

Correlations of droplet formation in T-junction microfluidic devices: from squeezing to dripping

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Abstract In this work, we have systematically analyzed the scaling law of droplet formation by cross-flow shear method in T-junction microfluidic devices. The droplet formation mechanisms can be distinguished by the capillary number for the continuous phase (Ca_c), which are the squeezing regime ($Ca_c < 0.002$), dripping regime ($0.01 < Ca_c < 0.3$), and the transient regime ($0.002 < Ca_c < 0.01$). Three corresponding correlations have been suggested in the different range of Ca_c . In the dripping regime, we developed a modified capillary number for the continuous phase (Ca'_c) by considering the influence of growing droplet size on the continuous phase flow rate. And the modified model could predict droplet diameter more accurately. In the squeezing regime, the final plug length was contributed by the growth and ‘squeeze’ stages based on the observation of dynamic break-up process. In the transient regime, we firstly suggested a mathematical model by considering the influences of the above two mechanisms. The correlations should be very useful for the application of controlling droplet size in T-junction microfluidic devices.

Keywords Scaling law · Monodispersed droplet · Cross-flow shear method · Microfluidic device

1 Introduction

The development of microfluidic systems which allow for the formation of microdrops inside microfluidic devices has received significant attention over the past 10 years (Kobayashi et al. 2001; Sugiura et al. 2004; Cristini and Tan 2004; Thorsen et al. 2001; Xu and Nakajima 2004; Garstecki et al. 2006; Anna et al. 2003; Xu et al. 2006a, b, c). Monodispersed droplets have been generated via a number of methods in microfluidic devices, including geometry-dominated break-up (Kobayashi et al. 2001; Sugiura et al. 2004), cross-flow shear in T-junction microchannel (Thorsen et al. 2001; Xu et al. 2006a, b, c; Garstecki et al. 2006; Cristini and Tan 2004; Husny and Cooper-White 2006), and hydrodynamic flow focusing (Anna et al. 2003; Xu and Nakajima 2004; Zhou et al. 2006). These methods enable formation of dispersions with highly attractive features, particularly the control over the size and narrow distribution of the sizes of individual droplets. With the rapid development of droplet formation techniques in microfluidic devices, several applications for the microfluidic chemical processing based on droplets have been demonstrated, including production of monodispersed microparticles (Nisisako et al. 2004; Xu et al. 2005; Utada et al. 2005; Gong et al. 2007), enhancement of mixing (Song et al. 2003; Cygan et al. 2005), crystallization of proteins (Zheng et al. 2004), synthesis of nanoparticles (Takagi et al. 2004; Yanagishita et al. 2004), and microchemical analysis (Kumemura and Korenaga 2006; Sun et al. 2006).

One of the most frequently used microfluidic geometries to produce monodispersed droplet is a T-junction by using the cross-flow shear method. The cross-flow shear method utilizes shear force, imposed by an immiscible cross-flow fluid at a T-junction, to generate droplets (drops or plugs),

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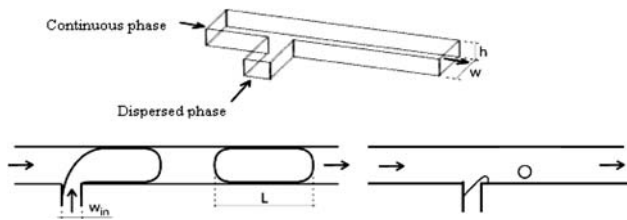


