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A USER/PROGRAMMER GUIDE FOR THE MICRO-MODELING OF MASONRY STRUCTURES

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Summary

This report details the micro-model for masonry structures to be available in version 7.1 of the DIANA finite element program. The use of the model is discussed and the new syntax is presented. Comprehensive examples, which include the phases of mesh generation, nonlinear analysis and interpretation of the results, are also given. Finally, all the expressions utilized in the computational code are included for future reference and maintenance.

Acknowledgments

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The calculations have been carried out with the Finite Element Package DIANA of TNO Building and Construction Research on a Silicon Graphics Indigo R4000 workstation of the Delft University of Technology.

1. Introduction

This report presents a comprehensive user's and programmer's guide for the micro-modeling strategy of masonry structures proposed in Lourenço (1996). The strategy consists of modeling units with elastic continuum elements and joints with inelastic interface elements. The composite interface model has been developed according to the plasticity theory.

Chapter 2 presents the additional DIANA syntax needed to use the interface masonry model, including the material data, the proposed automatic arc-length procedures, new layout specifications and an external masonry pre-processor.

Chapter 3 reviews experimental data available for the Dutch materials and provides recommendations for use.

Chapters 4 and 5 present the steps of a nonlinear analysis of two masonry structures, including pre- and post-processing of the results. Chapter 4 includes a masonry pier with a point load and Chapter 5 includes a masonry shear wall with an opening.

Appendix A gives the complete formulation of the interface composite model.

Appendix B includes the source code of the special masonry pre-processor.

2. DIANA additional syntax

This section details the additional DIANA syntax for the use of the interface composite model.

2.1 Material data

In the following, the syntax of the nonlinear material data input for the composite interface model is detailed. The model sets a nonlinear relation between tractions (i.e. stresses) and relative displacements across the interface. The tractions are a normal traction t_n and a shear traction t_t . The relative displacements are a normal displacement Δu_n and a shear displacement Δu_t .

Apart from the input described in this section, the linear stiffness must always be specified as described in Volume *Linear Static Analysis*.

Masonry inelastic behavior may be specified according to the following syntax:

syntax

```
'MATERI'
```

1	5 6	12 13	80
---	-----	-------	----

```

MASINT
GAPVAL   $ft_r$ 
MODE1    $mo1_n$ 
MO1VAL   $mo1_r$ 
FRCVAL   $ch_r$   $tph_r$   $tps_r$  [ $tphu_r$   $tpsu_r$   $unconf_r$ ]
MODE2    $mo2_n$ 
MO2VAL   $mo2_r$ 
CAPVAL   $fm_r$   $cs_r$ 
MODEC    $moc_n$ 
MOCVAL   $moc1_r$   $moc2_r$ 

```

MASINT indicates use of the composite yield surface for masonry, see Figure 1.



Figure 1 - Composite interface model

GAPVAL ft is the tensile strength f_t .

MODE1 $mo1$ indicates the mode I tension softening criterion. Only exponential softening is considered in the current implementation, see Figure 2.

$$mo1 = 4$$

MO1VAL $mo1$ is the fracture energy G_f^I , defining the area under the diagram for mode I.

FRCVAL describes the friction criterion: ch is the cohesion c , tph is the initial tangent of the friction angle ϕ , tps is the initial tangent of the dilatancy angle ψ , $tphu$ is the tangent of the residual friction angle ϕ_r , tps_u is the tangent of the residual dilatancy angle ψ_r , and $unconf$ is the value σ_{unconf} of the confining normal stress for which the initial dilatancy angle is zero.

$$\tan \psi \leq \tan \phi$$

$$\sigma_{unconf} \leq 0$$

MODE2 $mo2$ indicates the mode II shear softening criterion. Only exponential softening is considered in the current implementation, see Figure 3.

$$mo2 = 4$$

MO2VAL $mo2$ is the fracture energy G_f^{II} , defining the area under the diagram for mode II.

CAPVAL describes the cap criterion: fm is the compressive strength of masonry f_m and the parameter cs controls the contribution of the shear traction to compressive failure via the elliptical cap $\sigma^2 + C_s \tau^2 = f_m$.

MODEC moc indicates the compression inelastic criterion. Only parabolic hardening followed by parabolic/exponential softening is considered in the current implementation, see Figure 4.

$$moc = 5$$

MOCVAL describes the inelastic law: $moc1$ is the compressive fracture energy G_{fc} and $moc2$ is the equivalent plastic relative displacement κ_p corresponding to the peak stress.

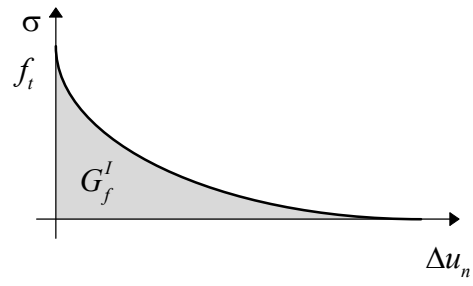


Figure 2 - Behavior of the model in tension (mode I)

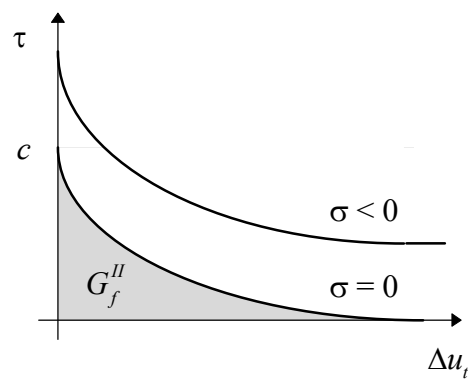


Figure 3 - Behavior of the model in shear (mode II)

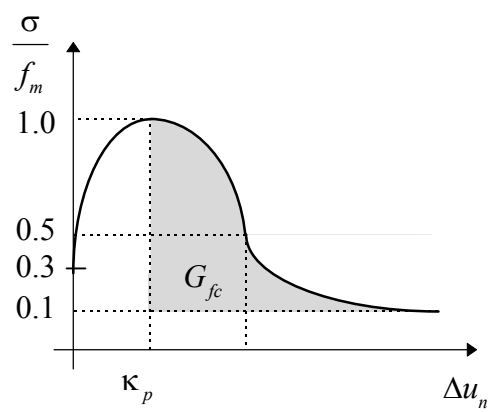


Figure 4 - Behavior of the model in compression

2.2 Indirect control selection SELECT ARCLEN

Two special optional command block of type SELECT ARCLEN has been created: INTTOT and INTREL.

In the first option (INTTOT), a loop over all the nodes connected via an interface element detects the maximum incremental relative displacement (normal or shear). The pair of nodes with the maximum incremental relative displacement is then used with the standard CMOD option. This way, the most critical pair of interface nodes automatically controls the iterative procedure without the need of any input from the user. It is recommended to adopt this new feature throughout the analysis.

In certain extreme cases, for load steps leading to very high energy releases, the second option must be used (INTREL), where the ratio incremental relative displacement / total relative displacement is adopted as control measure.

syntax

```
SELECT ARCLEN INTTOT
END SELECT ARCLEN
```

syntax

```
SELECT ARCLEN INTREL
END SELECT ARCLEN
```

2.3 Layout specification LAYOUT

Additional syntax commands for plotting of analysis results have been created (in bold).

syntax

```
LAYOUT
  NODES DATA.DEVFM
  ELEMEN DATA.VFASLIC1234567
END LAYOUT
```

NODES DATA specifies the plotting style of nodal analysis results.

DATA . E draws only the contour (edges) of the deformed model.

ELEMEN DATA specifies the plotting style of element analysis results.

DATA.F4 or DATA.F5 plot the data for interface elements with a triangle.

DATA.F6 or DATA.F7 plot the data for interface elements with a thick line.









	DATA.F4	DATA.F5	DATA.F6	DATA.F7
positive values				
negative values				

Figure 5 - Additional plotting style of element results as figures for interfaces

2.4 Special masonry pre-processor MAKE_WALL

A pre-processor for making regular masonry meshes has been created. This mesh generator creates a masonry pattern, in the xy plane, for eight-noded plane stress elements and six-noded line interface elements. Presently, this is an external, interactive module. The complete source code is given in Appendix B.

A typical example of the screen output of the program with the list of data that the user must provide (in bold) is the following:

screen

```

make_wall diana.dat ↵
Title: Example of pre-processing ↵
Cracks in the middle of the units? [0/1]
1 ↵
Interface in the bottom of first course? [0/1]
1 ↵
Interface in the top of last course? [0/1]
1 ↵
Each course contains an integer number of units? [0/1]
1 ↵
First course starts with full unit? [0/1]
1 ↵
Number of courses?
6 ↵

Number of complete units per course?
4 ↵
Number of x divisions per unit?
(must be even number)
4 ↵

```

```
Number of y divisions per unit?  
2 ↵  
Dimension x of unit?  
100. ↵  
Dimension y of unit?  
50. ↵  
Fake half_thickness of joints?  
0.0 ↵  
Fake half_thickness of cracks?  
0.0 ↵  
  
*** CREATED FILE diana.dat ***
```

The command `make_wall diana.dat` indicates to create a data file with the name `diana.dat`. The data required by the program are (0 - No, 1 - Yes):

1. Title:

The title of the analysis.

2. Cracks in the middle of the units? [0/1]

Whether potential vertical cracks in the middle of the units are to be included in the model.

3. Interface in the bottom of first course? [0/1]

Whether a masonry joint is to be included in the bottom of the model.

4. Interface in the top of last course? [0/1]

Whether a masonry joint is to be included in the top of the model.

5. Each course contains an integer number of units? [0/1]

Choose between two possible course configurations, see Figure 6.

6. First course starts with full unit? [0/1]

Whether the first (bottom) course starts with a full unit or half unit, for both configurations of Figure 6.

7. Number of courses?

The number of masonry courses in the model, see Figure 6.

8. Number of complete units per course?

The number of complete units per course, see Figure 6.

9. Number of x divisions per unit? (must be even number)

The number of division (finite elements) per unit in the x direction, see Figure 7.

10. Number of y divisions per unit?

The number of division (finite elements) per unit in the y direction, see Figure 7.

11. `Dimension x of unit?`

The width of the unit added with the thickness of the mortar joint, see Figure 7.

12. `Dimension y of unit?`

The height of the unit added with the thickness of the mortar joint, see Figure 7.

13. `Fake half_thickness of joints?`

A possible (virtual) thickness given to the interfaces to allow easier later manipulation or to obtain nicer graphical output, see Figure 7. The value 0.0 represents the true interface thickness and, even if a different value is provided, *a non-zero thickness is not included in the analysis*. This means that the (fake) dimensions of the unit must always represent the (real) dimensions of the unit plus the (real) thickness of the joints.

