

# The TPTP Problem Library

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## Abstract

This report provides a detailed description of the TPTP Problem Library for automated theorem proving systems. This library is available via Internet, and is intended to form a common basis for the development of and experimentation with automated theorem provers. To support this goal, this report provides

- the motivations for building the library;
- a discussion of troublesome issues, and how they have been resolved;
- a description of the library structure, including overview information;
- information on each problem contained in the library;
- descriptions of supplementary utility programs;
- guidelines for obtaining and using the library.

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# 1 Introduction

This technical report describes the TPTP (Thousands of Problems for Theorem Provers) Problem Library. The TPTP is a library of problems for automated theorem proving (ATP) systems, for the clause normal form (CNF) of 1st order logic. The TPTP is comprehensive, and thus provides an overview of, and a simple, unambiguous reference mechanism for, ATP problems. The TPTP problems are presented in a specifically designed, easy to understand format, and automatic conversion to other known ATP formats is provided.

The principal motivation for this project is to move the testing and evaluation of ATP systems from the previously ad hoc situation onto a firm footing. This became necessary, as results being published often do not accurately reflect the capabilities of the ATP system being considered. A common library of problems is necessary for meaningful system evaluations, meaningful system comparisons, repeatability of testing, and the production of statistically significant results. The TPTP is such a library. Since its first release in 1993, many researchers have used the TPTP as an appropriate and convenient basis for ATP system evaluation.

A Quick Installation Guide for the TPTP is given in Section 4.1 on page 34. Please be sure to read the guidelines for using TPTP problems and presenting results, given in Section 4.2.

This technical report serves as a manual explaining the structure and use of the TPTP. It also explains much of the reasoning behind the development of the TPTP, and thus implicitly explains the design decisions made. It contains the motivations for building the TPTP, a full description of the TPTP contents and organization, details of some utilities for manipulating the TPTP, and guidelines for obtaining and using the TPTP.

## What's New in TPTP v1.2.1 (since v1.2.0):

- There have been 233 bugfixes done, in the domains BOO GEO GRP HEN NUM PUZ RNG SET SYN.
- If the axiomatization used in a problem has been formed by reducing and augmenting an existing axiomatization, and the result is complete but also non-standard due to redundancy, this is noted with (**Non-standard**) in the `% Version` field.
- The `% Syntax` field has been extended to include counts of range restricted clauses, and the arity ranges of the predicate and function symbols.
- The `tptp2X` utility has been extended and improved :
  - One new output format: SPASS.
  - Two new transformations: `to_equality` and `add_equality`.
  - The equality removal has been renamed to `rm_equality`, and now fails if the equality axiomatization is incomplete.
  - The shorten transformation no longer shortens `equal` to `eq`.
- In problems where the equality axiomatization was incomplete, the `equal/2` predicate has been renamed to `equalish/2`.
- The clause type information has been reviewed and 4 corrections were made. Throughout the TPTP the problem type `theorem` has been replaced with `conjecture`.
- The TPTP technical report (this document) has been updated.

## 1.1 Previous Problem Collections

A large number of interesting problems have accumulated over the years in the ATP community. Besides publishing particularly interesting individual problems, from early on researchers collected problems in order to obtain a basis for experimentation. The first major publication<sup>1</sup> in this regard was [MOW76], which provides an explicit listing of clauses for 63 problems, many of which are still relevant today. In the same year Wilson and Minker [WM76] documented 86 problems which have since commonly been used for ATP testing. The problem clauses are not supplied in [WM76], however. A second major thrust was provided by [Pel86], which lists 75 problems. Other more recent papers are [BLM<sup>+</sup>86], [Qua92a], [MW92], and [McC93], to name a few. The Journal of Automated Reasoning's Problem Corner also provided interesting challenge problems. However, problems published in hardcopy form are often not suitable for testing ATP systems, because they have to be transcribed to electronic form. This is a cumbersome, error-prone process, and is feasible for only very small numbers of problems. A problem library in electronic form was made publicly available by Argonne National Laboratories (in Otter format, [McC94]) in 1988 [ANL]. This library has been a major source of problems for ATP researchers. Other electronic collections of problems are available, but have not been announced officially (e.g., that distributed with the SPRFN ATP system [SPR]). Although some of these collections provide significant support to researchers, and formed the early core of the TPTP library, none (with the possible exception of the ANL library) was specifically designed to serve as a common basis for ATP research. Rather, these collections typically were built in the course of research into a particular ATP system. As a result there are several factors that limit their usefulness as a common basis for research. In particular, previously existing problem collections

- are often hard to discover and obtain.  
System development and system evaluations typically rely on a small set of test problems, depending on the collections of problems available to the researcher.
- need to be transformed to suit the syntax of the ATP system being considered.  
The problem format used in a collection may not be appropriate for the desired purpose, and a comparatively large effort is required just to make the problems locally usable (which in practice often means that such a collection of problems is simply ignored).
- are often limited in scope and size.  
The problems used are often homogeneous, and thus cannot be used for a broad test of the capabilities of the ATP system under consideration. If there are too few problems, statistically significant testing is not possible.
- may be outdated.  
The problems may insufficiently reflect the current state-of-the-art in ATP research.
- are sometimes designed and tuned (regarding clause selection, clause ordering, and literal ordering) for a particular ATP system.  
Using a collection designed and tuned for a particular ATP system may lead to biases in results.

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<sup>1</sup>To our knowledge, the first circulation of problems for testing ATP systems was due to L. Wos in the late sixties.

- provide no indication of the difficulty or significance of the problems.  
The significance and difficulty of a problem, with respect to the current state-of-the-art in ATP systems, is hard to assess by newcomers to the field. Existing test problems are often not adequate anymore (e.g., Schubert’s Steamroller [Sti86]), while others may be solvable only with specialized techniques (e.g., LIM+ [Ble90]) and therefore are much too hard to start with.
- are inconsistent in their presentation of equally named problems.  
Many copies and variants of the same “original” problem may exist in different libraries. This means that unambiguous identification of problems, and therefore a clear interpretation of performance figures, for given problems, has become difficult.
- are usually undocumented.  
It is hard to obtain information on problem semantics, the original problem source, and the particular style of axiomatization. It also contributes to the problem of unambiguous problem identification.
- are almost always unserved.  
They do not provide a mechanism for adding new problems or correcting errors in existing problems, and cannot be used to electronically distribute new and corrected problems to the ATP community. This in turn perpetuates the use of old and erroneous problems.
- provide no guidelines for their use.  
Quite often, inadequate system evaluations are performed. As a consequence, results that provide little indication of the system properties are reported.

The problem of meaningfully interpreting results is even worse than indicated. Commonly a few problems are selected and hand-tuned (clauses and literals are arranged in a special order, irrelevant clauses are omitted, lemmas are added in, etc) specifically for the ATP system being tested. The presentation of a problem can significantly affect the nature of the problem, and changing the clauses clearly makes a different problem altogether. Nevertheless the problem may be referenced under the same name as it was presented elsewhere. As a consequence the experimental results reveal little. Some researchers avoid this ambiguity by listing the clause sets explicitly, but obviously this usually cannot be done for a large number of problems or for large individual problems. The only satisfactory solution to these issues is a common and stable library of problems. The TPTP is such a library.

## 1.2 What is Required?

The goal for building the TPTP has been to overcome previous drawbacks, and to centralize the burden of problem collection and maintenance to one place. The TPTP tries to address all relevant issues. In particular, the TPTP

- is easy to discover and obtain.  
Awareness of the TPTP is assured by extensive formal and informal announcements. The TPTP is available by anonymous ftp, and is thus easily available to the research community.

- is easy to use.  
Problems are presented in a specifically designed, easy to understand format. Automatic conversion to other known formats is also provided, thus eliminating the necessity for transcription.
- spans a diversity of subject matters.  
This reduces biases in the development and testing of ATP systems, which arise from the use of a limited scope of problems. It also provides an overview of the domains that ATP systems are used in.
- is large enough for statistically significant testing.  
In contrast to common practise, an ATP system should be evaluated over a large number of problems, rather than a small set of judiciously selected examples. The large size of the TPTP makes this possible.
- is comprehensive.  
The TPTP contains all problems known to the community. There is no longer a need to look elsewhere.
- is up-to-date.  
As new problems appear in the literature and elsewhere (see the paragraph Sources on page 7), they are added to the TPTP as soon as possible.
- is independent of any particular ATP system.  
The problem clauses are arranged so as to be modular and human-readable, rather than arranged for a particular ATP system.
- contains problems varying in difficulty.  
The difficulty of problems in the TPTP ranges from very simple problems through to open problems. This allows all interested researchers, from newcomers to experts, to rely on the same problem library.
- will provide a rating for the difficulty of each problem.  
This is important for several reasons: (1) It simplifies problem selection according to the user's intention. (2) It allows the quality of an ATP system to be judged. (3) Over the years, changes in the problem ratings will provide an indicator of the advancement in ATP. The problem ratings are currently being worked on, and will be part of a future TPTP release.
- provides statistics for each problem and the library as a whole.  
This provides information about the syntactic nature of the problems.
- has an unambiguous naming scheme.  
This provides unambiguous problem reference, and makes the comparison of results meaningful. See Section 2.4 for details.
- is well structured and documented.  
This allows effective and efficient use of library. Useful background information, such as an overview of ATP application domains, is provided.
- documents each problem.  
This contributes to the unambiguous identification of each problem.

- provides a mechanism for adding new problems.  
The TPTP contains standard axiomatizations that can be used in new problems. This simplifies the construction of new problems (see Section 4.3). A template is provided for submission of new problems. The TPTP is thus a channel for making new problems available to the community, in a simple and effective way.
- provides a mechanism for correcting errors in existing problems.  
TPTP users can report errors, and these are corrected immediately. Patched TPTP releases are made regularly.
- provides guidelines for its use in evaluating ATP systems.  
A standard library of problems together with evaluation guidelines makes reported results meaningful and reproducible by others. This will in turn simplify and improve system comparisons, and allow ATP researchers to accurately gauge their progress.

The development of the TPTP problem library is an ongoing project, with the aim to provide all of the desired properties. Typical issues that have to be considered when building and maintaining a problem library are listed below, together with some clue of how they have been attacked in the TPTP.

- Accuracy  
Problems are thoroughly checked before release, and errors are corrected on notice.
- Consistency  
A modular problem representation is used (see Section 2.2).
- Documentation of the problems and axiomatizations  
Important information is taken from the source of the problem or axiomatization, and presented with the problem or axiomatization. In some cases the original authors have been contacted to obtain more information.
- Comprehensiveness  
All problem sources known to the ATP community are considered. The library is updated whenever new problems are found or proposed (see also the paragraph Sources on page 7).
- Unambiguous identification of problems  
A naming scheme has been developed to provide unambiguous names for problems and axiomatizations (see Section 2.4).

**Current Limitations of the TPTP.** The current release of the TPTP library is limited to problems expressed in 1st order logic, presented in clause normal form. There are no problems in first order form, for induction, or for non-classical theorem proving. However, see Section 5 for upcoming and planned extensions.

## 2 Inside the TPTP

**Scope.** Release v1.2.1 of the TPTP contains 2044 abstract problems, which result in 2752 ATP problems, due to alternative presentations (see Section 2.2). Tables 1, 2, and 3 provide some statistics about release v1.2.1 of the TPTP.

Number of problem domains	25
Number of abstract problems	2044
Number of generic problems	85
Number of problems	2752
Number of non-Horn problems	1486 (54%)
Number of range restricted problems	105 (4%)
Number of problems with equality	1920 (70%)
Number of pure equality problems	493 (18%)
Number of satisfiable problems	$\geq 59$ (2%)
Number of propositional problems	42 (2%)
... being non-Horn	30 (1%)
... being satisfiable	6 (0%)
Total number of clauses	323074
Total number of literals	743104

Table 1: Statistics on the TPTP.

The problems in the TPTP are syntactically diverse, as is indicated by the ranges of the values in Tables 2 and 3. The problems in the TPTP are also semantically diverse, as is indicated by the range of domains that are covered. The problems are grouped into 25 domains, covering topics in the fields of logic, mathematics, computer science, engineering, and others. The domains are presented and discussed in Section 2.1.

**Sources.** The problems have been collected from various sources. The two principal sources have been existing electronic problem collections and the ATP literature. Other sources include logic programming, mathematics, puzzles, and correspondence with ATP researchers. Many people and organizations have contributed towards the TPTP. In particular, the foundations of the TPTP were laid with David Plaisted’s SPRFN collection; many problems have been taken from Argonne National Laboratory’s ATP problem library (special thanks to Bill McCune here); Art Quaife has provided several hundred problems in set theory and algebra; the Journal of Automated Reasoning, CADE Proceedings, and Association for Automated Reasoning Newsletters have provided a wealth of material; smaller numbers of problems have been provided by a number of further contributors (see the Acknowledgements at the end of Section 5).

**Releases.** The TPTP is managed in the manner of a software product, in the sense that fixed releases are made. Each release of the TPTP is identified by a release number, in the form v<Version>.<Edition>.<Patch level>. The Version number enumerates major new releases of the TPTP, in which important new features have been added. The Edition number is incremented each time new problems are added to the current version. The

Measure	Minimum	Maximum	Average	Median
Number of clauses	2	504	118	54
Percentage of non-Horn clauses	0%	99%	5%	4%
... in non-Horn problems	2%	99%	9%	5%
Percentage of unit clauses	0%	100%	34%	22%
Percentage of range restricted clauses	0%	100%	60%	63%
Number of literals	2	1512	273	129
Percentage of equality literals	0%	100%	43%	46%
... in equality problems	19%	100%	61%	47%
Maximal clause size	1	25	4	5
Number of predicate symbols	1	48	9	3
Percentage of propositions	0%	67%	0%	0%
Minimal predicate arities	0	5	1	1
Maximal predicate arities	1	10	2	3
Number of functors	1	93	23	9
Percentage of constants	0%	100%	50%	50%
Minimal functor arities	0	2	0	0
Maximal functor arities	0	8	2	2
Number of variables	0	1094	269	130
Percentage of singletons	0%	100%	8%	7%
Maximal term depth	1	14	4	4

Table 2: Statistics for non-propositional TPTP problems.

Patch level is incremented each time errors, found in the current edition, are corrected. All non-trivial changes are recorded in a history file, as well as in the file for an affected problem.

## 2.1 The TPTP Domain Structure

This section provides the structure according to which the problems are grouped into domains. Some information about the domains is also given.

Measure	Minimum	Maximum	Average	Median
Number of clauses	3	82	24	18
Percentage of non-Horn clauses	0%	81%	25%	25%
... in non-Horn problems	8%	81%	35%	33%
Percentage of unit clauses	0%	100%	19%	13%
Number of literals	4	232	64	40
Maximal clause size	1	11	3	3
Number of predicate symbols	2	63	13	11

Table 3: Statistics for propositional TPTP problems.



An attempt has been made to classify the totality of the TPTP problems in a systematic and natural way. The resulting domain scheme reflects the natural hierarchy of scientific domains, as presented in standard subject classification literature. The current classification is based mainly on the Dewey Decimal Classification (DDC) [Dew89] and the Mathematics Subject Classification (MSC) [MSC92] used for the Mathematical Reviews by the American Mathematical Society. Five main fields are defined: logic, mathematics, computer science, engineering, and other. Each field contains further subdivisions, called *domains*. Each domain is identified by a three-letter mnemonic. These mnemonics are also part of the problem naming scheme (see Section 2.4). The TPTP domains constitute the basic units of our classification. The full classification scheme is shown in Figure 1.

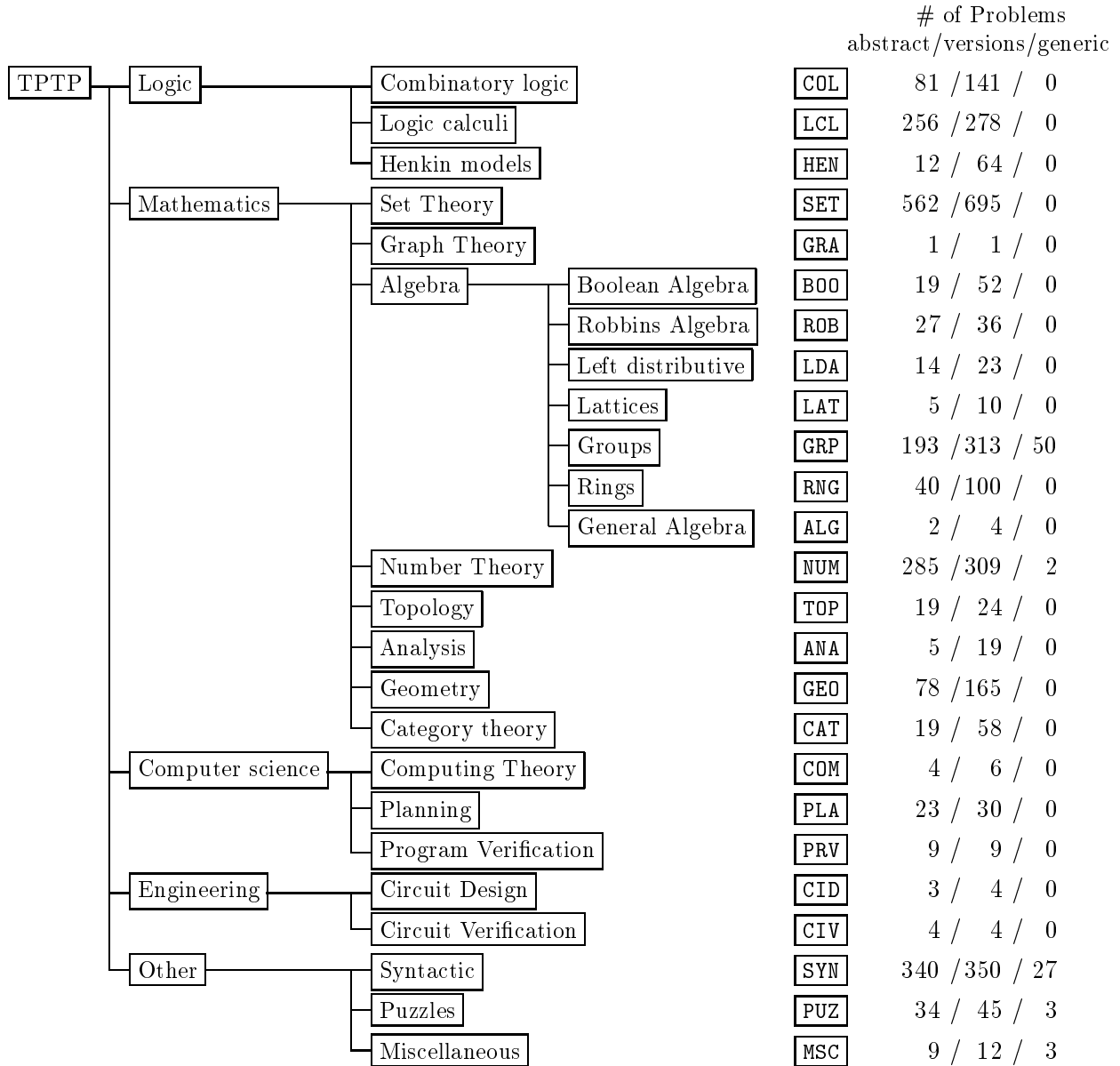


Figure 1: The domain structure of the TPTP.

A brief description of the domains, with a non-ATP reference for a general introduction and a generic ATP reference, is given below. For each domain, appropriate DDC and MSC

numbers are also given:

COL *Combinatory Logic.*

Combinatory logic is about applying one function to another. It can be viewed as an alternative foundation of mathematics (or, due to its Turing-completeness, as a programming language). More formally, it is a system satisfying two combinators and satisfying reflexivity, symmetry, transitivity, and two equality substitution axioms for the function that exists implicitly for applying one combinator to another.

Indices : MSC 03B40

References : General [CF58, CHS72, Bar81], ATP [WM88b].

LCL *Logic Calculi.*

A logic calculus defines axioms and rules of inference that can be used to prove theorems. This domain currently contains the following logical calculi:

- Implication/Negation 2 valued modal
- Implication/Negation 2 valued sentential (CN-calculus)
- Implicational propositional (IC-calculus, negation-free part of sentential calc.)
- Implication/Falsehood 2 valued sentential (C0-calculus)
- Disjunction/Negation 2 valued sentential (AN-calculus)
- Many valued sentential (MV-calculus)
- Equivalential (EC-calculus, theorems represent group identity in Boolean groups)
- R (under some constraint, theorems represent identity in Abelian groups)
- Left group (LG-calculus, under some constraint theorems represent formulas equal to identity in groups)
- Right group (RG-calculus, theorems are related to identity in groups)
- Wajsberg Algebra.

The following relations hold between theorems of the above calculi: LG theorems  $\subset$  L theorems  $\subset$  EC theorems, RG theorems  $\subset$  R theorems  $\subset$  EC theorems.

Indices : DDC 511.3, MSC 03XX

References : General [Luk63], ATP [MW92]

HEN *Henkin Models.*

Henkin models provide a generalized semantics for higher order logics. This leads to a larger class of models and, as a consequence, fewer true sentences. However, in contrast to standard semantics, complete and correct calculi can be found.

Indices : MSC 03CXX

References : General [Hen50, Leb83].

SET *Set Theory.*

Classically, a set is a totality of certain definite, distinguishable objects of our intuition or thought - called the elements of the set. Due to paradoxes that arise from such a naive definition, mathematicians now regard the notion of a set as an undefined, primitive concept [How72]. In this domain, Naive and Neumann-Bernays-Gödel axiom sets are used.

Indices : DDC 511.322, MSC 03EXX, 04XX

References : General [Neu25, Qui69], ATP [Qua92b].

GRA *Graph Theory.*

A graph consists of a finite non-empty set of points together with a prescribed set of pairs of points.

Indices : MSC 05CXX, 68R10

References : General [Har69, BB70], ATP –.

- BOO** *Boolean Algebra.*  
 A Boolean algebra is a set of elements with two binary operations which are idempotent, commutative, and associative. These operations are mutually distributive, there exist universal bounds 0, 1, and there is a unary operation of complementation.  
 Indices : DDC 511.324, MSC 06EXX  
 References : General [Whi61, BM65, BB70], ATP -.
- ROB** *Robbins Algebra.*  
 Problems which demand conditions that make a near-Boolean algebra Boolean (the Robbins problem).  
 References : General [HMT71], ATP [Win90].
- LDA** *Left Distributive Algebra.*  
 LD-algebras are related to large cardinals. Under a very strong large cardinal assumption, the free-monogenic LD-algebra can be represented by an algebra of elementary embeddings. Theorems about this algebra can be proved from a small number of properties, suggesting the definition of an embedding algebra.  
 References : General -, ATP [Jec93a].
- LAT** *Lattice Theory.*  
 A lattice is a set of elements, with two binary operations which are idempotent, commutative, and associative, and which satisfy the absorption law.  
 Indices : MSC 06BXX  
 References : General [BM65], ATP [McC88].
- GRP** *Group Theory.*  
 A group is a system of elements which is closed under a single-valued binary operation which is associative, and relative to which there exists an element satisfying the identity law, and with each element another element (called its inverse) satisfying the inverse law.  
 Indices : DDC 512.2, MSC 20  
 References : General [Bou89, BM65], ATP [MOW76].
- RNG** *Ring Theory.*  
 A ring is a system of elements which is an Abelian group under an operation of addition, and which is closed under a binary operation of multiplication, the latter being associative, and distributive with respect to addition.  
 Indices : DDC 512.4, MSC 13XX, 16XX  
 References : General [Bou89, BB70], ATP [MOW76].
- ALG** *Algebra.*  
 An algebra is a set with a system of operations defined on it.  
 Indices : DDC 512  
 References : General [Bou89, BM65, BB70], ATP -.
- NUM** *Number Theory.*  
 Number theory is the study of integers and their properties.  
 Indices : MSC 11YXX  
 References : General [HW92], ATP [Qua92b].
- TOP** *Topology.*  
 Topology is the study of properties of geometric configurations (e.g., point sets) which are unaltered by elastic deformations (homeomorphisms, i.e., functions that are 1-1 mappings between sets such that both the function and its inverse are continuous).

- Indices : DDC 514, MSC 46AXX  
References : General [Kel55, Mun75], ATP [WM89].
- ANA *Analysis.*  
Analysis is a branch of mathematics concerned with functions and limits. The main parts of analysis are differential calculus, integral calculus, and the theory of functions.  
Indices : DDC 515, MSC 26XX  
References : General [Ros90], ATP [Ble90].
- GEO *Geometry.*  
Geometry is a branch of mathematics that deals with the measurement, properties, and relationships of points, lines, angles, surfaces, and solids. Here: plane geometry, based on Tarski's axiom system for Euclidean geometry.  
Indices : DDC 516, MSC 51  
References : General [Tar51, Tar59], ATP [Qua92b].
- CAT *Category Theory.*  
A category is a mathematical structure together with the morphisms that preserve this structure.  
Indices : MSC 18XX  
References : General [Mac71], ATP [MOW76].
- COM *Computing Theory.*  
Computing theory is a subfield of computer science dealing with theoretical issues such as decidability (whether or not a given problem admits an algorithmic solution), completeness (does an algorithm always find a solution if one exists?), correctness (are only solutions produced?), and computational complexity (the resource requirements of algorithms).  
Indices : DDC 004-006, MSC 68
- PLA *Planning.*  
Planning is the process of determining the sequence of actions to be performed by an agent, to reach a desired state. The initial state and the desired state are provided.  
Indices : MSC 68T99  
References : General [AKPT91], ATP [Pla81, Pla82].
- PRV *Program Verification.*  
Program verification formally establishes that a computer program does the task it is designed for. This typically requires extracting and examining the semantics of the program being verified.  
Indices : DDC 005.14, MSC 68Q60  
References : General -, ATP [WOLB92, MOW76].
- CID *Circuit Design.*  
Circuits are formed by inter-connecting logic gates. Circuit design is used to form a circuit that will transform given input patterns to required output patterns.  
Indices : DDC 621.395, MSC 94CXX  
References : General [Hay93], ATP [WW83].
- CIV *Circuit Verification.*  
Circuit verification is used to ensure that a previously designed circuit performs the desired transformation of input patterns to required output patterns. One approach is to check the performance of the circuit for every possible combination of given inputs. Other techniques are also used.

- Indices : DDC 621.395, MSC 94CXX  
References : General [Hay93], ATP [Woj83].
- SYN *Syntactic.*  
Syntactic problems have no obvious semantic interpretation.
- PUZ *Puzzles.*  
Puzzles are designed to test the ingenuity of humans.  
References : General [Car86, Smu78b, Smu78a].
- MSC *Miscellaneous.*  
A collection of problems which do not fit well into any other domain.

## 2.2 Problem Versions and Standard Axiomatizations.

There are often many ways to formulate a problem for presentation to an ATP system. Thus, in the TPTP, there are often alternative presentations of a problem. The alternative presentations are called *versions* of the underlying *abstract problem*. As the problem versions are the objects that ATP systems must deal with, they are referred to simply as problems, and the abstract problems are referred to explicitly. Each problem is stored in a separate physical file. The primary reason for different versions of an abstract problem, is the use of different axiomatizations. This issue is discussed below. A secondary reason is different formulations of the theorem to be proved.

### Different Axiomatizations

Commonly, many different axiomatizations of a theory exist. In the TPTP an axiomatization is *standard* if it is complete (in the sense that it captures some closed theory) and it has not had any lemmas added. (Note: A standard axiomatization may be redundant, because some axioms are dependent on others. In general, it is not known whether or not an axiomatization is minimal, and thus the possibility of redundancy in standard axiomatizations must be tolerated.) In the TPTP, standard axiomatizations are kept in separate axiom files, and are included in problems as appropriate. If an axiomatization uses equality, the required axioms of substitution are kept separate from the theory specific axioms. The equality axioms of reflexivity, symmetry, and transitivity, which are also required when equality is present, are also kept separately. By using different standard axiomatizations of a particular theory, different versions of a problem can be formed. A side effect of separating out the axioms into axiom files is that the clause order in the TPTP presentation of problems is typically different from that of any original presentation. This reordering is acceptable because the performance of a decent ATP system should not be very dependent on a particular clause ordering in the TPTP.

Within the ATP community, some problems have been created with *non-standard* axiomatizations. A non-standard axiomatization is formed by modifying a standard axiomatization. The standard axiomatization may be *reduced* (i.e., axioms are removed) and the result is an *incomplete* axiomatization, or it may be *augmented* (i.e., lemmas are added) and the result is a *redundant* axiomatization. Non-standard axiomatizations are typically used to find a proof of a theorem (based on the axiomatization) using a particular ATP system. In any 'real' application of an ATP system, a standard axiomatization of the application domain would typically have to be used, at least initially. Thus the use of standard axiomatizations is desirable, because it reflects such 'real' usage. In the TPTP,

for each collected problem that uses a non-standard axiomatization, a new version of the problem is created with a standard axiomatization.

