Theory and Practice
in Parallel Job Scheduling

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Abstract

Parallel job scheduling has gained increasing recognition in recent years as a distinct area of study. However, there is concern about the divergence of theory and practice in the field. We review theoretical research in this area, and recommendations based on recent results. This is contrasted with a proposal for standard interfaces among the components of a scheduling system, that has grown from requirements in the field.

1   Introduction

There has been considerable interest in parallel job scheduling in recent years [41], and it has gained recognition as a distinct research topic that is largely unrelated to the better known problem of DAG scheduling [1]. Very many approaches have been proposed and implemented [20]. The differences lie in the targetted systems, the assumptions made, and the mechanisms used.

We shall concentrate on distributed memory massively parallel processors (MPPs), which currently dominate the supercomputing arena. By this we mean machines in which physical memory is packaged with the processors, forming so-called "processing elements" (PEs), as opposed to machines in which memory is global and independent of the processors. The implication is that memory is typically allocated

in conjunction with the processors, rather than being treated as a distinct resource. However, this does not preclude a shared address space model of computation, and indeed many recent systems provide hardware support for different levels of memory sharing.

There are a growing number of high performance computing facilities that support large diverse workloads of parallel jobs on multicomputers that have tens to thousands of processors. The typical way that they are currently used is that:

1. The system is divided into "partitions" consisting of different numbers of processors. Most processors are allocated to partitions devoted to serving parallel jobs. One partition is typically set aside for support of interactive work through time-slicing of its processors. Another may be devoted to service tasks, such as running a parallel file system. The configuration of partitions may be changed on a regular basis (for example, by providing larger partitions for parallel jobs at night or over weekends, at the expense of the interactive partition).

2. A (large) number of queues are established, each one corresponding to a specific combination of job characteristics. (For example, one queue might correspond to jobs that require as many as 32 processors, and are expected to run no longer than 15 minutes.) Some queues are served at higher priority than others, so the user tends to submit a job to the highest priority queue for which the job qualifies based on its expected resource requirements.

3. Each partition is associated with one or more queues, and its processors serve as a pool for those queues. Whenever some processors are free, the associated queues are searched in order of priority for one that is non-empty. The

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first job in that non-empty queue is then activated in the partition, and it runs until it completes, provided the number of free processors is sufficient. Within each queue jobs are processed strictly in first-come-first-served order. (If the jobs in a single queue have highly variable execution times, then short jobs will commonly be delayed by long jobs preceding them; this pitfall is avoided by having a number of queues, and placing jobs among them based on their expected execution times, and then giving higher priority to the queues containing the jobs with smaller execution times.) A relatively recent innovation in some production systems is the use of a scheduler that allows non-FCFS processing in a queue. (For example, the EASY scheduler does "back-filling", which amounts to allowing smaller jobs to jump ahead of larger ones under certain conditions [50].)

Thus:

- the number of processors assigned to a job is fixed by the user;

- once initiated the job runs to completion.

While there exist some innovations that have been introduced into production systems, such as non-FCFS service and support for swapping, the general trend is to retain the same framework, and moreover, to cast it into a standard. This exposes the problems of the divergence between theory and practice [26]. In fact, there is considerable theoretical work lately that tries to be more directly relevant to practice, but falls outside of the above framework. For example, theoretical analysis underscores the effectiveness of preemption in achieving low average response times, and also shows that considerable benefits are possible if the scheduler is allowed to tailor the partition sizes in accordance with the current system load. Notably, much of this work is based on workload models that are derived from measurements at supercomputer installations.

We survey the theoretical background in Section 2, and the specific recommendations that are made in Section 3. The standardization effort based on practical work at large installations is reviewed in Section 4. Finally, we discuss this state of affairs and present our conclusions in Section 5.

2 Survey of Theoretical Results

Various kinds of scheduling or sequencing problems have been addressed since the fifties by theoretical researchers from the areas of computer science, operations research, and discrete mathematics. The challenge of efficient job management on computers has frequently been named as a key reason to address this kind of problems. This is especially true for job scheduling on parallel systems with a large number of processors or nodes. Hence a direct use of many of these theoretical results in real applications would seem to be natural. However, in reality these theoretical results are rarely cited in more application oriented work and almost never used in commercial systems.

By reviewing some of the results in theoretical job scheduling we therefore want to address the questions:

- What kind of help can designers of commercial scheduling systems expect to obtain from the solution of theoretical problems?

- Is it useful for researchers and developers targeting the design of new scheduling systems for real machines to spend their time studying theoretical papers as well?

- If yes, which of those papers are most likely to prove really helpful?

- Is there any purpose to generate abstract models of real machines and real scheduling problems which may be interesting for theoreticians?

2.1 Classification of Theoretical Results

A substantial divergence has already been noted between practical approaches and theoretical concepts in general. But in addition there is also a large diversity among theoretical methods. Therefore, it may not be appropriate to talk about theoretical work in this area as a uniform block. Hence, in order to address some of the above mentioned questions we first wish to provide a rough classification of different theoretical models and results. Also, we want to establish a connection between the various theoretical environments and situations arising in real multiprocessors.

2.1.1 Cost metric

For the discussion of the various cost metrics we use the following notations:

t_i	completion time of job i in a schedule
d_i	deadline of job i
s_i	release time of job i
w_i	weight of job i

Here, the completion time t_i is the time when the computer system has finally completed work on this job. Note that no information is provided on whether the job has been successfully completed or whether it has been removed from the system for other reasons. Next, the release time s_i is the earliest time the computer system can start working on job i. Usually, the release time of a job is identical with its submission time or arrival time, that is the time a computer system becomes aware of the new job for the first time. However, in some studies it is assumed that the scheduling system is already aware of all jobs at time 0, but job i cannot be started before some time $s_i \geq 0$. The meaning of the deadline d_i is not defined in a unique way: Not meeting the deadline for a specific job, i.e. $t_i > d_i$, may either cause the job to fail or may only result in additional costs. The weight w_i of a job is a way to prioritize one job over another.

Obviously, scheduling problems arise if different jobs compete with each other over the allocation of system resources. The assignment of those resources to a specific job will result in some costs for this job. In many theoretical papers the cost of a schedule is simply the sum of the individual job costs for all jobs. This cost function serves as basis to compare and evaluate different schedules. Assuming a job system τ the following metrics are commonly used:

Makespan (throughput)	$\max_{i \in \tau} t_i$
Deadline misses	$\lvert \{i \in \tau \mid t_i > d_i\} \rvert$
Weighted completion time	$\sum_{i \in \tau} w_i t_i$
Weighted flow (response) time	$\sum_{i \in \tau} w_i (t_i - s_i)$
Weighted tardiness	$\sum_{i \in \tau} w_i \max\{0, t_i - d_i\}$

Note that response time and flow time usually have the same meaning. The origin of these criteria often goes back to the fifties. For instance Smith [83] showed in 1956 that the sum of the weighted completion times for a system of jobs on a single processor can be minimized if the tasks are scheduled by increasing execution time to weight ratio, the so called Smith ratio. If all jobs have unit weight this algorithm becomes the well known shortest-job first method.

These metrics allow a relatively simple evaluation of algorithms which may be one reason they have been frequently used in theoretical scheduling up to now. Also, some of the metrics are closely related to each other.

Example 1 *A schedule with optimal weighted completion time also has the optimal weighted flow time, provided both schedules obey the same model constraints. However, it is much easier to find a schedule which deviates a constant factor from the optimum in case of the weighted completion time metric than for the weighted flow time metric, as shown by Kellerer et al. [43] and by Leonardi and Raz [48].*

Looking at the problem from another perspective we can state that in a business environment one would expect an optimal job scheduler to simply achieve two goals:

1. Satisfy the users.

2. Maximize the profit.

Undoubtedly, there is a strong qualitative relation between the abovementioned theory criteria and the commercial goals. For instance, a reduction of the job response time will most likely improve user satisfaction. But to our knowledge a quantitative link between the two types of criteria has never been established.