14. `Fake half_thickness of cracks?`

A possible (virtual) thickness given to the interfaces to allow easier later manipulation, see Figure 7. For novice users the value 0.0 is suggested.

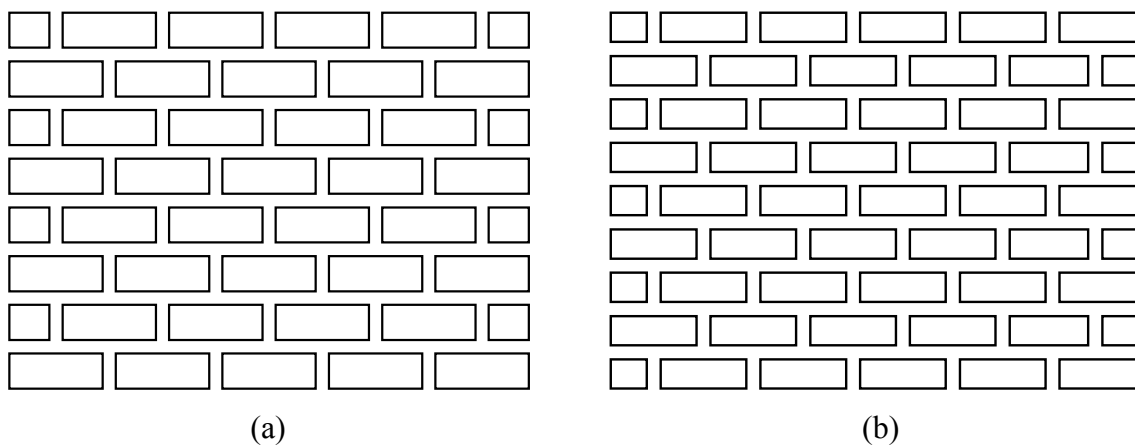


Figure 6 - Examples of input: (a) courses with an integer number of units, wall with eight courses and first course starts with a full unit ; (b) courses without an integer number of units, wall with nine courses and first course does not start with a full unit.

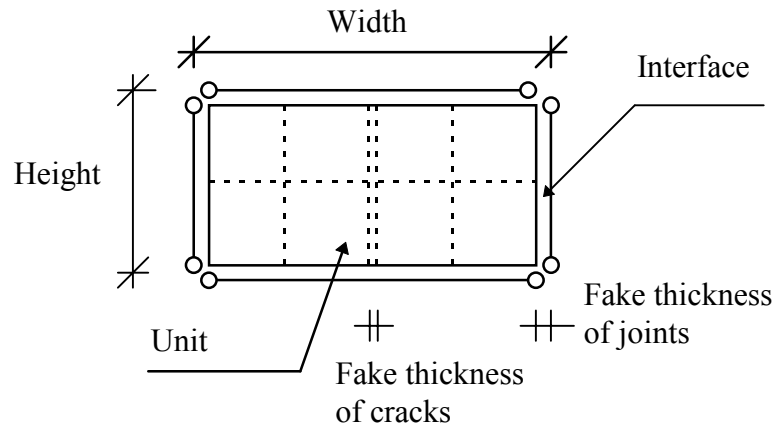


Figure 7 - Detail of a single unit and neighboring interfaces: Four divisions (elements) along the x direction and two divisions (elements) along the y direction. *The number of elements along the x axis must be even for proper connection with neighboring units.*

The data file automatically generated with the given input is partially shown below. It is noted that four groups have been generated UNIT, JBED, JHEAD and UCRAC for the unit elements, bed joint elements, head joint elements and elements representing the potential cracks in the units. A picture of these groups is given in Figure 8. A Gauss 2×2 and a Lobatto 3-point integration schemes are suggested for the continuum and interface elements, respectively.

diana.dat

```

Example of pre-processing
'COORDINATES'
  1  0.0000000E+00  0.0000000E+00  0.0000000E+00
  2  0.1250000E+02  0.0000000E+00  0.0000000E+00
  3  0.2500000E+02  0.0000000E+00  0.0000000E+00
  4  0.3750000E+02  0.0000000E+00  0.0000000E+00
  5  0.5000000E+02  0.0000000E+00  0.0000000E+00
                                     1078 lines skipped
1084 0.3500000E+03  0.3000000E+03  0.0000000E+00
1085 0.3625000E+03  0.3000000E+03  0.0000000E+00
1086 0.3750000E+03  0.3000000E+03  0.0000000E+00
1087 0.3875000E+03  0.3000000E+03  0.0000000E+00
1088 0.4000000E+03  0.3000000E+03  0.0000000E+00
'GROUPS'
ELEMEN
  1  UNIT   / 1-192 /
  2  JBED   / 193-304 /
  3  JHEAD  / 305-346 /
  4  UCRAC  / 347-388 /

'ELEMENTS'
CONNECT
  1  CQ16M   41    42    43    82    107    106    105    81
  2  CQ16M   43    44    45    83    109    108    107    82

```

3	CQ16M	46	47	48	85	112	111	110	84
<i>186 lines skipped</i>									
190	CQ16M	977	978	979	1005	1043	1042	1041	1004
191	CQ16M	980	981	982	1007	1046	1045	1044	1006
192	CQ16M	982	983	984	1008	1048	1047	1046	1007
193	CL12I	1	2	3	41	42	43		
194	CL12I	3	4	5	43	44	45		
195	CL12I	6	7	8	46	47	48		
<i>190 lines skipped</i>									
386	CL12I	965	997	1029	964	996	1028		
387	CL12I	911	939	975	910	938	974		
388	CL12I	975	1003	1039	974	1002	1038		

MATERI
 / UNIT / 1
 / JBED / 2
 / JHEAD / 3
 / UCRAC / 4

DATA
 / UNIT / 1
 / JBED / 2
 / JHEAD / 2
 / UCRAC / 2

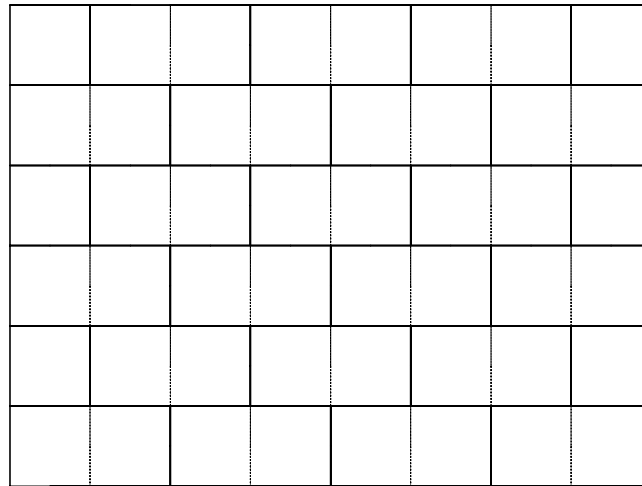
GEOMET
 / UNIT / 1
 / JBED / 2
 / JHEAD / 2
 / UCRAC / 2

'MATERI'
 1 YOUNG 1.D+4
 POISON 0.2
 2 DSTIF 1.D+3 1.D+3
 3 DSTIF 1.D+3 1.D+3
 4 DSTIF 1.D+6 1.D+6

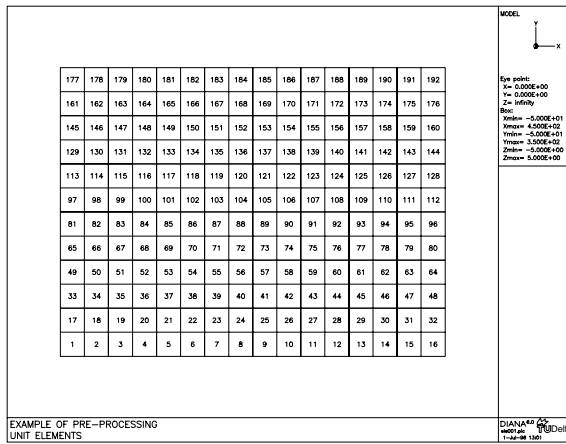
'GEOMET'
 1 THICK 1.D+2
 2 CONFIG MEMBRA
 ZAXIS 0. 0. 1.
 THICK 1.D+2

'DATA'
 1 NGAUS 2 2
 2 NLOBAT 3

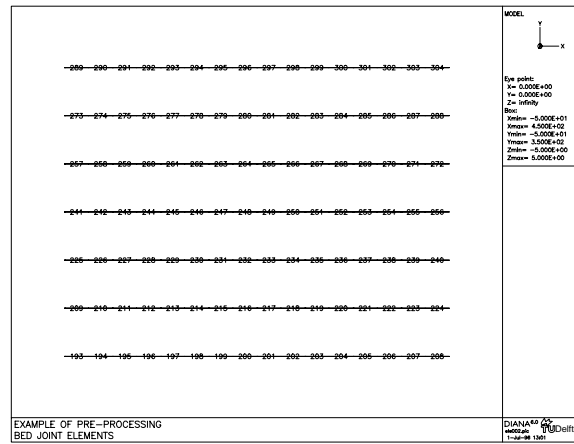
'END'



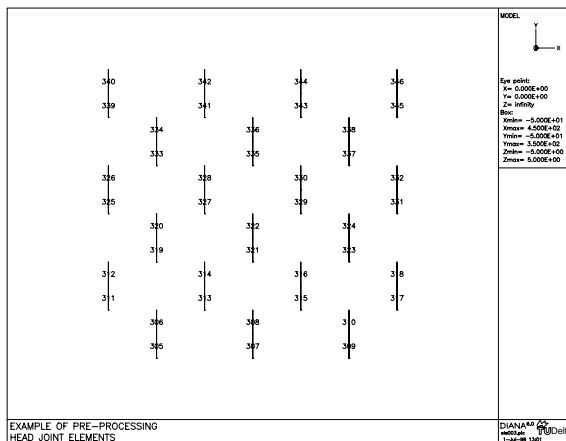
(a)



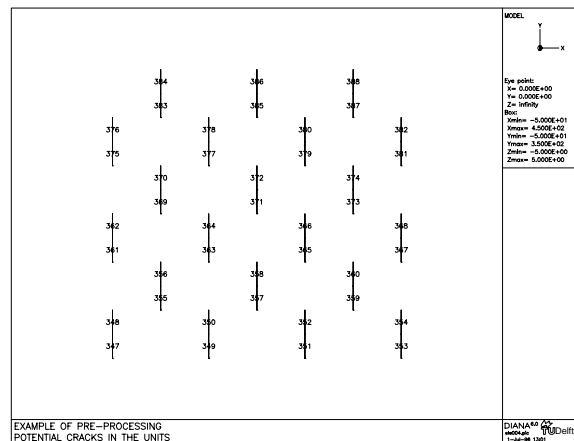
(b)



(c)



(d)



(e)

Figure 8 - Automatically generated mesh for (a) masonry wall: (b) unit elements; (c) bed joint elements; (d) head joint elements and (e) potential cracks in the units.