Fig. 1 A schematic illustration of the T-junction microfluidic device (Garstecki et al. 2006)

as shown in Fig. 1. The droplets generated with this method are highly monodispersed with an equal spacing between drops. A lot of work upon droplet formation by cross-flow shear method has been carried out, and the effects of the operational conditions were investigated with different kinds of geometries and working systems. Thorsen et al. (2001) firstly considered droplet formation within a T-junction microchannel. They found that the droplet size decreased with the increase of continuous phase flow rate and continuous phase viscosity in drops flow. They presented a model to predict the droplet size by using the forces balance analyzing of the interfacial force to the viscous force imposed by the continuous phase fluid. Nisisako et al. (2002) and Cristini and Tan (2004) gained similar results in drops flow. While in plugs, flow at low values of capillary number for the continuous phase (herein, $Ca_c = \frac{\mu_c u_c}{\gamma}$, where u_c is the mean flow velocities of the continuous phases, γ the interfacial tension, and μ_c the continuous phases viscosity), the scaling of droplet size was much different. Several groups (Tice et al. 2003; Garstecki et al. 2006; Menech et al. 2008) focused on the scaling law of droplet formation at low values of Ca_c ($Ca_c < 10^{-2}$). They observed experimentally and in numerical simulations (Garstecki et al. 2006; Menech et al. 2008) there was a critical value of capillary number ($Ca_{CR} \sim 10^{-2}$), which distinguished the mechanisms of break-up and the flow regimes of drops flow and plugs flow. When $Ca_c < 10^{-2}$, the interfacial force dominated the cross-flow shear force caused by the continuous phase fluid, and the break-up was determined by the pressure drop across the plug as it formed; when $Ca_c > 10^{-2}$, the cross-flow shear force started to play an important role in the process of break-up, and two-phase flow was in drops flow regime. Then, a quantitative model for the size of plug was suggested by Garstecki et al. (2006) on the basis of dynamic observation and analysis when $Ca_c < 10^{-2}$. The model agreed well with the experimental data in the plugs flow regime. While in the drops flow regime, it was found that (Menech et al. 2008) the droplet formation is strongly affected by the geometry confinement, and the model suggested by Thorsen et al. (2001) is not accurate.

In our previous work (Xu et al. 2006a, b, c), the influences of two-phase flow rate, continuous phase viscosity,

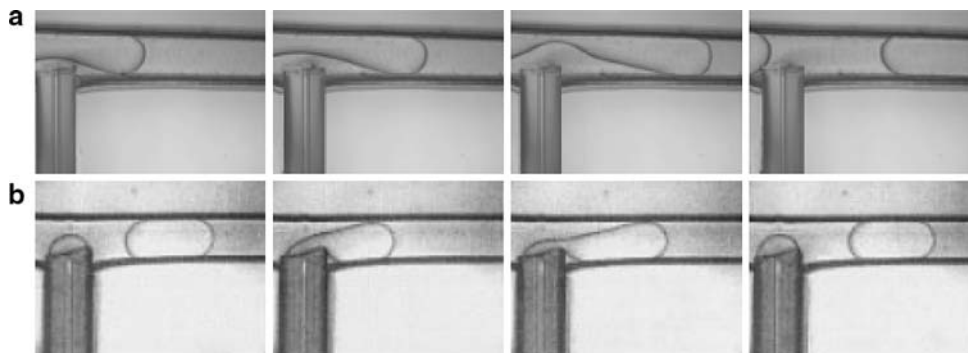
and interfacial tension on droplet size were systematically investigated in a T-junction microfluidic device. We also found the different scaling law under different flow patterns. Additionally, the effects of experimental conditions on droplet size in the transient regime were different to that of both the drops flow and plugs flow. So the mechanism of break-up in the transient regime was different.

From the previous review of droplet formation by using cross-flow shear method in T-junction microdevices, the mechanisms of break-up are different in the different regimes. In the squeezing regime, the model suggested by Garstecki et al. (2006) agrees well with the experimental data. In the dripping regime, the model using the forces balance analyzed by Thorsen et al. (2001) and Cristini and Tan (2004) cannot predict the droplet size accurately, and the model should be modified. While in the transient regime, the quantitative model has not been reported yet. So the in-depth understanding of mechanisms of droplet formation in T-junction microchannels is still lacking. In this paper, we attempt to systematically discuss and analyze the scaling of droplet size in different regimes based on our previous experimental work (Xu et al. 2006a, b, c). Firstly, the different two-phase flow patterns (drops flow, plugs flow, and the transient regime) were divided by the capillary number for the continuous phase Ca_c . Then, the corresponding quantitative models were developed based on the analysis of scaling of droplet formation under different range of Ca_c . Finally, we summarized our observations in conclusions.