Example 2 *Assume that a job i needs approximately 3 hours of computation time. If the user submits the job in the morning (9am) he may expect to receive the results after lunch. It probably does not matter to him whether the job is started immediately or delayed for an hour as long as it is done by 1pm. Any delay beyond 1pm may cause annoyance and thus reduce user satisfaction, i.e. increase costs. This corresponds to tardiness scheduling. However, if the job is not completed before 5pm it may be sufficient if the user gets*

his results early next morning. Moreover, he may be able to deal with the situation easily if he is informed at the time of submission that execution of the job by 5pm cannot be expected. Also, if the user is charged for the use of system resources, he may be willing to postpone execution of his job until nighttime when the charge is reduced.

The use of metrics such as throughput and response time in many commercial installations may be due to the simplicity of the evaluation, or it may be a sign of some non-obvious influence from theory. On the other hand, a good management policy for a commercial system may require that different metrics are used during different times of the day: During daytime many users will actually wait for the completion of their submitted jobs. Thus a response time metric is appropriate. However, during the night it is best to maximize the throughput of jobs.

Example 3 *Fig. 1 shows the load of a multiprocessor over the course of a day. For reasons of simplicity each job is described as a rectangle. Black rectangles denote idle processors due to fragmentation. However, note that multiprocessors do not necessarily require a linear one-dimensional processor space. But this way it is easier to visualize jobs. As shown in the figure, during periods of high user activity small jobs are given preference even if some processors remain idle due to fragmentation of the processor space. Jobs are allocated resources such that the shortest response time is achieved. On the other hand during periods of low user activity large batch jobs are started. Also moldable jobs are run in a way to increase efficiency, i.e. using less processors but requiring more execution time.*

Therefore, recent studies, e.g. Charkrabarti et al. [8], explicitly address the problem of bicriteria scheduling where scheduling methods are introduced which generate good schedules with respect to the makespan and the weighted completion time metric.

2.1.2 The Model

A large variety of different machine and scheduling models have been used in studies of scheduling problems. The constraints incorporated into these models directly affect operations of the scheduler. They are at least partly inspired by the way real systems are managed and how parallel applications are written.

In the following we roughly classify these models according to five criteria:

1. Partition Specification

Each parallel job is executed in a *partition* that consists of a number of processors. The size of such a partition may depend on the multiprocessor, the application, and the load of multiprocessor [26]. Moreover, the size of the partition of a specific job may change during the lifetime of this job in some models:

1. **Fixed.** The partition size is defined by the system administrator and can be modified only by reboot.

2. **Variable.** The partition size is determined at submission time of the job based on user request.

3. **Adaptive.** The partition size is determined by the scheduler at the time the job is initiated, based on the system load, and taking the user request into account.

4. **Dynamic.** The partition size may change during the execution of a job, to reflect changing requirements and system load.

Feldmann et al. [27] have considered fixed partitions generated by different architectures such as hypercubes, trees, or meshes. Many other authors use the variable partitioning paradigm, in which each job requires a specific number of processors but can be scheduled on any subset of processors of the system. An example of a theoretical study based on the adaptive approach is the work of Turek et al. [89]. Here, the application does not require a specific number of processors, but can use different numbers. However, once a partition for a job has been selected its size cannot change anymore. Finally, in dynamic partitioning the size of a partition may change at run time. This model has, for instance, been used by Deng et al. [12].

2. Job Flexibility

As already mentioned advanced partitioning methods must not only be supported by the multiprocessor system but by the application as well. Therefore, Feitelson and Rudolph [26] characterize applications as follows:
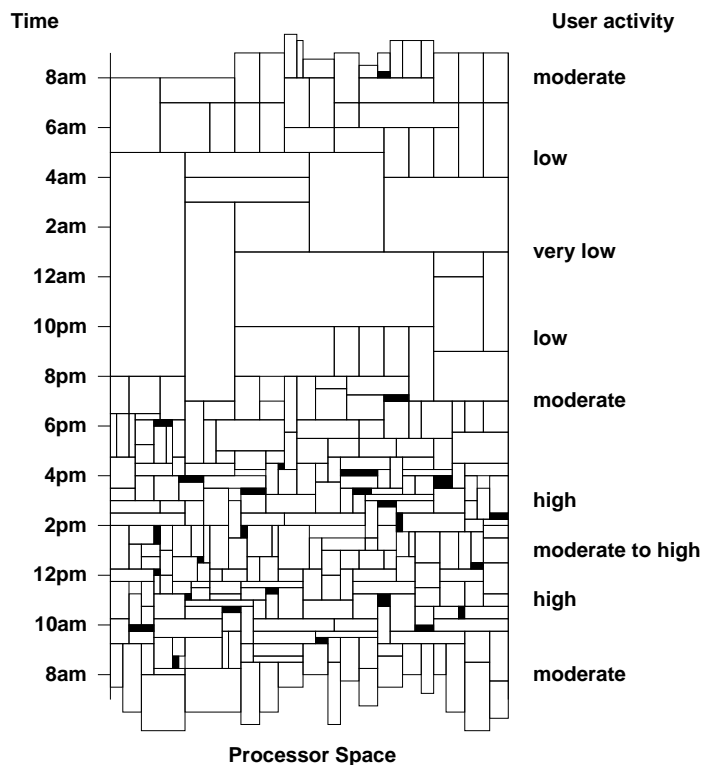
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Figure 1: *Workload of a parallel computer over the course of a day.*

1. **Rigid jobs.** The number of processors assigned to a job is specified external to the scheduler, and precisely that number of processors are dedicated to the job throughout its execution.

2. **Moldable jobs.** The number of processors assigned to a job is determined by the system scheduler within certain constraints when the job is first activated, and it uses that many processors throughout its execution.

3. **Evolving jobs.** The job goes through different phases that require different numbers of processors, so the number of processors allocated may change during the job's execution in response to the job requesting more processors or relinquishing some. Each job is allocated at least the number of processors it requires at each point in its execution (but it may be allocated more to avoid the overheads of reallocation at each phase).

4. **Malleable jobs.** The number of processors assigned to a job may change during the job's execution, as a result of the system giving it addi-

tional processors or requiring that the job release some.

The manner in which an application is written determines which of the four types is used[1]. The more effort devoted to writing the application with the intention of promoting it to one of the later types, the better a good scheduler can perform with respect to both the particular job, and the whole workload. Generally, a scheduler can start a job sooner if the job is moldable or even malleable than if it is rigid [88].

If jobs are *moldable*, then processor allocations can be selected in accordance with the current system load, which delays the onset of saturation as system load increases [26]. It is generally not difficult to write an application so that it is moldable, and is able to execute with processor allocations over some range (e.g., any power of two from four to 256). *Evolving* jobs arise when applications go through distinct phases, and their natural parallelism is different in

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[1] Some theoretical studies use different terminology. For example, Ludwig and Tiwari [51] speak about "malleable" jobs which are equivalent to moldable jobs in our terminology.

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different phases. For such jobs, system calls are inserted at the appropriate points in the application code to indicate where parallelism changes [95].

Certain parallel applications, such as those based on the "work crew" model[2], can be modified to be *malleable* relatively easily. An increased processor allocation allows more processors to take work from the queue, while a reduction means that some processors cease picking up work and are deallocated [68]. In most cases, however, it is more difficult to support malleability in the way an application is written. One way of attaining a limited form of malleability is by creating as many threads in a job as the largest number of processors that would ever be used, and then using multiplexing (or *folding* [52, 39]) to have the job execute on a lesser number of processors. Alternatively, a job can be made malleable by inserting application specific code at particular synchronization points to repartition the data in response to any change in processor allocation. The latter approach is somewhat more effective, but it requires more effort from the application writer, as well as significantly more system support. Much of the required mechanisms for supporting malleable job scheduling is present in facilities for checkpointing parallel jobs [67]. Hence, a combined benefit can be derived if processor allocations are changed only at times when checkpoints are taken.