There are some TPTP problems in which the axioms cannot be obtained by reducing or augmenting a standard axiomatization. These axiomatizations are called **special** axiomatizations. Typically, such axiomatizations are each used in only one problem.

### Equality Axiomatization

In the TPTP equality is represented using the `equal/2` predicate, written in prefix notation like all other predicates. The `equal/2` predicate is used only if the equality axiomatization in the problem is complete, i.e., including the axioms of reflexivity, symmetry, transitivity, function substitution for all functors, and predicate substitution for all predicate symbols. If the equality axiomatization is not complete, but the 'intention' is to represent equality, the `equalish/2` predicate is used. The TPTP problems containing the `equal/2` predicate do contain a complete equality axiomatization.

Many ATP systems have built in mechanisms, e.g., paramodulation, that make some or all of the equality and substitution axioms unnecessary. If any of these axioms are removed when the problems are submitted to an ATP system, then the removal must be explicitly noted in reported results (see Section 4.2). The `tptp2X` utility (see Section 3.1) can be used to remove equality axioms.

## 2.3 Problem Generators

Some abstract problems have a generic nature, and particular instances of the abstract problem are formed according to some size parameter(s). An example of a generic problem is the  $N$ -queens problem: place  $N$  queens on a  $N \times N$  chess board such that no queen attacks another. The clauses for any size of this problem can be generated automatically, for any size of  $N \geq 2$  (note that for this problem satisfiability depends on the problem size).

Up to TPTP v1.1.3, the TPTP simply contained problem files for particular sizes of generic problems. This, however, was undesirable. Firstly, only a finite number of different problem sizes could be included, and therefore a desired size may be missing. Secondly, even a small number of different problem sizes for each generic problem could consume a considerable amount of disk space. To overcome these problems the TPTP now contains *generator* files. Generator files are used to generate instances of generic problems, according to user supplied size parameters. The generators are used in conjunction with the `tptp2X` utility, and a full description of their use is given in Section 3.1.

For convenience, the TPTP still contains a particular instance of each generic problem. The size chosen for each such instance is a compromise between being large enough to be non-trivial for the SETHEO ATP system [LSBB92] and small enough to avoid using too much disk space. As result data for other systems are obtained, these sizes might change in the next TPTP release, in order to remove the current bias towards the SETHEO system. An unsatisfiable size is chosen where ever one exists. The statistics in Tables 1, 2, and 3 take into account these instances of generic problems.

## 2.4 Problem, Generator, and Axiomatization Naming

Providing unambiguous names for all problems is necessary in a problem library. A naming scheme has been developed for the TPTP, to provide unique, stable names for abstract problems, problems, generators, and axiomatizations. Files are assigned names according to the schemes depicted in Figures 2 and 3. The `DDDNNN` combination provides an unambiguous name for an abstract problem or axiomatization. The `DDDNNN-V[.SSS]` combination provides an unambiguous name for a problem or generator, and the `DDDNNN-E` combination provides an unambiguous name for a group of axioms. The complete file names are unique within the TPTP.

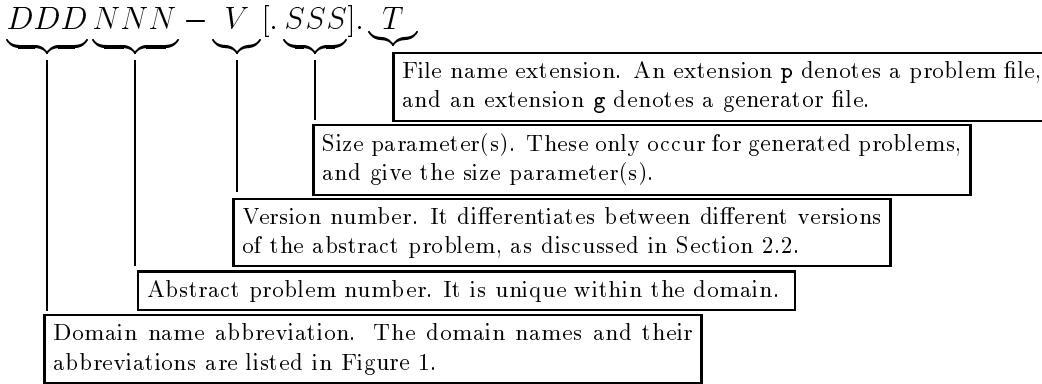


Figure 2: Problem file naming scheme.

The abstract problem numbers within each domain are not always successive. This is because some numbers have already been allocated to non-CNF problems, which will be part of a future TPTP release (see Section 5.1).

The version numbers used for each abstract problem do not always start at 1, and are not necessarily contiguous. This arises out of assigning (where ever possible) the same version number to all problems that come from the same source, within each domain.

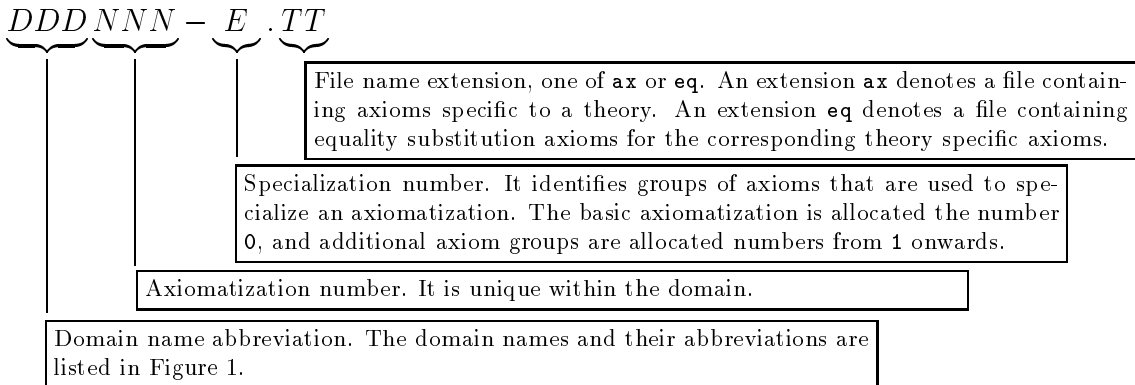


Figure 3: Axiom file naming scheme.

If a file is ever removed from or renamed in the TPTP, then the extension is changed to

`.rm`. The file is not physically removed, and a comment is added to the file to explain what has happened. This mechanism maintains the unique identification of problems and axiomatizations.

**Semantic Names.** Abstract problems and axiomatizations have also been allocated semantic names. The semantic names can be used to augment file names, so as to provide an indication of the file contents. While these names are provided for users who like to work with mnemonic names, only the standard syntactic names are guaranteed to provide unambiguous reference. The semantic names are formed from a set of abbreviations, which are listed in Appendix 9.1. The semantic names can be added to the syntactic file names using the `tptp_naming` script, as described in Section 3.2. Syntactic names of the form `DDDNN-K.Ext` and `DDDNN-K.SSS.Ext` are transformed to `DDDNN-K=SemanticName.Ext` and `DDDNN-K.SSS=SemanticName.Ext`, respectively. The TPTP is distributed without the semantic names in use.

## 2.5 Problem Presentation

The physical presentation of the TPTP problem library is such that ATP researchers can easily use the problems. The TPTP file format, for problem files and axiom files, has three main sections. The first section is a header section that contains information for the user. This information is not for use by ATP systems (see Section 4.2). The second section contains `include` instructions for axiom files. The last section contains the clauses that are specific to the problem or axiomatization. TPTP generator files have three sections, different from the problem and axiom files. The header section of generator files is similar to that of problem and axiom files, but with place-holders for information that is filled in based on the size of problem and the clauses generated. Following that comes Prolog source code to generate the clauses, and finally data describing the permissible sizes and the chosen TPTP size for the problem. More details are given in Section 3.1.7.

The syntax of all files is that of Prolog. This conformance makes it trivial to manipulate the files using Prolog. All information in the files that is not for use by ATP systems is formatted as Prolog comments, with a leading `%`. All the information for ATP systems is formatted as Prolog facts. A utility is provided for converting TPTP files to other known ATP system formats (see Section 3.1). A description of the information contained in TPTP files is given below.

### 2.5.1 The Header Section

This section contains information about the problem, for the user. It is divided into four parts. The first part identifies and describes the problem. The second part provides information about occurrences of the problem. The third part gives the problem's ATP status and a table of syntactic measurements made on the problem. The last part contains general information about the problem. An example of a TPTP header, extracted from the problem file `GRP039-7.p`, is shown in Figure 4.

**The `% File` field.** This field contains three items of information. The first item is the problem's name. This is displayed in the format `<Abstract problem name>=<Semantic name>-<Problem version>[.<Size>]`.



```

%-----
% File      : GRP039=SubGI2Norm-7 : TPTP v1.2.1. Bugfixed v1.0.1.
% Domain   : Group Theory (Subgroups)
% Problem  : Subgroups of index 2 are normal
% Version  : [McCharen, et al., 1976] (equality) axioms : Augmented.
% English  : If 0 is a subgroup of G and there are exactly 2 cosets
%           in G/0, then 0 is normal [that is, for all x in G and
%           y in 0, x*y*inverse(x) is back in 0].

% Refs    : McCharen J.D., Overbeek R.A., Wos L.A. (1976), Problems and
%           Experiments for and with Automated Theorem Proving Programs
%           IEEE Transactions on Computers C-25(8), 773-782.
% Source   : [McCharen, et al., 1976]
% Names    : GP2 [McCharen, et al., 1976]

% Status   : unsatisfiable
% Syntax   : Number of clauses      : 25 ( 2 non-Horn; 13 unit; 12 RR)
%           Number of literals     : 43 ( 28 equality)
%           Maximal clause size    : 4
%           Number of predicates   : 2 ( 0 propositional; 1-2 arity)
%           Number of functors     : 8 ( 5 constant; 0-2 arity)
%           Number of variables    : 38 ( 0 singleton)
%           Maximal term depth     : 3

% Comments : Used to define a subgroup of index two is a theorem which
%           says that {for all x, for all y, there exists a z such that
%           ... (some lines removed here for brevity)
% Bugfixes : v1.0.1 - Duplicate axioms multiply_inverse_left and
%           multiply_inverse_right removed.
%-----

```

Figure 4: Example of a problem file header (GRP039-7.p).

The current TPTP release number is given next, followed by the TPTP release in which the problem was released or last bugfixed (i.e., the clauses were changed). The abstract problem name in Figure 4 is GRP039, the semantic name is SubGI2Norm, and the problem version is 7. The TPTP release is v1.2.1, and the problem clauses were last bugfixed in release v1.0.1.

**The % Domain field.** The domain field identifies the domain, and possibly a subdomain, from which the problem is drawn (see Section 2.1). The domain corresponds to the first three letters of the problem name. The domain of the problem of Figure 4 is Group Theory, and the subdomain is Subgroups.

**The % Problem field.** This field provides a one-line, high-level description of the abstract problem. In axiom files, this field is called % Axioms, and provides a one-line, high-level description of the axiomatization. Thus, the problem of Figure 4 proves that Subgroups of index 2 are normal.

**The % Version field.** This field gives information that differentiates this version of the problem from other versions of the problem. The first possible differentiation is the axiomatization that is used. If a specific axiomatization is used, a citation is provided. In the problem of Figure 4, the axiomatization used is that of [McCharen, et al., 1976]. If the axiomatization is a pure equality axiomatization (uses only the `equal/2` predicate) then this is noted too, as is the case in Figure 4. The second possible differentiation is the status of the axiomatization, as discussed in Section 2.2. The axiomatization used may be an original axiomatization, or it may have been derived from an existing axiomatization. If it is an original axiomatization and is standard, then no further information is given in this part of the % Version field. If it is an `Incomplete` original axiomatization, then this is noted alone. If the axiomatization used has been derived from an `Incomplete` existing axiomatization, then this is noted followed by a `>` separator. The derivation information is given next. The derivation information tells whether the previously existing axiomatization has been `Reduced`, `Augmented`, or both. In all cases where an axiomatization has been `Reduced`, and in cases where an `Incomplete` axiomatization has been `Augmented`, the resultant status of the axiomatization is noted next, after a `>`. The resultant status is one of `Complete` or `Incomplete`. Altogether, there are 12 possibilities:

- `<empty>`. Indicates that the axiomatization is original and standard, i.e., it is complete and has had no lemmas added (it may be redundant).
- `Incomplete`. Indicates that the axiomatization is original and incomplete.
- `Reduced > Complete`. Indicates that a standard existing axiomatization has had axioms removed, and the result is complete. The existing axiomatization is necessarily redundant.
- `Reduced > Incomplete`. Indicates that a standard existing axiomatization has had axioms removed, and the result is non-standard due to incompleteness.
- `Augmented`. Indicates that a standard existing axiomatization has had lemmas added, and the result is non-standard due to redundancy.
- `Reduced & Augmented > Complete`. Indicates that a standard existing axiomatization has had axioms removed and lemmas added, and the result is complete. If the axiomatization is non-standard due to redundancy, this is noted with `(Non-standard)` after `Complete`.
- `Reduced & Augmented > Incomplete`. Indicates that a standard existing axiomatization has had axioms removed and lemmas added, and the result is non-standard due to incompleteness.
- `Incomplete > Reduced > Incomplete`. Indicates that an incomplete existing axiomatization has had axioms removed, and the result is non-standard due to incompleteness.
- `Incomplete > Augmented > Complete`. Indicates that an incomplete existing axiomatization has had axioms added, and the result is complete.
- `Incomplete > Augmented > Incomplete`. Indicates that an incomplete existing axiomatization has had lemmas added, and the result is non-standard due to incompleteness.
- `Incomplete > Reduced & Augmented > Complete`. Indicates that an incomplete existing axiomatization has had axioms removed and lemmas added, and the result is complete. If the axiomatization is non-standard due to redundancy, this is noted with `(Non-standard)` after `Complete`.
- `Incomplete > Reduced & Augmented > Incomplete`. Indicates that an incomplete existing axiomatization has had axioms removed and lemmas added, and the result is

non-standard due to incompleteness.

In the problem of Figure 4, a standard axiomatization has been **Augmented**, and has become non-standard due to redundancy.

The third possible differentiation between problem versions is in the theorem formulation. Variations in the theorem formulation are noted in a **Theorem formulation** entry, e.g.,

```
% Version : [McCharen, et al., 1976] (equality) axioms.
```

```
% Theorem formulation : Explicit formulation of the commutator.
```

**The % English field.** This field provides a full description of the problem, if the one-line description in the **% Problem** field is too terse.

**The % Refs field.** This field provides a list of references to items in which the problem has been presented. Other references that are cited in the header section are also listed.

**The % Source field.** The problems in the TPTP have been (physically) obtained from a variety of sources, both hardcopy and electronic. In this field the source of the problem is acknowledged, usually as a citation. If the problem was sourced from an existing problem collection then the collection name is given in [ ] brackets. The problem collections used thus far are:

- ANL - the Argonne National Laboratory library [ANL],
- OTTER - the collection distributed with the Otter ATP system [McC90, McC94]
- Quaife - Art Quaife's collection of set theory (based) problems [Qua92d]
- ROO - the problems used for testing the ROO ATP system [LM92]
- SPRFN - the collection distributed with the SPRFN ATP system [SPR],
- TPTP - the problem first ever appeared in the TPTP [SS96],
- SETHEO - the collection used for testing the SETHEO ATP system [LSBB92].

The problem of Figure 4 was taken from [McCharen, et al., 1976].

**The % Names field.** Problems which have appeared in other problem collections or the literature, often have names which are known in the ATP community. This field lists all such names known to us for the problem, along with the source of the name. If the source is an existing problem collection then the collection name is cited, as in the **% Source** field. If the source of a name is the literature then a citation is given. If a problem is not given a name in a paper, a citation is given and "-" is used as the known name. Problems which first appeared in the TPTP have source TPTP, and no other name. In generator files all known names for instances of the abstract problem are listed, with the instance size given before the source. A reverse index, from known names to TPTP names, is in Appendix 9.2, and is also distributed with the TPTP (see Section 2.6). The problem of Figure 4 is called GP2 in [McCharen, et al., 1976].

**The % Status field.** This field gives the ATP status of the problem, one of **satisfiable**, **unsatisfiable**, **open**, or **unknown**. In Figure 4, the status is **unsatisfiable**.

**The % Syntax field.** This field lists various syntactic measures of the problem's clauses. The measures are: the number of clauses, the number of non-Horn clauses, the number of unit clauses, the number of range restricted clauses, the number of literals, the number of equality literals, the maximal clause size (measured by number of literals), the number of distinct predicate symbols, the number of distinct propositional variables, the minimal and maximal predicate symbol arities, the number of distinct function symbols, the number of distinct constants, the minimal and maximal functor arities, the number of distinct variables, the number of singleton variables (variables that appear only once in a clause), and the maximal term depth (with constants and variables having depth 1). See Tables 2 and 3 for a summary of this information over the entire TPTP.

**The % Comments field.** This field contains free format comments about the problem, e.g., the significance of the problem, or the reason for creating the problem.

**The % Bugfixes field.** This field describes any bugfixes that have been done to the clauses of the problem. Each entry gives the release number in which the bugfix was done, and attempts to pinpoint the bugfix accurately. In the problem of Figure 4, a bugfix was made in release v1.0.1, by removing the duplicate `multiply_inverse_left` and `multiply_inverse_right` clauses.

### 2.5.2 The Include Section

The include section contains `include` instructions for TPTP axiom files. An example of an include section, extracted from the problem file `GRP039-7.p`, is shown in Figure 5.

```
%-----
%---Include the axioms of equality
include('Axioms/EQU001-0.ax').
%---Include the axioms for group theory in equality form
include('Axioms/GRP004-0.ax').
%---Include the subgroup axioms in equality formulation
include('Axioms/GRP004-1.ax').
%-----
```

Figure 5: Example of a problem file include section (`GRP039-7.p`).

Each of the `include` instructions indicates that the clauses in the named axiom file should be included at that point. Axiom files are presented in the same format as problem files, and `include` instructions may also appear in axiom files. If required, full versions of TPTP problems (without `include` instructions) can be created by using the `tptp2X` utility (see Section 3.1).

### 2.5.3 The Clauses Section

TPTP problems are presented in clause normal form. The literals that make up a clause are presented as a Prolog list of terms (i.e., in `[]`). Each literal is a term whose functor is either `++` or `--`, indicating a positive or negative literal, respectively. The atom of the

literal is the single argument of the sign, in the form of a Prolog term. Thus predicate symbols and functors start with lower case alphanumeric, and variables start with upper case alphabetic (variables may not start with an `_`). The signs `++` and `--` are assumed to be defined as prefix operators in Prolog.

Each clause has a name, in the form of a Prolog atom. Each clause also has a type, one of `axiom`, `hypothesis`, or `conjecture`. The `hypothesis` and `conjecture` clauses are those that are derived from the negation of the conjecture to be proved. These clauses are only of type `hypothesis` if they can clearly be determined as such; otherwise they are of type `conjecture`<sup>2</sup>.

The name, type, and literal list of each clause are bundled as the three arguments of a Prolog fact, whose predicate symbol is `input_clause`. These facts are in the clause section of the problem file.

An example of a clause section, extracted from the problem file `GRP039-7.p`, is shown in Figure 6.

```
%-----
%---Redundant two axioms
input_clause(right_identity,axiom,
  [[+equal(multiply(X,identity),X)]].

input_clause(right_inverse,axiom,
  [[+equal(multiply(X,inverse(X)),identity)]].

  <some clauses omitted>

%---Denial of theorem
input_clause(b_in_02,hypothesis,
  [[+subgroup_member(b)]].

input_clause(b_times_a_inverse_is_c,hypothesis,
  [[+equal(multiply(b,inverse(a)),c)]].

input_clause(a_times_c_is_d,hypothesis,
  [[+equal(multiply(a,c),d)]].

input_clause(prove_d_in_02,conjecture,
  [--subgroup_member(d)]].
%-----
```

Figure 6: Example of a problem file clause section (`GRP039-7.p`).

---

<sup>2</sup>The input formats of some existing ATP systems cannot capture the information regarding clause type. If such systems require clause selections, e.g., when choosing which clause(s) to focus on initially, that selection is made without the benefit of this information. Furthermore, for some systems clause selections have to be specified in their input files. This is usually done by the user (which may render the system incomplete, as is the case for some Model Elimination based ATP systems that we know of). For such systems, the `tptp2X` utility (see Section 3.1) provides a default selection.

## 2.6 Physical Organization

The TPTP is physically organized into six subdirectories, as follows:

- **Axioms** - The axiom files directory.
- **Problems** - The problem files directory with subdirectories for each domain. The domain name abbreviations, as described in Section 2.1, are used as subdirectory names. The subdirectories contain the problem files.
- **Generators** - The generator files directory.
- **Documents** - A directory containing documents that relate to the TPTP :
  - **Abbreviations** - A list of the abbreviations used in the semantic names of abstract problems and axiomatizations, as given in Appendix 9.1.
  - **History** - A history of the changes made to the TPTP up to the current release.
  - **AxiomList** - A list of the axiomatizations in the TPTP, giving their syntactic names, semantic names, number of specializations, and one-line descriptions. This summarizes the axioms table given in Section 6.
  - **GeneratorList** - A list of the generic problems in the TPTP, giving their syntactic names, semantic names, permissible sizes, TPTP size, and one-line descriptions. This summarizes the generators table given in Section 7.
  - **ProblemList** - A list of all the abstract problems in the TPTP, giving their syntactic names, semantic names, number of versions, and one-line descriptions. With the **ProblemStatistics**, this summarizes the problems table given in Section 8.
  - **ProblemStatistics** - A list of all the problems in the TPTP, giving the **% Status** value and the **% Syntax** field values. With the **ProblemList**, this summarizes the problems table given in Section 8.
  - **ProblemStatistics.rm\_eq** - A list of all the problems in the TPTP, giving the **% Status** value and the **% Syntax** field values after removing all equality axioms from the problem (done using `tptp2X`, see Section 3.1).
  - **ReadMe** - General information about the TPTP.
  - **ReverseIndex** - An index from existing known names for problems to their TPTP file names, as given in Appendix 9.2.
  - **Synopsis** - Statistics on the TPTP, as given in Tables 1, 2, and 3, and a chart showing the structure of the TPTP problem domains, as given in Figure 1.
  - **Template** - A template for submitting new TPTP problems.
  - **Users** - A list of registered TPTP users. Registered users receive notification of TPTP patches, and other information relevant to the TPTP. If you would like to have your name added to or removed from this list, please let us know. Our addresses are given in Section 4.3.

The files in the **Documents** directory contain comprehensive online information about the TPTP. They summarize much of the information contained in this report, in specific files. This format provides quick access to the data, using standard system tools (e.g., `grep`, `awk`).

- **Scripts** - A directory containing C shell scripts that may be used with the TPTP. Currently there is only one script (see Section 3.2).
- **TPTP2X** - The directory containing the tptp2X utility, described in Section 3.1.

## 2.7 The TPTP Listings

In Sections 6, 7, and 8, listings of all the axiomatizations, generators, and problems in the TPTP are given. All listings are structured according to the domain hierarchy described in Section 2.1, with each domain listed separately.

For all listings, there is a delimited section for each abstract problem. The first line in each section gives information about the abstract problem, and each of the following lines gives information about a particular problem version. See Figure 7 for an extract of the actual problem listing. The legend describes the information given. The axiom listing follows a similar convention. The generators listing cannot show syntactic entity counts, since these are problem size dependent. Instead, the generators listing shows the permissible size values and the size contained in the TPTP.

Syntactic name	Semantic name	Description	V	Cl	Av	nH	Eq
V#	Other names	References					
<b>Domain ANA (5 abstract problems, 17 problems)</b>							
ANA001	MinVal	Attaining minimum (or maximum) value					
-1	AM8	[WB87]	c	18	2.0	16%	-
ANA002	IntmedVal	Intermediate value theorem					
-1		[WB87]	c	18	2.0	27%	-
-2		[WB87]	c	18	2.0	27%	-
-3	IMV	[WB87]	c	17	3.0	29%	-
-4	ivt.lop	[WB87]	c	17	3.0	29%	-
ANA003	SumContFuncLem1	Lem. 1 for the sum of 2 continuous functions is continuous					
-1	probl.ver2.in	[MOW76]	c	38	2.0	-	47%
-2	BL1, probl.ver1.in	[MOW76]	I	17	2.0	-	5%
-3		[Ble90, Ble92]	c	50	2.0	10%	40%
-4	Problem 1, Bledsoe-P1, p1.lop	[Ble90, LM92, Ble92]	I	12	2.0	33%	-
...	...	...	...	...	...	...	...

### Legend

- Syntactic name: The abstract problem's syntactic name (In the axiom listing this is extended with either **ax** to indicate theory specific axioms or **eq** to indicate equality substitution axioms).
- Semantic name: The abstract problem's semantic name.
- Description : The one-line description of the abstract problem.
- V# : The version number for each problem (For axiom files, this is the specialization number).
- Other names : Other known names for the problem version, as listed in the **% Names** field of the problem header.
- References : A list of citations to items in which the problem has been presented, as listed in the **% Refs** field of the problem header.
- V : A condensed summary of what makes the version different from others, as contained in the **% Version** field in the problem header: I = Incomplete, S = Complete and Standard, N = Complete and Non-standard, or "-" = Special for those problems which cannot be obtained from a standard axiomatization.
- Cl : The number of clauses in the problem.
- Av : The average number of literals per clause in the problem.
- nH : The percentage of non-Horn clauses in the problem, or "-" for Horn problems.
- Eq : The percentage of equality literals in the problem, or "-" for problems without equality.
- : An additional "P" at the end of a line denotes a propositional problem.

Figure 7: Example for problem listing.

## 3 Utility Programs and Scripts

### 3.1 The tptp2X Utility

The tptp2X utility is a multi-functional utility for reformatting, transforming, and generating TPTP problem files. In particular, it

- Converts from the TPTP format to formats used by existing ATP systems.
- Applies various transformations to the clauses of TPTP problems.
- Controls the generation of TPTP problem files from TPTP generator files.

The tptp2X utility is written in Prolog, and should run on most Prolog systems<sup>3</sup>. There is some code that is specific to the BinProlog, SICStus 2.1, Quintus, and Eclipse Prolog dialects. Before using tptp2X, it is necessary to install the code for the dialect of Prolog that is to be used. This and other installation issues are described next.

#### 3.1.1 Installation

The tptp2X utility consists of the following files:

- `tptp2X` - A `tcsh` script for running the tptp2X utility.
- `tptp2X_install` - A `csh` script for installing the tptp2X utility.
- `tptp2X.config` - Configuration file with site specific information.
- `tptp2X.main` - The main source code file of the tptp2X utility.
- `tptp2X.read` - Procedures for reading TPTP problem files.
- `tptp2X.generate` - Procedures for using TPTP generator files.
- `tptp2X.syntax` - Procedures for extracting syntactic measures from files.
- `transform.<TRAN>` - Procedures for doing `<TRAN>` transformations on TPTP problems, where `<TRAN>` is one of `arrange`, `equality`, `magic`, `shorten`.
- `format.<ATP>` - Procedures for outputting clauses in `<ATP>` format, where `<ATP>` is one of `kif`, `leantap`, `tap` (for 3TAP format), `meteor`, `mgtp`, `otter`, `pftp`, `setheo`, `spass`, `sprfn`, `tftp`.

Installation of the tptp2X utility requires simple changes in the `tptp2X` script and the files `tptp2X.config` and `tptp2X.main`. These changes can be made by running `tptp2X_install`, which will prompt for required information. Otherwise, to install tptp2X by hand, the following must be attended to:

- In the `tptp2X` script file:
  - `TPTPDirectory` must be set to the absolute path name of the TPTP directory.
  - `PrologInterpreter` must be set to the absolute path name of the Prolog interpreter.
  - `PrologArguments` must be set to any command line arguments for the Prolog interpreter.
  - The `Gawk` variable must be set to the absolute path name of `gawk` or `awk`.

---

<sup>3</sup>In particular, the tptp2X code will run on BinProlog 5.00. BinProlog is written by Paul Tarau of the University of Moncton (Canada), and is freely available by anonymous ftp, from `clement.info.umoncton.ca:BinProlog`.



- In the `tptp2X.config` file:
  - The appropriate facts for the desired Prolog dialect must be uncommented.
  - The absolute path name of the TPTP directory must be set in the `tptp_directory/1` fact.
- In the `tptp2X.main` file:
  - If your Prolog interpreter does not support `compile/1` for loading source code, the `compile/1` directives must be changed to something appropriate, e.g., `[]`.