2 Two-phase flow patterns under different range of Ca_c

From the previous work (Cristini and Tan 2004; Garstecki et al. 2006; Menech et al. 2008), capillary number for the continuous phase is an important parameter to distinguish two-phase flow patterns and the mechanisms of break-up in T-junction microdevices. So we can divide the two-phase flow patterns by Ca_c and discuss the mechanisms of droplet formation in different flow regimes. Herein, we use the experimental data of our previous work (Xu et al. 2006a, b, c). The microdevice in this case has an embedded capillary with a diameter of 40 μm perpendicular to the main channel with 200 μm wide \times 150 μm high, which is somewhat different from typical T-junction devices. And we used the embedded capillary as the dispersed fluid channel and continuous fluid channel separately. Figure 2 gives the micrographs of typical droplet formation process. In the experiments, the typical value of two-phase velocity was in the range of 0.001–0.1 m/s, μ_c was in the range of 0.68–10.84 mPa s, and γ in the range of 1.6–3.6 m N/m. So the range of Ca_c was mainly from 10^{-4} to 0.3. It can be seen from Fig. 3 that there are three typical flow regimes

Fig. 2 The micrographs of typical droplet formation process. **a** The capillary was used for supplying the continuous fluid (Xu et al. 2006a, b, c). **b** The capillary was used for supplying the dispersed fluid (Xu et al. 2006a, b, c)



under different values of Ca_c : plugs flow ($l > 2w$, where l is the length of dispersed droplet and w is the width of the channel), drops flow ($l < w$) and the transient regime ($w < l < 2w$). (1) When $10^{-4} < Ca_c < 0.002$, the cross-flow shear force caused by the continuous phase fluid is much lower comparing to the interfacial force and cannot rupture the dispersed phase to drops. So the two-phase flow is in plugs flow regime. In this regime, the interfacial force dominates the shear force, and the dynamics of break-up is dominated by the pressure drop across the plug as it forms, which we call the squeezing regime. (2) When $0.01 < Ca_c < 0.3$, the cross-flow shear force is large enough to play an important role in the process of break-up, and the two-phase flow is in drops flow regime. In this regime, the dynamics of break-up is dominated by the forces balance between shear force and interfacial force, which we call the dripping regime. (3) When $0.002 < Ca_c < 0.01$, the

two-phase flow is in the transient regime. In this regime, the dynamics of break-up is dominated by both the earlier two mechanisms. In the following section, we will discuss the scaling of droplet formation under the different range of Ca_c and draw the corresponding models separately.

3 Driving forces of droplet formation and correlations in different regimes

From the earlier mentioned analysis, there are three regimes that distinguish the mechanisms of droplet formation under the different range of Ca_c .

When $0.01 < Ca_c < 0.3$, the two-phase flow is in the dripping regime. In this regime, the dynamics of break-up is dominated by the forces balance between the shear force and interfacial force

In the previous work (Thorsen et al. 2001; Cristini and Tan 2004), Ca_c was used to represent the balance of cross-flow shear force and Laplace pressure caused by the interfacial tension. So the drops diameter could be described by the equation

$$d_d/d_i \sim 1/Ca_c, \tag{1}$$

where d_i means the cross-section dimension of the microchannel. From Eq. 1 the droplet diameter decreases with the increase of Q_w and continuous phase viscosity μ_c , which is in agreement with the experimental results. Figure 4 shows the comparison between the predicted values and experimental data (Xu et al. 2006a, b, c) under the drops flow patterns. When $Ca_c > 0.2$, they are in good agreement. While $0.01 < Ca_c < 0.2$, the predicted values are rather larger than the experimental results. The main reason for the difference is the influence of droplet size on the continuous phase velocity across the forming droplet when the droplet size is equivalent to the microchannel dimensions. So we modify the capillary number for the continuous phase by considering the effect of droplet size. For a rectangular microchannel with the width w and the height h , the cross-sectional area of a droplet with diameter