For stable applications that are widely and frequently used by many users, the effort required to make them malleable may be well justified. Otherwise, it is probably not worthwhile to write applications so that they are malleable.

3. Level of Preemption Supported

Another issue is the extent to which individual threads or entire jobs can be preempted and potentially relocated during the execution of a job:

1. **No Preemption.** Once a job is initiated it runs to completion while holding all its assigned processors throughout its execution.

2. **Local Preemption.** Threads of a job may be preempted, but each thread can only be resumed later on the same processor. This kind of preemption does not require any data movement between processors.

3. **Migratable Preemption.** Threads of a job may be suspended on one processor and subsequently resumed on another.

4. **Gang Scheduling.** All active threads of a job are suspended and resumed simultaneously. Gang scheduling may be implemented with or without migration.

While many theoretical scheduling studies only use a model without preemption, more recently preemption has also been taken into account. Schwiegelshohn [72] uses a gang scheduling model without migration. The work of Deng et al. [12] is based upon migratable preemption.

In a real system the preemption of a job requires that all the job's threads be stopped in a consistent state (i.e., without any messages being lost), and the full state of each thread must be preserved. The memory contents associated with the job may be either explicitly written out of memory, or may be implicitly removed over time by a process such as page replacement. Whether or not the data of a job is removed from memory when the job is preempted depends in part on the memory requirements of the preempting job and the total amount of memory available.

In addition migratable preemption needs the mechanism of moving a thread from one processor to another, while preserving all existing communication paths to other threads. Also, when a thread is migrated, its associated data must follow. In message passing systems, this requires that the data be copied from one processor to another. In shared memory systems, the data can be transferred a cache line or page at a time as it is referenced. Preemption may have great benefit in leading to improved performance, even if it it used infrequently and on only a small fraction of all jobs.

Preemption in real machines has an overhead cost which is ignored in some theoretical studies. Motwani et al. [56] address the overhead by minimizing the number of preemptions. In order to compare a preemptive schedule with non-preemptive ones Schwiegelshohn [72] included in his model a time penalty for each preemption which increases the cost of the schedule.

4. Amount of Job and Workload Knowledge Available

Systems differ in the type, quantity, and accuracy of information available to and used by the scheduler.

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[2] In the "work crew" model, processors pick up relatively small and independent units of computation from a central queue.

Characteristics of individual jobs that are useful in scheduling include (i) the total processing requirement, and (ii) the speedup characteristics of the job. Full knowledge of the latter requires knowing the execution time of the job for each number of processors on which it might be executed. Partial knowledge is provided by characteristics such as average parallelism (the average number of processors busy when the job is allocated ample processors), and maximum parallelism (the largest number of processors that a job can make use of at any point in its execution).

Workload information is also useful in choosing a scheduling policy. For example, workload measurements at a number of high-performance computing facilities have indicated that the variability in processing requirements among jobs is extreme, with most jobs having execution times of a few seconds, but a small number having execution times of many hours. The coefficient of variation[3], or CV, of the service times of jobs has been observed to be in the four to seventy range at several centers [9, 65, 22]. This implies that a mechanism to prevent short jobs from being delayed by long jobs is mandatory.

The knowledge available to the scheduler may be at one of the following levels:

1. **None.** No prior knowledge is available or used in scheduling, so all jobs are treated the same upon submission.

2. **Workload.** Knowledge of the overall distribution of service times in the workload is available, but no specific knowledge about individual jobs. Again, jobs are treated the same, but policy attributes and parameters can be tuned to fit the workload.

3. **Class.** Each submitted job is associated with a "class", and some key characteristics of jobs in the class are known, including, for example, estimates of processing requirement, maximum parallelism, average parallelism, and possibly more detailed speedup characteristics.

4. **Job.** The execution time of the job on any given number of processors is known exactly.

Job knowledge, which is defined to be exact, is unrealistic in practice. However, assuming omniscience

in modeling studies makes it possible to obtain an optimistic bound on performance that is not attainable in practice. Presuming job knowledge in modeling studies sets a standard in performance against which practically realizable scheduling algorithms, which use class knowledge at most, can be compared.

While in many theoretical studies of scheduling problems all job information is assumed to be available, there are a few papers which explicitly address the so called "non-clairvoyant scheduling", see e.g. Motwani et al. [56]. Also, on-line scheduling has been addressed more frequently in recent years. For instance Shmoys et al. [79] discussed makespan scheduling if the job characteristics are not known until the release time and the execution time requirements of the job are also not available before the job has been executed to completion.

Many systems make no effort at all to use information that accompanies a job submission to estimate the resource requirements of the job. However, smallest demand type disciplines (e.g., "Least Work First" (LWF)) can be used to yield low average response times if the resource demand of each job is known (precisely or approximately). For example, in many current systems jobs are submitted to one of a large number of queues, and the queue selected indicates such information as the number of processors needed, a limit on the execution time, and other parameters. Thus, each queue corresponds to a job class. In these systems, this information can be used implicitly through the way queues are assigned to (fixed) partitions, and the relative priorities assigned to the queues.

Any information provided by the user relating to job resource requirements must be used carefully both because it is prohibitively difficult for the user to consistently provide information with high accuracy, and also because the user may be motivated to deceive the scheduler intentionally. Thus, sources from which to gain knowledge about job resource requirements must be broadened to include:

- consider user provided information (while recognizing that it is historically quite unreliable, in part because users aren't careful about making good estimates);

- measure efficiency during execution [60], and increase processor allocations only for jobs that are using their currently allocated processors effectively;

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[3] The coefficient of variation of a distribution is its standard deviation divided by its mean.

- keep track of execution time and speedup knowledge from past executions on a class by class basis, and use that information.

All identifying characteristics associated with the submission of a job can potentially be used to determine its class. These characteristics include the user id, the file to be executed, the memory size specified, and possibly others. An estimate of the execution time of a job being scheduled can be obtained from retained statistics on the actual resource usage of jobs from the same (or a similar) class that have been previously submitted and executed. Recent work has demonstrated the feasibility and potential benefit of this approach [32]. A small database can be kept to record resource consumption of jobs on a class by class basis. This is very useful particularly for large jobs that are executed repeatedly.

5. Memory Allocation

In some systems, memory as well as processors may be a limiting resource on performance. This is particularly true in shared-memory systems, where the allocation of memory is relatively decoupled from the allocation of processors. Thus there are two types of memory to consider:

1. **Distributed Memory.** Typically each processor and its associated memory is allocated as a unit, since a thread must use message passing to access data not in the local memory of the processor on which it is running.

2. **Shared Memory.** Data stored remotely from a processor can be accessed directly (albeit at higher cost than for locally stored data), so there are situations where the ideal resource allocation does not distribute memory among applications in the same proportions as processors.

It is commonly assumed that the memory requirements of a job are known precisely at the time the job is initiated possibly because the user is required to indicate the (maximum) memory requirement of the job. Only recently has memory in addition to processors been taken into account in scheduling algorithms [66, 74, 63, 62].

2.1.3 Algorithmic Methods

A large number of theoretical papers deal with the issue of intractability for many scheduling problems [29]. In the area of parallel job scheduling the most important contributions are made by Du and Leung [14] for preemptive and non-preemptive gang scheduling using makespan as criterion, and by Bruno, Coffman, and Sethi [7] and McNaughton [54] for preemptive and non-preemptive weighted completion time scheduling on a parallel computer.