3. Recommendations about input data

The research on masonry has been scarce when compared with other structural materials and experimental data which can be used as input for the model is limited. In the following, some results available in the literature are presented and some recommendations for the use of the model are given.

3.1 Tension mode

The parameters needed are the bond tensile strength f_t and the bond fracture energy G_f^I . The factors that affect the bond between unit and mortar are highly dependent on the units (material, strength, perforation, size, air dried or pre-wetted, etc.), on the mortar (composition, water contents, etc.) and on workmanship (proper filling of the joints, vertical loading, etc.).

For the materials normally used in the Netherlands the following values have been obtained, CUR (1994),

Table 1 - Material data for tension

Unit/mortar combination ^a	f_t (N/mm ²)	G_f^I (Nmm/mm ²)
VE.B	0.33	0.010
VE.C	0.32	0.013
JG.B	0.51	0.018
JG.C	0.87	0.006
KZ.B	0.03	- ^b
KZ.C	0.10	- ^b

^a VE denotes the Vijf Eiken soft mud clay unit, JG denotes the Joost Gele wire cut clay unit, B denotes 1:2:9 mortar (cement:lime:sand per volume) and C denotes 1 : ½ : 4 ½ mortar.

^b not available.

It is clear that a recommendation for the value of the bond tensile strength based on the unit type or mortar type is impossible. Nevertheless, an average value of the bond mode I fracture energy equal to 0.012 Nmm/mm² can be, in principle, adopted.

3.2 Shear mode

The parameters needed for most applications are the bond strength c , the friction angle measured by $\tan\phi$ and the dilatancy angle measured by $\tan\psi$. More advanced applications of the model may require variable friction and dilatancy angles in which case the three additional material parameters indicated in Section 2.1 must be provided. It is noted that a variable friction angle yields a non-constant mode II fracture energy, see Lourenço (1996). In the following, it is assumed that the friction and dilatancy angles can be considered constant.

The bond shear strength depends also on the influence factors given in the Section 3.1. For the materials normally used in the Netherlands the following values have been obtained, CUR (1994),

Table 2 - Material data for shear

Unit/mortar combination	c (N/mm ²)	G_f^{II} (Nmm/mm ²)
VE.B	0.65	0.065 ^a
VE.C	0.85	0.053 ^a
JG.B	0.88	0.129 ^a
JG.C	1.85	0.134 ^a
KZ.B	0.15	0.013 ^a
KZ.C	0.28	0.031 ^a

^a the bond mode II fracture energy depends on the level of the normal stress which is only partially accounted for in the model.

It can be seen that an average ratio between the bond shear strength and the bond tensile strength cannot be established, see also CUR (1994). Nevertheless, an average value for the bond mode II fracture energy of $\frac{1}{10}c$ can be, in principle, adopted.

Independently from the type of unit or mortar, the value of 0.75 can be adopted for the tangent of the friction angle, CUR (1994) and Atkinson *et al.* (1988). Similarly, a value of 0.0 can be adopted for the tangent of the dilatancy angle, Lourenço (1996).

3.3 Cap mode

The parameters needed for the cap mode are the masonry uniaxial compressive strength f_m , the shape of the elliptical cap given by C_s , the compressive fracture energy G_{fc} and

the equivalent relative displacement κ_p which corresponds to the uniaxial compressive strength.

It is a current practice to define the uniaxial compressive strength of masonry from the uniaxial compressive strengths of the unit and mortar, see e.g. EuroCode 6 (CEN, 1995). For the materials normally used in the Netherlands the following values have been obtained, CUR (1994),

Table 3 - Material data for compression

Unit/mortar combination	f_m (N/mm ²)
VE.C	8.7 ^a
JG.C	16.3 ^a
KZ.C	20.0 ^a

^a these values were obtained with a stack bond prism. Different compressive strengths should be adopted for the head and bed joints to simulate anisotropic behavior.

For the parameter C_s , a value of 9.0 can be adopted, Lourenço (1996).

Not much data exists about the post-peak behavior of masonry prisms. For an estimate of the compressive fracture energy, it is recommended to adopt the values proposed for concrete in the Model Code 90 (CEB-FIP, 1991), see Figure 9. The equivalent relative displacement κ_p , can be calculated so that the total masonry strain equals 0.2 %, see EuroCode 6.

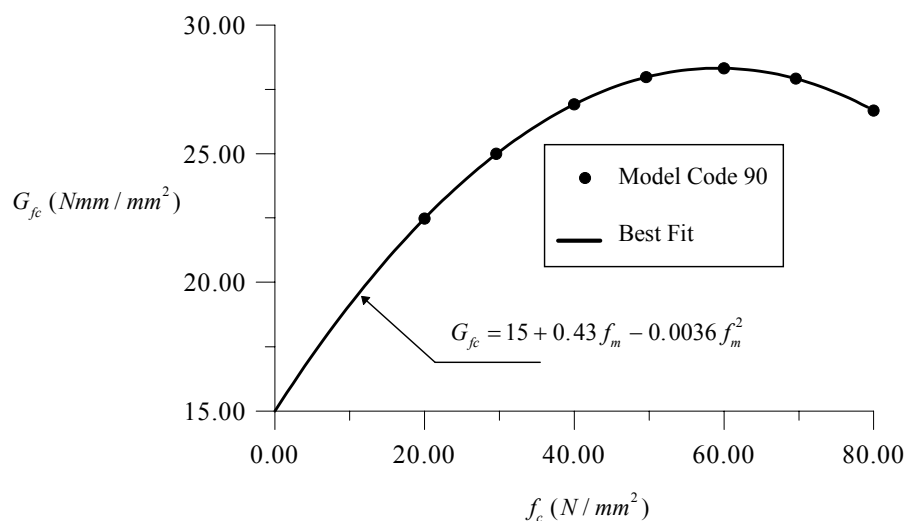


Figure 9 - Compressive fracture energy according to the Model Code 90

3.4 Example

The values suggested to use as input of the model, in the case of masonry made with units and normal strength mortar currently used in the developed countries, are condensed below.

file.dat

'MATERI'			
1	DSTIF	k_n	k_t
	MASINT		
	GAPVAL	f_t	
	MODE1	4	
	MO1VAL	0.012	
	FRCVAL	c	0.75 0.0
	MODE2	4	
	MO2VAL	$c/10$	
	CAPVAL	f_m	9.0
	MODEC	5	
	MOCVAL	G_{fc}	k_p

The interface elastic stiffness values can be calculated from the thickness of the joint h_j , the Young's moduli of unit and joint, E_u and E_j , respectively, and the shear moduli of unit and joint, G_u and G_j , respectively, as, CUR(1994),

$$k_n = \frac{E_u E_j}{h_j (E_u - E_j)}$$

$$k_t = \frac{G_u G_j}{h_j (G_u - G_j)}$$

The different strength values f_t , c and f_m are given from the available experimental data or tests in collected samples. The compressive fracture energy is given by, see Figure 5,

$$G_{fc} = 15 + 0.43 f_m - 0.0036 f_m^2$$

and the equivalent relative displacement reads

$$\kappa_p = \left\{ 0.002 - f_m \left[\frac{1}{E_u} + \frac{1}{k_n (h_u + h_j)} \right] \right\} f_m$$

in order to obtain a masonry strain of 0.2 % at peak stress.

The input parameters for the model are, therefore:

- the elastic properties of the interface
 k_n and k_t (or E_u, G_u, ν_u and E_j, G_j, ν_j and h_j)
- tensile strength of the joint
 f_t
- shear strength of the joint (cohesion)
 c
- compressive strength of masonry
 f_m

4. Example 1 - Masonry pier with point load

This example illustrates the use of DIANA for the analysis of a masonry pier with a point load, see Figure 10. In the center of the pier a splitting crack arises which propagates in a catastrophic manner after peak load. The computed crack path is straight and vertical indicating that the crack jumps from head joint to head joint right through the unit. The chosen material parameters represent the inelastic behavior according to Chapter 3.

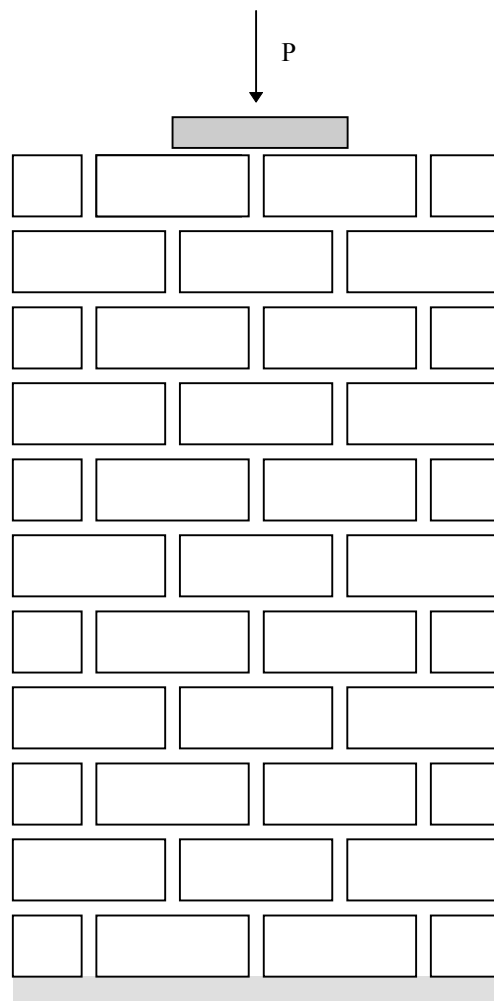


Figure 10 - Masonry pier with point load

4.1 Mesh generation

The full mesh is generated using the external masonry pre-processor `make_wall`. The run-command is `make_wall mesh.dat` and the interactive input data are shown below. The units are $140 \times 50 \times 100 \text{ mm}^3$ and the joints are 10 mm thick. Note that a

non-zero fake_interface thickness is used to avoid showing interpenetration of the units. This is a representation of the true thickness of the joint that is not taken into account in the analysis. In reality, the interfaces have zero thickness and the dimensions of the continuum elements must be enlarged by the unit joint thickness.