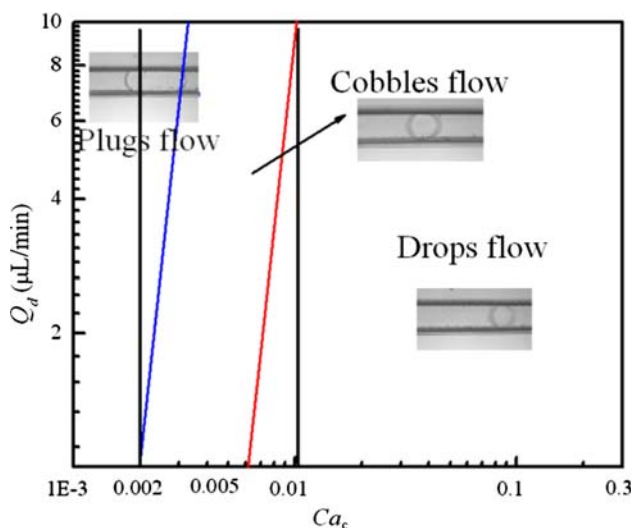


Fig. 3 Two-phase flow patterns under different values of capillary number for the continuous phase Ca_c (Xu et al. 2006a, b, c). The two oblique lines to the abscissa are the boundaries between the plugs, cobbles and drops flow. The two vertical lines are the boundaries between the squeezing, transient and dripping regimes

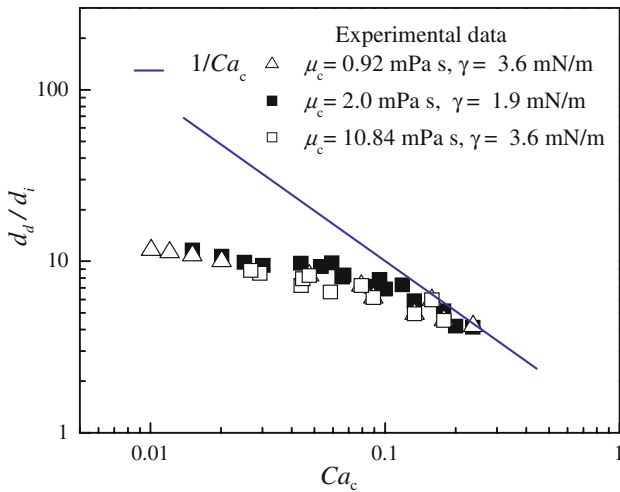


Fig. 4 Comparison of droplet diameter between the predicted values from Eq. 1 and the experimental data from our previous work (Xu et al. 2006a, b, c)

d_d is equal to $\frac{\pi}{4}d_d^2 \approx 0.785d_d^2$, so the modified continuous phase velocity is approximately equal to

$$u'_c = u_c \frac{wh}{wh - 0.785d_d^2} \tag{2}$$

where d_d is the diameter of the droplet, u_c is the average velocity of continuous phase in the channel, $u = Q_c/wh$. So the modified capillary number for the continuous phase Ca'_c is

$$Ca'_c = \frac{\mu_c u'_c}{\gamma} = Ca_c \cdot \frac{wh}{wh - 0.785d_d^2} \tag{3}$$

From Eqs. (1) and (3),

$$\frac{d_d}{d_i} \approx \frac{1}{Ca'_c} = \frac{1}{Ca_c} \cdot \frac{wh - 0.785d_d^2}{wh} \tag{4}$$

Equation 4 is the modified model for the droplet size in drops flow when $Ca > 0.01$. To verify the modified model, we gained the calculated values of droplet diameter from Eq. 4. Figure 5 shows the comparison of droplet diameter between the predicted values and experimental data in the references (Xu et al. 2006a, b, c; Husny and Cooper-White 2006). It can be seen that the modified model predicts the size well for a wide range of Ca'_c from 0.06 to 0.8 (the value of Ca_c is from 0.01 to 0.75 correspondingly). For larger values of Ca_c (when $Ca_c > 1$), the difference between Ca_c and Ca'_c is rather small. So Eq. 4 can be simplified to Eq. 1, which predicted the droplet size very well (Cristini and Tan 2004). From these results, it is necessary to consider the influence of droplet size on cross-flow shear force under the dripping regime, especially when the droplet size is equivalent to the microchannel dimensions.