Except for the fact that there is no hope for a simple optimal algorithm little help can be expected from this work for practical scheduling systems. Furthermore, most real systems must deal with a significant number of additional constraints, like unknown parameters of jobs. Therefore even for polynomial problems, it is unlikely that an optimal schedule can be achieved. Moreover, a typical scheduler is subject to real time conditions that do not allow the use of high order polynomial algorithms. Hence, approaches to find optimal solutions for scheduling problems, e.g. with branch and bound algorithms [5], are only used under special circumstances. This is especially true for problems involving a large number of jobs. In addition, those algorithms often produce only a small improvement due to the good results of many heuristics.

With the intractability of many scheduling problems being established, many theoretical researchers turned their attention towards the design of polynomial algorithms which guarantee a small deviation from the optimal schedule for any job system. While in some cases this deviation from the optimum is minimized regardless of the algorithmic complexity [71], other work analyzes the performance of particular simple algorithms, like list scheduling methods [42, 94]. The latter group promises to be of the greatest help for the selection of scheduling methods in real systems. Therefore, we will look more closely at this group in the following. Moreover, these algorithmic methods are also used for determining the cost deviation from the optimum in the on-line case or if some job properties, e.g. the execution time, are unknown. This is called competitive analysis introduced by Sleator and Tarjan [81]. It is especially noteworthy that the area of approximation algorithms is considered to be one of the most flourishing areas of theoretical computer science in recent years.

Although many of the approximation algorithms have a low computational complexity and produce schedules that are close to the optimum, they are usually not the method of choice in commercial installations. Apart from lack of knowledge about these

algorithms there are two principal reasons for this:

1. **Worst Case Analysis.** The worst case approximation factor is usually of little relevance to a practical problem since a schedule that approaches the worst case is often unacceptable for a production schedule. For instance, the makespan approximation factor for list schedules of non-preemptive parallel job schedules is 2. In other words, up to 50% of the nodes of a multiprocessor system may be left idle. However, these high costs are only encountered for a few job systems which may never be part of real workloads.

   Example 4 *Turek et al. [90] proposed so called SMART schedules for the off-line non-preemptive completion time scheduling of parallel jobs. They proved an approximation factor of 8 [73] and gave a worst case example with a deviation of 4.5. However, applying the algorithm on job systems obtained from the traces of the Intel Paragon at the San Diego Supercomputing Center gave an average deviation from the optimum by 2.0. This result was further improved to the factor 1.4 by using the job order of the SMART schedule as input for a list schedule [34].*

2. **Model Limitations.** Some theoretical methods are based on restricted models which deviate significantly from real life situations. For instance the above mentioned SMART algorithm generates non-preemptive off-line schedules and requires the knowledge of the execution time of all jobs. On the other hand, the consideration of more complex constraints may make any general approximation algorithm impossible [43, 48]. Moreover, there may be additional user demands with little influence on the cost function which cannot be easily incorporated into these algorithms.

   Example 5 *In many computing centers it was noted that a non-negligible number of parallel batch jobs failed to run more than a minute due to reasons such as an incorrectly specified data file. Therefore, some users request that their job should be started immediately after submission, then interrupted after 1 minute and finally resumed and completed at a later time.*

Nevertheless, the theoretical analysis of algorithms can be of invaluable help even for practical purposes. The evaluation of any schedule can be either done by comparing this schedule against the optimal schedule or against schedules generated by other methods. But only the deviation from the optimal schedule can determine whether there is enough room for improvement to motivate further algorithmic research. Unfortunately, the optimal schedule cannot be obtained easily. But many theory papers dealing with approximation algorithms also use lower bounds for the optimal schedule to determine the approximation factor, e.g. the squashed area bound introduced by Turek et al. [90]. The same bounds can also be applied for the evaluation of a heuristic schedule for a real workload provided the same cost metric is used.

Moreover, the theoretical analysis may be able to pinpoint the conditions which may lead to a bad schedule. These methods can also be applied to any practical approach and help to determine critical workloads. If the evaluation of real traces reveals that such critical workloads rarely or even never occur then they can either be ignored or the approach can be enhanced with a procedure to specifically handle those situations.

Example 6 *For instance Kawaguchi and Kyan's LRF schedule [42] can be easily extended to parallel jobs. As long as no parallel job requires more than 50% of the processors, this will only increase the approximation factor from 1.21 to 2 [88]. However, if jobs requiring more processors are allowed in addition, no constant approximation factor can be guaranteed.*

Finally, as already mentioned the costs of the schedules generated by theoretical approximation methods are usually very low for the average workload. Even if they do not comply directly with all constraints of a real scheduling environment, they can be used as building blocks of a practical scheme. For instance an off-line algorithm can be applied to a subset of jobs whenever a new job arrives.

2.2 Some Specific Studies

2.2.1 Workload Characterization

Several workload characterization studies of production high-performance computing facilities have been carried out. They reveal characteristics of actual workloads that can be exploited in scheduling.

Feitelson and Nitzberg noted that repeated runs of the same application occurred frequently, and later runs tended to have similar resource consumption patterns as the corresponding earlier ones [22]. Hotovy studied a quite different system, yet found many of the same observations to hold [38]. Gibbons also analyzed workload data from the Cornell site in addition to two sites where parallel applications are executed on a network of workstations [31]. He found that, in all three systems, classifying the jobs by user, program executed, and requested degree of parallelism led to classes of jobs in which execution time variability is much lower than in the overall workload.

Feitelson studied the memory requirements of parallel jobs in a CM-5 environment. He found that memory is a significant resource in high-performance computing, although he observed that users typically request more processors than naturally correspond to their memory requirements [18]. Jann et al. have produced a workload model based on measurements of the workload on the Cornell Theory Center SP2 machine [40]. This model is intended to be used by other researchers, leading to easier and more meaningful comparison of results. Nguyen at al. have measured the speedup characteristics of a variety of applications [59].

2.2.2 Scheduling in practice

Several groups have modified NQS implementations to allow queue reordering in order to achieve better packing. Lifka et al. have developed a scheduler on top of LoadLeveler with the feature that the strict FCFS order of activating jobs is relaxed [50, 80]. In this scheduler, known as "EASY", jobs are scheduled in a FCFS order to run at the earliest time that a sufficient number of processors are available for them. However, this can mean that smaller jobs may be executed before bigger jobs that arrived earlier, whenever they can do so without delaying the previously scheduled jobs. It was found that user satisfaction was greatly increased since smaller jobs tended to get through faster, because they could bypass the very big ones, yet the users still have the predictability of knowing just after submission when they can expect that their job will complete.

Henderson describes the Portable Batch System (PBS), another system in which performance gains are achieved by moving away from strict FCFS scheduling [36]. Wan et al. developed a scheduler

that uses a variation of a 2-D buddy system to do processor allocation for the Intel Paragon[91].

2.2.3 Thread-oriented scheduling

Nelson, Towsley, and Tantawi compared four cases in which parallel jobs were scheduled in either a *centralized* or *de-centralized* fashion, and the threads of a job were either spread across all processors or were all executed on one processor [58]. They found that best performance resulted from centralized scheduling and spreading the threads across processors. Among the other options, decentralized scheduling of split tasks beat centralized scheduling with no splitting under light load, but the reverse is true under heavy load.

2.2.4 Load-based scheduling

Because the efficiency of parallel jobs generally decreases as their processor allocation increases, it is necessary to decrease processor allocations to moldable jobs as the overall system load increases in order to avoid system saturation [78]. Zahorjan and McCann found that allocating processors to evolving jobs according to their dynamic needs led to much better performance than either run-to-completion with a rigid allocation or round-robin [96]. For the overhead parameters they chose, round-robin beat run-to-completion only at quite low system loads.

Ghosal et al. propose several processor allocation schemes based on the *processor working set* (PWS), which is the number of allocated processors for which the ratio of execution time to efficiency is minimized [30]. (The PWS differs from the average parallelism of the job by at most a factor of two [17].) The best of the variants of PWS gives jobs at most their processor working set, but under heavy load gives fewer and fewer processors to each job, thus increasing efficiency and therefore system capacity.