Input data

screen

```

make_wall mesh.dat ↵
Title:Example1 for users/programmers report - Pier with point load ↵
Cracks in the middle of the units? [0/1]
1 ↵
Interface in the bottom of first course? [0/1]
1 ↵
Interface in the top of last course? [0/1]
0 ↵
Each course contains an integer number of units? [0/1]
1 ↵
First course starts with full unit? [0/1]
0 ↵
Number of courses?
11 ↵
Number of complete units per course?
3 ↵
Number of x divisions per unit?
(must be even number)
4 ↵
Number of y divisions per unit?
2 ↵
Dimension x of unit?
150. ↵
Dimension y of unit?
60. ↵
Fake half_thickness of joints?
5.0 ↵
Fake half_thickness of cracks?
0.0 ↵
*** CREATED FILE mesh.dat ***

```

The external mesh generator produces a file mesh.dat. The generated mesh is evaluated with the graphic output device of Module POST. The command file shown below produces plot files ele000.pic, ele001.pic and ele002.pic, with the mesh and element numbers for the units, joints and potential cracks in the units, respectively. The run command is

```
diana mesh.dat mesh.com
```

Commands

mesh.com

```

*FILOS
  INITIA
*INPUT
*POST
MODEL
  SELECT ELEMEN UNIT /
END MODEL
LAYOUT
  ELEMEN.N
END LAYOUT
OUTPUT GRAPHI FI="ele"
  TEXT "Unit Elements"
END OUTPUT
MODEL
  SELECT ELEMEN JBED JHEAD /
END MODEL
OUTPUT GRAPHI FI="ele"
  TEXT "Joint Elements"
END OUTPUT
MODEL
  SELECT ELEMEN UCRAC /
END MODEL
OUTPUT GRAPHI FI="ele"
  TEXT "Potential Crack Elements"
END OUTPUT
*END

```

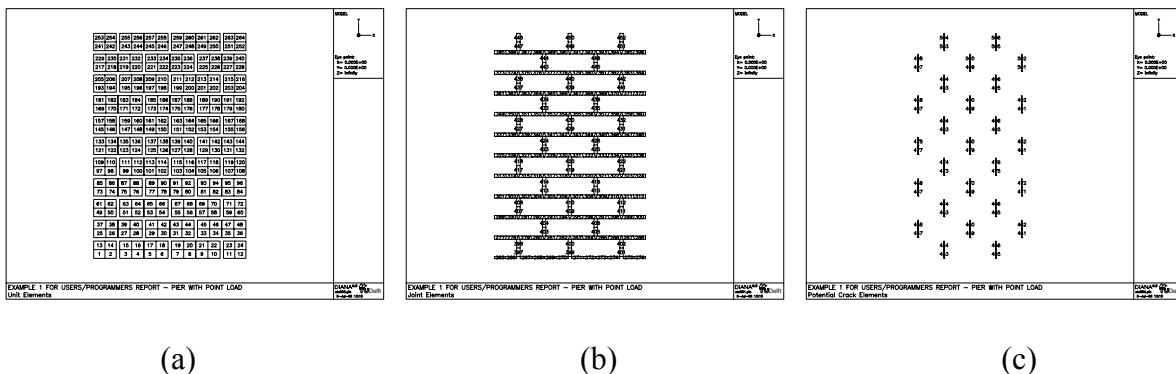


Figure 11 - Generated mesh:

(a) Unit elements; (b) joint elements; (c) potential unit crack elements.

The file `mesh.dat` contains the node coordinates and element connectivity. This file is to be completed with the material and loading data. The material parameters correspond to the masonry behavior described in Chapter 3. At the top of the pier, the force is applied with an infinitely rigid plate, modeled by tying the vertical displacement of the nodes under the plate. At the bottom of the pier, the (mid-) nodes belonging to the symmetry axis are also tied to have symmetric horizontal displacements. The completed data file for the analysis `example1.dat` is shown below.

`example1.dat`

Example 1 for users/programmers report - Pier with point load

'COORDINATES'

```

1 0.5000000E+01 0.0000000E+00 0.0000000E+00
2 0.2125000E+02 0.0000000E+00 0.0000000E+00
3 0.3750000E+02 0.0000000E+00 0.0000000E+00
4 0.5375000E+02 0.0000000E+00 0.0000000E+00

```

1408 lines skipped

```

1413 0.3962500E+03 0.6550000E+03 0.0000000E+00
1414 0.4125000E+03 0.6550000E+03 0.0000000E+00
1415 0.4287500E+03 0.6550000E+03 0.0000000E+00
1416 0.4450000E+03 0.6550000E+03 0.0000000E+00

```

'GROUPS'

ELEMEN

```

1 UNIT / 1-264 /
2 JBED / 265-396 /
3 JHEAD / 397-452 /
4 UCRAC / 453-506 /

```

'ELEMENTS'

CONNECT

```

1 CQ16M 31 32 33 62 81 80 79 61
2 CQ16M 33 34 35 63 83 82 81 62
3 CQ16M 36 37 38 65 86 85 84 64
4 CQ16M 38 39 40 66 88 87 86 65

```

156 lines skipped

```

261 CQ16M 1359 1360 1361 1382 1409 1408 1407 1381
262 CQ16M 1361 1362 1363 1383 1411 1410 1409 1382
263 CQ16M 1364 1365 1366 1385 1414 1413 1412 1384
264 CQ16M 1366 1367 1368 1386 1416 1415 1414 1385
265 CL12I 1 2 3 31 32 33
266 CL12I 3 4 5 33 34 35
267 CL12I 6 7 8 36 37 38
268 CL12I 8 9 10 38 39 40

```

130 lines skipped

```

503 CL12I 1301 1327 1349 1300 1326 1348
504 CL12I 1349 1375 1397 1348 1374 1396
505 CL12I 1311 1333 1359 1310 1332 1358
506 CL12I 1359 1381 1407 1358 1380 1406

```

MATERI

```

/ UNIT / 1
/ JBED / 2
/ JHEAD / 2
/ UCRAC / 3

```

DATA

```

/ UNIT / 1
/ JBED / 2
/ JHEAD / 2
/ UCRAC / 2

```

GEOMET

```

/ UNIT / 1
/ JBED / 2
/ JHEAD / 2
/ UCRAC / 2

```

```

: Up to here this file was produced by the
: diana's external masonry mesh generator

```

'MATERI'

```

1 YOUNG 15000.
  POISON 0.2

```

```

: hj = 10 mm
: Eu = 15000. Gu = 15000 / 2 / ( 1 + 0.2 ) = 6250
: Ej = 6000. Gj = 6000 / 2 / ( 1 + 0.2 ) = 2500
: kn = 15000 * 3000 / ( 10 * ( 15000 - 3000 ) ) = 1000
: ks = 6250 * 2500 / ( 10 * ( 6250 - 2500 ) ) = 417
: ft = 0.15 c = 0.3 fm = 12.

```



```

:          Gfc = 15 + 0.43 * 12 - 0.0036 * 12 * 12 = 20
:          kp  = 12*(0.002-12*(1/15000+1/1000/(10.+50.)))=0.001
2  DSTIF  1000. 417.
   MASINT
   GAPVAL 0.15
   MODEL  4
   MOLVAL 0.012
   FRCVAL 0.3 0.75 0.0
   MODE2  4
   MO2VAL 0.03
   CAPVAL 12. 9.0
   MODEC  5
   MOCVAL 20. 0.001
3  DSTIF  1.D+6 1.D+6
   DISCRA 1
   DCRVAL 0.75
   MODEL  2
   MOLVAL 0.025
'GEOMET'
1  THICK  1.D+2
2  CONFIG MEMBRA
   ZAXIS  0. 0. 1.
   THICK  1.D+2
'DATA'
1  NGAUS  2 2
2  NLOBAT 3
'TYINGS'
EQUAL TR 2
: Simulates infinitely rigid plate
/ 1397-1405 / 1406
: Pair of nodes at the bottom of the pier
: with symmetric horizontal displacement
FIX TR 1
15 16 TR 1 -1.0
'SUPPOR'
: Bottom of pier
/ 1-30 / TR 2
'LOADS'
CASE 1
NODAL
: Vertical force of 1000 N
/ 1397-1406 / F 2 -125.0
'END'

```

An additional DIANA-job, with the file `supload.com`, generates the graphic output file `supload000.pic` to check the loads and supports. The run command is

```
diana example1.dat supload.com
```

Commands

`supload.com`

```

*FILOS
  INITIA
*INPUT
*ELASSE
*POST
MODEL
  SELECT ELEMEN UNIT JBED /
  HIDDEN

```

```

END MODEL
LAYOUT
  MODEL.E
END LAYOUT
OUTPUT GRAPHI FI="loa"
LOAD
SUPPORT
  TEXT "Check Loads and Supports. Plot Edges only"
END OUTPUT
*END

```

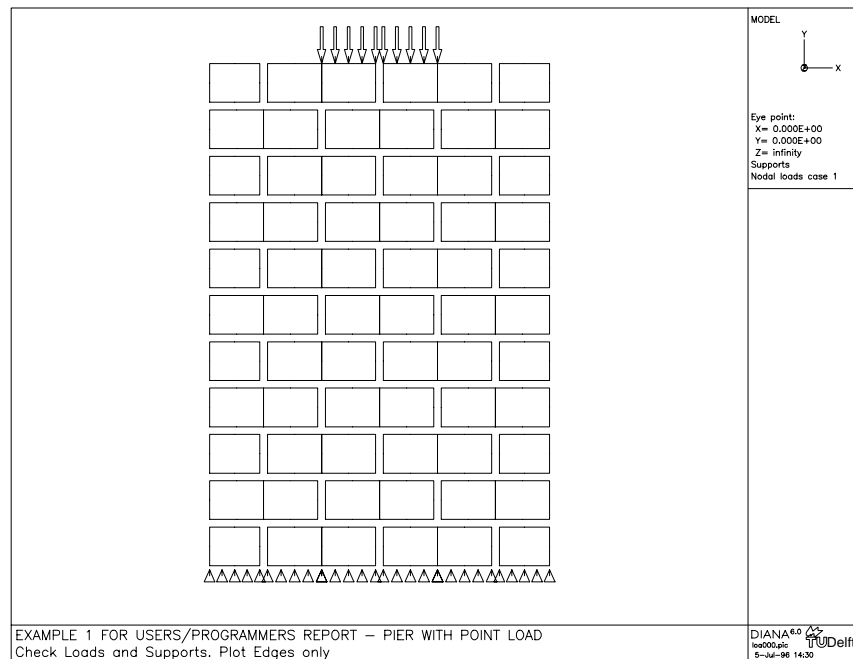


Figure 12 - Supports and loads for masonry pier with point load

4.2 Nonlinear analysis

It is necessary that the nonlinear analysis starts after a linear static analysis where most checks about the model are performed and the global stiffness matrix is assembled for the first time. Also a series of commands are necessary to define the types of nonlinearity in the model and the combinations of loads applied to the model. Then, we run this initial job

```
diana example1.dat non.com
```

Commands

non.com

```

*FILOS
  INITIA
*INPUT
*ELASSE
*ELMAT
*LOADS

```

```

*ORDER
*SOLVE
*NONLIN
SEGMENT INITIA/IN30LL
INITIA
  ANALYS PHYSIC
  OPTION TANGEN NONSYM
  USE
    INTERF
  END USE
END INITIA
LOADIN
  LOAD(1): (1) 1.0 /
END LOADIN
*END

```

The nonlinear analysis is performed under the special interface arc-length procedure, `SELECT ARCLEN INTTOT`. We execute a first load step of 20.0 (= 20 kN), which is still completely linear. This is followed by eight load steps of 10.0, four steps of 2.5 and five steps of 0.5 up to peak load. The (small) critical steps close to a sharp snap-back are controlled with the maximum incremental / total relative displacement (`SELECT ARCLEN INTREL`) in the interface. Afterwards, we return to the standard `INTTOT` arc-length control. The unloading is traced with ten steps of 5.0 and twenty steps of 1.0. After each run, we run Module POST, to make plots of the deformed structure, the tensile principal stresses and the normal opening of the joints as a representation of cracking in the joints and units.