When $10^{-4} < Ca_c < 0.002$, the two-phase flow is in the squeezing regime. In this regime, the dynamics of break-up

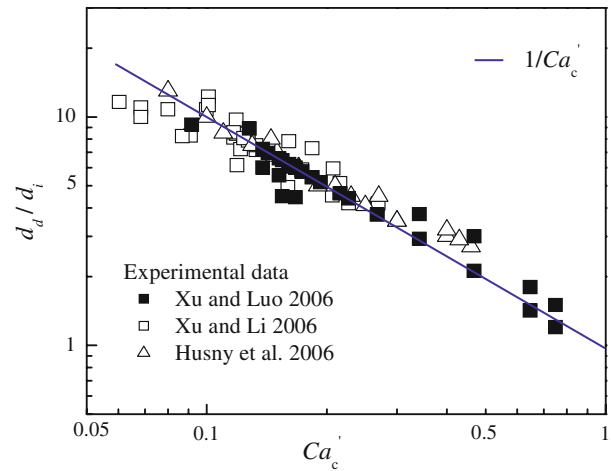


Fig. 5 Comparison of droplet diameter between the predicted values from Eq. 4 and the experimental data from the references. The microdevice in this case has an embedded capillary with diameter of 40 μm for supplying a continuous fluid perpendicular to the main channel (dispersed fluid channel) with 200 μm wide \times 150 μm high (filled square). The same T-junction microdevices was used, while the main channel was used as the continuous fluid channel and the embedded capillary was used as the dispersed fluid channel (open square). A rectangular T-junction microdevice was used in this case. The dimensions of the width in this case were 27.5 and 275 μm for the dispersed phase and the continuous phase, respectively, and the depth was 100 μm (open triangle)

is dominated by the pressure drop across the plug as it forms.

On the basis of dynamic observation of break-up process, Garstecki et al. (2006) identified the final length of a plug is contributed by two steps, as shown in Fig. 6. First the tip of the dispersed phase enters and blocks the main channel. At this moment the ‘growth length’ of the plug is equal to: $L_1 = \epsilon w$, herein ϵ is a parameter dependent on the geometry of the channel, usually equal to 1. Then the increased pressure in the continuous phase fluid starts to ‘squeeze’ the neck of dispersed thread. The thickness of the neck (of characteristic width d) decreases at a rate which is approximately equal to the mean speed of the continuous

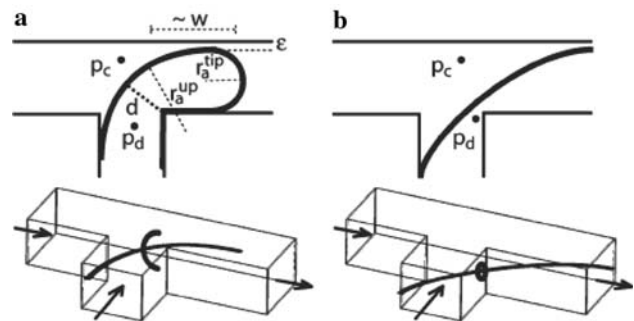


Fig. 6 A schematic illustration of the break-up process of a plug at the junction of the microchannels. a the growing stage, b the squeeze stage. (Garstecki et al. 2006)