Setia, Squillante, and Tripathi use a queuing theoretic model to investigate how parallel processing overheads cause efficiency to decrease with larger processor allocations [75]. In a later study, they go on to show that dynamic partitioning of the system beats static partitioning at moderate and heavy loads [76]. Naik, Setia and Squillante show that dynamic partitioning allows much better performance than fixed partitioning, but that much of the difference in performance can be obtained by using knowledge of job characteristics, and assigning non-preemptive priori-

ties to certain job classes for admission to fixed partitions [57].

McCann and Zahorjan found that "efficiency-preserving" scheduling using folding allowed performance to remain much better than with equipartitioning (EQUI) as load increases [52]. Padhye and Dowdy compare the effectiveness of treating jobs as moldable to that of exploiting their malleability by folding [61]. They find that the former approach suffices unless jobs are irregular (i.e., evolving) in their pattern of resource consumption. Similarly, in the context of quantum-based allocation of processing intervals, Chiang et al. showed that static processor allocations (for which jobs need only be moldable) led to performance nearly as good as that obtained by dynamic processor allocation (which requires that jobs be malleable) [10].

2.2.5 Non-work-conserving scheduling

Downey has studied the problem of scheduling in an environment where moldable jobs are activated from an FCFS queue, and run to completion [13]. He suggests how to use predictions of the expected queuing time for awaiting the availability of different numbers of processors in order to decide when a particular job should be activated. The tradeoff is between starting a job sooner with fewer processors and delaying its start (causing processors to be left idle) until a larger number of processors is available. Algorithms that leave processors idle in anticipation of future arrivals were also investigated by Rosti et al. [70] and Smirni et al. [82].

2.2.6 Time-slicing and space-slicing scheduling

Many variations of scheduling algorithms based on time-slicing and space-slicing have been proposed and evaluated. Time-slicing is motivated by the high variability and imperfect knowledge of service times, while space-slicing is motivated by the goal of having processors used with high efficiency.

Gang scheduling is compared to local scheduling and is found to be superior by Feitelson and Rudolph [25]. Squillante et al. and Wang et al. have analyzed a variation of gang scheduling that involves providing service cyclically among a set of fixed partition configurations, each having a number of partitions equal to some power of two [86, 93]. They find that long jobs benefit substantially from this approach, but only at

the cost of longer response times for short jobs. Feitelson and Rudolph and Hori et al. analyze a more flexible policy in which there is time slicing among multiple active sets of partitions [24, 37].

Lee et al. have studied the interaction of gang scheduling and I/O, and found that many jobs may tolerate the perturbations caused by I/O [46]. Feitelson and Jette have demonstrated that the preemptions inherent in time-slicing allow the system to escape from bad processor allocation decisions, boosting utilization over space-slicing for rigid jobs, and avoiding the need for non-work conserving algorithms [21].

Several studies have revealed that EQUI does very well, even when some moderate charge for the overhead of frequent preemptions is made [87, 49]. Squillante has provided an analysis of the performance of dynamic partitioning [85]. Dussa et al. compared space-slicing against no partitioning, and found that space-partitioning pays off [15]. On the other hand, coscheduling is compared to local scheduling and is found to be superior by Dusseau, Arpaci, and Culler [16].

2.2.7 Knowledge-based scheduling

Majumdar, Eager and Bunt showed that, under high variability service time distributions, round-robin (RR) was far better than FCFS, but that policies based on knowledge of the processing requirement (such as least work first) were still better. Knowledge of the average parallelism of a job makes it possible to allocate each job an appropriate number of processors to make it operate at a near-optimal ratio of execution time to efficiency [17]. With the knowledge of how many processors each job uses, policies for packing the jobs into frames for gang scheduling are investigated by Feitelson [19]. Sobalvarro and Weihl describe a discipline in which processor pairs that communicate frequently are identified, and it is assured that the corresponding threads are all activated at the same time [84]. A similar scheme for shared memory was described by Feitelson and Rudolph [23].

Taking system load and minimum and maximum parallelism of each job into account as well, still higher throughputs can be sustained [78]. Chiang et al. show that use of knowledge of some job characteristics plus permission to use a single preemption per job allows run-to-completion policies to approach ideal (i.e., no overhead) EQUI [9], and Anastasiadis et al. show that, by setting the processor allocation

of moldable jobs based on some known job characteristics, disciplines with little or no preemption can do nearly as well as EQUI [3].

2.2.8 Other factors in scheduling

McCann and Zahorjan studied the scheduling problem where each job has a minimum processor allocation due to its memory requirement [53]. They find that a discipline based on allocation by a buddy system consistently does well. Alverson et al. describe the scheduling policy for the Tera MTA, which includes consideration of memory requirements [2]. Brecht has carried out an experimental evaluation of scheduling in systems where processors are identified with clusters or *pools*, and intracluster memory access is faster than intercluster access [6]. A surprising result is that *worst-fit* scheduling, where each job is allocated to the pool with the most available processors, beats *best-fit* scheduling, where jobs are placed where they come closest to filling out a pool. This is a result of using a model of evolving jobs, where it is best to leave these jobs space to grow. Yue describes the creation of evolving jobs by selecting (in the compiler) at the top of each loop what degree of parallelism should be used for that loop [95].

2.2.9 Experiments with parallel scheduling

Many of the results of the modeling studies described above have been corroborated by experimental studies in which various policies were implemented in real systems.

Gibbons has experimented with a number of scheduling disciplines for scheduling rigid jobs in a network of workstations environment. His conclusions include:

- Activating jobs in Least Expected Work First (LEWF) order rather than FCFS reduces the resulting average response time by factors from two to six in various circumstances.

- If service times are unknown or if only estimates are available, then "back-filling" (as in EASY) reduces average response times by a factor of two or more. (If service times are known exactly, then back-filling has less relative benefit.)

- Whether back-filling is used or not, knowledge of service times is very helpful (particularly if

preemption is supported). Having job knowledge and using it leads to response times that are a factor of three to six smaller than for the case of no knowledge. When the knowledge is restricted to class knowledge based on the a small database that records execution characteristics of jobs, the average response times are roughly half those with no knowledge.

- If some knowledge (class or job) is available, then preemption is much less valuable than in the case where no knowledge is available and bad decisions are made (which can only be corrected by preemption).

Parsons has experimented with a broader class of disciplines, most of which exploit moldable and malleable jobs. His positive observations include:

- If migratable preemption is supported at low cost, then very good performance can be achieved, even if no service time knowledge is available. (Also, malleability is not of much additional benefit.)

- If only local preemption is supported, then class knowledge of service times is needed in order to do well by using LEWF order for activation.

- When preemption is not supported, class knowledge and LEWF order are helpful (roughly halving average response times), but not as much as with local preemption supported.

- In (typical) environments where the distribution of service times has very high variance, LERWF does very well when some service time knowledge is available; otherwise, if malleability doesn't lead to excessive overhead, then a simple rule like EQUI does well.

Some additional observations on the negative side are:

- The value of local preemption is restricted by the fragmentation that occurs because jobs must be restarted on the same set of processors on which they previously ran. (In this case, either clever packing strategies or even fixed partitioning are beneficial, because the dependencies among jobs are then limited [26].)

- Even with moldable jobs, performance is poor unless preemption is supported, because if inappropriate allocations are occasionally made to

very long jobs, then only preemption can remedy the situation.

3 Recommendations and Future Directions

The current state-of-the-art regarding scheduling on large-scale parallel machines is to use simple and inflexible mechanisms. In essence, the number of processors used for each job is chosen by the user, some sufficiently large partition acquired, and the job is run to completion. A few recent systems support preemption, so that a parallel job can be interrupted and possibly swapped out of memory, but many installations choose not to use this option due to high associated overheads and lack of adequate I/O facilities.

3.1 Recommendations based on modeling studies

In this section, we present and justify five recommendations for how the current state-of-the-art can be improved through the use of some approaches and techniques that have been investigated in modeling studies that use either analysis or simulation.