### 3.1.2 Using `tptp2X`

The most convenient way of using the `tptp2X` utility is through the `tptp2X` script. The use of this script is:

```
tptp2X [-h] [-q<Level>] [-i] [-s<Size>] [-t<Transform>] [-f<Format>] [-d<Directory>] <TPTPFiles>
```

The `-h` flag specifies that usage information should be output. The `-q<Level>` flag specifies the level of quietness at which the script should operate. There are three quietness levels; 0 is verbose mode, 1 suppresses informational output from the Prolog interpreter, and 2 suppresses all informational output except lines showing what files are produced. The default quietness level is 1. The `-i` flag specifies that the script should enter interactive mode after processing all other command line parameters. Interactive mode is described below. The other command line parameter values are:

- `-s<Size>` : This specifies the required sizes when generating problems. `<Size>` is either an integer, a `<Low>..<High> integer size range, or a : separated list of <Sizes>.
 
  - An integer directly specifies the required problem size.
  - Each integer in a size range is used to generate a separate set of clauses.
  - A : separated string of <Sizes> is used for generators that require multiple parameters, one <Size> for each size parameter required. For example, -s3..5:2 means the three sizes 3:2, 4:2, and 5:2.`

`-s<Size>` is ignored for problem (`.p`) files.

- `-t<Transform>` : Specifies transformations to be applied to the clauses. `<Transform>` is either a single transformation, a `+` separated string of transformations, or a comma separated list of `<Transform>`s.
  - A single transformation is applied directly to the clauses.
  - Each transformation in a `+` separated string is applied to the clauses serially.
  - Each `<Transform>` in a list of `<Transform>`s is used to create a separate set of transformed clauses.

The transformations are:

- `lr`, to reverse the literal ordering in the clauses.
- `cr`, to reverse the clause ordering in the problem.

- `clr`, to do both reversals.
  - `random`, to randomly reorder the clauses and literals in the problem.  
The rearrangement of clauses and/or literals in a problem facilitates testing the sensitivity of an ATP system to the order in which the clauses and literals are presented.
  - `rm_equality:<Remove>`, to remove equality axioms.  
<Remove> is a string that indicates which equality axioms to remove. The characters that can be in the string are:
    - \* `r`, to remove reflexivity,
    - \* `s`, to remove symmetry,
    - \* `t`, to remove transitivity,
    - \* `f`, to remove function substitution,
    - \* `p`, to remove predicate substitution.
- For example, `-t rm_equality:stfp` would indicate to remove symmetry, transitivity, function substitution, and predicate substitution. This transformation works only if the equality axiomatization is complete (i.e., including the axioms of reflexivity, symmetry, transitivity, function substitution for all functors, and predicate substitution for all predicate symbols), using `equal/2` as the equality predicate. (All TPTP problems containing the `equal/2` predicate do contain a complete equality axiomatization; see Section 2.2.)
- `add_equality`, to add missing equality axioms to a problem. If the problem contains the `equal/2` predicate, then a check is made to see if the equality axiomatization is complete. If not, the missing equality axioms are added to the problem.
  - `to_equality`, to convert the problem to a pure equality representation. Every non-equality literal is converted to an equality literal (using the `equal/2` predicate) with the same sign. The arguments of the new equality literal are the atom of the non-equality literal and the constant `true`.
  - `magic`, to do Mark Stickel’s magic set transformation [Sti94].
  - `shorten`, to replace all the symbols in the problem by short, meaningless symbols. This is useful if you are only interested in the syntax of the problem, and do not want to read through the long, meaningful symbols that are often used in TPTP problems. Note that `equal/2` is not shortened.
  - `none`, to do nothing (same as omitting it, but required for advanced use; see Section 3.1.5).

The default <Transform> is `none`.

- `-f<Format>` : Specifies the format in which the output is to be written. The available output formats are:
  - `kif`, to convert to the KIF format [GF92].
  - `leantap`, to convert to the leanTAP format [BP95];
  - `tap`, to convert to the 3TAP format [HBG94].
  - `meteor`, to convert to the METEOR format [Ast92];

- `mgtp`, to convert to the MGTP format [FHKF92];
- `otter:<SoS>:'<Otter options>'`,  
to convert to the Otter `.in` format [McC94].  
<SoS> specifies the Set-of-Support to use. It can be one of:
  - \* `conjecture`, to use the clauses whose type is `conjecture`,
  - \* `hypothesis`, to use the clauses whose type is `hypothesis` or `conjecture`,
  - \* `positive`, to use the positive clauses,
  - \* `negative`, to use the negative clauses,
  - \* `unit`, to use the unit clauses,
  - \* `all`, to use all clauses,
  - \* `none`, to use no clauses.
 <Otter options> is a quoted (to avoid UNIX shell errors), comma separated list of Otter options, which will be output before the clause lists. See the Otter Reference Manual and Guide [McC94] for details of the available options. For example, `-f otter:none:'set(auto),assign(max_seconds,5)'` would configure Otter to use its `auto` mode with a time limit of 5 seconds. As the `auto` mode is commonly used with Otter, the `tptp2X` script allows the abbreviation `-f otter` to specify `-f otter:none:'set(auto)'`. If no <Transform> is specified then `-f otter` also sets `-t equality:stfp`.
- `tptp`, to convert to the TPTP format [Sti84];
- `setheo:<Style>`, to convert to the SETHEO `.lop` format [STvdK90].  
<Style> specifies the style of SETHEO clauses to write. It can be one of:
  - \* `sign`, to write the atoms of the negative and positive literals of each clause in the antecedent and consequent of an implication, respectively;
  - \* `type` In the `type` style, if there are no negative `axiom` or `hypothesis` clauses, then the `sign` style is used. Otherwise in all negative `axiom` and `hypothesis` clauses the first literal is negated to form the consequent of an implication, with the remaining literals' atoms being written as the antecedent. Further, in all `conjecture` clauses all positive literals are negated so that all literals' are written in the antecedent of an implication.
 The default style is `sign`, i.e., the abbreviation `-fsetheo` means `-fsetheo:sign`.
- `spass`, to convert to the SPASS format [WGR96, Wei96];
- `sprfn`, to convert to the SPRFN format [Pla88];
- `tptp`, to convert to the TPTP format, substituting `include` instructions with the actual clauses.

The default <Format> is `tptp`.

- `-d<Directory>` : Specifies the top level directory below which the output files are to be placed. If the <Directory> value is `-`, then all output files are written to standard output. Otherwise the output files associated with an input file are placed in a subdirectory below the <Directory>, named according to the domain (the first 3 characters) of the input file.

The default <Directory> is a subdirectory below the `TPTP Problems` directory, named according to the <Format>.

- `<TPTPFiles>` : Lists the input files which are to be processed. As a shortcut, the three letter domain names can be given, which processes all problems in those domains. If specific files names are not absolute, then `tptp2X` looks in the current working directory, the **Generators** directory, the **Problems** directory, and the domain directories, for the file. If the file name `-` is specified then input is taken from standard input and all output is written to standard output (overriding any `<Directory>` specification).

The default `<TPTPFiles>` are all TPTP problem files.

A common first use of `tptp2X` is to convert TPTP problems to another format. To convert all TPTP problems to another format, the use is `tptp2X -f<Format>`, e.g., `tptp2X -fotter`. To limit the conversion to one or more domains, the domain names are specified after the `<Format>`, e.g., `tptp2X -fleantap ALG GRP LDA`. If you are a new TPTP user, these are probably the uses that you want to start with.

### 3.1.3 The `tptp2X` Output Files

The output files produced by `tptp2X` are named according to the TPTP file name and the options used. The name of the TPTP problem (the input file name without the `.p` or `.g`) forms the basis of the output file names. For generated files the size parameters are appended to the base name, separated from the base name by a `..`. Then, for each transformation applied a suffix is appended. The suffixes for the transformations are:

| Transformation       | Suffix          |
|----------------------|-----------------|
| none                 |                 |
| lr                   | +lr             |
| cr                   | +cr             |
| clr                  | +clr            |
| random               | +ran            |
| shorten              | +short          |
| magic                | +nhms           |
| rm_equality:<Remove> | +rm_eq-<Remove> |
| add_equality         | +eq             |
| to_equality          | +2eq            |

Finally an extension to indicate the output format is appended to the file name. The suffixes for the output formats are:

| Format  | Extension |
|---------|-----------|
| kif     | .kif      |
| leanTAP | .leantap  |
| tap     | .3tap     |
| meteor  | .me       |
| mgtp    | .mgtp     |
| otter   | .in       |
| pttp    | .pttp     |
| setheo  | .lop      |
| spass   | .spass    |
| sprfn   | .sprfn    |
| tptp    | .tptp     |

To further record how a tptp2X output file has been formed, the tptp2X parameters are listed as an entry in the % Comments field of the output file.

### Example

```
~/TPTP/TPTP2X> tptp2X -t1r,cr,clr -fpptp ../Problems/ALG/ALG001-1.p
```

```
-----
TPTP2X directory      = /home/geoff/TPTP/TPTP2X
TPTP directory        = /home/geoff/TPTP
Prolog interpreter    = /usr/local/bin/sicstus
Files to convert      = ../Problems/ALG/ALG001-1.p
Size                  =
Transformation        = 1r,cr,clr
Format to convert to  = pttp
Output directory      = /home/geoff/TPTP/Problems/pttp
-----
```

```
Made the directory /home/geoff/TPTP/Problems/pttp/ALG
ALG001-1 -> /home/geoff/TPTP/Problems/pttp/ALG/ALG001-1+1r.pttp
ALG001-1 -> /home/geoff/TPTP/Problems/pttp/ALG/ALG001-1+cr.pttp
ALG001-1 -> /home/geoff/TPTP/Problems/pttp/ALG/ALG001-1+clr.pttp
~/TPTP/TPTP2X>
```

This run applies three separate transformations to the problem ALG001-1. The transformations are literal order reversal, clause order reversal, and reversal of both literal and clause order. The transformed problems are output in pttp format, in the directory pttp/ALG below the TPTP Problems directory. The file names are ALG001-1+1r.pttp, ALG001-1+cr.pttp, and ALG001-1+clr.pttp.

### Example

```
~/TPTP/TPTP2X> tptp2X -q2 -s3..5 -fotter -d~/geoff/tmp ../Generators/SYN001-1.g
SYN001-1 -> /home/geoff/tmp/SYN/SYN001-1.003+eq_stfp.in
SYN001-1 -> /home/geoff/tmp/SYN/SYN001-1.004+eq_stfp.in
SYN001-1 -> /home/geoff/tmp/SYN/SYN001-1.005+eq_stfp.in
~/TPTP/TPTP2X>
```

This run generates three sizes of the generic problem SYN001-1. The sizes are 3, 4, and 5. The output files are formatted for Otter, to use its auto mode. The files are

placed in `~geoff/tmp/SYN`, and are named `SYN001-1.003.lop`, `SYN001-1.004.lop`, and `SYN001-1.005.lop`. The quietness level is set to 2, thus suppressing all informational output except the lines showing what files are produced.

### Example

```
~/TPTP/TPTP2X> tptp2X -q2 -tmagic+shorten - < ~geoff/TPTP/Problems/GRP/GRP001-1.p
%-----
% File      : GRP001=SqrComm-1 : TPTP v1.1.3. Released v1.0.0.
% Domain   : Group Theory
% Problem  : X^2 = identity => commutativity
           <Lots of output>
input_clause(clause_41,theorem,
             [--p2(c8,c7,c9)]).
%-----
~/TPTP/TPTP2X>
```

This run uses the `tptp2X` script as a filter, to apply the non-Horn magic set transformation and then the symbol shortening transformation to `GRP001-1.p`. Output is written to standard output. The quietness level is set to 2, and as the output is to standard output, all informational output is suppressed.

#### 3.1.4 The `tptp2X` Interactive Mode

If the `-i` flag is set, the `tptp2X` script enters interactive mode after processing all other command line parameters. In interactive mode the user can change the value of any of the command line parameters. The user is prompted for the `<TPTPFiles>`, the `<Size>`, the `<Transform>`, the `<Format>`, and the `<Directory>`. In each prompt the current value is given. The user may respond by specifying a new value or by entering `<cr>` to accept the current value. The prompt-respond loop continues for each parameter until the user accepts the current value for the parameter.

## Example

```
~/TPTP/TPTP2X> tptp2X -q0 -d~/geoff/tmp -i
---- Interactive mode -----
Files to convert      [Problems/*/*.p] : ../Problems/GRP/GRP001-1.p
Files to convert      [../Problems/GRP/GRP001-1.p] :
Size                  [] :
Transformation        [none] : lr+equality:stfp
Transformation        [lr+equality:stfp] :
Format to convert to  [tptp] : setheo
Format to convert to  [setheo] :
Output directory      [/home/geoff/tmp] :
---- End of Interactive mode -----
-----
TPTP2X directory      = /home/geoff/TPTP/TPTP2X
TPTP directory        = /home/geoff/TPTP
Prolog interpreter    = /usr/local/bin/sicstus
Files to convert      = ../Problems/GRP/GRP001-1.p
Size                  =
Transformation        = lr+equality:stfp
Format to convert to  = setheo:sign
Output directory      = /home/geoff/tmp
-----
Made the directory /home/geoff/tmp/GRP
SICStus 2.1 #9: Thu Apr 21 09:39:25 +1000 1994
{compiling /home/2/geoff/TPTP/TPTP2X/tptp2X.main...}
  <Lots of informational output>
{/home/2/geoff/TPTP/TPTP2X/tptp2X.main compiled, 19906 msec 248400 bytes}

yes

yes
GRP001-1 -> /home/geoff/tmp/GRP/GRP001-1+lr+eq_stfp.lop

yes
~/TPTP/TPTP2X>
```

This run converts the problem GRP001-1 to a SETHEO format file. The literals are reversed and all equality clauses except reflexivity are removed. The top level output directory is specified as `~/geoff/tmp`, below which the subdirectory `GRP` is made. The output file is named `GRP001-1+lr+eq_stfp.lop`. Verbose mode is used, so all informational output is given.

The following sections are only of interest to real Prolog users. If you do not want to use Prolog directly, skip to Section 3.2 on page 34.

### 3.1.5 Running `tptp2X` from within Prolog

The `tptp2X` utility may also be run from within the Prolog interpreter. The `tptp2X.main` file has to be loaded, and the entry point is then `tptp2X/5`, in the form:

```
?-tptp2X(<TPTPFile>,<Size>,<Transform>,<Format>,<Directory>).
```

The parameters are similar to the `tptp2X` script command line parameters. A summary, including differences (!), is given here. See Section 3.1.2 for parameter options.

- `<TPTPFile>` is the name of a single TPTP file. If the file name is not absolute, then it is considered to be relative to the directory specified in the `tptp_directory/1` fact in the `tptp2X.config` file (!). If the file name is `user` (!), then input is taken from standard input.
- `<Size>` is either an integer, a `:` separated string of `<Size>s`, a `<Low>..<High>` integer size range, or a Prolog list of `<Size>s` (!). Each `<Size>` in a Prolog list of `<Size>s` is used in all possible ways to generate separate sets of clauses.
- `<Transform>` is either a single transformation specifier, a `+` separated string of `<Transform>s` (!), or a Prolog list (!) of `<Transform>s`.
- `<Format>` is an output format or a Prolog list (!) of output formats. An output file is written for each output format specified. For the `otter` format, the syntax is `otter:<SoS>:[<Otter options>]` (!), i.e., the Otter options form a Prolog list.
- `<Directory>` specifies the directory in which the output files are to be placed. If the `<Directory>` is `user` (!) then output is sent to standard output.

### Example

```
~/TPTP/TPTP2X> sicstus
SICStus 2.1 #9: Thu Apr 21 09:39:25 +1000 1994
| ?- ['tptp2X.main'].
{consulting /home/2/geoff/TPTP/TPTP2X/tptp2X.main...}
  <Lots of informational output>
{/home/geoff/TPTP/TPTP2X/tptp2X.main consulted, 19158 msec 256800 bytes}

yes
| ?- tptp2X('Generators/SYN010-1.g',3:[2,4],[lr,cr]+magic,kif,'.').
{compiling /home/geoff/TPTP/Generators/SYN010-1.g...}
{/home/geoff/TPTP/Generators/SYN010-1.g compiled, 246 msec 2240 bytes}
SYN010-1 -> ./SYN010-1.003:002+lr+nhms.kif
SYN010-1 -> ./SYN010-1.003:002+cr+nhms.kif
SYN010-1 -> ./SYN010-1.003:004+lr+nhms.kif
SYN010-1 -> ./SYN010-1.003:004+cr+nhms.kif

yes
| ?- ^D
~/TPTP/TPTP2X>
```

This run generates two sizes of the generic problem SYN010-1, and does two transformation sequences on each of the two sets of clauses, to produce four output files. The sizes are 3:2 and 3:4. The first transformation sequence is literal order reversal followed by the non-Horn magic set transformation, and the second transformation sequence is clause order reversal followed by the non-Horn magic set transformation. The files are output in KIF format in the current directory. The file names are

SYN010-1.003:002+lr+nhms.kif, SYN010-1.003:002+cr+nhms.kif,  
 SYN010-1.003:004+lr+nhms.kif, and SYN010-1.003:004+cr+nhms.kif.

Note that the TPTP file name is quoted in the query, to form a Prolog atom.



### 3.1.6 Writing your own Transformations and Output Formats

The transformations and output formatting are implemented in Prolog, in the files `transform.<TRAN>` and `format.<ATP>`, respectively. It is simple to add new transformations and output formats to the `tptp2X` utility, by creating new transformation and format files. New files should follow the structure of the existing files. Typically, a new file can be created by modifying a copy of one of the existing files.

The entry point in a transformation file is `<Transform>/6`, where `<Transform>` is the principle symbol of the transformation specification (currently one of `none`, `lr`, `cr`, `clr`, `random`, `shorten`, `magic`, `rm_equality`, `add_equality`, `to_equality`). The first three arguments are inputs: a list of the problem's clauses, the variable dictionary (a bit complicated), and the transformation specification. The next three arguments are outputs: the transformed clauses, the transformed variable dictionary (typically the same as the input dictionary), and the transformation suffix. As well as the `<Transform>/6` entry point, a `<Transform>_file_information/2` fact must be provided. The two arguments of the `<Transform>_file_information/2` fact are the atom `transform` and a description of the possible transformation specifications (as used in the third argument of `<Transform>/6`). See the existing `transform.<TRAN>` files for examples.

The entry point in a format file is `<Format>/2`, where `<Format>` is the principle symbol of the output format specification (currently one of `kif`, `leantap`, `tap`, `meteor`, `mgtp`, `otter`, `pftp`, `setheo`, `spass`, `sprfn`, `tptp`). The two arguments are inputs: a list of the problem's clauses, and the format specification. As well as the `<Format>/2` entry point, a `<Format>_format_information/2` fact and a `<Format>_file_information/2` fact must be provided. The two arguments of the `<Format>_format_information/2` fact are a character that can be used to start a comment in the output file and the format extension, both as Prolog atoms. The two arguments of the `<Format>_file_information/2` fact are the atom `format` and a description of the possible format specifications (as used in the second argument of `<Format>/2`). See the existing `format.<ATP>` files for examples.

New transformation and format files must be compiled in with the other `tptp2X` files. This is done by adding a compile query in the `tptp2X.main` file, alongside the queries that compile in the existing files.

If you are in doubt, please contact Geoff Sutcliffe for help.

### 3.1.7 Writing your own Problem Generators

The TPTP generators are implemented in Prolog. It is simple to write new generators. New files should follow the structure of the existing files.

The entry point in a generator file is `<Problem name>/3`, where `<Problem name>` is the file name without the `.g` suffix. The first argument is an input: the size parameter for generation. The second and third arguments are outputs: the clauses generated and the status of the clauses. The clauses must be a Prolog list of clauses in TPTP `input_clause/3` format. The status value must be one of `unsatisfiable`, `satisfiable`, `open`, or `unknown`. A `<Problem name>_file_information/3` fact must also be provided. The three arguments of the fact are the atom `generator`, a description of the possible size parameters (as used in the first argument of `<Problem name>/3`), and the TPTP size for this problem (this is hard to determine!). See the existing generator files for examples.

If you are in doubt, please contact Geoff Sutcliffe for help.

## 3.2 The tptp\_naming Script

This script renames TPTP files with either their syntactic or syntactic=semantic names, using the names given in the % File field of the header (see Section 2.4).

Usage: `tptp_naming syntactic|semantic <List of problem files>`

### Example

```
~/TPTP/Scripts> tptp_naming semantic Problems/GRP/GRP001*
Problems/GRP/GRP001-1.p renames to Problems/GRP/GRP001=SqrComm-1.p
Problems/GRP/GRP001-2.p renames to Problems/GRP/GRP001=SqrComm-2.p
Problems/GRP/GRP001-3.p renames to Problems/GRP/GRP001=SqrComm-3.p
Problems/GRP/GRP001-4.p renames to Problems/GRP/GRP001=SqrComm-4.p
Problems/GRP/GRP001-5.p renames to Problems/GRP/GRP001=SqrComm-5.p
~/TPTP/Scripts>
```

This use of `tptp_naming` adds the semantic name to all versions of the abstract problem GRP001.

## 4 You and the TPTP

### 4.1 Quick Installation Guide

This section explains how to obtain and install the TPTP, and how to syntax-convert the TPTP problems.

#### 4.1.1 Obtaining the TPTP via FTP

The distribution consists of three files:

- `ReadMe-v1.2.1` (8.9 kByte) contains an overview of the TPTP.
- `TR-v1.2.1.ps.gz` (0.42 MByte, 1.9 MByte unpacked) contains this version of the TPTP technical report.
- `TPTP-v1.2.1.tar.gz` (0.73 MByte, 11.4 MByte unpacked) contains the library (including a copy of the `ReadMe-v1.2.1` file).

There also might be a file called `BuggedProblems-v1.2.1`, containing a list of files that have been found to contain errors, in the current release (bugs that have been discovered after the release has been distributed).

Ftp instructions for obtaining the TPTP from Australia or Germany:

```
prompt> cd <the directory where you want the TPTP to reside>
prompt> ftp -i ftp.cs.jcu.edu.au          # or: ftp -i 137.219.17.4
      # or use alternatively
      ftp -i flop.informatik.tu-muenchen.de # or: ftp -i 131.159.8.35
Name (ftp.cs.jcu.edu.au:<your login-name>): ftp
331 Guest login ok, send your complete e-mail address as password.
Password:<your full email address>
ftp> cd pub/research/tptp-library      # on ftp.cs.jcu.edu.au
      cd pub/tptp-library              # on flop.informatik.tu-muenchen.de
ftp> binary
ftp> mget *
ftp> quit
```

Or use the World Wide Web (WWW) with either of the following URLs :

```
http://www.cs.jcu.edu.au/ftp/users/GSutcliffe/TPTP.html
http://wwwjessen.informatik.tu-muenchen.de/~suttner/TPTP.html.
```

#### 4.1.2 Installing the TPTP

```
prompt> gunzip -c TPTP-v1.2.1.tar.gz | tar xvf -
prompt> TPTP-v1.2.1/TPTP2X/tptp2X_install
      <... the script will then ask for required information>
```

If you don't have any Prolog installed, you need to get one first. BinProlog is freely available via anonymous ftp from `clement.info.umoncton.ca:BinProlog`.

#### 4.1.3 Converting Problems to Other Syntax

```
prompt> TPTP-v1.2.1/TPTP2X/tptp2X <desired_syntax>
```

As `<desired_syntax>`, choose any one of `kif`, `leantap`, `tap`, `meteor`, `mgtp`, `otter`, `pttp`, `setheo`, `spass`, `sprfn`, or `tptp`. The `tptp` option simply expands `include` directives (see Section 2.5) in problems, producing files in the TPTP Prolog-style syntax. `tptp2X` offers MUCH more than this. See Section 3.1 for a detailed description of the utility, including information on how to produce output in your own syntax.

## 4.2 Important: Using the TPTP

By providing this library of ATP problems, and a specification of how these problems should be presented to ATP systems, it is our intention to place the testing, evaluation, and comparison of ATP systems onto a firm footing. For this reason, you should abide by the following conditions when using TPTP problems and presenting your results:

- The TPTP release number must be stated, and each problem must be referenced by its unambiguous syntactic name.

- No clauses/literals may be changed, added, or removed without explicit notice (this holds also for removing equality axioms when built-in equality is provided by the prover).
- The clauses/literals may not be rearranged without explicit notice. If clause or literal reordering is done using the `tptp2X` utility, (see Section 3.1), the reordering must be explicitly noted.
- The header information in each problem may not be used by the ATP system without explicit notice. Any information that is given to the ATP system, other than that in the `input_clauses`, must be explicitly noted (including any system switches or default settings).

Abiding by these rules will allow unambiguous identification of the problem, the arrangement of clauses, and further input to the ATP system. If you follow these rules, please make this clear in any presentation of your results, by an explicit statement. We propose that you state “These results were obtained in compliance with the guidelines for use of TPTP v1.2.1”. By making this clear statement, ATP researchers are assured of your awareness of our guidelines. Conversely, it will become clear when the guidelines may have been ignored.

### 4.3 Please contact us if ...

Please contact one of us if:

- You find any mistakes in the TPTP.
- You are able to provide further information for a TPTP problem.
- You want to contribute a problem to the TPTP. Please use the problem template that comes with the distribution (in the Documents directory - see Section 2.6) and fill in header information as far as possible. Any unambiguous representation will do for the clauses.
- You have further suggestions for improving the TPTP library.

Our contact addresses are:

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## 5 The Future

### 5.1 Current Activities

Currently a new version of the TPTP is being built. It will contain two important new features.

Firstly, in addition to the current CNF syntax, problems in FOF (First Order Format, i.e., including quantifiers) syntax will be integrated into the TPTP. This will extend the TPTP user community to researchers working on non-normal form systems. Also, ATP

systems with automatic conversion to clause normal form will be able to derive additional information regarding a given problem, such as which functors are Skolem functors. For systems unable to deal with FOF, we also will provide a clause normal form transformation in the `tptp2X` utility. Over a hundred FOF problems have already been collected. Everybody is invited to submit problems in FOF syntax for inclusion. Please contact us for details if you would like to contribute.

Secondly, each problem will obtain an individual difficulty rating. The problem ratings are currently being worked on. As part of this, we are collecting performance data for state-of-the-art theorem provers. The data collection will become part of future releases of the TPTP. TPTP users are invited to submit performance data for their ATP systems. Please contact us for details if you would like to contribute. Note that, as advances in automated theorem proving are made, problem ratings should decrease. Therefore the long term development of the individual problem ratings will provide an objective measure of progress in the field.

The next major release will also contain a summary of work that references the TPTP. This will allow users to compare published results obtained for different systems, and also will give an overview on the usage of the TPTP. Finally, it will include a BibTeX file containing the references found in this report.

## 5.2 Further Plans

We have several short and long term plans for further development of the TPTP. The main ideas are listed here.

- ATP system evaluation guidelines.  
General guidelines outlining the requirements for ATP system evaluation will be produced.
- The BSTP Benchmark Suite.  
A benchmark suite (the BSTP) will be selected from the TPTP. The BSTP will be a small collection of problems, and will provide a minimal set of problems on which an ATP system evaluation can be based. The BSTP will be accompanied by specific guidelines for computing a performance index for an ATP system.
- Various translators.  
Translators between various logical forms will be provided.
  - from non-Horn to Horn form
  - from 1st order to propositional form
- Other logics.  
The TPTP may be extended to include problems expressed in non-classical and higher order logics.