The first step, is performed with the run command

```
diana example1.dat nonlin1.com
```

Commands

nonlin1.com

```

*NONLIN/CI33LL
SEGMENT EXECUT/XQ31LL
SELECT
  NODES 1405 /
  ELEMENT NONE //
  END ELEMEN
END SELECT
OUTPUT TABULA NONLIN
  DISPLA TOTAL GLOBAL
END OUTPUT
SELECT ARCLEN INTTOT
END SELECT ARCLEN
EXECUTE LOAD(1) STEPS
  LINE SEARCH
  SIZE.P 20.0(1) /
  PERFOR.R NEWTON REGULA MI=15
  NORM ENERGY NEWREF CONTIN CO=1.d-6 AB=1.d+4
END EXECUTE STEPS
*POST/CI30LL

```

```

SEGMENT WRITE/WR30LL
MODEL
  SELECT ELEMEN UNIT /
  HIDDEN
END MODEL
LAYOUT
  MODEL.E LI=..
  ELEMEN.
  NODES. DATA.E LI=-
END LAYOUT
OUTPUT GRAPHI NONLIN FI="i"
  TEXT "Incremental displacements"
  DISPLA INCREM
END OUTPUT
MODEL
  SELECT ELEMEN UNIT /
  HIDDEN
END MODEL
LAYOUT
  MODEL.E LI=-
  ELEMEN. DATA.F
END LAYOUT
OUTPUT GRAPHI NONLIN FI="s"
  TEXT "Tensile principal stresses"
  STRESS TOTAL PRINCI XX YY INTPNT FR=0.D0
END OUTPUT
LAYOUT
  MODEL.E LI=-
  ELEMEN. DATA.F6
END LAYOUT
OUTPUT GRAPHI NONLIN FI="u"
  TEXT "Relative opening displacement normal to interface"
  STRAIN FORCE N INTPNT FR=0.d0
END OUTPUT
*END

```

We can continue the nonlinear analysis using almost identical command files. For the next two command files, we just change the SIZE line in the EXECUTE LOAD(1) STEPS block as given below. The run commands are

```

diana example1.dat nonlin2.dat
diana example1.dat nonlin3.dat

```

Commands	nonlin2.com
<hr/>	
*NONLIN/CI33LL	<i>14 lines skipped</i>
SIZE.P 10.0(8) /	<i>3 lines skipped</i>
*POST	
: like nonlin1.com	<i>16 lines skipped</i>
<hr/>	

Commands	nonlin3.com
-----------------	-------------

```
*NONLIN/CI33LL
SIZE.P 2.5(4) /
*POST
:   like nonlin1.com
```

14 lines skipped
3 lines skipped
16 lines skipped

A very sharp snap-back is obtained at peak load due to the sudden energy release in the straight crack that arises under the load. For the next steps, we must also change the SELECT ARCLLEN line as given below. The run command is

diana example1.dat nonlin4.dat

Commands nonlin4.com

```
*NONLIN/CI33LL
SELECT ARCLLEN INTREL
END SELECT ARCLLEN
EXECUTE LOAD(1) STEPS
  LINE SEARCH
  SIZE.P 0.5(5) /
  PERFOR.R NEWTON REGULA MI=15
  NORM ENERGY NEWREF CONTIN CO=1.d-6 AB=1.d+4
END EXECUTE STEPS
*POST
:   like nonlin1.com
```

11 lines skipped
16 lines skipped

After peak load, it is possible to return to the more stable arc-length procedure where the maximum incremental relative displacement is adopted as control parameter. For the next steps, we change again the SELECT ARCLLEN line as given below. The run command is

diana example1.dat nonlin5.dat

Commands nonlin5.com

```
*NONLIN/CI33LL
SELECT ARCLLEN INTTOT
END SELECT ARCLLEN
EXECUTE LOAD(1) STEPS
  LINE SEARCH
  SIZE.P 5.0(10) 1.0(20) /
  PERFOR.R NEWTON REGULA MI=15
  NORM ENERGY NEWREF CONTIN CO=1.d-6 AB=1.d+4
END EXECUTE STEPS
*POST
:   like nonlin1.com
```

11 lines skipped
16 lines skipped

After each load step, the selected data for node 1405 is written to the output file `diana.tb` as specified in the `SELECT` block. A selection of the tabulated output of the last load step is given below.

Nonlinear output

nonlin5.com

```

Analysis type      : NONLIN
Step nr.          :    48
Load factor       :   0.4564E+02
Result            : DISPLA TOTAL  TRANSL
Axes              : GLOBAL

      Nodes      TDtX      TDtY      TDtZ
      1405      -0.8003E-02 -0.1123E+00  0.0000E+00

```

4.3 Interpretation of the results

From the tabulated output, it is possible to obtain a force-displacement diagram with the scan filter. The run command is

```
scan < diana.tb >> xy.dat
```

Filter

scan

```

awk 'BEGIN { displa_line=10;
           f = "%15.4e %15.4e\n"
           printf f, 0.0, 0.0
         }
     /TDtX/ { displa_line = 0 }
     {
     displa_line += 1
     if ( displa_line == 2 ) { disp = $3 }
     if ( displa_line == 8 ) { force = $4
     printf f, -disp, force }
     }

```

The force-displacement diagram for the rigid plate is given in Figure 13. The rising portion of the curve appears to be almost linear, indicating that the effect of cracking prior to reaching the maximum load is negligible. After reaching the maximum load, a very sudden decrease of both the load and the displacement occurs. The other figures show the plots produced after steps 1, 9, 13, 18 and 48. For each load step, we plot the incremental deformed mesh, plotted with a solid line, the tensile principal stresses at the

integration points, plotted with a solid line, and the normal opening of all interface elements, plotted with a variable thickness solid line.

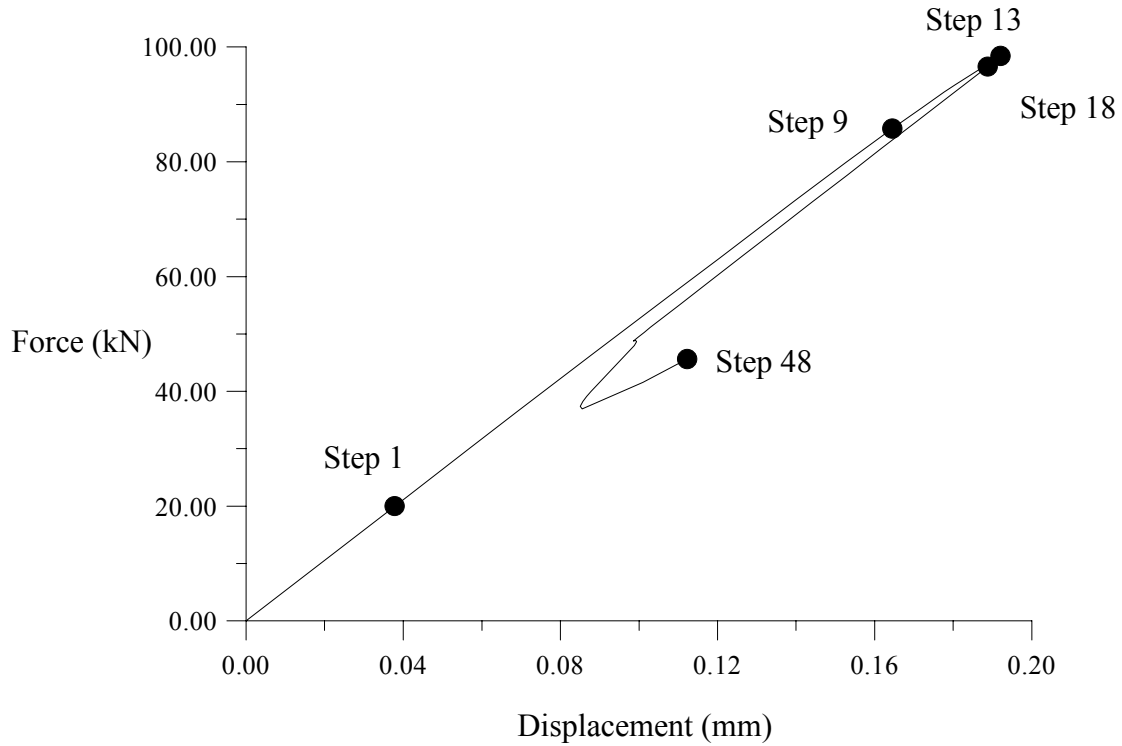
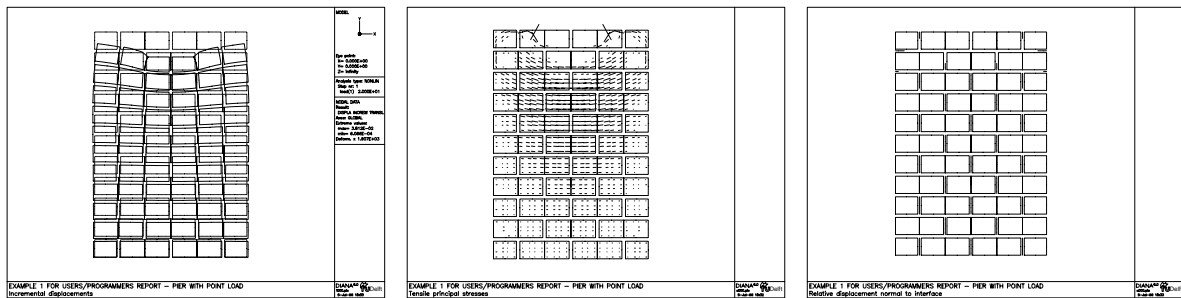
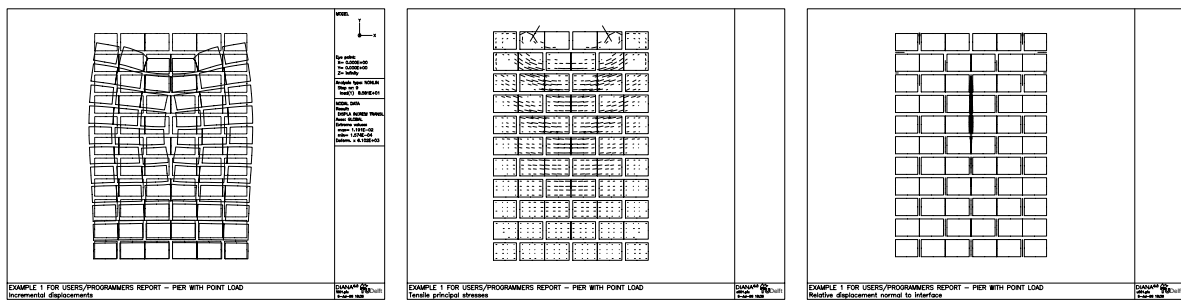