After the modeling studies described in Section 2.2, as well as numerous others, a great deal has been learned about how "in theory" multiprogrammed multiprocessor scheduling should be done. As in many other fields of study, putting the theoretical results into practice in production environments raises numerous issues that must be resolved. However, based on an aggregation of the results from the modeling studies, the recommendations below emerge. (Note that all the suggested approaches have been demonstrated to be feasible through prototype implementations and experimentation.)

Recommendation 1: Provide system support for parallel job preemption and migration.

It has been seen that preemption is crucial to obtaining the best performance, and that local preemption alone does not suffice, due to the limitation of not being able to change the set of jobs on which to execute. Supporting the ability to change the number of processors assigned to a job is desirable to best handle evolving and malleable jobs, but the marginal gain in performance is not substantial. Hence it is justified

only if it can be provided with little additional effort (as a part of checkpointing procedures, for example).

Recommendation 2: Write applications to be at least moldable, and evolving, if it is natural to do so.

Since system loads vary with time, and users generally do not know when they submit a job what the load conditions will be at the time the job is activated, it is desirable that jobs be moldable rather than rigid, so that available processors can be fully exploited at light load, but still efficient use of processors can be assured at heavy load.

If jobs are naturally evolving (such as a cyclic fork join structure, with relatively long sequential periods), then writing the job as evolving (with annotations or commands to dynamically acquire and release processors) makes it possible to greatly increase the efficiency with which the job utilizes the processors assigned to it.

Writing jobs to be malleable is much more work, and this is typically justified only for applications that consume a significant portion of a system's capacity, because they are either very large or invoked very frequently.

Recommendation 3: Base processor allocations on both job characteristics and the current load on the system.

Jobs make more efficient use of their assigned processors when they have fewer than when they have more [17, 78]. Hence, as the workload volume increases, it is necessary to reduce the number of processors assigned on average to each job. At light load, processor availability is not an issue, so each job can be given as many processors as it can use, even if they are not being used at high efficiency. This leads to low average response times. At heavy load, the multiprocessing overhead merely detracts from the overall system capacity, so giving jobs a small number of processors (even one in the limit as long as memory requirements don't preclude this extreme possibility) is the most appropriate action. By doing this, the throughput capacity of the system can be maximized.

When specific processor allocations are selected by users, they tend to be overly aggressive or optimistic. The numbers selected by users are typically suitable for light load conditions, but they lead to unacceptably low processor efficiency at heavy load. Consider a case where there are N statistically identical jobs

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to run on P processors. Assuming the jobs are moldable, the scheduler has the options to either (1) run them one at a time with all P processors, or (2) run them in pairs with half the processors each. Both the mean and the variance of the response times are lower with the latter approach unless [77]:

$$S(P) > \left[2 - \frac{2}{N + 2} \right] \cdot S(P/2)$$

This condition seldom holds when either the number of processors or the number of jobs is moderately large.

Since users cannot practically know the load on the system at the time they submit a job, it is best if they identify a range of acceptable processor allocations, and then leave the choice within that range to the scheduler. The current workload volume can be taken into account either by just observing the occupancy of the queues in which jobs await initiation, or by tracking some prediction of overall load as it varies in daily or weekly cycles.

Recommendation 4: To improve average response times, move away from FCFS and run-to-completion scheduling, and instead schedule first jobs that are most likely to complete soon, using preemption when necessary.

In uniprocessor scheduling, it is known that RR scheduling protects against highly variable service time distributions by making average response time independent of the service time distribution (assuming preemption overhead is negligible). Further, if the service time distribution is know to have high variability, then feedback (FB) disciplines can exploit this, and yield lower average response times as the variability of the service time distribution grows [11].

When no knowledge of service times is available and malleability can be exploited, the ideal EQUI discipline, which attempts to assign an equal number of processors to each job available for execution is optimal. EQUI is analogous to RR in a uniprocessor context in its ability to schedule relatively well even with no service time knowledge. If malleability is impractical due to lack of system support or jobs aren't written to exploit it, then some form of preemptive scheduling based on time-slicing, such as gang-scheduling should be used [21, 92, 65].

In current practice, if queues for jobs with smaller execution times tend to have higher priority, then this is consistent with the idea of using available service time knowledge to favor the jobs that are expected to complete most promptly. If better knowledge of job service times than queue identities is available, then it is best to try to activate the jobs in order of increasing expected remaining service time [64]. If the service times are known to be highly variable, but the service times of individual jobs cannot be predicted in advance, then the discipline that executes the job with least acquired service first is best because it emulates the behavior of least expected remaining work first.

Recommendation 5: Make use of information about job characteristics that is either provided directly, or measured, or remembered.

Users already provide information about the execution characteristics of their jobs, in the encoded form of a queue identifier. User supplied estimates cannot be directly believed, but the information is generally positively correlated with truth, and that is sufficient to make better scheduling possible. (A good scheduling policy will penalize users who intentionally misestimate the characteristics of the jobs they submit.)

In addition to information available before the job is initiated, it has been demonstrated that it is feasible to measure some job characteristics (such as efficiency) while the job is executing [60]. Then, assuming the job is malleable, the system can take appropriate action with respect to giving additional processors, or taking some away from the job. Finally, if some historical information is retained, then observed behavior of previous jobs with certain characteristics can be used to predict (approximately) the behavior of new jobs with similar characteristics.

3.2 Future Directions

3.2.1 Future theoretical work

Algorithmic approaches and results from theoretical scheduling studies have influenced how scheduling is done in practice. However, the time delay for this influence to be felt has been relatively long.

Some recent work has been intended to bridge the gap between theory and practice. This work, ideally involving collaboration between theoreticians and practitioners, may prove fruitful for both sides. Such work may include some of the following aspects:

1. **Model Definition.** New abstract models can be defined based on real machines. These models may include such new aspects as:

   (a) different preemption penalty costs associated with local preemption and job migration,

   (b) a relation between execution time and allocated processors for moldable, evolving, and malleable jobs,

   (c) prevention of job starvation by guaranteeing a completion time for each job at the submission time of job,

   (d) pricing policies that are based on some combination of resource consumption by the job, and job characteristics that may or may not be known at the time the job is submitted,

   (e) cyclic load patterns that motivate delaying some large jobs to time periods of lower overall demand (e.g., "off hours").

2. **Workload Knowledge.** Recently, a large number of studies addressed the issue of workloads on commercial multiprocessors [22, 38, 18]. Although it may be difficult to integrate this type of knowledge into the theoretical analysis of algorithms directly, it should be possible to generate benchmarks for the evaluation of algorithms. This would allow a fair comparison among various scheduling algorithms and provide an alternative method to worst case analysis.

3. **Analysis of Heuristics.** The analytical methods provided by theoreticians should also be used for the evaluation of practical approaches. This may yield new knowledge about potential weaknesses of these heuristics.

3.2.2 Future practical work

Scheduling algorithms consistent with the recommendations in Section 3.1 have been developed and implemented in prototype form. The experimental results based on the prototype implementation indicate that preemption with migration can lead to substantially reduced average response times.

Relative to common current practice for parallel job scheduling, the analytic modeling work (backed up by some prototype implementations) indicates

the possibility of substantial improvements is several ways:

- Rather than using run-to-completion disciplines, preemption with migration can be very helpful, possibly in conjunction with malleability.

- Rather than FCFS activation of jobs, average response times can be reduced by instead activating first jobs that are expected to finish most quickly.

- Rather than having the user specify the number of processors on which the job should be executed, instead allow the system to bind the processor allocation at initiation time, taking into account the current load on the system.

As approaches to specify parallel job scheduling across a variety of systems begin to converge, it is very important that the process retain sufficient flexibility that these improvements in scheduling, that are apparent from the analytic studies and will be incorporated into practice in the next few years, can be accommodated and promoted.