## 5.3 Acknowledgements

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Location abbreviations:

|   |   |
|---|---|
| ANL = Argonne National Laboratory           | SUNY = State University of New York               |
| LMU = Ludwig-Maximilian-Universität München | TUM = Technische Universität München              |
| MPIS = Max-Planck-Institut Saarbrücken      | UCB = University of California at Berkeley        |
| NJIT = New Jersey Institute of Technology   | UNC = University of North-Carolina at Chapel Hill |
| PSU = Pennsylvania State University         | UNM = University of New Mexico, Albuquerque       |
| SRI = Stanford Research International       |   |

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## 6 The TPTP v1.2.1 Axiom Sets Listing

| Syntactic name | V# | Semantic name | References                    | Description   | V | Cl | Av  | nH  | Eq   |
|----------------|----|---------------|-------------------------------|---|---|----|-----|-----|------|
| ALG001         | ax | GodelAlg1     |                               | Abstract algebra axioms, based on Godel set theory  |   |    |     |     |      |
|                | -0 |               | [BLM <sup>+</sup> 86, McC92b] |   | c | 24 | 2.8 | 29% | 18%  |
| ALG001         | eq | GodelAlg1Subs |                               | Substitution axioms for abstract algebra axioms     |   |    |     |     |      |
|                | -0 |               | [BLM <sup>+</sup> 86]         |   | c | 34 | 2.4 | -   | 67%  |
| ANA001         | ax | Limits1       |                               | Analysis (limits) axioms for continuous functions   |   |    |     |     |      |
|                | -0 |               | [MOW76]                       |   | c | 14 | 1.9 | -   | 18%  |
| ANA001         | eq | Limits1Subs   |                               | Substitution axioms for analysis (limits) axioms    |   |    |     |     |      |
|                | -0 |               | [MOW76]                       |   | c | 8  | 2.3 | -   | 77%  |
| ANA002         | ax | Limits2       |                               | Analysis (limits) axioms for continuous functions   |   |    |     |     |      |
|                | -0 |               | [Ble90, Ble92]                |   | c | 26 | 1.7 | 7%  | 13%  |
| ANA002         | eq | Limits2Subs   |                               | Substitution axioms for analysis (limits) axioms    |   |    |     |     |      |
|                | -0 |               | [Ble90]                       |   | c | 14 | 2.1 | -   | 86%  |
| BOO001         | ax | B3Alg         |                               | Ternary Boolean algebra (equality) axioms           |   |    |     |     |      |
|                | -0 |               | [Wos88, Win82]                |   | c | 9  | 1.4 | -   | 100% |
| BOO002         | ax | BoolAlg1      |                               | Boolean algebra axioms                              |   |    |     |     |      |
|                | -0 |               | [Whi61, MOW76]                |   | c | 22 | 2.7 | -   | 3%   |
| BOO002         | eq | BoolAlg1Subs  |                               | Substitution axioms for Boolean algebra axioms      |   |    |     |     |      |
|                | -0 |               | [Whi61, MOW76]                |   | c | 11 | 2.5 | -   | 57%  |
| BOO003         | ax | EqBoolAlg1    |                               | Boolean algebra (equality) axioms                   |   |    |     |     |      |
|                | -0 |               | [Whi61, MOW76]                |   | c | 19 | 1.3 | -   | 100% |
| BOO004         | ax | EqBoolAlg2    |                               | Boolean algebra (equality) axioms                   |   |    |     |     |      |
|                | -0 |               | [Ver94]                       |   | c | 13 | 1.4 | -   | 100% |
| CAT001         | ax | Catgry1       |                               | Category theory axioms                              |   |    |     |     |      |
|                | -0 |               | [Mit67]                       |   | c | 18 | 2.5 | -   | 2%   |
| CAT001         | eq | Catgry1Subs   |                               | Substitution axioms for category theory axioms      |   |    |     |     |      |
|                | -0 |               | [Mit67]                       |   | c | 10 | 2.6 | -   | 53%  |
| CAT002         | ax | EqCatgry1     |                               | Category theory (equality) axioms                   |   |    |     |     |      |
|                | -0 |               | [Qua89a]                      |   | c | 11 | 1.7 | -   | 100% |
| CAT003         | ax | Catgry2       |                               | Category theory axioms                              |   |    |     |     |      |
|                | -0 |               | [Sco79]                       |   | c | 17 | 2.2 | 11% | 40%  |
| CAT003         | eq | Catgry2Subs   |                               | Substitution axioms for category theory axioms      |   |    |     |     |      |
|                | -0 |               | [Sco79]                       |   | c | 9  | 2.3 | -   | 71%  |
| CAT004         | ax | Catgry3       |                               | Category theory axioms                              |   |    |     |     |      |
|                | -0 |               | [Sco79]                       |   | c | 11 | 1.9 | -   | 33%  |
| CAT004         | eq | Catgry3Subs   |                               | Substitution axioms for category theory axioms      |   |    |     |     |      |
|                | -0 |               | [Sco79]                       |   | c | 7  | 2.4 | -   | 64%  |
| CID001         | ax | Logic         |                               | Definitions of AND, OR and NOT                      |   |    |     |     |      |
|                | -0 |               | [WOLB92]                      |   | c | 10 | 1.0 | -   | 100% |
| CID001         | eq | LogicSubs     |                               | Substitution axioms for AND, OR and NOT             |   |    |     |     |      |
|                | -0 |               | [WOLB92]                      |   | - | 5  | 2.0 | -   | 100% |
| CID002         | ax | Logic         |                               | Definitions of AND, OR and NOT                      |   |    |     |     |      |
|                | -0 |               | [WOLB92]                      |   | c | 6  | 1.0 | -   | 100% |
| COL001         | ax | TRC           |                               | Type-respecting combinators                         |   |    |     |     |      |
|                | -0 |               | [Jec93b]                      |   | c | 17 | 1.5 | 5%  | 100% |
| EQU001         | ax | Equality      |                               | Reflexivity, symmetry and transitivity, of equality |   |    |     |     |      |
|                | -0 |               | [Jec93b]                      |   | - | 3  | 2.0 | -   | 100% |
| FIE001         | ax | Semantic      |                               | Ordered field axioms.                               |   |    |     |     |      |
|                | -0 |               | [Drä93]                       |   | x | 26 | 2.8 | 11% | 31%  |
| FIE002         | ax | Semantic      |                               | Ordered field axioms.                               |   |    |     |     |      |
|                | -0 |               | [Drä93]                       |   | l | 44 | 2.1 | 6%  | 26%  |
| FIE003         | ax | Semantic      |                               | Ordered field axioms.                               |   |    |     |     |      |
|                | -0 |               | [Drä93]                       |   | e | 25 | 3.0 | 12% | -    |
| FIE004         | ax | Semantic      |                               | Ordered field axioms.                               |   |    |     |     |      |
|                | -0 |               | [Drä93]                       |   | l | 34 | 2.9 | 8%  | 12%  |
| FIE005         | ax | Semantic      |                               | Ordered field axioms.                               |   |    |     |     |      |
|                | -0 |               | [Drä93]                       |   | l | 33 | 2.4 | 9%  | 57%  |
| FIE006         | ax | Semantic      |                               | Ordered field axioms.                               |   |    |     |     |      |
|                | -0 |               | [Drä93]                       |   | b | 49 | 2.3 | 8%  | 68%  |
| GEO001         | ax | Tarski1       |                               | Tarski geometry axioms                              |   |    |     |     |      |
|                | -0 |               | [Tar59, MOW76, Wos88]         |   | c | 20 | 3.2 | 30% | 12%  |
|                | -1 |               | [Tar59, MOW76]                |   | c | 4  | 2.5 | 25% | -    |
| GEO001         | eq | Tarski1Subs   |                               | Substitution axioms for geometry axioms             |   |    |     |     |      |
|                | -0 |               | [Tar59, MOW76, Wos88]         |   | c | 32 | 2.2 | -   | 80%  |
|                | -1 |               | [Tar59, MOW76]                |   | c | 3  | 3.0 | -   | 33%  |
| GEO002         | ax | Tarski2       |                               | Tarski geometry axioms                              |   |    |     |     |      |
|                | -0 |               | [Tar59, MOW76, Qua89b]        |   | c | 18 | 3.1 | 27% | 12%  |
|                | -1 |               | [Tar59, MOW76, Qua89b]        |   | c | 4  | 2.5 | 25% | -    |
|                | -2 |               | [Tar59, MOW76, Qua89b]        |   | c | 1  | 1.0 | -   | 100% |
|                | -3 |               | [Tar59, MOW76, Qua89b]        |   | c | 1  | 1.0 | -   | 100% |
| GEO002         | eq | Tarski2Subs   |                               | Substitution axioms for geometry axioms             |   |    |     |     |      |
|                | -0 |               | [Tar59, MOW76, Qua89b]        |   | c | 32 | 2.2 | -   | 80%  |
|                | -1 |               | [Tar59, MOW76, Qua89b]        |   | c | 3  | 3.0 | -   | 33%  |
|                | -2 |               | [Tar59, MOW76, Qua89b]        |   | c | 2  | 2.0 | -   | 100% |
|                | -3 |               | [Tar59, MOW76, Qua89b]        |   | c | 4  | 2.0 | -   | 100% |
| GEO003         | ax | Hilbert1      |                               | Hilbert geometry axioms                             |   |    |     |     |      |
|                | -0 |               | [Ben92]                       |   | c | 31 | 5.6 | 58% | 24%  |
| GEO003         | eq | Hilbert1Subs  |                               | Substitution axioms for geometry axioms             |   |    |     |     |      |
|                | -0 |               | [Ben92]                       |   | c | 24 | 2.3 | -   | 71%  |
| GRP001         | ax | Monoids1      |                               | Monoid axioms                                       |   |    |     |     |      |
|                | -0 |               | [MOW76]                       |   | c | 6  | 2.3 | -   | 7%   |
| GRP002         | ax | SemiGr1       |                               | Semigroup axioms                                    |   |    |     |     |      |
|                | -0 |               | [MOW76]                       |   | c | 4  | 3.0 | -   | 8%   |



| Syntactic name<br>V#           | Semantic name<br>References  | Description  | V           | Cl            | Av                | nH            | Eq                  |
|--------------------------------|--|--|-------------|---------------|-------------------|---------------|---------------------|
| GRP002<br>eq<br>-0             | SemiGr1Subs<br>[MOW76]   | Substitution axioms for semigroup axioms                 | c           | 5             | 2.6               | -             | 53%                 |
| GRP003<br>ax<br>-0<br>-1<br>-2 | Group1<br>[MOW76, Wos88]<br>[MOW76, Wos88]<br>[Wosb]                     | Group theory axioms                                      | c<br>c<br>c | 8<br>2<br>1   | 2.0<br>3.0<br>4.0 | -<br>-<br>-   | 6%<br>-<br>-        |
| GRP003<br>eq<br>-0<br>-1<br>-2 | Group1Subs<br>[MOW76, Wos88]<br>[MOW76, Wos88]<br>[Wosb]                 | Substitution axioms for group theory axioms              | c<br>c<br>c | 6<br>1<br>1   | 2.5<br>3.0<br>3.0 | -<br>-<br>-   | 60%<br>33%<br>33%   |
| GRP004<br>ax<br>-0<br>-1<br>-2 | EqGroup1<br>[MOW76, Wos88]<br>[MOW76]<br>[Fuc94, Sch95]                  | Group theory (equality) axioms                           | -<br>c<br>c | 6<br>3<br>16  | 1.5<br>3.0<br>1.3 | -<br>-<br>-   | 100%<br>22%<br>100% |
| GRP005<br>ax<br>-0             | Group2<br>[MOW76, Wos88, Ver92]  | Group theory axioms                                      | c           | 7             | 2.4               | -             | -                   |
| GRP006<br>ax<br>-0             | NamedGr1<br>[MOW76]  | Group theory (Named groups) axioms                       | c           | 11            | 2.2               | -             | 4%                  |
| GRP006<br>eq<br>-0             | NamedGr1Subs<br>[MOW76]  | Substitution axioms for group theory axioms              | c           | 12            | 2.5               | -             | 60%                 |
| HEN001<br>ax<br>-0             | Henkin1<br>[MOW76]   | Henkin model axioms                                      | c           | 9             | 2.3               | -             | 9%                  |
| HEN001<br>eq<br>-0             | Henkin1Subs<br>[MOW76]   | Substitution axioms for Henkin model axioms              | c           | 7             | 2.7               | -             | 47%                 |
| HEN002<br>ax<br>-0             | Henkin2<br>[MOW76]   | Henkin model axioms                                      | c           | 7             | 1.6               | -             | 27%                 |
| HEN002<br>eq<br>-0             | Henkin2Subs<br>[MOW76]   | Substitution axioms for Henkin model axioms              | c           | 4             | 2.5               | -             | 60%                 |
| HEN003<br>ax<br>-0             | EqHenkin<br>[MOW76]  | Henkin model (equality) axioms                           | c           | 7             | 1.6               | -             | 100%                |
| LAT001<br>ax<br>-0<br>-1<br>-2 | EqLatt1<br>[Bum65, McC88, Wos88]<br>[Bum65, McC88]<br>[Bum65, McC88]     | Lattice theory (equality) axioms                         | c<br>c<br>c | 17<br>5<br>8  | 1.3<br>2.6<br>2.6 | -<br>-<br>12% | 100%<br>46%<br>38%  |
| LAT002<br>ax<br>-0             | Latt1<br>[MOW76, Wos88]  | Lattice theory axioms                                    | c           | 20            | 2.4               | -             | 4%                  |
| LAT002<br>eq<br>-0             | Latt1<br>[MOW76, Wos88]  | Substitution axioms for the lattice theory axioms        | c           | 10            | 2.6               | -             | 53%                 |
| LCL001<br>ax<br>-0<br>-1<br>-2 | WjAlg1<br>[FRT84, Bon91, MW92]<br>[FRT84, Bon91]<br>[FRT84, AB90, Bon91] | Wajsberg algebra axioms                                  | c<br>c<br>c | 7<br>10<br>10 | 1.4<br>2.0<br>1.4 | -<br>-<br>-   | 100%<br>70%<br>100% |
| LCL002<br>ax<br>-0<br>-1       | WjAlg2<br>[FRT84, AB90, Bon91]<br>[FRT84, AB90, Bon91]                   | Alternative Wajsberg algebra axioms                      | c<br>c      | 11<br>10      | 1.3<br>1.4        | -<br>-        | 100%<br>100%        |
| LCL003<br>ax<br>-0             | PropLog<br>[WR27, O'R89, SE94]   | Propositional logic deduction axioms                     | c           | 8             | 1.6               | -             | -                   |
| LDA001<br>ax<br>-0             | EmbdgAlg<br>[Jec93a]   | Embedding algebra axioms                                 | I           | 13            | 2.1               | 15%           | 44%                 |
| NUM001<br>ax<br>-0<br>-1<br>-2 | RecFunc1<br>[LS74]<br>[LS74]<br>[LS74]                                   | Number theory axioms                                     | I<br>c<br>c | 6<br>3<br>3   | 1.3<br>2.3<br>2.3 | -<br>-<br>33% | -<br>-<br>-         |
| NUM002<br>ax<br>-0             | AddAlg<br>[LS74]   | Number theory (equality) axioms                          | c           | 12            | 1.8               | -             | -                   |
| NUM003<br>ax<br>-0             | GodelNum1<br>[BLM <sup>+</sup> 86, McC92b]                               | Number theory axioms, based on Godel set theory          | c           | 54            | 4.0               | 59%           | 7%                  |
| NUM003<br>eq<br>-0             | GodelNum1Subs<br>[BLM <sup>+</sup> 86, McC92b]                           | Number theory axioms, based on Godel set theory          | c           | 27            | 2.0               | -             | 96%                 |
| NUM004<br>ax<br>-0             | Ordinals<br>[Qua92c]   | Number theory (ordinals) axioms, based on MBG set theory | c           | 46            | 2.3               | 8%            | 21%                 |
| NUM004<br>eq<br>-0             | OrdinalsSubs<br>[Qua92c]   | Substitution axioms for number theory axioms             | c           | 31            | 2.4               | -             | 65%                 |
| PLA001<br>ax<br>-0<br>-1       | Blocks1<br>[G.J73, SE94]<br>[G.J73, SE94]                                | Blocks world axioms                                      | c<br>c      | 10<br>20      | 3.1<br>1.1        | -<br>-        | -<br>-              |
| PRV001<br>ax<br>-0             | ProgVer1<br>[MOW76]  | Program verification axioms                              | c           | 12            | 1.9               | 8%            | 39%                 |
| PRV001<br>eq<br>-0             | ProgVer1Subs<br>[MOW76]  | Substitution axioms for program verification axioms      | c           | 3             | 2.0               | -             | 100%                |
| PRV002<br>ax<br>-0             | ProgVer2<br>[MOW76]  | Program verification axioms                              | c           | 22            | 2.4               | 9%            | 5%                  |
| PRV002<br>eq<br>-0             | ProgVer2Subs<br>[MOW76]  | Substitution axioms for program verification axioms      | c           | 4             | 2.5               | -             | 40%                 |
| PUZ001<br>ax<br>-0             | MarsVns<br>[Rap95]   | Mars and Venus axioms                                    | -           | 16            | 2.4               | 25%           | 2%                  |
| PUZ001<br>eq<br>-0             | MarsVnsSubs<br>[Rap95]   | Substitution axioms for Mars and Venus axioms            | -           | 10            | 2.9               | -             | 37%                 |
| PUZ002<br>ax<br>-0             | TTLiars1<br>[Smu78b, LO85a]  | Truth-tellers and Liars axioms for two types of people   | c           | 6             | 2.7               | 33%           | -                   |
| PUZ003<br>ax<br>-0             | TTLiars2<br>[Smu78b]   | Truth-tellers and Liars axioms for three types of people | c           | 8             | 2.9               | 37%           | -                   |
| RNG001<br>ax<br>-0             | Rings1<br>[MOW76, Wos88]   | Ring theory axioms                                       | c           | 17            | 2.9               | -             | 4%                  |

| Syntactic name<br>V#                 | Semantic name<br>References                       | Description                                 | V                | Cl               | Av                       | nH                       | Eq               |
|--------------------------------------|---|---|------------------|------------------|--------------------------|--------------------------|------------------|
| RNG001<br>eq<br>-0                   | Rings1Subs<br>[MOW76, Wos88]                      | Substitution axioms for ring theory axioms  | C                | 11               | 2.5                      | -                        | 57%              |
| RNG002<br>ax<br>-0                   | EqRings1<br>[PS81]                                | Ring theory (equality) axioms               | C                | 19               | 1.3                      | -                        | 100%             |
| RNG003<br>ax<br>-0                   | AltRing1<br>[Ste87]                               | Alternative ring theory (equality) axioms   | C                | 25               | 1.4                      | -                        | 100%             |
| RNG004<br>ax<br>-0                   | AltRing2<br>[AH90]                                | Alternative ring theory (equality) axioms   | C                | 22               | 1.3                      | -                        | 100%             |
| RNG005<br>ax<br>-0                   | EqRings2<br>[Wos88, LW91]                         | Ring theory (equality) axioms               | C                | 14               | 1.4                      | -                        | 100%             |
| ROB001<br>ax<br>-0<br>-1             | Robbins1<br>[HMT71, Win90]<br>[HMT71, Win90]      | Robbins algebra axioms                      | C<br>C           | 6<br>8           | 1.5<br>1.9               | -<br>-                   | 100%<br>60%      |
| SET001<br>ax<br>-0<br>-1<br>-2<br>-3 | Naive1<br>[LS74]<br>[LS74]<br>[LS74]<br>[LS74]    | Set theory membership and subsets axioms    | C<br>C<br>C<br>C | 6<br>6<br>6<br>6 | 2.3<br>3.3<br>3.3<br>3.3 | 16%<br>33%<br>33%<br>66% | -<br>-<br>-<br>- |
| SET002<br>ax<br>-0                   | Naive2<br>[MOW76]                                 | Set theory axioms                           | C                | 21               | 2.1                      | 14%                      | -                |
| SET002<br>eq<br>-0                   | Naive2Subs<br>[MOW76]                             | Substitution axioms for set theory axioms   | C                | 11               | 2.4                      | -                        | -                |
| SET003<br>ax<br>-0                   | GodelSet1<br>[BLM <sup>+</sup> 86, Wos88, McC92b] | Set theory axioms based on Godel set theory | C                | 141              | 2.5                      | 14%                      | 13%              |
| SET003<br>eq<br>-0                   | GodelSet1Subs<br>[BLM <sup>+</sup> 86, Wos88]     | Substitution axioms for set theory axioms   | C                | 122              | 2.2                      | -                        | 82%              |
| SET004<br>ax<br>-0<br>-1             | NBG1<br>[Qua92a]<br>[Qua92a, Qua92c]              | Set theory axioms based on NBG set theory   | C<br>C           | 91<br>21         | 2.0<br>1.8               | 8%<br>-                  | 21%<br>27%       |
| SET004<br>eq<br>-0<br>-1             | NBG1Subs<br>[Qua92a]<br>[Qua92a, Qua92c]          | Substitution axioms for set theory axioms   | C<br>C           | 65<br>7          | 2.2<br>2.4               | -<br>-                   | 79%<br>64%       |
| SYN001<br>ax<br>-0                   | RPT63<br>[SE94]                                   | Synthetic domain theory for EBL             | C                | 368              | 2.9                      | -                        | -                |
| TOP001<br>ax<br>-0                   | Topology<br>[WM89]                                | Point-set topology axioms                   | I                | 109              | 3.1                      | 21%                      | -                |

# 7 The TPTP v1.2.1 Generators Listing

| Syntactic name<br>V# | Semantic name<br>References   | Description  | V | Valid Sizes                                | TPTP<br>Size |
|----------------------|-------------------------------|--|---|--|--------------|
| GRP123               | 321COILS                      | (3,2,1) conjugate orthogonality                            |   |  |              |
| -1                   | [FSB93, Sla93, Zha94a, SFS95] |  | C | $X \geq 1$                                 | 3            |
| -2                   | [FSB93, Sla93, Zha94a, SFS95] |  | A | $X \geq 1$                                 | 3            |
| -3                   | [FSB93, Sla93, Zha94a, SFS95] |  | A | $X \geq 1$                                 | 3            |
| -4                   | [FSB93, Sla93, Zha94a, SFS95] |  | A | $X \geq 1$                                 | 3            |
| -6                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 3            |
| -7                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -8                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -9                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| GRP124               | 312COILS                      | (3,1,2) conjugate orthogonality                            |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 3            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -3                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -4                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -6                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 3            |
| -7                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -8                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -9                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 4            |
| GRP125               | Schroeder                     | (a.b).(b.a) = a  |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 3            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -3                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -4                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| GRP126               | SteinLaw3                     | (a.b).(b.a) = b  |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 3$                                 | 3            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 3$                                 | 3            |
| -3                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 3$                                 | 3            |
| -4                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 3$                                 | 3            |
| GRP127               | QG5                           | ((b.a).b).b) = a   |   |  |              |
| -1                   | [Ben85, FSB93, Sla93, SFS95]  |  | C | $X \geq 1$                                 | 3            |
| -2                   | [Ben85, FSB93, Sla93, SFS95]  |  | A | $X \geq 1$                                 | 3            |
| -3                   | [Ben85, FSB93, Sla93, SFS95]  |  | A | $X \geq 1$                                 | 3            |
| -4                   | [Ben85, FSB93, Sla93, SFS95]  |  | A | $X \geq 1$                                 | 3            |
| GRP128               | SchroederLaw1                 | (a.b).b = a.(a.b)  |   |  |              |
| -1                   | [BZ92, FSB93, Sla93, SFS95]   |  | C | $X \geq 1$                                 | 3            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -3                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| -4                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 3            |
| GRP129               | QG7                           | a.(b.a) = (b.a).b  |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 2            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| -3                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| -4                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| GRP130               | QG8                           | (a.(a.b)).b = a  |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 2            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| -3                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| -4                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| GRP131               | 321COILSNoIdem                | (3,2,1) conjugate orthogonality, no idempotence            |   |  |              |
| -1                   | [FSB93, Sla93, Zha94a, SFS95] |  | C | $X \geq 1$                                 | 2            |
| -2                   | [FSB93, Sla93, Zha94a, SFS95] |  | A | $X \geq 1$                                 | 2            |
| GRP132               | 312COILSNoIdem                | (3,1,2) conjugate orthogonality, no idempotence            |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 2            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| GRP133               | SchroederNoIdem               | (a.b).(b.a) = a, no idempotence                            |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 2            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| GRP134               | SteinLaw3NoIdem               | (a.b).(b.a) = b, no idempotence                            |   |  |              |
| -1                   | [FSB93, Sla93, SFS95]         |  | C | $X \geq 1$                                 | 2            |
| -2                   | [FSB93, Sla93, SFS95]         |  | A | $X \geq 1$                                 | 2            |
| GRP135               | QG5NoIdem                     | ((b.a).b).b) = a, no idempotence                           |   |  |              |
| -1                   | [Ben85, FSB93, Sla93, SFS95]  |  | C | $X \geq 1$                                 | 2            |
| -2                   | [Ben85, FSB93, Sla93, SFS95]  |  | A | $X \geq 1$                                 | 2            |
| MSC007               | Pigeon                        | Cook pigeon-hole problem                                   |   |  |              |
| -1                   | [CR79, Pel86]                 |  | C | $X \geq 2$                                 | 5            |
| -2                   | [CR79, Pel86, Pel88]          |  | C | $X \geq 2$                                 | 2            |
| MSC008               | LatSq                         | The (in)constructability of Graeco-Latin Squares           |   |  |              |
| -1                   | [Rob63]                       |  | C | $X \geq 2, X \bmod 4 = 2$                  | 2            |
| NUM283               | Factorial                     | Calculation of factorial                                   |   |  |              |
| -1                   |                               |  | C | $X \geq 1$                                 | 5            |
| NUM284               | Fibonacci                     | Calculation of fibonacci numbers                           |   |  |              |
| -1                   |                               |  | C | $X \geq 1$                                 | 10           |
| PUZ015               | Checkers1                     | Checkerboard and Dominoes : Opposing corners removed       |   |  |              |
| -2                   | [Sti93]                       |  | C | $X \geq 2$                                 | 3            |
| PUZ016               | Checkers2                     | Checkerboard and Dominoes : Row 1, columns 2 and 3 removed |   |  |              |
| -2                   | [Sti93]                       |  | C | $X \geq 3$                                 | 3            |
| PUZ034               | NQueens                       | N queens problem   |   |  |              |
| -1                   |                               |  | C | $X \geq 2$                                 | 3            |
| SYN001               | Allways                       | All signed combinations of some propositions.              |   |  |              |
| -1                   | [NS72, LS74, WM76, Pel86]     |  | - | $X \geq 1$                                 | 5            |
| SYN002               | OddEven                       | Odd and Even Problem                                       |   |  |              |
| -1                   | [SA92]                        |  | - | $X \geq 1, Y > X$<br>$(X + Y) \bmod 2 = 1$ | 7:8          |

| Syntactic name<br>V# | Semantic name<br>References | Description   | V | Valid Sizes          | TPTP<br>Size |
|----------------------|-----------------------------|---|---|----------------------|--------------|
| SYN003<br>-1         | Implies1<br>[Pla82]         | Implications that form a contradiction              | - | $X \geq 2$           | 6            |
| SYN004<br>-1         | Implies2<br>[Pla82]         | Implications that form a contradiction              | - | $X \geq 2$           | 7            |
| SYN005<br>-1         | Or1<br>[Pla82]              | Disjunctions that form a contradiction              | - | $X \geq 1$           | 10           |
| SYN010<br>-1         | Letz<br>[LMG94]             | Example for Proposition 5.2 in [Letz, et al., 1994] | - | $X \geq 1, Y \geq 1$ | 5:5          |
| SYN085<br>-1         | DAPs1<br>[Pla94]            | Plaisted problem s(1,SIZE)                          | - | $X \geq 0$           | 10           |
| SYN086<br>-1         | DAPs2<br>[Pla94]            | Plaisted problem s(2,SIZE)                          | - | $X \geq 1$           | 3            |
| SYN087<br>-1         | DAPs3<br>[Pla94]            | Plaisted problem s(3,SIZE)                          | - | $X \geq 1$           | 3            |
| SYN088<br>-1         | DAPs4<br>[Pla94]            | Plaisted problem s(4,SIZE)                          | - | $X \geq 1$           | 10           |
| SYN089<br>-1         | DAPt2<br>[Pla94]            | Plaisted problem t(2,SIZE)                          | - | $X \geq 1$           | 2            |
| SYN090<br>-1         | DAPt3<br>[Pla94]            | Plaisted problem t(3,SIZE)                          | - | $X \geq 1$           | 8            |
| SYN091<br>-1         | DAPsyms2<br>[Pla94]         | Plaisted problem sym(s(2,SIZE))                     | - | $X \geq 1$           | 3            |
| SYN092<br>-1         | DAPsyms3<br>[Pla94]         | Plaisted problem sym(s(3,SIZE))                     | - | $X \geq 1$           | 3            |
| SYN093<br>-1         | DAPut2<br>[Pla94]           | Plaisted problem u(t(2,SIZE))                       | - | $X \geq 1$           | 2            |
| SYN094<br>-1         | DAPut3<br>[Pla94]           | Plaisted problem u(t(3,SIZE))                       | - | $X \geq 1$           | 5            |
| SYN095<br>-1         | DAPmt2<br>[Pla94]           | Plaisted problem m(t(2,SIZE))                       | - | $X \geq 1$           | 2            |
| SYN096<br>-1         | DAPmt3<br>[Pla94]           | Plaisted problem m(t(3,SIZE))                       | - | $X \geq 1$           | 8            |
| SYN097<br>-1         | DAPsymut2<br>[Pla94]        | Plaisted problem sym(u(t(2,SIZE)))                  | - | $X \geq 1$           | 2            |
| SYN098<br>-1         | DAPsymut3<br>[Pla94]        | Plaisted problem sym(u(t(3,SIZE)))                  | - | $X \geq 1$           | 2            |
| SYN099<br>-1         | DAPsymmt2<br>[Pla94]        | Plaisted problem sym(m(t(2,SIZE)))                  | - | $X \geq 1$           | 3            |
| SYN100<br>-1         | DAPsymmt3<br>[Pla94]        | Plaisted problem sym(m(t(3,SIZE)))                  | - | $X \geq 1$           | 5            |
| SYN101<br>-1         | DAPnt2<br>[Pla94]           | Plaisted problem n(t(2,SIZE1),SIZE2)                | - | $X \geq 1, Y \geq 1$ | 2:2          |
| SYN102<br>-1         | DAPnt3<br>[Pla94]           | Plaisted problem n(t(3,SIZE1),SIZE2)                | - | $X \geq 1, Y \geq 1$ | 7:7          |
| SYN302<br>-1         | DAPa<br>[Pla94]             | Plaisted problem a(SIZE)                            | - | $X \geq 1$           | 3            |
| SYN313<br>-1         | Decide11<br>[Fer94]         | Problem for testing satisfiability                  | - | $X \geq 1, Y \geq 1$ | 1:2          |
| SYN314<br>-1         | Decide12<br>[Fer94]         | Problem for testing satisfiability                  | - | $X \geq 0, Y \geq 0$ | 2:1          |