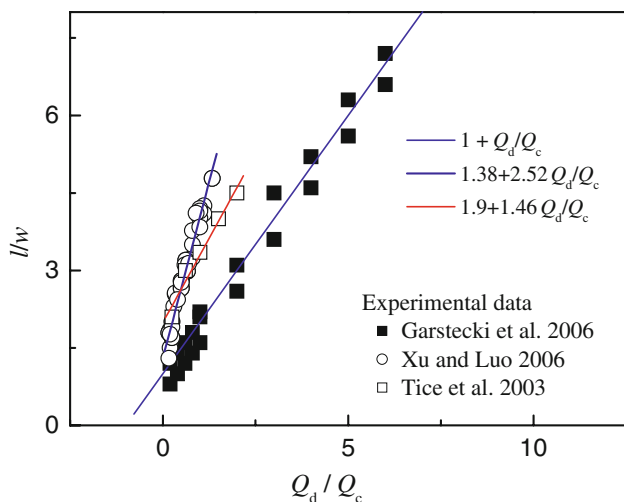


Fig. 7 Comparison of plug length between the fitting results from Eq. 5 and the experimental data from the references. A rectangular T-junction microdevice was used in this case (*filled square*). The dimensions of the width in this case were 50 and 100 μm for the dispersed phase and the continuous phase respectively. The depth was 33 μm . The microdevice in this case has an embedded capillary with diameter of 40 μm for supplying a continuous fluid perpendicular to the main channel (dispersed fluid channel) with 200 μm wide \times 150 μm high (*open circle*). A rectangular T-junction microdevice was used in this case (*open square*). The dimensions of the width were both 50 μm for the dispersed phase and the continuous phase

fluid: $u_c = Q_c/hw$. During this process the plug elongates at rate $u_d = Q_d/hw$. So the ‘squeeze length’ of the plug is $L_2 \approx d/u_c \cdot u_d = d \cdot Q_d/Q_c$. The final length of the plug is therefore equal to $L = L_1 + L_2 = \varepsilon \cdot w + d \cdot Q_d/Q_c$. It is convenient to non-dimensionalize this equation to

$$l/w - \varepsilon = \omega \cdot Q_d/Q_c, \tag{5}$$

where ε and ω are the fitting parameters. The values of ε and ω are mainly affected by the different geometries. We used Eq. 5 to fit the experimental data in the references (Tice et al. 2003; Xu et al. 2006a, b, c; Garstecki et al. 2006). Figure 7 gives the different scaling under the different geometries that have been reported. From these results, the model suggested by Garstecki et al. (2006) can accurately predict the droplet size in the squeezing regime.

When $0.002 < Ca_c < 0.01$, the two-phase flow is in the transient regime. In this regime, the dynamics of break-up is dominated by both of the mechanisms.

The model describing the scaling of droplet size in this regime has not been reported yet. Considering the two types of influences on the plug length, one is the dynamic break-up of the interface, which could be effected by the two-phase flow ratio Q_d/Q_c mostly; the other is the equilibrium between shear force of the continuous flow and interfacial force, which could be affected by capillary number for the continuous phase Ca_c mostly. We assume the plug length can be predicted as

$$l/w - \varepsilon = k(Q_d/Q_c)^\alpha \left(\frac{1}{Ca_c}\right)^\beta \tag{6}$$

Herein, α and β represent the ratio of the earlier two mechanisms, respectively. There are almost no experiments that discussed the scaling law of plugs size in this regime, except for our previous studies (Xu et al. 2006a, b, c; Tan et al. 2008). So we used Eq. 6 to fit the experimental data in our previous work. The resulted equations are

$$l/w = 0.75 \left(\frac{Q_d}{Q_c}\right)^{1/3} \left(\frac{1}{Ca_c}\right)^{1/5} \tag{7}$$

$$l/w = 1.59 \left(\frac{Q_d}{Q_c}\right)^{1/5} \left(\frac{1}{Ca_c}\right)^{1/5} \tag{8}$$

The calculated results from Eqs. (7) and (8) appear to provide a good fit across the whole range of data, as shown in Fig. 8. The differences of exponent between Eqs. (7) and (8) are mainly caused by the different geometries (we used the T-junction and cross-junction geometries separately). From these results, Eq. 6 is relatively accurate in predicting the droplet size in the transient regime.