4 The PSCHED Standard Proposal

Theoretical research like that described in Section 2 tends to focus on algorithmics and easily measurable metrics, while abstracting away from the details. System administrators, on the other hand, cannot abstract away from real-life concerns. They are also faced with unmeasurable costs and constraints, such as interoperability (will machines work together?) and software lifetime (how soon will parts of the system need to be replaced?). Moreover, achieving the maturity and stability required of production software is much harder than building a prototyope. Finally, they need to cater to users and administrators with many different needs, leading to the creation of rather elaborate systems [4, 45].

As a result of such concerns, there is much interest in standardizing various software components. In recent years, message passing libraries were standardized through the MPI effort. Similarly, the PSCHED proposal aims at standardizing the interactions among various components involved in parallel job scheduling.

4.1 Background

Deferred processing of work under the control of a scheduler has been a feature of most proprietary operating systems from the earliest days of multi-user systems in order to maximize utilization of the computer.

The arrival of the UNIX system proved to be a dilemma to many hardware providers and users because it did not include the sophisticated batch facilities offered by the proprietary systems. This omission was rectified in 1986 by NASA Ames Research Center who developed the Network Queuing System (NQS) as a portable Unix application that allows the routing and processing of batch "jobs" in a network. To encourage its usage, the product was later put into the public domain.

The supercomputing technical committee began as a "Birds Of a Feather" (BOF) at the January 1987 Usenix meeting. There was enough general interest to form a supercomputing attachment to the /usr/group working groups. The /usr/group working groups later turned into the IEEE POSIX standard effort.

Due to the strong hardware provider and customer acceptance of NQS, it was decided to use NQS as the basis for the POSIX Batch Environment amendment in 1987. Other batch systems considered at the time included CTSS, MDQS, and PROD. None were thought be have both the functionality and acceptability of NQS. This effort was finally approved as a formal standard on December 13, 1994 as IEEE POSIX 1003.2d. The standard committee decided to postpone addressing issues such as programmatic interface and resource control. The supercomputing working group has since been inactive.

PBS was developed at NASA Ames Research Center as a second generation batch queue system that conforms to the IEEE Std. 1003.2d-1994. The project started in June 1993, and was first released in June 1994 [36].

However, both NQS and PBS were designed to schedule serial jobs, and have no understanding of the needs of parallel jobs. The only support for parallelism is regarding "processors" as another resource during allocation, on the same standing as time, memory, or software licenses. To run efficiently, all parts of a parallel job needed to be scheduled to run at the same time. Without support from the batch queue system, most of the large installation of MPP systems had reverted to space slicing and an "all jobs run to completion" policy.

4.2 Outline of Psched

The idea of creating a metacenter is the force behind the PSCHED project at NASA Ames Research Center. A metacenter is a computing resource where jobs can be scheduled and run on a variety of machines physically located in different facilities [35]. This concept ran into several road blocks:

- Some schedulers are tightly integrated with the message passing library: Condor and PVM.

- Almost all schedulers are tightly integrated with the batch queue system.

- Lack of support for parallel jobs.

The Numerical Aerospace Simulation facility (NAS), as part of a Cooperative Research Agreement involving several NASA centers, IBM, Pratt and Whitney, Platform Computing and others, has formed an informal group with the goal of developing a set of "standard" API calls relating to job and resource management systems. The goal of the PSCHED API is to allow a site to write a scheduler that could schedule a variety of parallel jobs: MPI-2, PVM, and SMP multi-tasking jobs to run on a collection of different machines.

To achieve this goal, we intend to standardize the interfaces between the different modules: message passing libraries, task manager, resource manager, and scheduler (see Fig. 2). The specific roles of these components are

Task Manager: An entity that provides task management services such as: spawn a task on a node, local or remote; deliver a signal from one task to another task within the same parallel application; and interface with a resource management function to provide information about nodes assigned to the set of tasks which make up a parallel application, to obtain additional resources (nodes), to free resources (nodes) no longer required, and to notify tasks of the need to checkpoint, suspend, and/or migrate.

Resource Manager: An entity that provides resource management services such as: monitor the resources available in the system, reserve or allocate resources for tasks, and release or deallocate resources no longer needed by tasks.

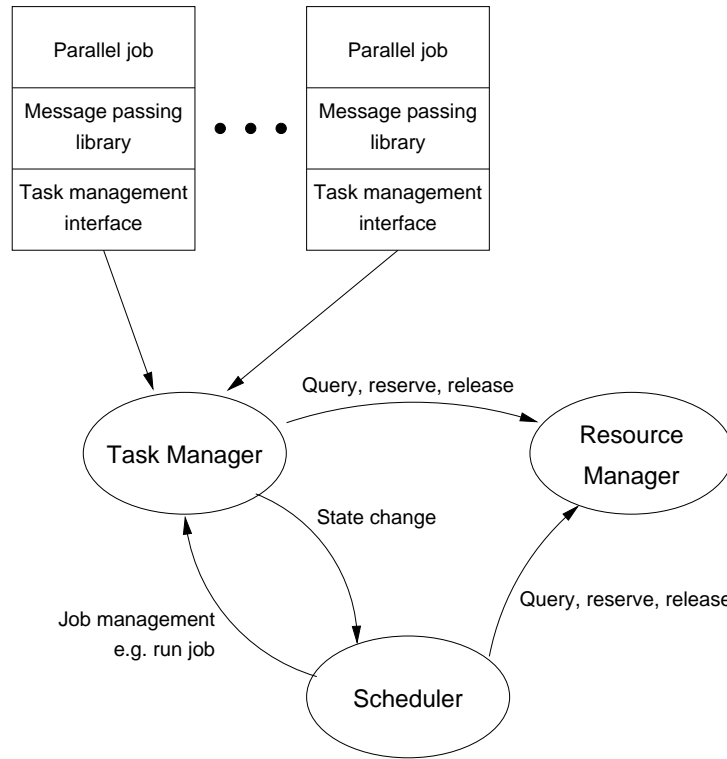**Scheduler:** An entity that schedules jobs. The scheduler is responsible for determining which

Figure 2: *Components of the PSCHED environment.*

task should be run on the system according to some site specific policy and the resources available in the system.

The PSCHED API is not an effort to standardize how any of these modules should be implemented. It is an effort to identify the minimal functionality needed from each module and then standardize its interface. For example, the scheduler is a user of the interfaces provided by the task manager and the resource manager. The scheduler waits for scheduling events from the task manager.

The PSCHED API is divided into two areas:

- A set of calls for use by parallel processing jobs to spawn, control, monitor, and signal tasks under the control or management of the job/resource management system. This set of calls should meet the needs of MPI-II, PVM, and other message passing implementations.

- A set of calls to be used by batch job schedulers. These calls will allow the development of consistent job/resource schedulers independent of

the job/resource management system used. The calls are intended to provide a standard means of obtaining information about the resources available in the processing environment and about the supply of jobs and their requirements.

Let us take a look at an example of how a parallel job would spawn a sub-task, adding more nodes to the running job. The job will call the message passing library, for example `MPI_Spawn` in MPI-II. The message passing library will interface with the task manager to spawn the new task to add more nodes to the existing task. The task manager will inform the scheduler of the request. The scheduler will make a decision based on its scheduling policy. If the policy allows the job to expand, the scheduler will request additional resources from the resource manager, then inform the task manager to start the new sub-task and allow the job to proceed.