## 8 The TPTP v1.2.1 Problems Listing

| Syntactic name<br>V#                                  | Semantic name<br>Other names                              | Description   | References                         | V | Cl  | Av  | nH  | Eq   |
|---|---|---|------------------------------------|---|-----|-----|-----|------|
| <b>Domain ALG (2 abstract problems, 4 problems)</b>   |   |   |                                    |   |     |     |     |      |
| ALG001  | CmpsnHomoms   | The composition of homomorphisms is a homomorphism            |                                    | - | 296 | 2.4 | 6%  | 40%  |
| -1  | Problem 221-223   |   | [BLM <sup>+</sup> 86]              | - | 269 | 2.3 | 7%  | 43%  |
| -2  | Problem 221-223, Test Problem 15                          |   | [Qua92a, Qua92b]                   | - | 190 | 2.0 | 4%  | 46%  |
| -3  | HO1, HO1  |   |                                    |   |     |     |     |      |
| ALG002  | OrdField  | In an ordered field, if $X > 0$ then $X^{-1} > 0$             |                                    | - | 14  | 2.0 | 14% | -    |
| -1  | Example 5, EX5-T?, ex5.lop, FEX5                          |   | [FLSY74, WM76]                     |   |     |     |     |      |
| <b>Domain ANA (5 abstract problems, 19 problems)</b>  |   |   |                                    |   |     |     |     |      |
| ANA001  | MinVal<br>AM8   | Attaining minimum (or maximum) value                          |                                    | - | 18  | 2.3 | 16% | -    |
| -1  |   |   | [WB87]                             |   |     |     |     |      |
| ANA002  | IntmedVal   | Intermediate value theorem                                    |                                    | - | 18  | 2.3 | 27% | -    |
| -1  |   |   | [WB87]                             | - | 18  | 2.3 | 27% | -    |
| -2  |   |   | [WB87]                             | - | 17  | 2.6 | 29% | -    |
| -3  | IMV   |   | [WB87]                             | - | 17  | 2.6 | 29% | -    |
| -4  | ivt.lop   |   | [WB87]                             | - | 17  | 2.6 | 29% | -    |
| ANA003  | SumContFuncLem1   | Lemma 1 for the sum of two continuous functions is continuous |                                    | - | 38  | 2.1 | -   | 47%  |
| -1  | probl.ver2.in   |   | [MOW76]                            | - | 17  | 2.2 | -   | -    |
| -2  | BL1, probl.ver1.in  |   | [MOW76]                            | - | 50  | 1.9 | 10% | 39%  |
| -3  |   |   | [Ble90, Ble92]                     | - | 12  | 2.3 | 33% | -    |
| -4  | Problem 1, Bledsoe-P1, p1.lop                             |   | [Ble90, LM92, Ble92]               |   |     |     |     |      |
| ANA004  | SumContFuncLem2   | Lemma 2 for the sum of two continuous functions is continuous |                                    | - | 38  | 2.1 | -   | 47%  |
| -1  |   |   | [MOW76]                            | - | 16  | 2.2 | -   | -    |
| -2  | BL2   |   | [MOW76]                            | - | 50  | 1.9 | 10% | 39%  |
| -3  |   |   | [Ble90, Ble92]                     | - | 13  | 2.2 | 30% | -    |
| -4  | Problem 2, p2.lop   |   | [Ble90, Ble92]                     | - | 16  | 2.0 | 25% | -    |
| -5  | Problem 3, p3.lop   |   | [Ble90, Ble92]                     |   |     |     |     |      |
| ANA005  | SumContFunc   | The sum of two continuous functions is continuous             |                                    | - | 38  | 2.1 | -   | 47%  |
| -1  | BL3   |   | [MOW76]                            | - | 16  | 2.2 | -   | -    |
| -2  | prob2.ver1.in   |   | [MOW76]                            | - | 50  | 1.9 | 10% | 39%  |
| -3  |   |   | [Ble90, Ble92]                     | - | 24  | 2.0 | 16% | -    |
| -4  | Problem 4, p4.lop   |   | [Ble90, Ble92]                     | - | 24  | 2.0 | 16% | -    |
| -5  | Problem 5, LIM+, p5.lop                                   |   | [Ble90, Ble92]                     |   |     |     |     |      |
| <b>Domain BOO (19 abstract problems, 52 problems)</b> |   |   |                                    |   |     |     |     |      |
| BOO001  | B3InvIvln<br>tba_gg.in                                    | In B3 algebra, inverse is an involution                       |                                    | - | 13  | 1.5 | -   | 100% |
| -1  |   |   |                                    |   |     |     |     |      |
| BOO002  | B3LId   | In B3 algebra, $X * X^{-1} * Y = Y$                           |                                    | - | 12  | 1.6 | -   | 100% |
| -1  | Problem 5, CADE-11 Comp. Eq-3,<br>THEOREM EQ-3, PROBLEM 3 |   | [LO85b, Ove90, Ove93, LM93, Zha93] |   |     |     |     |      |
| -2  | Test Problem 13, Lemma for Axiom Independence             |   | [Wos88]                            |   |     |     |     |      |
| BOO003  | MultiDem  | Multiplication is idempotent ( $X * X = X$ )                  |                                    | - | 37  | 2.6 | -   | 25%  |
| -1  | B2 part 1, prob2_part1.ver1.in                            |   | [Whi61, MOW76, OMW76]              | - | 23  | 1.3 | -   | 100% |
| -2  | prob2_part1.ver2.in                                       |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TA  |   | [Ver94]                            |   |     |     |     |      |
| BOO004  | AddIdem   | Addition is idempotent ( $X + X = X$ )                        |                                    | - | 37  | 2.6 | -   | 25%  |
| -1  | B2 part 2, prob2_part2.ver1                               |   | [Whi61, MOW76, OMW76]              | - | 23  | 1.3 | -   | 100% |
| -2  | prob2_part2.ver2.in                                       |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TA  |   | [Ver94]                            |   |     |     |     |      |
| BOO005  | AddBnd  | Addition is bounded ( $X + 1 = 1$ )                           |                                    | - | 37  | 2.6 | -   | 25%  |
| -1  | B3 part 1, B5, prob3_part1.ver1.in                        |   | [Whi61, MOW76, OMW76]              | - | 23  | 1.3 | -   | 100% |
| -2  | prob3_part1.ver2.in                                       |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TB  |   | [Ver94]                            |   |     |     |     |      |
| BOO006  | MultiBnd  | Multiplication is bounded ( $X * 0 = 0$ )                     |                                    | - | 37  | 2.6 | -   | 25%  |
| -1  | B3 part 2, B6, prob3_part2.ver1                           |   | [Whi61, MOW76, OMW76]              | - | 23  | 1.3 | -   | 100% |
| -2  | prob3_part2.ver2.in                                       |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TB  |   | [Ver94]                            |   |     |     |     |      |
| BOO007  | ProdAssoc   | Product is associative ( $(X * Y) * Z = X * (Y * Z)$ )        |                                    | - | 41  | 2.4 | -   | 25%  |
| -1  | Established lemma   |   | [Whi61, MOW76, Ver92]              | - | 23  | 1.3 | -   | 100% |
| -2  | associativity   |   | [Ver92]                            | - | 17  | 1.5 | -   | 100% |
| -4  | TD  |   | [Ver94]                            |   |     |     |     |      |
| BOO008  | SumAssoc  | Sum is associative ( $(X + Y) + Z = X + (Y + Z)$ )            |                                    | - | 41  | 2.4 | -   | 25%  |
| -1  | B1, Theorem 4, prob1.ver1.in                              |   | [Whi61, MOW76, OMW76]              | - | 23  | 1.3 | -   | 100% |
| -2  | prob1.ver2.in   |   |                                    | - | 35  | 2.1 | -   | 31%  |
| -3  | boolAss.in, bool.in                                       |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TD  |   | [Ver94]                            |   |     |     |     |      |
| BOO009  | MultiAbsb   | Multiplication absorption ( $X * (X + Y) = X$ )               |                                    | - | 37  | 2.6 | -   | 25%  |
| -1  | B4 part 1, prob4_part1.ver1                               |   | [Whi61, MOW76, OMW76]              | - | 23  | 1.3 | -   | 100% |
| -2  | prob4_part1.ver2.in                                       |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TC  |   | [Ver94]                            |   |     |     |     |      |
| BOO010  | AddAbsb   | Addition absorption ( $X + (X * Y) = X$ )                     |                                    | - | 37  | 2.6 | -   | 25%  |
| -1  | B4 part 2, prob4_part2.ver1                               |   | [Whi61, MOW76, OMW76]              | - | 23  | 1.3 | -   | 100% |
| -2  | prob4_part2.ver2.in                                       |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TC  |   | [Ver94]                            |   |     |     |     |      |
| BOO011  | InvAId  | Inverse of additive identity = Multiplicative identity        |                                    | - | 37  | 2.6 | -   | 26%  |
| -1  | B7, prob7.ver1  |   | [Whi61, MOW76]                     | - | 23  | 1.3 | -   | 100% |
| -2  | prob7.ver2.in   |   |                                    | - | 17  | 1.5 | -   | 100% |
| -4  | TG  |   | [Ver94]                            |   |     |     |     |      |

| Syntactic name<br>V#           | Semantic name<br>Other names                           | Description<br>References  | V | Cl | Av  | nH | Eq   |
|--------------------------------|--|--|---|----|-----|----|------|
| BOO012<br>-1<br>-2<br>-3<br>-4 | InvIvln<br>B8<br>prob8.ver2.in<br>B8, prob8.ver1<br>TF | Inverse is an involution<br>[Whi61, MOW76]<br>[Whi61, MOW76]<br>[Ver94]  | - | 37 | 2.6 | -  | 26%  |
| BOO013<br>-1<br>-2<br>-3<br>-4 | InvUnq<br>B9<br>prob9.ver2.in<br>B9, prob9.ver1<br>TE  | The inverse of X is unique<br>[Whi61, MOW76]<br>[Whi61, MOW76]<br>[Ver94]  | - | 41 | 2.4 | -  | 25%  |
| BOO014<br>-1<br>-2<br>-3<br>-4 | DeMorgan1<br>prob10.ver2.in<br>B10, prob.10.ver1<br>TH | DeMorgan for inverse and product $(X+Y)^{-1} = (X^{-1}) * (Y^{-1})$<br>[Whi61, MOW76]<br>[Whi61, MOW76]<br>[Ver94] | - | 39 | 2.5 | -  | 25%  |
| BOO015<br>-1<br>-2<br>-4       | DeMorgan2<br>DeMorgan's Laws<br>prob10.ver2.in<br>TH   | DeMorgan for inverse and sum $(X^{-1} + Y^{-1}) = (X * Y)^{-1}$<br>[MOW76, Ver92]<br>[Ver94]                       | - | 39 | 2.5 | -  | 25%  |
| BOO016<br>-1<br>-2             | ProdSum<br>Established lemma                           | Relating product and sum $(X * Y = Z \rightarrow X + Z = X)$<br>[Whi61, MOW76]                                     | - | 38 | 2.5 | -  | 25%  |
| BOO017<br>-1<br>-2             | SumProd<br>Established lemma                           | Relating sum and product $(X + Y = Z \rightarrow X * Z = X)$<br>[Whi61, MOW76]                                     | - | 38 | 2.5 | -  | 25%  |
| BOO018<br>-4                   | InvMid<br>TG   | Inverse of multiplicative identity = Additive identity<br>[Ver94]  | - | 17 | 1.5 | -  | 100% |
| BOO019<br>-1                   | IndpAx<br>A1, Example 4                                | Prove the independance of Ternary Boolean algebra axiom<br>[Win82, BCP94]  | - | 12 | 1.6 | -  | 100% |

### Domain CAT (19 abstract problems, 58 problems)

|                                |  |   |   |    |     |   |     |
|--------------------------------|--|---|---|----|-----|---|-----|
| CAT001<br>-1<br>-2<br>-3<br>-4 | Monom1<br>C1, p1.ver1.in<br>p1.ver2.in<br>p1.ver3.in | XY monomorphism => Y monomorphism<br>[Mit67, MOW76]<br>[Qua89a]<br>[Sco79]<br>[Sco79]                         | - | 36 | 2.3 | - | 27% |
| CAT002<br>-1<br>-2<br>-3<br>-4 | Monom2<br>C2, p2.ver1.in<br>p2.ver2.in<br>p2.ver3.in | X and Y monomorphisms, XY well-defined => XY monomorphism<br>[Mit67, MOW76]<br>[Qua89a]<br>[Sco79]<br>[Sco79] | - | 37 | 2.4 | - | 27% |
| CAT003<br>-1<br>-2<br>-3<br>-4 | Epim1<br>C3, p3.ver1.in<br>p3.ver2.in<br>p3.ver3.in  | XY epimorphism => X epimorphism<br>[Mit67, MOW76]<br>[Qua89a]<br>[Sco79]<br>[Sco79]                           | - | 36 | 2.3 | - | 27% |
| CAT004<br>-1<br>-2<br>-3<br>-4 | Epim2<br>C4, p4.ver1.in<br>p4.ver2.in<br>p4.ver3.in  | X and Y epimorphisms, XY well-defined => XY epimorphism<br>[MOW76]<br>[Qua89a]<br>[Sco79]<br>[Sco79]          | - | 37 | 2.4 | - | 27% |
| CAT005<br>-1<br>-3<br>-4       | DomUnqRId<br>C5, p5.ver1.in<br>p5.ver3.in            | Domain is the unique right identity<br>[Mit67, MOW76]<br>[Sco79]<br>[Sco79]                                   | - | 34 | 2.4 | - | 27% |
| CAT006<br>-1<br>-3<br>-4       | CodUnqLId<br>C6, p6.ver1.in<br>p6.ver3.in            | Codomain is the unique left identity<br>[Mit67, MOW76]<br>[Sco79]<br>[Sco79]                                  | - | 34 | 2.4 | - | 27% |
| CAT007<br>-1<br>-3             | DomEqCod<br>C7, p7.ver1.in<br>p7.ver3.in             | If domain(x) = codomain(y) then xy is defined<br>[Mit67, MOW76]<br>[MOW76, Sco79]                             | - | 33 | 2.4 | - | 27% |
| CAT008<br>-1                   | DomXCodY<br>C8, p8.ver1.in                           | If xy is defined then domain(x) = codomain(y)<br>[Mit67, MOW76]   | - | 33 | 2.4 | - | 27% |
| CAT009<br>-1<br>-3<br>-4       | DomXYDomY<br>p9.ver1.in<br>p9.ver3.in                | If xy is defined, then domain(xy) = domain(y)<br>[Mit67]<br>[Sco79]<br>[Sco79]                                | - | 33 | 2.4 | - | 27% |
| CAT010<br>-1<br>-4             | CodXYCodX<br>p10.ver1.in                             | If xy is defined, then codomain(xy) = codomain(x)<br>[Mit67]<br>[Sco79]                                       | - | 33 | 2.4 | - | 27% |
| CAT011<br>-1<br>-2<br>-3<br>-4 | DomIdem<br>p11.ver1.in<br>p11.ver2.in<br>p11.ver3.in | domain(domain(x)) = domain(x)<br>[Mit67]<br>[Qua89a]<br>[Sco79]<br>[Sco79]                                    | - | 32 | 2.4 | - | 28% |
| CAT012<br>-1<br>-3<br>-4       | CodOfDom<br>p12.ver1.in<br>p12.ver3.in               | codomain(domain(x)) = domain(x)<br>[Mit67]<br>[Sco79]<br>[Sco79]  | - | 32 | 2.4 | - | 28% |
| CAT013<br>-1<br>-3<br>-4       | DomOfCod<br>p13.ver1.in<br>p13.ver3.in               | domain(codomain(x)) = codomain(x)<br>[Mit67]<br>[Sco79]<br>[Sco79]  | - | 32 | 2.4 | - | 28% |

| Syntactic name<br>V#                 | Semantic name<br>Other names  | Description                            | References   | V | Cl | Av  | nH | Eq  |
|--------------------------------------|---|--|--|---|----|-----|----|-----|
| CAT014<br>-1<br>-2<br>-3<br>-4       | CodDdem<br>p14.ver1.in<br>p14.ver2.in<br>p14.ver3.in  | codomain(codomain(x)) = codomain(x)    | [Mit67]<br>[Qua89a]<br>[Sco79]<br>[Sco79]            | - | 32 | 2.4 | -  | 28% |
| CAT015<br>-3<br>-4                   | Exist<br>p15.related.in   | Prove something exists                 | [Sco79]<br>[Sco79]                                   | - | 31 | 2.2 | 9% | 54% |
| CAT016<br>-3<br>-4                   | DomEx<br>p16.ver3.in  | If x exists, then domain(x) exists     | [Sco79]<br>[Sco79]                                   | - | 31 | 2.1 | 6% | 54% |
| CAT017<br>-3<br>-4                   | CodEx<br>p17.ver3.in  | If x exists, then codomain(x) exists   | [Sco79]<br>[Sco79]                                   | - | 31 | 2.1 | 6% | 54% |
| CAT018<br>-1<br>-3<br>-4             | FactEx<br>p18.ver1.in<br>p18.ver3.in  | If xy and yz exist, then so does x(yz) | [Mit67]<br>[Sco79]<br>[Sco79]                        | - | 34 | 2.4 | -  | 26% |
| CAT019<br>-1<br>-2<br>-3<br>-4<br>-5 | Indisc<br>p15.ver1.in<br>p15.ver2.in<br>p15.ver3.no2.in, p15.ver3.no4.in<br>p15.ver3.no1.in | Axiom of Indiscernibles                | [Mit67]<br>[Qua89a]<br>[Sco79]<br>[Sco79]<br>[Sco79] | - | 34 | 2.4 | -  | 31% |

### Domain CID (3 abstract problems, 4 problems)

|                    |  |                                    |                      |   |    |     |   |     |
|--------------------|--|------------------------------------|----------------------|---|----|-----|---|-----|
| CID001<br>-1       | OrNand<br>design_or.ver1.clauses                       | Design an OR gate using NAND gates | [WOLB92]             | - | 21 | 1.9 | - | 64% |
| CID002<br>-1       | Intchg<br>interchange.ver1.clauses                     | Interchange inputs to outputs      | [WOLB92]             | - | 58 | 1.7 | - | 59% |
| CID003<br>-1<br>-2 | TwoInv<br>two.inverter.ver1.in<br>two.inverter.ver2.in | Invert 3 inputs with 2 not gates   | [WOLB92]<br>[WOLB92] | - | 69 | 2.0 | - | 61% |

### Domain CIV (4 abstract problems, 4 problems)

|              |                                    |                                  |          |   |    |     |   |     |
|--------------|------------------------------------|----------------------------------|----------|---|----|-----|---|-----|
| CIV001<br>-1 | Intchg<br>intchg_val.ver1.clauses  | Interchange inputs to outputs    | [WOLB92] | - | 61 | 1.3 | - | 92% |
| CIV002<br>-1 | TwoInv<br>two.inverter.val.ver1.in | Invert 3 inputs with 2 not gates | [WOLB92] | - | 62 | 1.2 | - | 89% |
| CIV003<br>-1 | Adder1                             | One bit Full Adder               | [WOLB92] | - | 65 | 1.3 | - | 92% |
| CIV004<br>-1 | Adder2                             | Two bit Full Adder               | [WOLB92] | - | 60 | 1.4 | - | 90% |

### Domain COL (81 abstract problems, 141 problems)

|   |  |   |  |   |    |     |   |      |
|---|--|---|--|---|----|-----|---|------|
| COL001<br>-1<br>-2  | WkFxdPtSK<br>C1  | Weak fixed point for S and K                        | [Smu78a, WM88a]<br>[WM88a]   | - | 8  | 1.6 | - | 100% |
| COL002<br>-1<br>-2<br>-3  | WkFxdPtSBCI<br>C1.1  | Weak fixed point for S, B, C, and I                 | [WM88a]<br>[WM88a]<br>[WM88a]  | - | 10 | 1.5 | - | 100% |
| COL003<br>-1<br>-2<br>-3<br>-4<br>-5<br>-6<br>-7<br>-8<br>-9<br>-10 | StrongFxdPtBW<br>C2, Test Problem 17, CADE-11 Comp. Eq-8,<br>CL2, EQ-8, Question 3, Quest. 5, PROBL. 8 | Strong fixed point for B and W                      | [Smu78a, MW87, WM88a, Wos88, Ove90]<br>[LW92, Wos93, Ove93, LM93, Zha93]<br>[Smu78a, MW87, WM88a, Wos93]<br>[Smu78a, MW87, WM88a, Wos93]<br>[Smu78a, MW87, WM88a, Wos93]<br>[Smu78a, MW87, WM88a, Wos93]<br>[Smu78a, MW87, WM88a, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93] | - | 9  | 1.7 | - | 100% |
| COL004<br>-1<br>-2<br>-3  | SK_U<br>C4   | Find combinator equivalent to U from S and K        | [WM88a]<br>[WM88a]<br>[WM88a]  | - | 10 | 1.7 | - | 100% |
| COL005<br>-1  | SWModel<br>C5, Question 15   | Find a model for S and W but not a weak fixed point | [WM88a, Zha92, Wos93]  | - | 8  | 1.6 | - | 100% |
| COL006<br>-1<br>-2<br>-3<br>-4                                      | StrongFxdPtSK<br>C6  | Strong fixed point for S and K                      | [WM88a]<br>[WM88a]<br>[WM88a]<br>[WM88a]   | - | 9  | 1.7 | - | 100% |
| COL007<br>-1  | WkFxdPtL   | Weak fixed point for L                              | [Smu78a, MW87, WM88a, MW88]  | - | 7  | 1.7 | - | 100% |
| COL008<br>-1  | WkFxdPtMB<br>Question 13   | Weak fixed point for M and B                        | [Smu78a, MW87, WM88a, MW88, Wos93]   | - | 8  | 1.6 | - | 100% |
| COL009<br>-1  | WkFxdPtBL2   | Weak fixed point for B and L2                       | [Smu78a, MW87, WM88a, MW88]  | - | 8  | 1.6 | - | 100% |

| Syntactic name<br>V#                 | Semantic name<br>Other names       | Description<br>References  | V                     | Cl                        | Av                              | nH                    | Eq                               |
|--------------------------------------|------------------------------------|--|-----------------------|---------------------------|---------------------------------|-----------------------|----------------------------------|
| COL010<br>-1                         | WkFxdPtBS2                         | Weak fixed point for B and S2<br>[Smu78a, MW87, WM88a, MW88]   | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL011<br>-1                         | WkFxdPtOQ1                         | Weak fixed point for O and Q1<br>[Smu78a, MW87, WM88a, MW88]   | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL012<br>-1                         | WkFxdPtU                           | Weak fixed point for U<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 7                         | 1.7                             | -                     | 100%                             |
| COL013<br>-1                         | WkFxdPtSL                          | Weak fixed point for S and L<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL014<br>-1                         | WkFxdPtLO                          | Weak fixed point for L and O<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL015<br>-1                         | WkFxdPtQM                          | Weak fixed point for Q and M<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL016<br>-1                         | WkFxdPtBML                         | Weak fixed point for B, M and L<br>[Smu78a, MW87, WM88a, MW88]   | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL017<br>-1                         | WkFxdPtBMT                         | Weak fixed point for B, M, and T<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL018<br>-1                         | WkFxdPtWQL                         | Weak fixed point for W, Q, and L<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL019<br>-1                         | WkFxdPtBST                         | Weak fixed point for B, S, and T<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL020<br>-1                         | WkFxdPtBSC                         | Weak fixed point for B, S, and C<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL021<br>-1                         | WkFxdPtBMV                         | Weak fixed point for B, M, and V<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL022<br>-1                         | WkFxdPtBOM                         | Weak fixed point for B, O, and M<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL023<br>-1                         | WkFxdPtBN                          | Weak fixed point for B and N<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL024<br>-1                         | WkFxdPtBMC                         | Weak fixed point for B, M, and C<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL025<br>-1                         | WkFxdPtBW<br>stage1.in & stage2.in | Weak fixed point for B and W<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL026<br>-1                         | WkFxdPtBW1                         | Weak fixed point for B and W1<br>[Smu78a, MW87, WM88a, MW88]   | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL027<br>-1                         | WkFxdPtBH                          | Weak fixed point for B and H<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL028<br>-1                         | WkFxdPtBN                          | Weak fixed point for B and N<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 8                         | 1.6                             | -                     | 100%                             |
| COL029<br>-1                         | StrongFxdPtU<br>Question 1         | Strong fixed point for U<br>[Smu78a, MW87, WM88a, MW88, Wos93]   | -                     | 8                         | 1.8                             | -                     | 100%                             |
| COL030<br>-1                         | StrongFxdPtSL                      | Strong fixed point for S and L<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.7                             | -                     | 100%                             |
| COL031<br>-1                         | StrongFxdPtLO                      | Strong fixed point for L and O<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.7                             | -                     | 100%                             |
| COL032<br>-1                         | StrongFxdPtQM                      | Strong fixed point for Q and M<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 9                         | 1.7                             | -                     | 100%                             |
| COL033<br>-1                         | StrongFxdPtBML                     | Strong fixed point for B, M and L<br>[Smu78a, MW87, WM88a, MW88]   | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL034<br>-1                         | StrongFxdPtBMT                     | Strong fixed point for B, M, and T<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL035<br>-1                         | StrongFxdPtWQL                     | Strong fixed point for W, Q, and L<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL036<br>-1                         | StrongFxdPtBST                     | Strong fixed point for B, S, and T<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL037<br>-1                         | StrongFxdPtBSC                     | Strong fixed point for B, S, and C<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL038<br>-1                         | StrongFxdPtBMV                     | Strong fixed point for B, M, and V<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL039<br>-1                         | StrongFxdPtBOM                     | Strong fixed point for B, O, and M<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL040<br>-1                         | StrongFxdPtBN<br>Question 5        | Strong fixed point for B and N<br>[Smu78a, MW87, WM88a, MW88, Wos93]   | -                     | 9                         | 1.7                             | -                     | 100%                             |
| COL041<br>-1                         | StrongFxdPtBMC                     | Strong fixed point for B, M, and C<br>[Smu78a, MW87, WM88a, MW88]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL042<br>-1<br>-2<br>-3<br>-4<br>-5 | StrongFxdPtBW1<br>Question 5       | Strong fixed point for B and W1<br>[Smu78a, MW87, WM88a, MW88, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93]      | -<br>-<br>-<br>-<br>- | 9<br>9<br>9<br>9<br>9     | 1.7<br>1.7<br>1.7<br>1.7<br>1.7 | -<br>-<br>-<br>-<br>- | 100%<br>86%<br>86%<br>86%<br>86% |
| COL043<br>-1<br>-2                   | StrongFxdPtBH<br>CL4, Question 5   | Strong fixed point for B and H<br>[Smu78a, MW87, WM88a, MW88, LW92, Wos93]<br>[WM88a, Wos93]   | -<br>-                | 9<br>10                   | 1.7<br>1.7                      | -<br>-                | 100%<br>88%                      |
| COL044<br>-1<br>-2<br>-3<br>-4<br>-5 | StrongFxdPtBN<br>CL3, Question 5   | Strong fixed point for B and N<br>[Smu78a, MW87, WM88a, MW88, LW92, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93]<br>[WM88a, Wos93] | -<br>-<br>-<br>-<br>- | 9<br>10<br>10<br>10<br>10 | 1.7<br>1.7<br>1.7<br>1.7<br>1.7 | -<br>-<br>-<br>-<br>- | 100%<br>88%<br>88%<br>88%<br>88% |
| COL045<br>-1                         | WkFxdPtBMS                         | Weak fixed point for B, M and S<br>[Smu78a, MW87, WM88a, Wos89]  | -                     | 9                         | 1.6                             | -                     | 100%                             |
| COL046<br>-1                         | StrongFxdPtBMS                     | Strong fixed point for B, M and S<br>[Smu78a, MW87, WM88a, Wos89]  | -                     | 10                        | 1.6                             | -                     | 100%                             |
| COL047<br>-1                         | LQModel<br>Question 7, Question 17 | Find a model for L and Q but not a strong fixed point<br>[Zha92, Wos93]  | -                     | 9                         | 1.7                             | -                     | 100%                             |