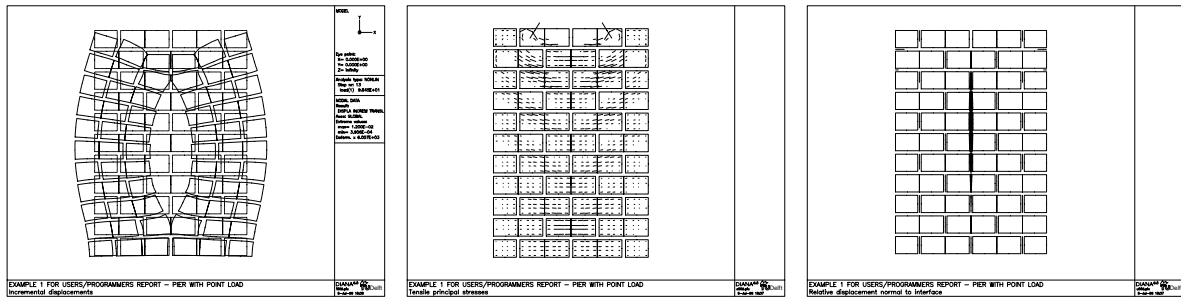
Figure 14 - Force-displacement diagram for masonry pier with point load



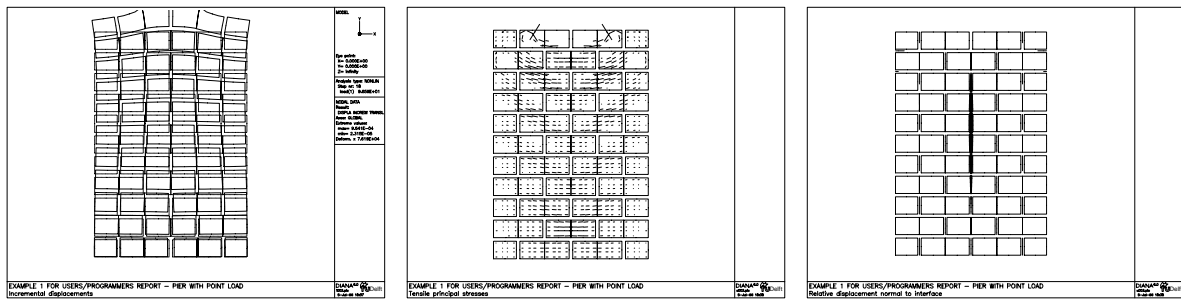
Step 1



Step 9

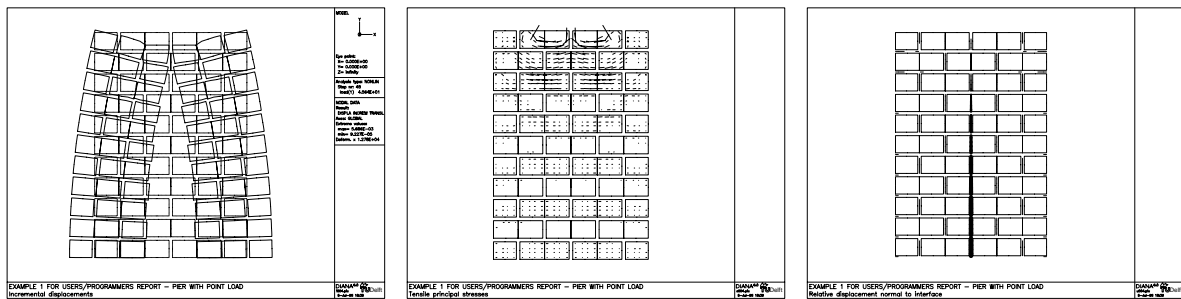


Step 13



Step 18

Figure 15 - Plots for masonry pier with point load: incremental deformed mesh, tensile principal stresses and normal opening of interfaces (cont.).



Step 48

Figure 15 - Plots for masonry pier with point load: incremental deformed mesh, tensile principal stresses and relative normal opening of interfaces (contd.).

5. Example 2 - Masonry shear wall with an opening

This example illustrates the use of DIANA for the analysis of a masonry shear wall with an opening, see Figure 16. An initial vertical load p is applied before shearing the wall with the horizontal force F . The opening in the center of the wall forces the compressive strut, which arises during loading, to spread around it. This leads to diagonal stepped cracks starting from two corners of the opening and bending cracks at the top and bottom of the smaller piers defined by the opening. At collapse, four rigid blocks are formed.

Potential cracks in the units have not been modeled to increase the legibility of the plots. Nevertheless, potential cracks in the units should always be included in the analysis, Lourenço (1996). The chosen material parameters represent the inelastic behavior according to Chapter 3.

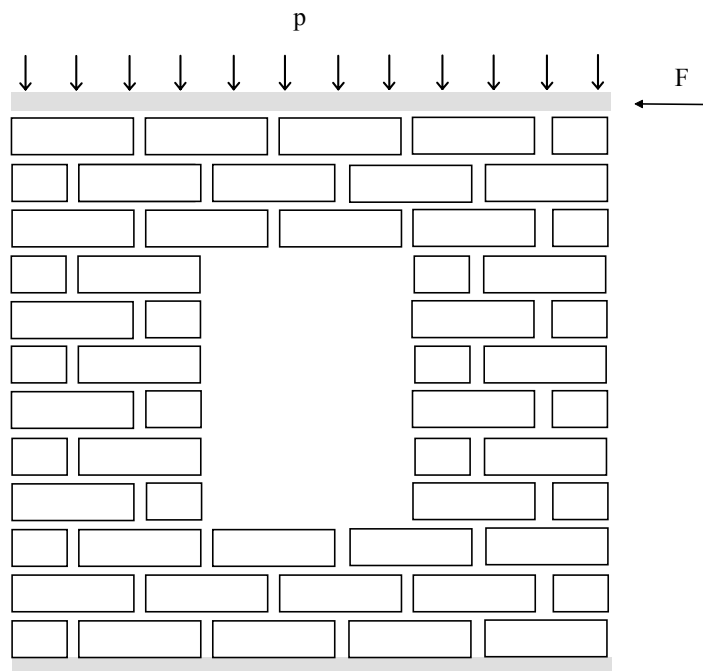


Figure 16 - Masonry pier with point load

5.1 Mesh generation

The full mesh is generated using the external masonry pre-processor `make_wall`. The run-command is `make_wall mesh.dat` and the interactive input data are shown below. The units are $140 \times 50 \times 100 \text{ mm}^3$ and the joints are 10 mm thick. Note that a non-zero `fake_interface` thickness is used to avoid showing interpenetration of the units.

This is a representation of the true thickness of the joint that is not taken into account in the analysis. In reality, the interfaces have zero thickness and the dimensions of the continuum elements must be enlarged by the unit joint thickness.

Input data

screen

```

make_wall mesh.dat ↵
Title: Example 2 for users/programmers report - Shear wall with an opening ↵
Cracks in the middle of the units? [0/1]
0 ↵
Interface in the bottom of first course? [0/1]
1 ↵
Interface in the top of last course? [0/1]
1 ↵
Each course contains an integer number of units? [0/1]
0 ↵
First course starts with full unit? [0/1]
0 ↵
Number of courses?
12 ↵
Number of complete units per course?
4 ↵
Number of x divisions per unit?
(must be even number)
4 ↵
Number of y divisions per unit?
2 ↵
Dimension x of unit?
150. ↵
Dimension y of unit?
60. ↵
Fake half_thickness of joints?
5.0 ↵
*** CREATED FILE mesh.dat ***

```

The external mesh generator produces a file `mesh.dat`. The generated mesh is evaluated with the graphic output device of Module POST. The command file shown below produces plot files `ele000.pic` and `ele001.pic`, with the mesh and element numbers for the units and joints, respectively. The run command is

```
diana mesh.dat mesh.com
```

Commands

`mesh.com`

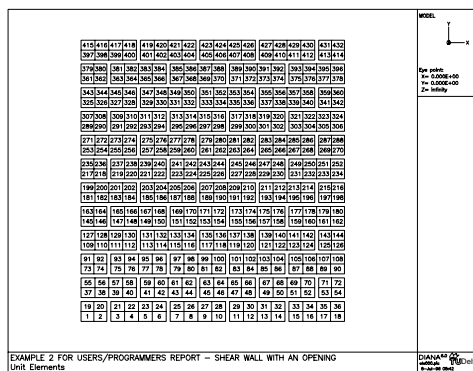
```

*FILOS
  INITIA
*INPUT
*POST
MODEL

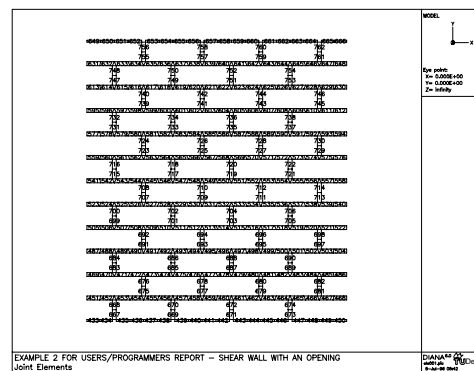
```

```

SELECT ELEMEN UNIT /
END MODEL
LAYOUT
ELEMEN.N
END LAYOUT
OUTPUT GRAPHI FI="ele"
TEXT "Unit Elements"
END OUTPUT
MODEL
SELECT ELEMEN JBED JHEAD /
END MODEL
OUTPUT GRAPHI FI="ele"
TEXT "Joint Elements"
END OUTPUT
*END
    
```