From the earlier discussion, the break-up of drops/plugs in T-junction microdevices is mainly caused by two different mechanisms: the dynamic break-up of the interface and the equilibrium between cross-flow shear force and interfacial force. There are three regimes which distinguish the mechanisms of droplet formation under the different range of Ca_c . In these regimes, the difference of scaling law is due to the different ratio of the earlier mentioned mechanisms that affect the break-up process. It also shows that the differences of geometries, wetting properties and working systems would cause the different values of parameters in Eqs. (5) and (6). So the models has some limitation, which should be modified for more generality in the forms and the exponents by considering the effects of geometries and the wetting properties in the further work, especially in the transition regime.

4 Conclusions

In this paper, we have systematically analyzed the scaling law of droplet formation by cross-flow shear method in T-junction microfluidic devices. Capillary number for the continuous phase (Ca_c) is an important parameter to distinguish two-phase flow patterns and the mechanisms of break-up. So we divided the two-phase flow patterns by Ca_c and discussed the correlations of droplet formation in three typical regimes: the dripping, squeezing and transient regimes separately. In the dripping regime, the dynamics of break-up was dominated by the balance between shear force and interfacial force. By considering the influence of

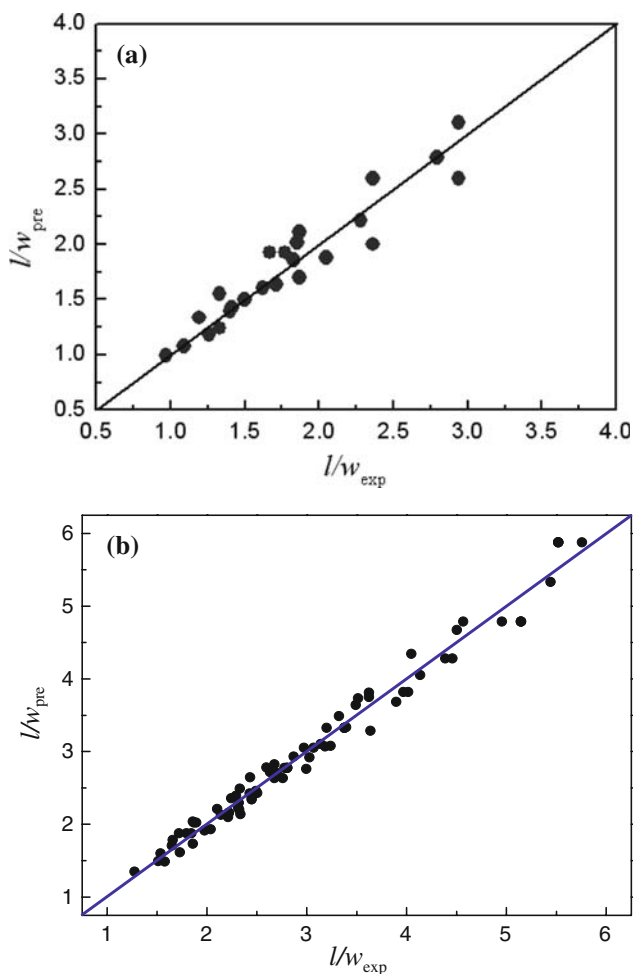


Fig. 8 Comparison of plug length between the fitting results from Eq. 6 and the experimental data from our previous experiments. **a** The T-junction microdevice (Xu et al. 2006a, b, c). **b** The cross-junction microdevice (Tan et al. 2008)

the droplet size on the continuous phase flow rate, we developed a modified parameter of capillary number (Ca_c') by using the local continuous phase flow rate at the droplet formation site. And the modified model could predict droplet diameter more accurately. In the squeezing regime, the dynamics of break-up was dominated by the pressure drop across the plug as it formed. According to the previous work (Garstecki et al. 2006), a mathematical model was suggested to predict the plug length. And the calculated values were in good agreement with the experimental data. In the transient regime, the dynamics of break-up was dominated by the two mechanisms mentioned earlier. Considering the two types of influences on the plug length, we firstly suggested a mathematical model which could predict the plug length accurately. The correlations presented in this work should be useful for in-depth understanding of the mechanisms of break-up by cross-flow shear method and the precise preparation of monodispersed droplets in T-junction microfluidic devices.

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