| Syntactic name<br>V# | Semantic name<br>Other names                                     | Description                               | References   | V   | Cl   | Av  | nH  | Eq   |
|----------------------|--|---|--|---|--|---|---|--|
| COL048               | -1   | WkFxdPtBWM                                | Weak fixed point for B, W, and M<br>[Smu78a, MW87, WM88a, MW88]  | -   | 9  | 1.6   | -   | 100%   |
| COL049               | -1   | StrongFxdPtBWM                            | Strong fixed point for B, W, and M<br>Problem 2, CADE-11 Comp. Eq-6, CL1,<br>THEOREM EQ-6, Question 2, PROBLEM 6<br>[Smu78a, MW87, WM88a, Ove90, LW92]<br>[Wos93, Ove93, LM93, Zha93]  | -   | 10   | 1.6   | -   | 100%   |
| COL050               | -1   | MBird01<br>bird1.ver1.in                  | The Significance of the Mockingbird<br>[Smu78a]  | -   | 10   | 1.7   | -   | 100%   |
| COL051               | -1   | MBird02<br>bird2.ver1.in                  | Egocentric mocking bird?<br>[Smu78a]   | -   | 10   | 1.7   | -   | 100%   |
| COL052               | -1<br>-2   | MBird03<br>bird4.ver1.in<br>bird4.ver2.in | A Question on Agreeable Birds<br>[Smu78a]<br>[Smu78a]  | -<br>-  | 12<br>16   | 1.7<br>1.8  | -<br>-  | 100%<br>79%  |
| COL053               | -1   | MBird04<br>bird5.ver1.in                  | An Exercise in Composition<br>[Smu78a]   | -   | 10   | 1.8   | -   | 100%   |
| COL054               | -1   | MBird05<br>bird6.ver1.in                  | Compatible Birds<br>[Smu78a]   | -   | 10   | 1.8   | -   | 100%   |
| COL055               | -1   | MBird06<br>bird7.ver1.in                  | Happy Birds<br>[Smu78a]  | -   | 7  | 1.9   | -   | 100%   |
| COL056               | -1   | MBird07<br>bird8.ver1.in                  | Normal Birds<br>[Smu78a]   | -   | 11   | 1.6   | -   | 100%   |
| COL057               | -1   | StrongFxdPtSBCI<br>CL5                    | Strong fixed point for S, B, C, and I<br>[LW92]  | -   | 11   | 1.5   | -   | 100%   |
| COL058               | -1<br>-2<br>-3   | Lark1                                     | If there's a lark, then there's an egocentric bird.<br>[Smu78a, GO86]<br>[Smu78a, GO86]<br>[Smu78a, GO86]  | -<br>-<br>-   | 7<br>7<br>7  | 1.7<br>1.7<br>1.7   | -<br>-<br>-   | 100%<br>100%<br>100%   |
| COL059               | -1   | Lark2                                     | L3 ((lark lark) lark) is not egocentric.<br>[Smu78a, GO86]   | -   | 13   | 1.4   | -   | 100%   |
| COL060               | -1<br>-2<br>-3   | BT_Q<br>CL-1                              | Find combinator equivalent to Q from B and T<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]   | -<br>-<br>-   | 11<br>8<br>8   | 1.7<br>1.6<br>1.6   | -<br>-<br>-   | 100%<br>100%<br>100%   |
| COL061               | -1<br>-2<br>-3   | BT_Q1<br>CL-2                             | Find combinator equivalent to Q1 from B and T<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]  | -<br>-<br>-   | 11<br>8<br>8   | 1.7<br>1.6<br>1.6   | -<br>-<br>-   | 100%<br>100%<br>100%   |
| COL062               | -1<br>-2<br>-3   | BT_C<br>CL-3                              | Find combinator equivalent to C from B and T<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]   | -<br>-<br>-   | 11<br>8<br>8   | 1.7<br>1.6<br>1.6   | -<br>-<br>-   | 100%<br>100%<br>100%   |
| COL063               | -1<br>-2<br>-3<br>-4<br>-5<br>-6                                 | BT_F<br>CL-4                              | Find combinator equivalent to F from B and T<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]   | -<br>-<br>-<br>-<br>-<br>-                          | 11<br>8<br>8<br>8<br>8<br>8                          | 1.7<br>1.6<br>1.6<br>1.6<br>1.6<br>1.6                                    | -<br>-<br>-<br>-<br>-<br>-                          | 100%<br>100%<br>100%<br>100%<br>100%<br>100%   |
| COL064               | -1<br>-2<br>-3<br>-4<br>-5<br>-6<br>-7<br>-8<br>-9<br>-10<br>-11 | BT_V<br>CL-5                              | Find combinator equivalent to V from B and T<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90] | -<br>-<br>-<br>-<br>-<br>-<br>-<br>-<br>-<br>-<br>- | 11<br>8<br>8<br>8<br>8<br>8<br>8<br>8<br>8<br>8<br>8 | 1.7<br>1.6<br>1.6<br>1.6<br>1.6<br>1.6<br>1.6<br>1.6<br>1.6<br>1.6<br>1.6 | -<br>-<br>-<br>-<br>-<br>-<br>-<br>-<br>-<br>-<br>- | 100%<br>100%<br>100%<br>100%<br>100%<br>100%<br>100%<br>100%<br>100%<br>100%<br>100% |
| COL065               | -1   | BT_G<br>CL-6                              | Find combinator equivalent to G from B and T<br>[WM88a, WWM <sup>+</sup> 90]   | -   | 12   | 1.8   | -   | 100%   |
| COL066               | -1<br>-2<br>-3   | BQW_P<br>CL-7                             | Find combinator equivalent to P from B, Q and W<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]<br>[WM88a, WWM <sup>+</sup> 90]  | -<br>-<br>-   | 12<br>9<br>9   | 1.7<br>1.6<br>1.6   | -<br>-<br>-   | 100%<br>100%<br>100%   |
| COL067               | -1   | StrongFxdPtBS<br>Question 4, Question 5   | Strong fixed point for B and S<br>[WM88a, Wos93]   | -   | 9  | 1.7   | -   | 100%   |
| COL068               | -1   | WeakFxdPtBS<br>Question 11                | Weak fixed point for B and S<br>[WM88a, Wos93]   | -   | 8  | 1.6   | -   | 100%   |
| COL069               | -1   | StrongFxdPtBL<br>Question 6               | Strong fixed point for B and L<br>[WM88a, Wos93]   | -   | 9  | 1.7   | -   | 100%   |
| COL070               | -1   | WeakFxdPtBN1<br>Question 12               | Weak fixed point for B and I1<br>[WM88a, Wos93, Zha94b]  | -   | 8  | 1.6   | -   | 100%   |
| COL071               | -1   | StrongFxdPtNQ<br>Question 14              | Strong fixed point for I and Q<br>[WM88a, Wos93, Zha95]  | -   | 9  | 1.7   | -   | 100%   |
| COL072               | -1   | StrongFxdPtBL<br>Question 16              | Strong fixed point for B and L<br>[WM88a, Wos93]   | -   | 9  | 1.7   | -   | 100%   |
| COL073               | -1   | StrongFxdPtBN1<br>Question 18             | Strong fixed point for B and I1<br>[WM88a, Wos93, Zha94b]  | -   | 9  | 1.7   | -   | 100%   |
| COL074               | -1<br>-2<br>-3   | UnSatTRC                                  | Unsatisfiable variant of TRC<br>[Jec93b]<br>[Jec93b]<br>[Jec93b]   | -<br>-<br>-   | 19<br>20<br>22                                       | 1.6<br>1.6<br>1.5   | 5%<br>5%<br>4%                                      | 100%<br>100%<br>100%   |

| Syntactic name<br>V# | Semantic name<br>Other names | Description  | References           | V | Cl | Av  | nH | Eq   |
|----------------------|------------------------------|--|----------------------|---|----|-----|----|------|
| COL075<br>-1<br>-2   | UnSatTRCLEm1                 | Lemma 1 for showing the unsatisfiable variant of TRC | [Jec93b]<br>[Jec93b] | - | 22 | 1.6 | 4% | 100% |
| COL076<br>-1<br>-2   | UnSatTRCLEm2                 | Lemma 2 for showing the unsatisfiable variant of TRC | [Jec93b]<br>[Jec93b] | - | 21 | 1.5 | 4% | 100% |
| COL077<br>-1         | TRC1a<br>Proposition 1a      | Abst Abst Abst Abst Abst Abst = Id                   | [Jec93b]             | - | 22 | 1.5 | 4% | 100% |
| COL078<br>-1<br>-2   | TRC1b<br>Proposition 1b      | Abst Abst Abst Abst = k(k(id))                       | [Jec93b]<br>[Jec93b] | - | 22 | 1.5 | 4% | 100% |
| COL079<br>-1<br>-2   | TRC2a<br>Proposition 2a      | Abst (Abst (Abst X)) = Abst X                        | [Jec93b]<br>[Jec93b] | - | 21 | 1.6 | 4% | 100% |
| COL080<br>-1<br>-2   | TRC2b<br>Proposition 2b      | Abst (Abst k(X)) = k(X)                              | [Jec93b]<br>[Jec93b] | - | 22 | 1.5 | 4% | 100% |
| COL081<br>-1<br>-2   | TRC2c<br>Proposition 2c      | Abst k(k(X)) = k(k(X))                               | [Jec93b]<br>[Jec93b] | - | 22 | 1.5 | 4% | 100% |

### Domain COM (4 abstract problems, 6 problems)

|                    |                     |                                    |  |   |    |     |     |     |
|--------------------|---------------------|------------------------------------|--|---|----|-----|-----|-----|
| COM001<br>-1       | 4StSp<br>SHORTBURST | A program correctness theorem      | [RRY <sup>+</sup> 72, WM76]                          | - | 11 | 1.5 | -   | -   |
| COM002<br>-1<br>-2 | 8StSp<br>BURSTALL   | A program correctness theorem      | [RRY <sup>+</sup> 72, WM76]<br>[RRY <sup>+</sup> 72] | - | 19 | 1.3 | -   | -   |
| COM003<br>-1<br>-2 | Halting             | The halting problem is undecidable | [Bur87b, Bur87a]<br>[Bur87a, Bru91]                  | - | 50 | 5.5 | 64% | -   |
| COM004<br>-1       | Resolution          | Part of completeness of resolution |  | - | 25 | 2.0 | -   | 54% |

### Domain GEO (78 abstract problems, 165 problems)

|                                      |   |   |  |   |    |     |     |     |
|--------------------------------------|---|---|--|---|----|-----|-----|-----|
| GEO001<br>-1<br>-2<br>-3<br>-4       | BtwnSymm<br>T1, Theorem 5, t1.ver1.in<br>T1                           | Betweenness is symmetric in its outer arguments         | [MOW76, OMW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]<br>[MOW76, Wos88]                            | - | 57 | 2.5 | 10% | 49% |
| GEO002<br>-1<br>-2<br>-3<br>-4       | XBtwnXY<br>T2, t2.ver1.in<br>T2                                       | For all points x and y, x is between x and y            | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]<br>[MOW76, Wos88]                                   | - | 56 | 2.5 | 10% | 50% |
| GEO003<br>-1<br>-2<br>-3             | YBtwnXY<br>T3, t3.ver1.in<br>T3                                       | For all points x and y, y is between x and y            | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]   | - | 56 | 2.5 | 10% | 50% |
| GEO004<br>-1<br>-2                   | MidPtEx<br>T4, t4.ver1.in<br>T4                                       | Every line segment has a midpoint                       | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]   | - | 57 | 2.5 | 10% | 50% |
| GEO005<br>-1<br>-2                   | IsosTriEx<br>T5, t5.ver1.in<br>T5                                     | Isosceles triangle based on line segment                | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]   | - | 57 | 2.5 | 10% | 50% |
| GEO006<br>-1<br>-2<br>-3             | Btwn3Pts<br>T6, t6.ver1.in<br>T6                                      | Betweenness for 3 points on a line                      | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]   | - | 60 | 2.5 | 11% | 50% |
| GEO007<br>-1<br>-2<br>-3             | Btwn4Pts<br>T7, t7.ver1.in<br>T7                                      | Betweenness for 4 points on a line                      | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]   | - | 60 | 2.4 | 10% | 49% |
| GEO008<br>-1<br>-2<br>-3             | Btwn5Pts<br>T8, Test Problem 10, Five Point Theorem, t8.ver1.in<br>T8 | Betweenness for 5 points on a line (Five point theorem) | [MOW76, SST83, Wos88]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]  | - | 59 | 2.5 | 10% | 49% |
| GEO009<br>-1<br>-2<br>-3             | IstInrConn<br>T9, t9.ver1.in<br>T9                                    | First inner connectivity property of betweenness        | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]   | - | 59 | 2.5 | 10% | 49% |
| GEO010<br>-1<br>-2<br>-3             | CollInvar<br>T10, t10.ver1.in<br>T10                                  | Collinearity is invariant                               | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]   | - | 64 | 2.6 | 10% | 44% |
| GEO011<br>-1<br>-2<br>-3<br>-4<br>-5 | AxPtsNotColl<br>T11, t11.ver1.in<br>T11<br>t11.ver2.in                | The axiom set points are not collinear                  | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b] | - | 63 | 2.6 | 11% | 46% |
| GEO012<br>-1<br>-2<br>-3             | Coll4Pts<br>T12, t12.ver1.in<br>T12                                   | Collinearity for 4 points                               | [MOW76, SST83]<br>[MOW76, SST83, Qua89b]<br>[MOW76, SST83, Qua89b]   | - | 68 | 2.5 | 10% | 46% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References   | V | Cl  | Av  | nH  | Eq  |
|----------------------|------------------------------|---|---|-----|-----|-----|-----|
| GEO013               | Coll5Pts                     | Collinearity for 5 points   |   |     |     |     |     |
| -1                   | T13, t13.ver1.in             | [MOW76, SST83]  | - | 67  | 2.5 | 10% | 45% |
| -2                   |                              | [MOW76, SST83, Qua89b]  | - | 65  | 2.4 | 9%  | 47% |
| -3                   | T13                          | [MOW76, SST83, Qua89b]  | - | 154 | 2.5 | 16% | 33% |
| GEO014               | EqidRefl                     | Ordinary reflexivity of equidistance                              |   |     |     |     |     |
| -2                   | D1                           | [SST83, Qua89b]   | - | 54  | 2.5 | 9%  | 52% |
| GEO015               | EqidSymm1                    | Equidistance is symmetric between its argument pairs              |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 51% |
| -3                   | D2                           | [SST83, Qua89b]   | - | 56  | 2.4 | 8%  | 51% |
| GEO016               | EqidSymm2                    | Equidistance is symmetric within its argument pairs               |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 51% |
| -3                   | D3                           | [SST83, Qua89b]   | - | 57  | 2.4 | 8%  | 50% |
| GEO017               | EqidSymmCor1                 | Corollary 1 to symmetries of equidistance                         |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 51% |
| -3                   | D4.1                         | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 50% |
| GEO018               | EqidSymmCor2                 | Corollary 2 to symmetries of equidistance                         |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 51% |
| -3                   | D4.2                         | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 50% |
| GEO019               | EqidSymmCor3                 | Corollary 3 to symmetries of equidistance                         |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 51% |
| -3                   | D4.3                         | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 50% |
| GEO020               | EqidSymmCor4                 | Corollary 4 to symmetries of equidistance                         |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 51% |
| -3                   | D4.4                         | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 50% |
| GEO021               | EqidSymmCor5                 | Corollary 5 to symmetries of equidistance                         |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 51% |
| -3                   | D4.5                         | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 50% |
| GEO022               | EqidTrans                    | Ordinary transitivity of equidistance                             |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 56  | 2.4 | 8%  | 51% |
| -3                   | D5                           | [SST83, Qua89b]   | - | 64  | 2.4 | 7%  | 46% |
| GEO024               | NullSegsCong                 | All null segments are congruent                                   |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 54  | 2.5 | 9%  | 52% |
| -3                   | D7                           | [SST83, Qua89b]   | - | 73  | 2.3 | 6%  | 49% |
| GEO025               | SumEqSeg                     | Addition of equal segments  |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 50% |
| -3                   | D8                           | [SST83, Qua89b]   | - | 78  | 2.2 | 6%  | 47% |
| GEO026               | ExtUnq                       | Extension is unique   |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 52% |
| -3                   | D9                           | [SST83, Qua89b]   | - | 79  | 2.2 | 6%  | 47% |
| GEO027               | ExtUnqCor1                   | Corollary 1 to unique extension                                   |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 56  | 2.4 | 8%  | 52% |
| -3                   | D10.1                        | [SST83, Qua89b]   | - | 78  | 2.3 | 7%  | 47% |
| GEO028               | ExtUnqCor2                   | Corollary 2 to unique extension                                   |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 56  | 2.4 | 8%  | 52% |
| -3                   | D10.2                        | [SST83, Qua89b]   | - | 78  | 2.3 | 7%  | 47% |
| GEO029               | ExtUnqCor3                   | Corollary 3 to unique extension                                   |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 53% |
| -3                   | D10.3                        | [SST83, Qua89b]   | - | 77  | 2.3 | 7%  | 48% |
| GEO030               | Out5SegCor                   | Corollary to the outer five-segment axiom                         |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 52% |
| -3                   | D11                          | [SST83, Qua89b]   | - | 106 | 2.3 | 13% | 43% |
| GEO031               | 2ndInr5Seg                   | Second inner five-segment theorem                                 |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 60  | 2.3 | 8%  | 50% |
| -3                   | D12                          | [SST83, Qua89b]   | - | 109 | 2.3 | 13% | 42% |
| GEO032               | DiffEqSeg                    | Equal difference between pairs of equal length line segments      |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 58  | 2.4 | 8%  | 50% |
| -3                   | D13                          | [SST83, Qua89b]   | - | 108 | 2.4 | 13% | 41% |
| GEO033               | 1stInr5Seg                   | First inner five-segment theorem                                  |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 60  | 2.3 | 8%  | 50% |
| -3                   | D14                          | [SST83, Qua89b]   | - | 111 | 2.4 | 13% | 40% |
| GEO034               | 1stInr5SegCor                | Corollary to the first inner five-segment theorem                 |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 57  | 2.4 | 8%  | 51% |
| -3                   | D15                          | [SST83, Qua89b]   | - | 109 | 2.4 | 13% | 40% |
| GEO035               | NullExt                      | A null extension does not extend a line                           |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 54  | 2.5 | 9%  | 53% |
| -3                   | E1                           | [SST83, Qua89b]   | - | 63  | 2.4 | 7%  | 46% |
| GEO036               | AxPtsEx                      | The 3 axiom set points are distinct                               |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 54  | 2.5 | 11% | 53% |
| -3                   | E2                           | [SST83, Qua89b]   | - | 95  | 2.4 | 14% | 44% |
| GEO037               | ExtSegEx                     | A segment can be extended   |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 54  | 2.5 | 9%  | 52% |
| -3                   | E3                           | [SST83, Qua89b]   | - | 98  | 2.4 | 13% | 44% |
| GEO038               | SegConsCor1                  | Corollary 1 to the segment construction axiom                     |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 55  | 2.5 | 9%  | 52% |
| -3                   | B0                           | [SST83, Qua89b]   | - | 65  | 2.4 | 7%  | 46% |
| GEO039               | IdBtwnCor                    | Corollary the identity axiom for betweenness                      |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 56  | 2.4 | 8%  | 52% |
| -3                   | B1                           | [SST83, Qua89b]   | - | 84  | 2.3 | 10% | 48% |
| GEO040               | BtwnASym                     | Antisymmetry of betweenness in its first two arguments            |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 56  | 2.4 | 8%  | 52% |
| -3                   | B2                           | [SST83, Qua89b]   | - | 87  | 2.3 | 10% | 47% |
| GEO041               | BtwnASymCor                  | Corollary to antisymmetry of betweenness in its first 2 arguments |   |     |     |     |     |
| -2                   |                              | [SST83, Qua89b]   | - | 56  | 2.4 | 8%  | 52% |
| -3                   | B3                           | [SST83, Qua89b]   | - | 88  | 2.3 | 10% | 47% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References  | V      | Cl        | Av         | nH        | Eq         |
|----------------------|------------------------------|--|--------|-----------|------------|-----------|------------|
| GEO042<br>-2<br>-3   | 1stBtwnInrTrans<br>B4        | First inner transitivity property of betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]               | -<br>- | 56<br>91  | 2.4<br>2.3 | 8%<br>12% | 51%<br>46% |
| GEO043<br>-2<br>-3   | 1stBtwnInrTransCor<br>B5     | Corollary to first inner transitivity property of betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]  | -<br>- | 56<br>92  | 2.4<br>2.3 | 8%<br>11% | 51%<br>45% |
| GEO044<br>-2<br>-3   | 1stBtwnOutTrans<br>B6        | First outer transitivity property for betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]              | -<br>- | 57<br>94  | 2.4<br>2.3 | 8%<br>11% | 51%<br>45% |
| GEO045<br>-2<br>-3   | 2ndBtwnOutTrans<br>B7        | Second outer transitivity property of betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]              | -<br>- | 57<br>95  | 2.4<br>2.3 | 8%<br>12% | 51%<br>45% |
| GEO046<br>-2<br>-3   | 2ndBtwnInrTrans<br>B8        | Second inner transitivity property of betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]              | -<br>- | 56<br>95  | 2.4<br>2.4 | 8%<br>13% | 51%<br>44% |
| GEO047<br>-2<br>-3   | 2ndBtwnInrTransCor<br>B9     | Corollary to second inner inner transitivity of betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]    | -<br>- | 56<br>96  | 2.4<br>2.4 | 8%<br>13% | 51%<br>43% |
| GEO048<br>-2<br>-3   | InrPtsTri<br>B10             | Inner points of triangle<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                       | -<br>- | 58<br>105 | 2.4<br>2.3 | 8%<br>12% | 50%<br>43% |
| GEO049<br>-2<br>-3   | SimSits<br>B11               | Theorem of similar situations<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                  | -<br>- | 58<br>121 | 2.4<br>2.4 | 8%<br>12% | 50%<br>40% |
| GEO050<br>-2<br>-3   | 1stBtwnOutConn<br>B12        | First outer connectivity property of betweenness<br>[Tar59, SST83, Qua89b]<br>[Tar59, SST83, Qua89b] | -<br>- | 58<br>122 | 2.4<br>2.4 | 8%<br>12% | 51%<br>40% |
| GEO051<br>-2<br>-3   | 2ndBtwnOutConn<br>B13        | Second outer connectivity property of betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]              | -<br>- | 58<br>123 | 2.4<br>2.5 | 8%<br>13% | 51%<br>39% |
| GEO052<br>-2<br>-3   | 2ndBtwnInrConn<br>B14        | Second inner connectivity property of betweenness<br>[SST83, Qua89b]<br>[SST83, Qua89b]              | -<br>- | 57<br>125 | 2.4<br>2.5 | 8%<br>15% | 51%<br>38% |
| GEO053<br>-2<br>-3   | EndPtUnq<br>B15              | Unique endpoint<br>[SST83, Qua89b]<br>[SST83, Qua89b]  | -<br>- | 56<br>126 | 2.4<br>2.6 | 8%<br>15% | 52%<br>37% |
| GEO054<br>-2<br>-3   | SegConsCor2<br>R2.1          | Corollary 2 to the segment construction axiom<br>[SST83, Qua89b]<br>[SST83, Qua89b]                  | -<br>- | 57<br>68  | 2.4<br>2.4 | 8%<br>7%  | 54%<br>48% |
| GEO055<br>-2<br>-3   | SegConsCor3<br>R2.2          | Corollary 3 to the segment construction axiom<br>[SST83, Qua89b]<br>[SST83, Qua89b]                  | -<br>- | 57<br>68  | 2.4<br>2.4 | 8%<br>7%  | 54%<br>48% |
| GEO056<br>-2<br>-3   | NullExtCor1<br>R3.1          | Corollary 1 to null extension<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                  | -<br>- | 58<br>71  | 2.4<br>2.3 | 8%<br>7%  | 55%<br>48% |
| GEO057<br>-2<br>-3   | NullExtCor2<br>R3.2          | Corollary 2 of null extension<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                  | -<br>- | 57<br>70  | 2.4<br>2.3 | 8%<br>7%  | 54%<br>48% |
| GEO058<br>-2<br>-3   | ReflcFixPtUnq<br>R4          | U is the only fixed point of reflection(U,V)<br>[SST83, Qua89b]<br>[SST83, Qua89b]                   | -<br>- | 58<br>73  | 2.4<br>2.3 | 8%<br>6%  | 55%<br>49% |
| GEO059<br>-2<br>-3   | DbfReflcCong<br>R5           | Congruence for double reflection<br>[SST83, Qua89b]<br>[SST83, Qua89b]                               | -<br>- | 57<br>79  | 2.4<br>2.4 | 8%<br>11% | 54%<br>48% |
| GEO060<br>-2         | ReflcIvln<br>R6              | Reflection is an involution<br>[SST83, Qua89b]   | -      | 57        | 2.4        | 8%        | 54%        |
| GEO061<br>-2<br>-3   | PtIntsc<br>I2                | Theorem of point insertion<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                     | -<br>- | 61<br>114 | 2.4<br>2.5 | 8%<br>13% | 53%<br>41% |
| GEO062<br>-2<br>-3   | IntscId<br>I3                | Insertion identity<br>[SST83, Qua89b]<br>[SST83, Qua89b]   | -<br>- | 60<br>116 | 2.4<br>2.5 | 8%<br>12% | 55%<br>41% |
| GEO063<br>-2<br>-3   | IntscCong<br>I4              | Insertion respects congruence in its last two arguments<br>[SST83, Qua89b]<br>[SST83, Qua89b]        | -<br>- | 60<br>117 | 2.4<br>2.5 | 8%<br>12% | 55%<br>41% |
| GEO064<br>-2<br>-3   | CollCor1<br>C2.1             | Corollary 1 to collinearity<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                    | -<br>- | 62<br>133 | 2.5<br>2.6 | 9%<br>15% | 47%<br>36% |
| GEO065<br>-2<br>-3   | CollCor2<br>C2.2             | Corollary 2 to collinearity<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                    | -<br>- | 62<br>133 | 2.5<br>2.6 | 9%<br>15% | 47%<br>36% |
| GEO066<br>-2<br>-3   | CollCor3<br>C2.3             | Corollary 3 to collinearity<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                    | -<br>- | 62<br>133 | 2.5<br>2.6 | 9%<br>15% | 47%<br>36% |
| GEO067<br>-2<br>-3   | 2PtsColl<br>C3               | Any two points are collinear<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                   | -<br>- | 62<br>142 | 2.6<br>2.6 | 9%<br>14% | 46%<br>34% |
| GEO068<br>-2<br>-3   | CollSimSits<br>C4            | Theorem of similar situations for collinear U, V, W<br>[SST83, Qua89b]<br>[SST83, Qua89b]            | -<br>- | 65<br>149 | 2.4<br>2.5 | 9%<br>14% | 46%<br>34% |
| GEO069<br>-2<br>-3   | CollEqn3<br>C5               | A property of collinearity<br>[SST83, Qua89b]<br>[SST83, Qua89b]                                     | -<br>- | 64<br>151 | 2.5<br>2.5 | 9%<br>15% | 47%<br>33% |

| Syntactic name<br>V#     | Semantic name<br>Other names                                  | Description  | References  | V | Cl | Av  | nH  | Eq  |
|--------------------------|---|--|---|---|----|-----|-----|-----|
| GEO070<br>-2<br>-3       | PtsNotColl<br>W1  | Non-collinear points in the bisecting diagonal theorem | [SST83, Qua89b]<br>[SST83, Qua89b]                          | - | 68 | 2.4 | 8%  | 46% |
| GEO071<br>-2<br>-3       | PtsNotCollCor1<br>W2.1  | Corollary 1 to non-collinear points theorem            | [SST83, Qua89b]<br>[SST83, Qua89b]                          | - | 61 | 2.3 | 8%  | 51% |
| GEO072<br>-2<br>-3       | PtsNotCollCor2<br>W2.2  | Corollary 2 to non-collinear points theorem            | [SST83, Qua89b]<br>[SST83, Qua89b]                          | - | 61 | 2.3 | 8%  | 51% |
| GEO073<br>-1<br>-2<br>-3 | DiagBsct<br>Test Problem 11, Bisecting Diagonal Theorem<br>W3 | The diagonals of a non-degenerate rectangle bisect     | [MOW76, SST83, Wos88]<br>[SST83, Qua89b]<br>[SST83, Qua89b] | - | 63 | 2.4 | 9%  | 48% |
| GEO074<br>-2             | OutPasch<br>Q2  | Prove the Outer Pasch Axiom                            | [SST83, Qua89b]   | - | 61 | 2.4 | 8%  | 54% |
| GEO075<br>-2             | EqIdRefl<br>Q3.1  | Show reflexivity for equidistance is dependent         | [SST83, Qua89b]   | - | 53 | 2.5 | 9%  | 52% |
| GEO076<br>-4             | PtNotOnLines<br>G15   | There is no point on every line                        | [Ben92]   | - | 60 | 4.0 | 30% | 37% |
| GEO077<br>-4             | 3PtsNotColl<br>G11A   | Three points not collinear if not on line              | [Ben92]   | - | 69 | 3.6 | 26% | 37% |
| GEO078<br>-4<br>-5       | 3PIPtsNotColl<br>G16  | Every plane contains 3 noncollinear points             | [Ben92]<br>[Ben92]  | - | 60 | 4.1 | 31% | 37% |
| GEO079<br>-1             | AltAngleEq<br>GEOMETRY THEOREM                                | The alternate interior angles in a trapezoid are equal | [Sla67]   | - | 6  | 1.8 | -   | -   |