(a)



(b)

Figure 17 - Generated mesh: (a) Unit elements; (b) joint elements

The file mesh.dat contains the node coordinates and element connectivity of a regular masonry pattern. It suffices to comment (:) the lines with the elements that have no physical correspondence to form the opening. The file is also to be completed with the material and loading data. The material parameters correspond to the masonry behavior described in Chapter 3. The top and bottom of the wall are assume to remain straight. A vertical force p equal to 1.0 N/mm^2 is applied before shearing the wall with the force F . The completed data file for the analysis example2.dat is shown below.

example2.dat

Example 2 for users/programmers report - Shear wall with an opening

```

'COORDINATES'
1 0.5000000E+01 0.0000000E+00 0.0000000E+00
2 0.2125000E+02 0.0000000E+00 0.0000000E+00
3 0.3750000E+02 0.0000000E+00 0.0000000E+00
4 0.5375000E+02 0.0000000E+00 0.0000000E+00

2107 0.6212500E+03 0.7200000E+03 0.0000000E+00
2108 0.6375000E+03 0.7200000E+03 0.0000000E+00
    
```

2102 lines skipped

2109 0.6537500E+03 0.7200000E+03 0.0000000E+00
 2110 0.6700000E+03 0.7200000E+03 0.0000000E+00

'GROUPS'

ELEMEN

1 UNIT / 1-432 /
 2 JBED / 433-666 /
 3 JHEAD / 667-762 /

'ELEMENTS'

CONNECT

1	CQ16M	42	43	44	84	108	107	106	83
2	CQ16M	44	45	46	85	110	109	108	84
3	CQ16M	47	48	49	87	113	112	111	86
4	CQ16M	49	50	51	88	115	114	113	87

126 lines skipped

131	CQ16M	622	623	624	660	688	687	686	659
132	CQ16M	624	625	626	661	690	689	688	660
:	133	CQ16M	626	627	628	662	692	691	661
:	134	CQ16M	628	629	630	663	694	693	662
:	135	CQ16M	631	632	633	665	697	696	664
:	136	CQ16M	633	634	635	666	699	698	665
:	137	CQ16M	635	636	637	667	701	700	666
:	138	CQ16M	637	638	639	668	703	702	667
139	CQ16M	640	641	642	670	706	705	704	669
140	CQ16M	642	643	644	671	708	707	706	670

7 lines skipped

148	CQ16M	725	726	727	764	791	790	789	763
149	CQ16M	727	728	729	765	793	792	791	764
150	CQ16M	729	730	731	766	795	794	793	765
:	151	CQ16M	732	733	734	768	798	797	767
:	152	CQ16M	734	735	736	769	800	799	768
:	153	CQ16M	736	737	738	770	802	801	769
:	154	CQ16M	738	739	740	771	804	803	770
:	155	CQ16M	741	742	743	773	807	806	772
:	156	CQ16M	743	744	745	774	809	808	773
157	CQ16M	745	746	747	775	811	810	809	774
158	CQ16M	747	748	749	776	813	812	811	775

272 lines skipped

431	CQ16M	2001	2002	2003	2027	2067	2066	2065	2026
432	CQ16M	2003	2004	2005	2028	2069	2068	2067	2027
433	CL12I	1	2	3	42	43	44		
434	CL12I	3	4	5	44	45	46		

56 lines skipped

491	CL12I	517	518	519	558	559	560		
492	CL12I	519	520	521	560	561	562		
:	493	CL12I	522	523	524	562	563	564	
:	494	CL12I	524	525	526	564	565	566	
:	495	CL12I	526	527	528	567	568	569	
:	496	CL12I	528	529	530	569	570	571	
:	497	CL12I	531	532	533	571	572	573	
:	498	CL12I	533	534	535	573	574	575	
499	CL12I	535	536	537	576	577	578		
500	CL12I	537	538	539	578	579	580		

258 lines skipped

759	CL12I	1928	1957	1992	1927	1956	1991		
760	CL12I	1992	2021	2056	1991	2020	2055		
761	CL12I	1937	1962	2001	1936	1961	2000		
762	CL12I	2001	2026	2065	2000	2025	2064		

: Up to here this file was produced by the
 : diana's external masonry mesh generator

MATERI

/ UNIT / 1
 / JBED / 2
 / JHEAD / 2

```

DATA
  / UNIT / 1
  / JBED / 2
  / JHEAD / 2
GEOMET
  / UNIT / 1
  / JBED / 2
  / JHEAD / 2
'MATERI'
  1  YOUNG  15000.
      POISON 0.2
:      hj = 10 mm
:      Eu = 15000.      Gu = 15000 / 2 / ( 1 + 0.2 ) = 6250
:      Ej = 6000.      Gj = 6000 / 2 / ( 1 + 0.2 ) = 2500
:      kn = 15000 * 3000 / ( 10 * ( 15000 - 3000 ) ) = 1000
:      ks = 6250 * 2500 / ( 10 * ( 6250 - 2500 ) ) = 417
:      ft = 0.15      c = 0.3      fm = 12.
:      Gfc = 15 + 0.43 * 12 - 0.0036 * 12 * 12 = 20
:      kp = 12*(0.002-12*(1/15000+1/1000/(10.+50.))) = 0.012
  2  DSTIF  1000. 417.
      MASINT
      GAPVAL 0.15
      MODE1  4
      MO1VAL 0.012
      FRCVAL 0.3 0.75 0.0
      MODE2  4
      MO2VAL 0.03
      CAPVAL 12. 9.0
      MODEC  5
      MOCVAL 20. 0.012
'GEOMET'
  1  THICK  1.D+2
  2  CONFIG MEMBRA
      ZAXIS  0. 0. 1.
      THICK  1.D+2
'DATA'
  1  NGAUS  2 2
  2  NLOBAT 3
'TYINGS'
EQUAL TR 1
: Simulates stiff concrete beam
/ 2070-2109 / 2110
EQUAL TR 2
/ 2070-2109 / 2110
'SUPPOR'
: Bottom of wall
/ 1-41 / TR 1 TR 2
'LOADS'
CASE 1
NODAL
: Vertical pressure of 1.0 N/mm2
/ 2070-2110 / F 2 -1646.5
CASE 2
NODAL
: Horizontal force of 1000 N
/ 2110 / F 1 -1000.
'END'
'END'

```

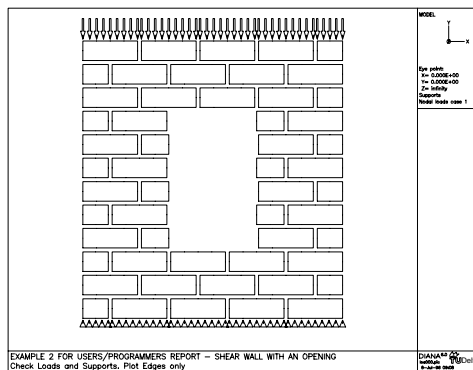
An additional DIANA-job, with the file `supload.com`, generates the graphic output file `supload000.pic` to check the removed elements, loads and supports. The run command is

```
diana example2.dat supload.com
```

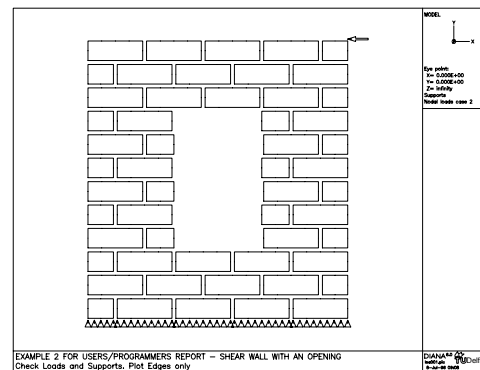
Commands

`supload.com`

```
*FILOS
INITIA
*INPUT
*ELASSE
*POST
MODEL
  SELECT ELEMEN UNIT JBED /
  HIDDEN
END MODEL
LAYOUT
  MODEL.E
END LAYOUT
OUTPUT GRAPHI FI="loa"
LOAD
SUPPORT
  TEXT "Check Loads and Supports. Plot Edges only"
END OUTPUT
*END
```



(a)



(b)

Figure 18 - Supports and loads for masonry shear wall: (a) load case 1; (b) load case 2

5.2 Nonlinear analysis

It is necessary that the nonlinear analysis starts after a linear static analysis where most checks about the model are performed and the global stiffness matrix is assembled for the first time. Also a series of commands are necessary to define the types of nonlinearity in the model and the combinations of loads applied to the model. Then, we run an initial job, which includes already the initial vertical load,

 diana example2.dat non.com

Commands

non.com

```

*FILOS
*INPUT
*ELASSE
*ELMAT
*LOADS
*ORDER
*SOLVE
*NONLIN
  SEGMENT INITIA/IN30LL
  SEGMENT EXECUT/XQ31LL
  INITIA
    ANALYS PHYSIC
    OPTION TANGEN NONSYM
    USE
      INTERF
    END USE
  END INITIA
  LOADIN
    LOAD(1): (1) 1.0 /
    LOAD(2): (2) 1.0 /
  END LOADIN
  SELECT
    NODES 2110 /
    ELEMENT NONE //
  END ELEMEN
  END SELECT
  OUTPUT TABULA NONLIN
    DISPLA TOTAL GLOBAL
  END OUTPUT
  EXECUTE LOAD(1) STEPS
    SIZE 0.5(2) /
    PERFOR NEWTON REGULA MI=15
    NORM ENERGY NEWREF CONTIN CO=1.d-6 AB=1.d+4
  END EXECUTE STEPS
*POST/CI30LL
  SEGMENT WRITE/WR30LL
  LAYOUT
    MODEL.E LI=..
    ELEMEN.
    NODES. DATA.E LI=-
  END LAYOUT
  OUTPUT GRAPHI NONLIN FI="d"
    TEXT "Total displacements"
    DISPLA TOTAL
  END OUTPUT
  LAYOUT
    MODEL.E LI=-
    ELEMEN. DATA.F
  END LAYOUT
  OUTPUT GRAPHI NONLIN FI="s"
    TEXT "Principal stresses"
    STRESS TOTAL PRINCI XX YY INTPNT
  END OUTPUT
  LAYOUT
    MODEL.E LI=-
    ELEMEN. DATA.F6
  END LAYOUT
  OUTPUT GRAPHI NONLIN FI="u"

```

```

TEXT "Relative displacement normal to interface"
  STRAIN FORCE N INTPNT FR=0.d0
END OUTPUT
*END

```

At this stage, nonlinearities were already encountered. We proceed, with the nonlinear analysis under the special interface arc-length procedure, `SELECT ARCLLEN INTTOT`. We execute a first small load step of 0.1 (= 0.1 kN) for `LOAD(2)` followed by five steps of 2.5. The small load step is necessary, because the structure must accommodate a completely different load. This is followed by fourteen load steps of 1.0 and one load step of 0.02 when the response is almost flat.