4.3 Implication on the Programming and Scheduling of Parallel Jobs

Obvious benefits of a standard like PSCHED include:

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```
main()
{
    tm_handle handle[3];

    /* connect to 3 different machines */
    tm_connect(server_1, NULL, &handle[0]);
    tm_connect(server_2, NULL, &handle[1]);
    tm_connect(server_3, NULL, &handle[2]);

    while (1) {
        /* wait for events from any of the servers */
        tm_get_event(handle, 3, &which_handle, &event, &job_id, &args);
        ack = process_event(handle[which_handle], event, job_id, args);
        /* acknowledge the event */
        tm_ack_event(handle[which_handle], event, job_id, ack);
    }
}

process_event(handle, tm_event, job_id, ...)
{
    switch (tm_event) {
        PSCHED_EVENT_JOB_ARRIVED:
            /* call policy routine */
            scheduler_policy(job_id, &run_this_job, resource_needed);
            /* if decided to run job, reserve the resource
             * and run job */
            if (run_this_job) {
                rm_reserve(resource_list, &resource);
                tm_run_job(handle, job_id, resource);
            }
            break;
        PSCHED_EVENT_JOB_EXITED:
            /* release the reource*/
            if (resource != PSCHED_RESOURCE_NULL)
                rm_release(resource);
            /* pick a new job to run */
            break;
        PSCHED_EVENT_YIELD:
            /* job is ready to yield some resource, determine
             * whether we want to shrink or expand the job.
             * call the task manager if any action is taken. */
            break;
        PSCHED_EVENT_CHECKPOINT:
            /* a good time to migrate the job if we wanted to */
            break;
        PSCHED_EVENT_REQUEUED:
            /* pick a new job to run */
            break;
```

Figure 3: *Example skeleton of PSCHED code components.*

```
    PSCHED_EVENT_ADD_RESOURCE:
        /* run policy routines */
        scheduler_policy(job_id, &run_this_job, additional_resource);
        if (run_this_job) {
                rm_reserve(resource_list, &resource);
                tm_add_resource(handle, job_id, resource);
        } else {
                /* tell server we can't fulfill the request
                 * or suspend the run and wait for the resource */
        }
        break;
    PSCHED_EVENT_RELEASE_RESOURCE:
        rm_release(rm_handle, resource);
        break;
    default:
        return UNKNOWN_EVENT;
    }
    return SUCCESS;
}

scheduler_policy(...)
{
    /* this is what the scheduler writters will concentrate on */
}
```

Figure 3: **(cont.)**

- real traces can be used in simulations to develop better algorithms

- new algorithms could be directly applied to running systems

- modularity of very complex pieces of software allows a mix and match of:

  - batch / task management system
  - scheduler
  - communication library (e.g., MPI, PVM)
  - scheduling simulators

The PSCHED API will be flexible enough to address some of the problems identified in Section 3 such as shrinking and expanding jobs, checkpointing and migrating jobs.

Hopefully this set of "standard" interfaces will free researchers from the need to port their work to different systems and let them concentrate on innovative scheduling algorithm and scheduler design. This will also make production machines more readily available for researchers. An example of such a scheduler is given in Fig. 3. Once written it should be very easily ported to another environment. The tm_ and rm_ calls are interfaces to the task manager and the resource manager respectively.

Areas that need standardization but are not currently addressed by PSCHED include:

- Moving jobs from one batch queue system to another.

- The accounting information kept by the batch queue system.

5   Discussion and Conclusions

The relationship between theory and practice is an interesting one. Sometimes theory is ahead of practice, and suggests novel approaches and solutions that greatly enhance the state of the art. Sometimes theory straggles behind, and only provides belated justification for well known practices. It is not yet

clear what role it will play in the field of parallel job scheduling.

The question of how much theory contributes to practice also depends on the metrics used to measure performance and quality. In the field of job scheduling, the three most common metrics are throughput, utilization, and response time. Throughput and utilization are actually related to each other: if we assume that the statistics of the workload are essentially static, then executing more jobs per unit time on average also leads to a higher utilization. This can go on until the system saturates. If users are satisfied with the system, and the system does not saturate, more jobs will be submitted, leading to higher utilization and throughput. The role of the scheduler is therefore to delay the onset of saturation, by reducing fragmentation and assuring efficient usage of processors [26]. Also, good support for batch jobs can move some of the load to off hours, further increasing the overall utilization.

In practice utilization is a very commonly used metric, as it is easy to measure and reflects directly on the degree to which large investments in parallel hardware are used efficiently. Throughput figures are hardly ever used. Reported utilization figures vary from 50% for the NASA Ames iPSC/860 hypercube [22], through around 70% for the CTC SP2 [38], 74% for the SDSC Paragon [91] and 80% for the Touchstone Delta [55], up to more than 90% for the LLNL Cray T3D [21]. Utilization figures in the 80–90% range are now becoming more common, due to the use of more elaborate batch queueing mechanisms [50, 80, 91] and gang scheduling [21]. These figures seem to leave only little room for improvement.

However, it should be noted that these figures only reflect one factor contributing to utilization. The real utilization of the hardware is the product of two factors: the fraction of PEs allocated to users, and the efficiency with which these PEs are used. The figures above relate to the first factor, and depend directly on the scheduling policies; they show that current systems can allocate nearly all the resources, with little loss to fragmentation. But the efficiency with which the allocated resources are used depends more on the application being run, and can be quite low. However, the system can still have an effect, because in most applications the efficiency trails off as processors are added. Thus allocating less processors under high loads should improve the second factor, and lead to higher overall utilization [44, 69, 52]. This is pos-

sible with moldable or malleable jobs, but not with rigid ones.

The case of the response time metric is more complex, because little direct evidence exists. Theory suggests that preemption be used to ensure good response times for small jobs [65], especially since workloads have a high variability in computational requirements [22]. This comes close on the heels of actual systems that implement gang scheduling for just this reason [47, 33, 28, 21].

Actually two metrics may be used to gauge the responsiveness of a system: the actual response time (or turnaround time, i.e. the time from submittal to termination), or the slowdown (the ratio of the response time on a loaded system to the response time on a dedicated system). Using actual response times places more weight on long jobs, and "doesn't care" if a short job waits a few minutes, so it may not reflect the users' notion of responsiveness. Slowdown reflects the rather reasonable notion that responsiveness should be measured against requirements, meaning that users should expect their jobs to take time that is proportional to the computation performed. However, for very short jobs, the denominator becomes very small, leading to a large slowdown, even though the actual response time may be quite short, well within the interactive range. It may therefore be best to combine the two metrics. Let T represent the response time on the loaded system, T_d the response time on a dedicated system, and T_h the threshold of interactivity (i.e. the time users are willing to wait). The combined metric for responsiveness as percieved by users would then be

$$ R = \begin{cases} T/T_d & \text{if } T_d > T_h \\ T/T_h & \text{if } T_d < T_h \end{cases} $$

For long jobs, this is the normal slowdown. For short jobs, this is the slowdown *relative to the interactivity threshold*, rather than relative to the very short runtime on a dedicated system. If we use T_h as the unit of time, then for short jobs the expression degenerates to the response time. We suggest the name "bounded slowdown" for this metric, as it is similar to the slowdown metric, but bounded away from high values for very short jobs.

Two possible roles for theory, that have relatively few parallels in practice, are how to use knowledge about specific jobs [77], and how to tune algorithmic parameters [92]. In practice, knowledge about jobs is limited to that supplied by the users, typically in

the form of choosing a queue with a certain combination of resource limits. This approach has two main drawbacks: first, it leads to a combinatorical explosion of queues, that are hard to deal with. Second, even with very many queues, the resolution in which requirements are expressed is necessarily very coarse, and user estimates are notoriously inaccurate anyway. Recent more theoretical work shows how data can be acquired automatically by the system, rather than relying on the users [60, 32, 13].

At the same time that theoretical work is focusing, at least to some degree, on practical concerns, practice in the field seems to be rather oblivious of this development. One reason is that the larger and more advanced installations have been developing rather elaborate scheduling facilities, which achieve reasonable results, so the pressure for searching for additional improvements outside is diminished. Another reason is the overwhelming concern for backwards compatability, portability, and interoperability, which leads to standards based on common practices and discourages innovations. It should be hoped, however, that the developed standards will be flexible enough to allow unanticipated advances to be incorporated in the future.

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