### Domain GRA (1 abstract problems, 1 problems)

|              |                        |                               |                |   |    |     |     |   |
|--------------|------------------------|-------------------------------|----------------|---|----|-----|-----|---|
| GRA001<br>-1 | Labels<br>Pelletier 74 | Clauses from a labelled graph | [Tse83, Pel86] | - | 12 | 2.7 | 58% | - |
|--------------|------------------------|-------------------------------|----------------|---|----|-----|-----|---|

### Domain GRP (193 abstract problems, 313 problems)

|                                      |   |  |   |   |     |     |    |      |
|--------------------------------------|---|--|---|---|-----|-----|----|------|
| GRP001<br>-1<br>-2<br>-3<br>-4<br>-5 | SqrComm<br>G6, CADE-11 Comp. 1,<br>THEOREM 1, xsquared.ver1.in<br>GPI, Problem 1, GT1, xsquared.ver2.in<br>Problem 228-231<br>Pelletier 65, x2_quant.in<br>Example 1, Example 4, Chang-Lee-2,<br>GROUP2, ROB2, EX2                                | $X^2 = \text{identity} \Rightarrow \text{commutativity}$     | [Rob63, Wosb, MOW76, WM76]<br>[Ove90, Ove93, LM93]<br>[MOW76, LO85b, LW92]<br>[BLM+ 86]<br>[Wosb, Pel86]<br>[Luc68, Lov69, Cha70]<br>[MRS72, RRY+ 72, WM76] | - | 20  | 2.0 | -  | 40%  |
| GRP002<br>-1<br>-2<br>-3<br>-4       | O3CmtrEqId<br>G6, Theorem 1, Test Pr. 2, Commutator Theorem,<br>CADE-11 Comp. 2, TH. 2, commutator.ver1.in<br>commutator.ver2.in<br>CADE-11 Comp. Eq-1, THEOREM EQ-1,<br>PROBLEM 1, comm.in<br>Problem 4, Test Problem 2, Commutator Theorem, GT3 | Commutator equals identity in groups of order 3              | [MOW76, OMW76, Wos88]<br>[Ove90, Ove93, LM93]<br>[MOW76]<br>[Ove90, Ove93, LM93, Zha93]<br>[MOW76, LO85b, Wos88, LW92]                                      | - | 25  | 1.9 | -  | 34%  |
| GRP003<br>-1<br>-2                   | LIdEqRId<br>Example 2, Chang-Lee-3, EX3   | The left identity is also a right identity                   | [Luc68, Cha70, CL73]<br>[Ver92]   | - | 5   | 2.2 | -  | -    |
| GRP004<br>-1<br>-2                   | RInvEx<br>Example 3, Chang-Lee-4, EX4   | Left inverse and identity $\Rightarrow$ Right inverse exists | [Luc68, Cha70, CL73]<br>[Ver92]   | - | 5   | 2.2 | -  | -    |
| GRP005<br>-1                         | SubSIdEl<br>Example 5, Chang-Lee-5, EX5   | Identity is in this subset of a group                        | [Luc68, Cha70, CL73]  | - | 9   | 2.0 | -  | -    |
| GRP006<br>-1                         | InvEl<br>Chang-Lee-6, EX6   | Inverse is in this group                                     | [Cha70, CL73]   | - | 9   | 2.0 | -  | -    |
| GRP007<br>-1                         | IdUnq<br>Problem 3, wos3  | The identity element is unique                               | [Wosb, MOW76, WM76]   | - | 20  | 2.0 | -  | 42%  |
| GRP008<br>-1                         | Unknown<br>Problem 4, wos4  | Unknown meaning  | [Wosb, MOW76, WM76]   | - | 24  | 2.3 | 4% | 38%  |
| GRP009<br>-1                         | LInvUnq<br>Problem 6, wos6  | The left inverse of an element is unique                     | [Wosb, MOW76, WM76]   | - | 20  | 2.0 | -  | 42%  |
| GRP010<br>-1<br>-4                   | InvSymm<br>Problem 7, wos7<br>Pelletier 64  | Inverse is a symmetric relationship                          | [Wosb, MOW76, WM76]<br>[Wosb, Pel86]  | - | 19  | 2.1 | -  | 41%  |
| GRP011<br>-4                         | LCanc<br>Pelletier 63   | Left cancellation  | [Wosb, Pel86]   | - | 11  | 1.5 | -  | 100% |
| GRP012<br>-1<br>-2<br>-3<br>-4       | InvOfProd<br>Problem 9, wos9<br>ls36, ls36  | Inverse of products = Product of inverses                    | [Wosb, MOW76, WM76]<br>[LS74, WM76]<br>[MOW76]<br>[MOW76]   | - | 20  | 2.0 | -  | 40%  |
| GRP013<br>-1                         | CmtrEqId<br>Problem 11, wos11   | Commutator equals identity in these conditions               | [Wosb, MOW76, WM76]   | - | 22  | 2.0 | -  | 37%  |
| GRP014<br>-1                         | ProdAssc<br>CADE-11 Comp. Eq-4, THEOREM EQ-4, PR. 4   | Product is associative in this group theory                  | [Ove90, Ove93, LM93, Zha93]   | - | 8   | 1.8 | -  | 100% |
| GRP015<br>-1                         | GroupEx<br>Problem 224-225  | $x, \langle x, X \rangle$ is a group                         | [BLM+ 86]   | - | 326 | 2.4 | 8% | 43%  |
| GRP016<br>-1                         | ReflHomom<br>Problem 226-227  | There is a homomorphism from a group to itself               | [BLM+ 86]   | - | 326 | 2.4 | 8% | 43%  |
| GRP017<br>-1                         | InvUnq<br>G2, invers1.ver1.in   | The inverse of each element is unique                        | [MOW76]   | - | 22  | 1.9 | -  | 40%  |

| Syntactic name<br>V#                             | Semantic name<br>Other names  | Description   | References  | V | Cl | Av  | nH | Eq   |
|--|---|---|---|---|----|-----|----|------|
| GRP018<br>-1                                     | XTimesId<br>Identity established,   | X times identity is X   | [MOW76, OMW76]  | - | 18 | 2.1 | -  | 44%  |
| GRP019<br>-1                                     | IdTimesX<br>Identity established,   | Identity times X is X   | [MOW76, OMW76]  | - | 18 | 2.1 | -  | 44%  |
| GRP020<br>-1                                     | InvXTimesX<br>Identity established,   | Inverse of X times X is the identity                          | [MOW76, OMW76]  | - | 18 | 2.1 | -  | 44%  |
| GRP021<br>-1                                     | XTimesInvX<br>Identity established,   | X times inverse of X is the identity                          | [MOW76, OMW76]  | - | 18 | 2.1 | -  | 44%  |
| GRP022<br>-1<br>-2                               | InvIvln<br>Identity established, wos8<br>Established lemma, Problem 2   | Inverse is an involution                                      | [Wosb, MOW76, OMW76, WM76]<br>[MOW76, LO85b]  | - | 18 | 2.1 | -  | 44%  |
| GRP023<br>-1<br>-2                               | InvOfId<br>Identity established,<br>Established lemma   | The inverse of the identity is the identity                   | [MOW76, OMW76]<br>[MOW76]   | - | 18 | 2.1 | -  | 44%  |
| GRP024<br>-4                                     | CmtrAssc<br>THEOREM (Levi)  | Associativity of commutator                                   | [Kur56, MOW76, ML92]  | - | 16 | 1.6 | 6% | 100% |
| GRP025<br>-1<br>-2<br>-3<br>-4                   | O2Isom<br>G8<br>G8<br>order2.ver3.in<br>order2.ver4.in  | All groups of order 2 are isomorphic                          | [MOW76]<br>[MOW76]<br>[MOW76]<br>[MOW76]  | - | 48 | 1.8 | 4% | 37%  |
| GRP026<br>-1<br>-2<br>-3<br>-4                   | O3Isom<br>G9<br>G9<br>order3.ver3.in<br>order3.ver4.in  | All groups of order 3 are isomorphic                          | [MOW76]<br>[MOW76]<br>[MOW76]<br>[MOW76]  | - | 61 | 1.7 | 3% | 35%  |
| GRP027<br>-1<br>-2                               | O5Cyclic<br>cyclic.ver3.in  | All groups of order 5 are cyclic                              | [MOW76]   | - | 41 | 2.0 | 2% | 45%  |
| GRP028<br>-1<br>-2<br>-3                         | SemiGRIdEx1<br>ALGEBRA THEOREM, Chang-Lee-1,<br>GROUP1, EX1<br>Example 1  | In semigroups, left and right solutions => right id exists    | [Sla67, Cha70, RRY+72, WM76]<br>[MOW76]<br>[Luc68, MOW76]                               | - | 4  | 1.8 | -  | -    |
| GRP029<br>-1<br>-2                               | SemiGRIdEx2<br>Problem 1, wos1, G5, ident2.ver1.in<br>G5  | In semigroups, left id and inverse => right id exists         | [Wosb, MOW76, WM76]<br>[MOW76]  | - | 17 | 2.2 | -  | 47%  |
| GRP030<br>-1                                     | SemiGLIdEqRI<br>Problem 2, wos2, G3, ident1.ver1.in   | In semigroups, left id and inverse => left id=right id        | [Wosb, MOW76, WM76]   | - | 16 | 2.3 | -  | 44%  |
| GRP031<br>-1<br>-2                               | SemiGRInvEx<br>Problem 5, wos5, G4, invers2.ver1.t<br>ls23, ls23  | In semigroups, left inverse and id => right inverse exists    | [Wosb, MOW76, WM76]<br>[LS74, WM76]   | - | 16 | 2.3 | -  | 44%  |
| GRP032<br>-3                                     | SubGIdEx<br>Problem 12, wos12   | In subgroups, there is an identity                            | [Wosb, WM76]  | - | 21 | 2.2 | -  | 37%  |
| GRP033<br>-3<br>-4                               | SubGGrpIdEx<br>Problem 13, wos13<br>Problem 13  | In subgroups, the identity is the group identity              | [Wosb, WM76]<br>[Wosb]  | - | 22 | 2.3 | -  | -    |
| GRP034<br>-3<br>-4                               | SubGInvClsd<br>Problem 14, wos14, wos_nie<br>ls26, ls26   | In subgroups, inverse is closed                               | [Wosb, MOW76, WM76]<br>[LS74, WM76]   | - | 21 | 2.2 | -  | 37%  |
| GRP035<br>-3                                     | SubGProdClsd<br>Problem 15, wos15   | In subgroups, product is closed                               | [Wosb, MOW76, WM76]   | - | 23 | 2.1 | -  | 35%  |
| GRP036<br>-3                                     | SubGIdUnq<br>Problem 16, wos16  | In subgroups, the identity element is unique                  | [Wosb, WM76]  | - | 27 | 2.1 | -  | 34%  |
| GRP037<br>-3                                     | SubGInvUnq<br>Problem 17, wos17   | In subgroups, the inverse of an element is unique             | [Wosb, WM76]  | - | 30 | 2.2 | -  | 33%  |
| GRP038<br>-3                                     | SubGGrpEl<br>Problem 18, wos18  | In subgroups, if a and b are members, then a.b^-1 is a member | [Wosb, WM76]  | - | 25 | 2.0 | -  | 33%  |
| GRP039<br>-1<br>-2<br>-3<br>-4<br>-5<br>-6<br>-7 | SubGI2Norm<br>NU2<br>wos19<br>G7, Theorem 3, Test Problem 1, index.ver1.in<br>index.ver2.in<br>subgroup.in<br>GP2 | Subgroups of index 2 are normal                               | [MOW76]<br>[MOW76, LW92]<br>[Wosb, WM76]<br>[MOW76, OMW76, Wos88]<br>[MOW76]<br>[MOW76] | - | 28 | 2.1 | 7% | 35%  |
| GRP040<br>-3<br>-4                               | SubGO2InvIvln<br>Problem 20, wos20  | In subgroups of order 2, inverse is an involution             | [Wosb]<br>[Wosb, WM76]  | - | 29 | 2.1 | 6% | 36%  |
| GRP041<br>-2                                     | EqRefl  | Reflexivity is dependent                                      | [Ver92]   | - | 8  | 2.3 | -  | -    |
| GRP042<br>-2                                     | EqSymm  | Symmetry is dependent   | [Ver92]   | - | 9  | 2.1 | -  | -    |
| GRP043<br>-2                                     | EqTrans   | Transitivity is dependent                                     | [Ver92]   | - | 10 | 2.0 | -  | -    |
| GRP044<br>-2                                     | ProdSubs1   | Product substitution 1 is dependent                           | [Ver92]   | - | 10 | 2.0 | -  | -    |
| GRP045<br>-2                                     | ProdSubs2   | Product substitution 2 is dependent                           | [Ver92]   | - | 10 | 2.0 | -  | -    |
| GRP046<br>-2                                     | MultSubs1   | Multiply substitution 1 is dependent                          | [Ver92]   | - | 9  | 2.1 | -  | -    |
| GRP047<br>-2                                     | MultSubs2   | Multiply substitution 2 is dependent                          | [Ver92]   | - | 9  | 2.1 | -  | -    |
| GRP048<br>-2                                     | InvSubs   | Inverse substitution is dependent                             | [Ver92]   | - | 9  | 2.1 | -  | -    |

| Syntactic name<br>V# | Semantic name<br>Other names             | Description<br>References   | V | Cl | Av  | nH | Eq   |
|----------------------|--|---|---|----|-----|----|------|
| GRP049<br>-1         | ProdInvAx1<br>C1                         | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP050<br>-1         | ProdInvAx2<br>Axiom C2                   | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP051<br>-1         | ProdInvAx3<br>C3, Axiom 2.1              | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP052<br>-1         | ProdInvAx4<br>C4                         | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP053<br>-1         | ProdInvAx5<br>C5                         | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP054<br>-1         | ProdInvAx6<br>C6                         | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP055<br>-1         | ProdInvAx7<br>C7                         | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP056<br>-1         | ProdInvAx8<br>C8                         | Single axiom for group theory, in product & inverse<br>[Kun92, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP057<br>-1         | ProdInvAx9<br>Axiom 1.2                  | Single axiom for group theory, in product & inverse<br>[Neu81, McC93]                 | - | 8  | 2.0 | -  | 100% |
| GRP058<br>-1         | ProdInvAx10<br>GT4, Axiom 3.1.1, sax1.in | Single axiom for group theory, in product & inverse<br>[LW92, McC93]                  | - | 8  | 2.0 | -  | 100% |
| GRP059<br>-1         | ProdInvAx11<br>Axiom 3.1.2               | Single axiom for group theory, in product & inverse<br>[McC93]                        | - | 8  | 2.0 | -  | 100% |
| GRP060<br>-1         | ProdInvAx12<br>Axiom 3.2.3               | Single axiom for group theory, in product & inverse<br>[McC93]                        | - | 8  | 2.0 | -  | 100% |
| GRP061<br>-1         | ProdInvAx13<br>Axiom 3.1.4               | Single axiom for group theory, in product & inverse<br>[McC93]                        | - | 8  | 2.0 | -  | 100% |
| GRP062<br>-1         | ProdInvAx14<br>Axiom 3.1.5               | Single axiom for group theory, in product & inverse<br>[McC93]                        | - | 8  | 2.0 | -  | 100% |
| GRP063<br>-1         | DivAx1<br>Axiom 1.1                      | Single axiom for group theory, in division<br>[HN52, McC93]                           | - | 11 | 1.9 | -  | 100% |
| GRP064<br>-1         | DivAx2<br>Axiom 3.2.1, sax2.in           | Single axiom for group theory, in division<br>[McC93]                                 | - | 11 | 1.9 | -  | 100% |
| GRP065<br>-1         | DivAx3<br>Axiom 3.2.2                    | Single axiom for group theory, in division<br>[McC93]                                 | - | 11 | 1.9 | -  | 100% |
| GRP066<br>-1         | DivIdAx1<br>Axiom 3.3.1                  | Single axiom for group theory, in division and identity<br>[McC93]                    | - | 12 | 1.8 | -  | 100% |
| GRP067<br>-1         | DivIdAx2<br>Axiom 3.3.2                  | Single axiom for group theory, in division and identity<br>[McC93]                    | - | 12 | 1.8 | -  | 100% |
| GRP068<br>-1         | DivIdAx3<br>Axiom 3.3.3                  | Single axiom for group theory, in division and identity<br>[McC93]                    | - | 12 | 1.8 | -  | 100% |
| GRP069<br>-1         | DivIdAx4<br>Axiom 3.3.4                  | Single axiom for group theory, in division and identity<br>[McC93]                    | - | 12 | 1.8 | -  | 100% |
| GRP070<br>-1         | DivInvAx1<br>Axiom 3.4.1                 | Single axiom for group theory, in division and inverse<br>[McC93]                     | - | 11 | 1.9 | -  | 100% |
| GRP071<br>-1         | DivInvAx2<br>Axiom 3.4.2                 | Single axiom for group theory, in division and inverse<br>[McC93]                     | - | 11 | 1.9 | -  | 100% |
| GRP072<br>-1         | DivInvAx3<br>Axiom 3.4.3                 | Single axiom for group theory, in division and inverse<br>[McC93]                     | - | 11 | 1.9 | -  | 100% |
| GRP073<br>-1         | DivInvAx4<br>Axiom 3.4.4                 | Single axiom for group theory, in division and inverse<br>[McC93]                     | - | 11 | 1.9 | -  | 100% |
| GRP074<br>-1         | DivInvAx5<br>Axiom 3.4.5                 | Single axiom for group theory, in division and inverse<br>[McC93]                     | - | 11 | 1.9 | -  | 100% |
| GRP075<br>-1         | DblDivIdAx1<br>Axiom 2.2                 | Single axiom for group theory, in double division and identity<br>[Neu86, McC93]      | - | 12 | 1.8 | -  | 100% |
| GRP076<br>-1         | DblDivIdAx2<br>Axiom 3.5.1               | Single axiom for group theory, in double division and identity<br>[McC93]             | - | 12 | 1.8 | -  | 100% |
| GRP077<br>-1         | DblDivIdAx3<br>Axiom 3.5.2               | Single axiom for group theory, in double division and identity<br>[McC93]             | - | 12 | 1.8 | -  | 100% |
| GRP078<br>-1         | DblDivIdAx4<br>Axiom 3.5.3               | Single axiom for group theory, in double division and identity<br>[McC93]             | - | 12 | 1.8 | -  | 100% |
| GRP079<br>-1         | DblDivIdAx5<br>Axiom 3.5.4               | Single axiom for group theory, in double division and identity<br>[McC93]             | - | 12 | 1.8 | -  | 100% |
| GRP080<br>-1         | DblDivIdAx6<br>Axiom 3.5.5               | Single axiom for group theory, in double division and identity<br>[McC93]             | - | 12 | 1.8 | -  | 100% |
| GRP081<br>-1         | DblDivInvAx1<br>Axiom 2.5                | Single axiom for group theory, in double division and inverse<br>[Neu86, McC93]       | - | 11 | 1.9 | -  | 100% |
| GRP082<br>-1         | DblDivInvAx2<br>Axiom 3.6.1              | Single axiom for group theory, in double division and inverse<br>[McC93]              | - | 11 | 1.9 | -  | 100% |
| GRP083<br>-1         | DblDivInvAx3<br>Axiom 3.6.2              | Single axiom for group theory, in double division and inverse<br>[McC93]              | - | 11 | 1.9 | -  | 100% |
| GRP084<br>-1         | ProdInvAbnAx1<br>GT6, Axiom 2.4          | Single axiom for Abelian group theory, in product and inverse<br>[Neu81, LW92, McC93] | - | 8  | 2.1 | -  | 100% |
| GRP085<br>-1         | ProdInvAbnAx2<br>GT5, Axiom 3.7.1        | Single axiom for Abelian group theory, in product and inverse<br>[LW92, McC93]        | - | 8  | 2.1 | -  | 100% |
| GRP086<br>-1         | ProdInvAbnAx3<br>Axiom 3.7.2             | Single axiom for Abelian group theory, in product and inverse<br>[McC93]              | - | 8  | 2.1 | -  | 100% |
| GRP087<br>-1         | ProdInvAbnAx4<br>Axiom 3.7.3             | Single axiom for Abelian group theory, in product and inverse<br>[McC93]              | - | 8  | 2.1 | -  | 100% |
| GRP088<br>-1         | DivAbnAx1<br>Axiom 2.3                   | Single axiom for Abelian group theory, in division<br>[Tar38, McC93]                  | - | 11 | 2.0 | -  | 100% |
| GRP089<br>-1         | DivAbnAx2<br>Axiom 3.8.1                 | Single axiom for Abelian group theory, in division<br>[McC93]                         | - | 11 | 2.0 | -  | 100% |
| GRP090<br>-1         | DivAbnAx3<br>Axiom 3.8.2                 | Single axiom for Abelian group theory, in division<br>[McC93]                         | - | 11 | 2.0 | -  | 100% |

| Syntactic name<br>V#   | Semantic name<br>Other names                       | Description<br>References   | V | Cl | Av  | nH | Eq   |
|--|--|---|---|----|-----|----|------|
| GRP091<br>-1   | DivAbnAx4<br>Axiom 3.8.3                           | Single axiom for Abelian group theory, in division<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP092<br>-1   | DivAbnAx5<br>Axiom 3.8.4                           | Single axiom for Abelian group theory, in division<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP093<br>-1   | DivIdAbnAx1<br>Axiom 3.9.1                         | Single axiom for Abelian group theory, in division and identity<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP094<br>-1   | DivIdAbnAx2<br>Axiom 3.9.2                         | Single axiom for Abelian group theory, in division and identity<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP095<br>-1   | DivIdAbnAx3<br>Axiom 3.9.3                         | Single axiom for Abelian group theory, in division and identity<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP096<br>-1   | DivInvAbnAx1<br>Axiom 3.10.1                       | Single axiom for Abelian group theory, in division and inverse<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP097<br>-1   | DivInvAbnAx2<br>Axiom 3.10.2                       | Single axiom for Abelian group theory, in division and inverse<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP098<br>-1   | DivInvAbnAx3<br>Axiom 3.10.3                       | Single axiom for Abelian group theory, in division and inverse<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP099<br>-1   | DbldivIdAbnAx1<br>Axiom 3.11.1                     | Single axiom for Abelian group theory, in double div and id<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP100<br>-1   | DbldivIdAbnAx2<br>Axiom 3.11.2                     | Single axiom for Abelian group theory, in double div and id<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP101<br>-1   | DbldivIdAbnAx3<br>Axiom 3.11.3                     | Single axiom for Abelian group theory, in double div and id<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP102<br>-1   | DbldivIdAbnAx4<br>Axiom 3.11.4                     | Single axiom for Abelian group theory, in double div and id<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP103<br>-1   | DbldivIdAbnAx5<br>Axiom 3.11.5                     | Single axiom for Abelian group theory, in double div and id<br>[McC93]  | - | 12 | 1.9 | -  | 100% |
| GRP104<br>-1   | DbldivInvAbnAx1<br>Axiom 3.12.1                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP105<br>-1   | DbldivInvAbnAx2<br>Axiom 3.12.2                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP106<br>-1   | DbldivInvAbnAx3<br>Axiom 3.12.3                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP107<br>-1   | DbldivInvAbnAx4<br>axiom 3.12.4                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP108<br>-1   | DbldivInvAbnAx5<br>Axiom 3.12.5                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP109<br>-1   | DbldivInvAbnAx6<br>Axiom 3.12.6                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP110<br>-1   | DbldivInvAbnAx7<br>Axiom 3.12.7                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP111<br>-1   | DbldivInvAbnAx8<br>Axiom 3.12.8                    | Single axiom for Abelian group theory, in double div and inv<br>[McC93]   | - | 11 | 2.0 | -  | 100% |
| GRP112<br>-1   | ProdInvAx15<br>GT2                                 | Single axiom for group theory, in product & inverse<br>[MP68, LW92, McC93]  | - | 8  | 2.1 | -  | 100% |
| GRP113<br>-1   | O4Eqn<br>Test Problem 7,                           | Lemma for proving all groups of order 4 are cyclic<br>[Wos88]   | - | 22 | 1.8 | 4% | 100% |
| GRP114<br>-1   | PosTimesNeg  | Product of positive and negative parts of X equals X<br>[Wos94a]  | - | 33 | 1.4 | -  | 100% |
| GRP115<br>-1   | O3AxO3<br>groups.exp3.in part 1                    | Derive order 3 from a single axiom for groups order 3<br>[Wosa]   | - | 7  | 1.7 | -  | 100% |
| GRP116<br>-1   | O3AxLId<br>groups.exp3.in part 2                   | Derive left identity from a single axiom for groups order 3<br>[Wosa]   | - | 7  | 1.7 | -  | 100% |
| GRP117<br>-1   | O3AxRId<br>groups.exp3.in part 3                   | Derive right identity from a single axiom for groups order 3<br>[Wosa]  | - | 7  | 1.7 | -  | 100% |
| GRP118<br>-1   | O3AxAssoc<br>groups.exp3.in part 4                 | Derive associativity from a single axiom for groups order 3<br>[Wosa]   | - | 7  | 1.7 | -  | 100% |
| GRP119<br>-1   | O4AxO4<br>groups.exp4.in part 1                    | Derive order 4 from a single axiom for groups order 4<br>[Wosa]   | - | 8  | 1.6 | -  | 100% |
| GRP120<br>-1   | O4AxLId<br>groups.exp4.in part 2                   | Derive left identity from a single axiom for groups order 4<br>[Wosa]   | - | 8  | 1.6 | -  | 100% |
| GRP121<br>-1   | O4AxRId<br>groups.exp4.in part 3                   | Derive right identity from a single axiom for groups order 4<br>[Wosa]  | - | 8  | 1.6 | -  | 100% |
| GRP122<br>-1   | O4AxAssoc<br>groups.exp4.in part 4                 | Derive associativity from a single axiom for groups order 4<br>[Wosa]   | - | 8  | 1.6 | -  | 100% |
| GRP123<br>-1.003<br>-2.003<br>-3.003<br>-4.003<br>-6.003<br>-7.003<br>-8.003<br>-9.003 | 321COILS<br>QG1, QG1, QG1, Bennett QG1<br><br>QG1a | (3,2,1) conjugate orthogonality<br>[FSB93, Sla93, Zha94a, SFS95]<br>[FSB93, Sla93, Zha94a, SFS95]<br>[FSB93, Sla93, Zha94a, SFS95]<br>[FSB93, Sla93, Zha94a, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95] | - | 16 | 2.1 | 6% | -    |
| GRP124<br>-1.003<br>-2.003<br>-3.003<br>-4.003<br>-6.003<br>-7.003<br>-8.003<br>-9.004 | 312COILS<br>QG2, QG2, QG2, Bennett QG2<br><br>QG2a | (3,1,2) conjugate orthogonality<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]                                 | - | 16 | 2.1 | 6% | -    |