After each run, we run Module POST, to make plots of the deformed structure, the principal stresses and the normal opening of the joints as a representation of cracking in the joints and units.

The new steps, are performed with the run commands

```

diana example1.dat nonlin1.com
diana example2.dat nonlin2.dat

```

Commands

nonlin1.com

```

*NONLIN/CI33LL
SEGMENT EXECUT/XQ31LL
SELECT
  NODES 2110 /
  ELEMENT NONE //
  END ELEMEN
END SELECT
OUTPUT TABULA NONLIN
  DISPLA TOTAL GLOBAL
END OUTPUT
SELECT ARCLLEN INTTOT
END SELECT ARCLLEN
EXECUTE LOAD(2) STEPS
  LINE SEARCH
  SIZE.P 0.1(1) 2.5(5) /
  PERFOR.R NEWTON REGULA MI=15
  NORM ENERGY NEWREF CONTIN CO=1.d-6 AB=1.d+4
END EXECUTE STEPS
*POST
:   like nonlin1.com

```

28 lines skipped

Commands

nonlin2.com

```

*NONLIN/CI33LL
SIZE.P 1.0(14) 0.02(1) /

```

13 lines skipped

3 lines skipped


```
*POST
:   like nonlin1.com
```

28 lines skipped

After each load step, the selected data for node 2110 is written to the output file `diana.tb` as specified in the `SELECT` block. A selection of the tabulated output of the last load step is given below.

Nonlinear output

nonlin2.com

```
Analysis type      : NONLIN
Step nr.          :    23
Load factor       :   0.2567E+02
Result           : DISPLA TOTAL  TRANSL
Axes             : GLOBAL
```

Nodes	TDtX	TDtY	TDtZ
2110	-0.1218E+01	0.8588E-01	0.0000E+00

5.3 Interpretation of the results

From the tabulated output, it is possible to obtain a force-displacement diagram with the scan filter. The run command is

```
scan < diana.tb >> xy.dat
```

Filter

scan

```
awk 'BEGIN { displa_line=10; load_line=0;
           f = "%15.4e %15.4e\n"
           printf f, 0.0, 0.0
         }
     /TDtY/ { displa_line = 0 }
     /Load/ { load_line = 1 }
     {
     displa_line += 1
     if ( load_line == 1 ) { force = $4
                           load_line = 0 }
     if ( displa_line == 2 ) { disp = $2
                             printf f, -disp, force }
     }
'
```

The horizontal force-horizontal displacement diagram for the top of the wall is given in Figure 19. A very ductile type of failure was encountered. This is due to the dry friction between the rigid blocks at the ultimate stage. Nevertheless, it is noted that inelastic (hardening) behavior in the cap can be observed in the compressed toes. The other figures show the plots produced after steps 2, 8 and 23. For each load step, we plot the

deformed mesh, plotted with a solid line, the principal stresses at the integration points, plotted with a solid and dashed line, and the normal opening of all interface elements, plotted with a variable thickness solid and dashed line.

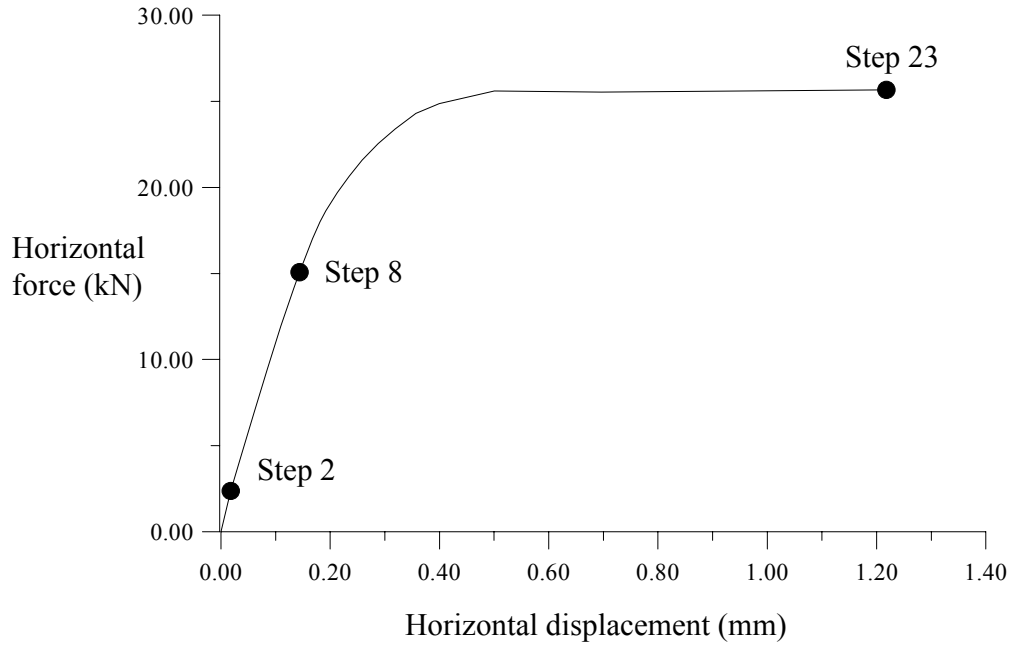
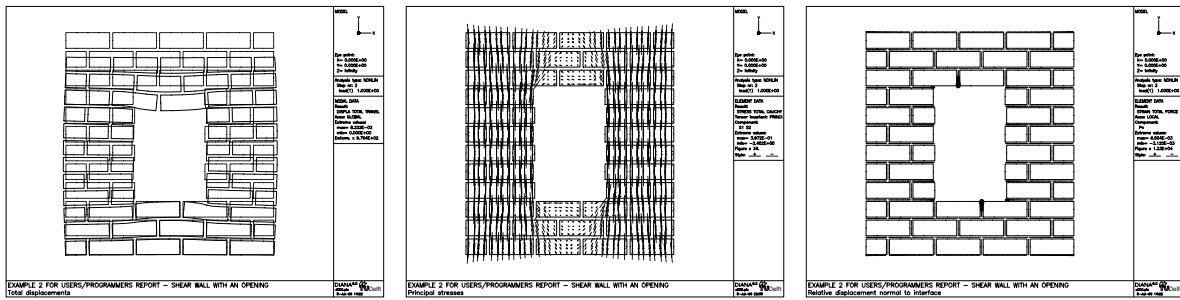
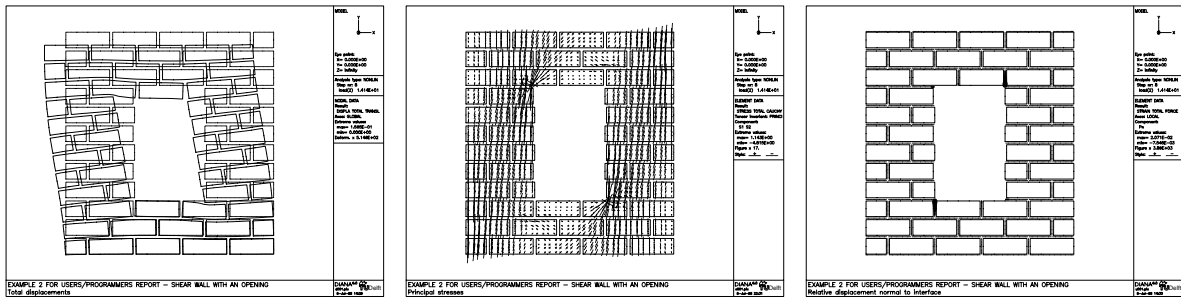


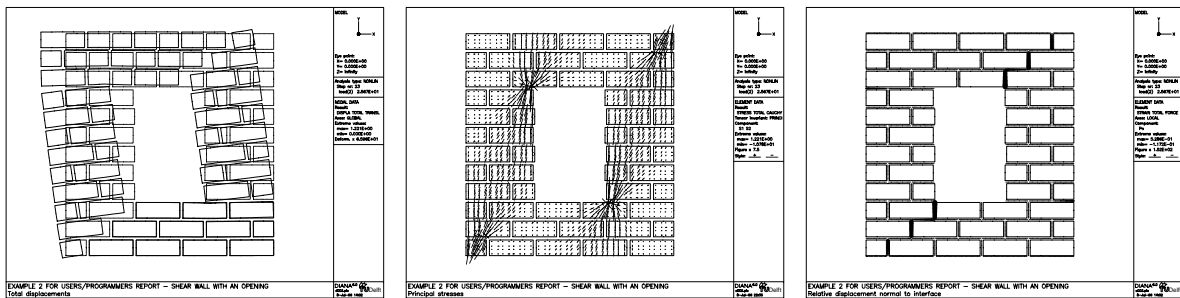
Figure 19 - Force-displacement diagram for masonry shear wall with an opening



Step 2



Step 8



Step 23

Figure 20 - Plots for masonry pier with point load: incremental deformed mesh, principal stresses and relative normal opening of interfaces

Bibliography

- ATKINSON, R.H., AMADEI, B.P., SAEB, S. and STURE, S. (1989) - Response of masonry bed joints in direct shear. *J. Struc. Engrg.*, ASCE, **115(9)**, p. 2276-2296.
- CEB (1991) - *CEB-FIP Model code 1990*. Bulletin D'Information no. **203**, **204** and **205**, Comite Euro-International du Beton, Lausanne, Switzerland.
- CEN (1995) - Eurocode 6: Design of masonry structures. ENV 1996-1-1:1995, CEN, Brussels, Belgium.
- CUR (1994) - *Structural masonry: an experimental/numerical basis for practical design rules* (in Dutch). Report **171**, CUR, Gouda, The Netherlands.
- LOURENÇO, P.B. (1996) - *Computational strategies for masonry structures*, Dissertation, Delft University of Technology, Delft, The Netherlands.
- SHELLEKENS, J.C.J. (1992) - *Computational strategies for composite structures*. Dissertation, Delft University of Technology, Delft, The Netherlands.

