efficiency in part because its input supply voltage was 1.2 V and switching losses were consequently significantly lower, which would not have been the case in a Li-Ion-supplied application (2.7-4.2 V) where switching losses would have been drastically increased (proportional to the square of the supply voltage).

#### VI. CONCLUSION

A fully integrated continuous, lossless, and accurate self-learning current-sensing 0.5 μm CMOS circuit was presented, and along with a current-mode switching buck DC-DC converter platform, designed, fabricated, and experimentally tested. Its overall sensing accuracy was 8.5% for a tunable inductor and ESR range of 3.5  $\mu$ H–14  $\mu$ H and 48 m $\Omega$ –384 m $\Omega$ , when state-of-the-art lossless and fully integrated solutions achieve between 20% and 40% only when knowing the power inductor's inductance. The driving novelty behind the system is its accurate self-learning feature, wherein the voltage gain and bandwidth of an on-chip G<sub>M</sub>-C filter are automatically matched to the power inductor's current frequency response during power-on-reset events to emulate the inductor current and indirectly measure the off chip power inductor's inductance and ESR. Even though the technique was only applied to a peak current-mode switching buck converter, the scheme extends to most inductor-based switching regulator topologies, such as boost and buck-boost converters, independent of the current ratings of the power stage and whether on- or off-chip power switches are used. The self-learning current-sensing feature proposed affords the designer the flexibility required to address emerging state-of-the-art challenges by allowing the power supply system to self-adjust and mode-hop according to its passive and active loading conditions, in the process optimizing speed and power efficiency performance, which are more critical than ever today, especially in portable, battery-powered applications.

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