| Syntactic name<br>V#                           | Semantic name<br>Other names                | Description<br>References  | V | Cl | Av  | nH  | Eq   |
|--|---|--|---|----|-----|-----|------|
| GRP125<br>-1.003<br>-2.003<br>-3.003<br>-4.003 | Schroeder<br>QG3, QG3, QG3, Bennett QG3     | (a.b).(b.a) = a<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]                              | - | 15 | 1.8 | 6%  | -    |
| GRP126<br>-1.003<br>-2.003<br>-3.003<br>-4.003 | SteinLaw3<br>QG4, QG4, QG4, Bennett QG4     | (a.b).(b.a) = b<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]                              | - | 15 | 1.8 | 6%  | -    |
| GRP127<br>-1.003<br>-2.003<br>-3.003<br>-4.003 | QG5<br>QG5, QG5, QG5, Bennett QG5           | ((b.a).b).b) = a<br>[Ben85, FSB93, Sla93, SFS95]<br>[Ben85, FSB93, Sla93, SFS95]<br>[Ben85, FSB93, Sla93, SFS95]<br>[Ben85, FSB93, Sla93, SFS95] | - | 15 | 1.8 | 6%  | -    |
| GRP128<br>-1.003<br>-2.003<br>-3.003<br>-4.003 | SchroederLaw1<br>QG6, QG6, QG6, Bennett QG6 | (a.b).b = a.(a.b)<br>[BZ92, FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]                      | - | 14 | 1.9 | 7%  | -    |
| GRP129<br>-1.002<br>-2.002<br>-3.002<br>-4.002 | QG7<br>QG7, QG7, QG7, Bennett QG7           | a.(b.a) = (b.a).b<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]                            | - | 9  | 2.2 | 11% | -    |
| GRP130<br>-1.002<br>-2.002<br>-3.002<br>-4.002 | QG8<br>QG8, Bennett QG8                     | (a.(a.b)).b) = a<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]                             | - | 9  | 2.2 | 11% | -    |
| GRP131<br>-1.002<br>-2.002                     | 321COILSNoIdem<br>QG1-ni                    | (3,2,1) conjugate orthogonality, no idempotence<br>[FSB93, Sla93, Zha94a, SFS95]<br>[FSB93, Sla93, Zha94a, SFS95]                                | - | 10 | 2.7 | 10% | -    |
| GRP132<br>-1.002<br>-2.002                     | 312COILSNoIdem<br>QG2-ni                    | (3,1,2) conjugate orthogonality, no idempotence<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]  | - | 10 | 2.7 | 10% | -    |
| GRP133<br>-1.002<br>-2.002                     | SchroederNoIdem<br>QG3-ni                   | (a.b).(b.a) = a, no idempotence<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]  | - | 9  | 2.2 | 11% | -    |
| GRP134<br>-1.002<br>-2.002                     | SteinLaw3NoIdem<br>QG4-ni                   | (a.b).(b.a) = b, no idempotence<br>[FSB93, Sla93, SFS95]<br>[FSB93, Sla93, SFS95]  | - | 9  | 2.2 | 11% | -    |
| GRP135<br>-1.002<br>-2.002                     | QG5NoIdem<br>QG5-ni                         | ((b.a).b).b) = a, no idempotence<br>[Ben85, FSB93, Sla93, SFS95]<br>[Ben85, FSB93, Sla93, SFS95]   | - | 9  | 2.2 | 11% | -    |
| GRP136<br>-1                                   | ASymLub<br>ax_antisyma                      | Prove anti-symmetry axiom using the LUB transformation<br>[Fuc94, Sch95]   | - | 28 | 1.4 | -   | 100% |
| GRP137<br>-1                                   | ASymGlb<br>ax_antisymb                      | Prove anti-symmetry axiom using the GLB transformation<br>[Fuc94, Sch95]   | - | 28 | 1.4 | -   | 100% |
| GRP138<br>-1                                   | Glb1Lub<br>ax_glb1a                         | Prove greatest lower-bound axiom using the LUB transformation<br>[Fuc94, Sch95]  | - | 28 | 1.4 | -   | 100% |
| GRP139<br>-1                                   | Glb1Glb<br>ax_glb1b                         | Prove greatest lower-bound axiom using the GLB transformation<br>[Fuc94, Sch95]  | - | 28 | 1.4 | -   | 100% |
| GRP140<br>-1                                   | Glb1C<br>ax_glb1c                           | Prove greatest lower-bound axiom using a transformation<br>[Fuc94, Sch95]  | - | 28 | 1.4 | -   | 100% |
| GRP141<br>-1                                   | Glb1D<br>ax_glb1d                           | Prove greatest lower-bound axiom using a transformation<br>[Fuc94, Sch95]  | - | 28 | 1.4 | -   | 100% |
| GRP142<br>-1                                   | Glb2Lub<br>ax_glb2a                         | Prove greatest lower-bound axiom using the LUB transformation<br>[Fuc94, Sch95]  | - | 26 | 1.4 | -   | 100% |
| GRP143<br>-1                                   | Glb2Glb<br>ax_glb2b                         | Prove greatest lower-bound axiom using the GLB transformation<br>[Fuc94, Sch95]  | - | 26 | 1.4 | -   | 100% |
| GRP144<br>-1                                   | Glb3Lub<br>ax_glb3a                         | Prove greatest lower-bound axiom using the LUB transformation<br>[Fuc94, Sch95]  | - | 26 | 1.4 | -   | 100% |
| GRP145<br>-1                                   | Glb3Glb<br>ax_glb3b                         | Prove greatest lower-bound axiom using the GLB transformation<br>[Fuc94, Sch95]  | - | 26 | 1.4 | -   | 100% |
| GRP146<br>-1                                   | Lub1Lub<br>ax_lub1a                         | Prove least upper-bound axiom using the LUB transformation<br>[Fuc94, Sch95]   | - | 28 | 1.4 | -   | 100% |
| GRP147<br>-1                                   | Lub1Glb<br>ax_lub1b                         | Prove least upper-bound axiom using the GLB transformation<br>[Fuc94, Sch95]   | - | 28 | 1.4 | -   | 100% |
| GRP148<br>-1                                   | Lub3C<br>ax_lub1c                           | Prove least upper-bound axiom using a transformation<br>[Fuc94, Sch95]   | - | 28 | 1.4 | -   | 100% |
| GRP149<br>-1                                   | Lub3D<br>ax_lub1d                           | Prove least upper-bound axiom using a transformation<br>[Fuc94, Sch95]   | - | 28 | 1.4 | -   | 100% |
| GRP150<br>-1                                   | Lub2Lub<br>ax_lub2a                         | Prove least upper-bound axiom using the LUB transformation<br>[Fuc94, Sch95]   | - | 26 | 1.4 | -   | 100% |
| GRP151<br>-1                                   | Lub2Glb<br>ax_lub2b                         | Prove least upper-bound axiom using the GLB transformation<br>[Fuc94, Sch95]   | - | 26 | 1.4 | -   | 100% |
| GRP152<br>-1                                   | Lub3Lub<br>ax_lub3a                         | Prove least upper-bound axiom using the LUB transformation<br>[Fuc94, Sch95]   | - | 26 | 1.4 | -   | 100% |
| GRP153<br>-1                                   | Lub3Glb<br>ax_lub3b                         | Prove least upper-bound axiom using the GLB transformation<br>[Fuc94, Sch95]   | - | 26 | 1.4 | -   | 100% |
| GRP154<br>-1                                   | Mono1Lub<br>ax_monola                       | Prove monotonicity axiom using the LUB transformation<br>[Fuc94, Sch95]  | - | 27 | 1.4 | -   | 100% |
| GRP155<br>-1                                   | Mono1Glb<br>ax_monolb                       | Prove monotonicity axiom using the GLB transformation<br>[Fuc94, Sch95]  | - | 27 | 1.4 | -   | 100% |
| GRP156<br>-1                                   | Mono1C<br>ax_monolc                         | Prove monotonicity axiom using a transformation<br>[Fuc94, Sch95]  | - | 27 | 1.4 | -   | 100% |

| Syntactic name<br>V#                 | Semantic name<br>Other names                    | Description<br>References  | V                     | Cl                         | Av                              | nH                    | Eq                                   |
|--------------------------------------|---|--|-----------------------|----------------------------|---------------------------------|-----------------------|--------------------------------------|
| GRP157<br>-1                         | Mono2Lub<br>ax_mono2a                           | Prove monotonicity axiom using the LUB transformation<br>[Fuc94, Sch95]  | -                     | 27                         | 1.4                             | -                     | 100%                                 |
| GRP158<br>-1                         | Mono2Glb<br>ax_mono2b                           | Prove monotonicity axiom using the GLB transformation<br>[Fuc94, Sch95]  | -                     | 27                         | 1.4                             | -                     | 100%                                 |
| GRP159<br>-1                         | Mono2C<br>ax_mono2c                             | Prove monotonicity axiom using a transformation<br>[Fuc94, Sch95]  | -                     | 27                         | 1.4                             | -                     | 100%                                 |
| GRP160<br>-1                         | RefLlub<br>ax_refla                             | Prove reflexivity axiom using the LUB transformation<br>[Fuc94, Sch95]   | -                     | 26                         | 1.4                             | -                     | 100%                                 |
| GRP161<br>-1                         | RefGlb<br>ax_reflb                              | Prove reflexivity axiom using the GLB transformation<br>[Fuc94, Sch95]   | -                     | 26                         | 1.4                             | -                     | 100%                                 |
| GRP162<br>-1                         | TransLub<br>ax_transa                           | Prove transitivity axiom using the LUB transformation<br>[Fuc94, Sch95]  | -                     | 28                         | 1.4                             | -                     | 100%                                 |
| GRP163<br>-1                         | TransGlb<br>ax_transb                           | Prove transitivity axiom using the GLB transformation<br>[Fuc94, Sch95]  | -                     | 28                         | 1.4                             | -                     | 100%                                 |
| GRP164<br>-1<br>-2                   | LOGLattDist<br>distrnu<br>distrun               | The lattice of each LOG is distributive<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]   | -<br>-                | 26<br>26                   | 1.4<br>1.4                      | -<br>-                | 100%<br>100%                         |
| GRP165<br>-1<br>-2                   | AppMono<br>lat1a<br>lat1b                       | An application of monotonicity<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]   | -<br>-                | 27<br>27                   | 1.4<br>1.4                      | -<br>-                | 100%<br>100%                         |
| GRP166<br>-1<br>-2<br>-3<br>-4       | MultiPosInc<br>lat2a<br>lat2b<br>lat3a<br>lat3b | Multiplication with a positive element increases a value<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]        | -<br>-<br>-<br>-      | 28<br>28<br>28<br>28       | 1.4<br>1.4<br>1.4<br>1.4        | -<br>-<br>-<br>-      | 100%<br>100%<br>100%<br>100%         |
| GRP167<br>-1<br>-2<br>-3<br>-4<br>-5 | ProdPosNeg<br>lat4<br>p19                       | Product of positive and negative parts<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95, Dah95] | -<br>-<br>-<br>-<br>- | 32<br>35<br>26<br>29<br>33 | 1.4<br>1.3<br>1.4<br>1.3<br>1.4 | -<br>-<br>-<br>-<br>- | 100%<br>100%<br>100%<br>100%<br>100% |
| GRP168<br>-1<br>-2                   | InrGrpAutoM<br>p01a<br>p01b                     | Inner group automorphisms are order preserving<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]  | -<br>-                | 27<br>27                   | 1.4<br>1.4                      | -<br>-                | 100%<br>100%                         |
| GRP169<br>-1<br>-2                   | InvRevEq<br>p02a<br>p02b                        | Inverses reverse inequalities<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]   | -<br>-                | 27<br>27                   | 1.4<br>1.4                      | -<br>-                | 100%<br>100%                         |
| GRP170<br>-1<br>-2<br>-3<br>-4       | GenMono<br>p03a<br>p03b<br>p03c<br>p03d         | General form of monotonicity<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]   | -<br>-<br>-<br>-      | 28<br>28<br>28<br>28       | 1.4<br>1.4<br>1.4<br>1.4        | -<br>-<br>-<br>-      | 100%<br>100%<br>100%<br>100%         |
| GRP171<br>-1<br>-2                   | PosElSemiG<br>p04a<br>p04c                      | Positive elements form a semigroup<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]   | -<br>-                | 28<br>28                   | 1.4<br>1.4                      | -<br>-                | 100%<br>100%                         |
| GRP172<br>-1<br>-2                   | NegElSemiG<br>p04b<br>p04d                      | Negative elements form a semigroup<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]   | -<br>-                | 28<br>28                   | 1.4<br>1.4                      | -<br>-                | 100%<br>100%                         |
| GRP173<br>-1                         | SubGNegEl<br>p05a                               | Each subgroup of negative elements is trivial<br>[Fuc94, Sch95, Dah95]   | -                     | 28                         | 1.4                             | -                     | 100%                                 |
| GRP174<br>-1                         | SubGPosEl<br>p05b                               | Each subgroup of positive elements is trivial<br>[Fuc94, Sch95]  | -                     | 28                         | 1.4                             | -                     | 100%                                 |
| GRP175<br>-1<br>-2<br>-3<br>-4       | PosInrAutoM<br>p06a<br>p06b<br>p06c<br>p06d     | Positivity is preserved under inner automorphisms<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]                      | -<br>-<br>-<br>-      | 27<br>27<br>27<br>27       | 1.4<br>1.4<br>1.4<br>1.4        | -<br>-<br>-<br>-      | 100%<br>100%<br>100%<br>100%         |
| GRP176<br>-1<br>-2                   | GenDist<br>p07                                  | General form of distributivity<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]  | -<br>-                | 26<br>27                   | 1.4<br>1.4                      | -<br>-                | 100%<br>100%                         |
| GRP177<br>-1<br>-2                   | LOGMono1<br>p08a<br>p08b                        | A consequence of monotonicity<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]  | -<br>-                | 29<br>29                   | 1.3<br>1.3                      | -<br>-                | 100%<br>100%                         |
| GRP178<br>-1<br>-2                   | LOGMono2<br>p09a<br>p09b                        | A consequence of monotonicity<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]  | -<br>-                | 30<br>30                   | 1.3<br>1.3                      | -<br>-                | 100%<br>100%                         |
| GRP179<br>-1<br>-2<br>-3             | GLBtoLUB<br>p10<br>p18                          | For converting between GLB and LUB<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]  | -<br>-<br>-           | 26<br>26<br>29             | 1.4<br>1.4<br>1.3               | -<br>-<br>-           | 100%<br>100%<br>100%                 |
| GRP180<br>-1<br>-2                   | GLBtoLUB1<br>p11                                | Consequence of converting between GLB and LUB<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]  | -<br>-                | 26<br>29                   | 1.4<br>1.3                      | -<br>-                | 100%<br>100%                         |
| GRP181<br>-1<br>-2<br>-3<br>-4       | DistLatt<br>p12<br>p12x                         | Distributivity of a lattice<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]  | -<br>-<br>-<br>-      | 28<br>31<br>30<br>33       | 1.4<br>1.3<br>1.3<br>1.3        | -<br>-<br>-<br>-      | 100%<br>100%<br>100%<br>100%         |
| GRP182<br>-1<br>-2<br>-3<br>-4       | PosNegId<br>p17a<br>p17b                        | Positive part of the negative part is identity<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95, Dah95]<br>[Fuc94, Sch95]<br>[Fuc94, Sch95]           | -<br>-<br>-<br>-      | 26<br>29<br>26<br>29       | 1.4<br>1.3<br>1.4<br>1.3        | -<br>-<br>-<br>-      | 100%<br>100%<br>100%<br>100%         |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References                                 | V | Cl | Av  | nH | Eq   |
|----------------------|------------------------------|---|---|----|-----|----|------|
| GRP183               | OrthElSubG                   | Orthogonal elements form a subgroup with orthogonal parts | - | 26 | 1.4 | -  | 100% |
| -1                   |                              | [Fuc94, Sch95]  | - | 26 | 1.4 | -  | 100% |
| -2                   | p20                          | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -3                   |                              | [Fuc94, Sch95]  | - | 26 | 1.4 | -  | 100% |
| -4                   | p20x                         | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| GRP184               | OrthElComm                   | Orthogonal elements commute and form a subgroup           | - | 26 | 1.4 | -  | 100% |
| -1                   |                              | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -2                   | p21                          | [Fuc94, Sch95]  | - | 26 | 1.4 | -  | 100% |
| -3                   |                              | [Fuc94, Sch95]  | - | 31 | 1.3 | -  | 100% |
| -4                   | p21x                         | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| GRP185               | AppMonoDist                  | Application of monotonicity and distributivity            | - | 26 | 1.4 | -  | 100% |
| -1                   |                              | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -2                   | p22a                         | [Fuc94, Sch95]  | - | 26 | 1.4 | -  | 100% |
| -3                   |                              | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -4                   | p22b                         | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| GRP186               | AppDistGrp                   | Application of distributivity and group theory            | - | 26 | 1.4 | -  | 100% |
| -1                   |                              | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -2                   | p23                          | [Fuc94, Sch95]  | - | 26 | 1.4 | -  | 100% |
| -3                   |                              | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -4                   | p23x                         | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| GRP187               | OrthElComm                   | Orthogonal elements commute                               | - | 27 | 1.4 | -  | 100% |
| -1                   | p33                          | [Fuc94, Sch95, Dah95]                                     | - | 27 | 1.4 | -  | 100% |
| GRP188               | LOGLatt1                     | Consequence of lattice theory                             | - | 26 | 1.4 | -  | 100% |
| -1                   |                              | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -2                   | p38a                         | [Fuc94, Sch95]  | - | 26 | 1.4 | -  | 100% |
| GRP189               | LOGLatt2                     | Consequence of lattice theory                             | - | 26 | 1.4 | -  | 100% |
| -1                   |                              | [Fuc94, Sch95]  | - | 29 | 1.3 | -  | 100% |
| -2                   | p38b                         | [Fuc94, Sch95]  | - | 27 | 1.4 | -  | 100% |
| GRP190               | LOGEst1                      | Something useful for estimations                          | - | 27 | 1.4 | -  | 100% |
| -1                   | p39a                         | [Fuc94, Sch95]  | - | 27 | 1.4 | -  | 100% |
| -2                   | p39c                         | [Fuc94, Sch95]  | - | 27 | 1.4 | -  | 100% |
| GRP191               | LOGEst2                      | Something useful for estimations                          | - | 27 | 1.4 | -  | 100% |
| -1                   | p39b                         | [Fuc94, Sch95]  | - | 27 | 1.4 | -  | 100% |
| -2                   | p39d                         | [Fuc94, Sch95]  | - | 27 | 1.4 | -  | 100% |
| GRP192               | EvenElGrp                    | Even elements implies trivial group                       | - | 27 | 1.4 | -  | 100% |
| -1                   | p40a                         | [Fuc94, Sch95]  | - | 27 | 1.4 | -  | 100% |
| GRP193               | LOGDistMono                  | A combination of distributivity and monotonicity          | - | 31 | 1.3 | -  | 100% |
| -1                   | p8_9a                        | [Fuc94, Sch95]  | - | 31 | 1.3 | -  | 100% |
| -2                   | p8_9b                        | [Fuc94, Sch95]  | - | 31 | 1.3 | -  | 100% |

### Domain HEN (12 abstract problems, 64 problems)

|        |                 |                                       |   |    |     |   |      |
|--------|-----------------|---------------------------------------|---|----|-----|---|------|
| HEN001 | XDivId          | $X/\text{identity} = \text{zero}$     | - | 20 | 2.4 | - | 36%  |
| -1     | H1, hp1.ver1.in | [MOW76]                               | - | 15 | 1.9 | - | 57%  |
| -3     | hp1.ver2.in     | [MOW76]                               | - | 11 | 1.6 | - | 100% |
| -5     | hp1.ver3.in     | [MOW76]                               | - | 20 | 2.4 | - | 36%  |
| HEN002 | 0DivX           | $\text{zero}/X = \text{zero}$         | - | 21 | 2.3 | - | 35%  |
| -1     | hp2.ver1.in     | [MOW76]                               | - | 15 | 1.9 | - | 57%  |
| -2     | H2              | [MOW76]                               | - | 16 | 1.8 | - | 58%  |
| -3     | hp2.ver2.in     | [MOW76]                               | - | 11 | 1.6 | - | 100% |
| -4     |                 | [MOW76]                               | - | 20 | 2.4 | - | 36%  |
| -5     | hp2.ver3.in     | [MOW76]                               | - | 22 | 2.2 | - | 34%  |
| HEN003 | XDivX           | $X/X = \text{zero}$                   | - | 15 | 1.9 | - | 57%  |
| -1     |                 | [MOW76]                               | - | 17 | 1.8 | - | 60%  |
| -2     | H3, hp3.ver1.in | [MOW76]                               | - | 11 | 1.6 | - | 100% |
| -3     | HP3             | [MOW76]                               | - | 20 | 2.4 | - | 36%  |
| -4     | hp3.ver2.in     | [MOW76]                               | - | 12 | 1.6 | - | 100% |
| -5     | hp3.ver3.in     | [MOW76]                               | - | 17 | 1.8 | - | 60%  |
| HEN004 | XDiv0           | $X/\text{zero} = X$                   | - | 20 | 2.4 | - | 36%  |
| -1     |                 | [MOW76]                               | - | 23 | 2.2 | - | 34%  |
| -2     | H4, hp4.ver1.in | [MOW76]                               | - | 15 | 1.9 | - | 57%  |
| -3     | HP4             | [MOW76]                               | - | 18 | 1.7 | - | 61%  |
| -4     |                 | [MOW76]                               | - | 12 | 1.6 | - | 100% |
| -5     | hp4.ver3.in     | [MOW76]                               | - | 17 | 1.8 | - | 60%  |
| -6     | hp4.ver2.in     | [MOW76]                               | - | 22 | 2.2 | - | 34%  |
| HEN005 | LeTrans         | The relation less_equal is transitive | - | 26 | 2.0 | - | 32%  |
| -1     | hp5.ver1.in     | [MOW76]                               | - | 17 | 1.8 | - | 50%  |
| -2     | H5              | [MOW76]                               | - | 21 | 1.6 | - | 55%  |
| -3     | HP5             | [MOW76]                               | - | 13 | 1.5 | - | 100% |
| -4     |                 | [MOW76]                               | - | 19 | 1.7 | - | 53%  |
| -5     | hp5.ver3.in     | [MOW76]                               | - | 23 | 2.2 | - | 34%  |
| -6     | hp5.ver2.in     | [MOW76]                               | - | 28 | 2.0 | - | 29%  |
| HEN006 | Eqn1            | $X/Y \leq Z \Rightarrow X/Z \leq Y$   | - | 16 | 1.8 | - | 51%  |
| -1     |                 | [MOW76]                               | - | 21 | 1.7 | - | 52%  |
| -2     | H6              | [MOW76]                               | - | 13 | 1.5 | - | 100% |
| -3     | HP6             | [MOW76]                               | - | 19 | 1.7 | - | 56%  |
| -4     |                 | [MOW76]                               | - | 27 | 2.0 | - | 31%  |
| -5     | hp6.ver3.in     | [MOW76]                               | - | 27 | 2.0 | - | 31%  |
| -6     | hp6.ver2.in     | [MOW76]                               | - | 27 | 2.0 | - | 31%  |
| -7     | hp6.ver1.in     | [MOW76]                               | - | 27 | 2.0 | - | 31%  |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References   | V | Cl | Av  | nH | Eq   |
|----------------------|------------------------------|---|---|----|-----|----|------|
| HEN007               | Eqn2                         | $X \leq Y \Rightarrow Z/Y \leq Z/X$<br>[MOW76]  | - | 23 | 2.2 | -  | 34%  |
| -1                   | H7                           | [MOW76]   | - | 29 | 2.1 | -  | 27%  |
| -2                   | HP7                          | [MOW76]   | - | 16 | 1.8 | -  | 51%  |
| -3                   | hp7.ver2.in                  | [MOW76]   | - | 22 | 1.7 | -  | 50%  |
| -4                   | hp7.ver3.in                  | [MOW76]   | - | 13 | 1.7 | -  | 100% |
| -5                   | hp7.ver1.in                  | [MOW76]   | - | 28 | 2.0 | -  | 29%  |
| -6                   |                              |   |   |    |     |    |      |
| HEN008               | Eqn3                         | $X \leq Y \Rightarrow X/Z \leq Y/Z$<br>[MOW76]  | - | 23 | 2.2 | -  | 34%  |
| -1                   | hp8.ver1.in                  | [MOW76]   | - | 30 | 2.2 | -  | 26%  |
| -2                   | H8                           | [MOW76]   | - | 16 | 1.8 | -  | 51%  |
| -3                   | HP8                          | [MOW76]   | - | 23 | 1.7 | -  | 47%  |
| -4                   | hp8.ver3.in                  | [MOW76]   | - | 12 | 1.6 | -  | 100% |
| -5                   | hp8.ver2.in                  | [MOW76]   | - | 19 | 1.7 | -  | 56%  |
| -6                   |                              |   |   |    |     |    |      |
| HEN009               | IdDivX1                      | Define $X'$ as $\text{identity}/X$ . Then $X' = X''$<br>[MOW76]                       | - | 23 | 2.2 | -  | 36%  |
| -1                   | H9, hp9.ver1.in              | [MOW76]   | - | 31 | 2.2 | -  | 26%  |
| -2                   | HP9                          | [MOW76]   | - | 19 | 1.7 | -  | 62%  |
| -3                   | hp9.ver3.in                  | [MOW76]   | - | 23 | 1.8 | -  | 48%  |
| -4                   | hp9.ver2.in                  | [MOW76]   | - | 14 | 1.8 | -  | 100% |
| -5                   |                              |   | - | 24 | 1.6 | -  | 59%  |
| -6                   |                              |   |   |    |     |    |      |
| HEN010               | IdDivX2                      | Define $X'$ as $\text{identity}/X$ . Then $X' = X' / (\text{identity}/X')$<br>[MOW76] | - | 23 | 2.2 | -  | 36%  |
| -1                   | H10                          | [MOW76]   | - | 32 | 2.3 | -  | 26%  |
| -2                   | HP10                         | [MOW76]   | - | 15 | 1.9 | -  | 57%  |
| -3                   | hp10.ver3.in                 | [MOW76]   | - | 24 | 1.8 | -  | 50%  |
| -4                   | hp10.ver2.in                 | [MOW76]   | - | 14 | 1.8 | -  | 100% |
| -5                   | hp10.ver1.in                 | [MOW76]   | - | 23 | 1.7 | -  | 53%  |
| -6                   |                              |   | - | 31 | 2.2 | -  | 26%  |
| -7                   |                              |   |   |    |     |    |      |
| HEN011               | OpComm                       | This operation is commutative<br>[MOW76]  | - | 26 | 2.0 | -  | 34%  |
| -1                   | H11, hp11.ver1.in            | [MOW76]   | - | 36 | 2.2 | -  | 25%  |
| -2                   | HP11                         | [MOW76]   | - | 20 | 1.6 | -  | 63%  |
| -3                   | hp11.ver2.in                 | [MOW76]   | - | 25 | 1.7 | -  | 51%  |
| -4                   | hp11.ver3.in                 | [MOW76]   | - | 19 | 1.6 | -  | 100% |
| -5                   |                              |   |   |    |     |    |      |
| HEN012               | XLeX                         | $X \leq X$  | - | 20 | 2.4 | -  | 36%  |
| -1                   | new.ver2.in                  |   | - | 15 | 1.9 | -  | 53%  |
| -2                   |                              |   |   |    |     |    |      |
| -3                   |                              |   |   |    |     |    |      |

### Domain LAT (5 abstract problems, 10 problems)

|        |                                 |  |   |    |     |    |      |
|--------|---------------------------------|--|---|----|-----|----|------|
| LAT001 | Eqn1                            | If $X' = U \vee V$ and $Y' = U \wedge V$ , then $U' = X \vee (Y \wedge V)$<br>[Bum65, GOBS69, McC88] | - | 28 | 1.6 | -  | 77%  |
| -1     | L1a                             |  |   |    |     |    |      |
| LAT002 | ExEqn1                          | If $X' = U \vee V$ and $Y' = U \wedge V$ , then $U'$ exists<br>[Bum65, GOBS69, McC88]                | - | 28 | 1.6 | -  | 77%  |
| -1     | L1b                             |  |   |    |     |    |      |
| LAT003 | Eqn2                            | A fairly complex equation to establish<br>[Bum65, GOBS69, McC88]                                     | - | 38 | 1.8 | 2% | 62%  |
| -1     | L2                              |  |   |    |     |    |      |
| LAT004 | Eqn3                            | A fairly complex equation to establish<br>[Bum65, GOBS69, McC88]                                     | - | 38 | 1.8 | 2% | 62%  |
| -1     | L3                              |  |   |    |     |    |      |
| LAT005 | SAMsLem                         | SAM's lemma<br>[GOBS69, MOW76]   | - | 29 | 2.1 | -  | -    |
| -1     | SAM's lemma, SAMslemma.ver1.in  | [GOBS69, MOW76]  | - | 31 | 1.8 | -  | -    |
| -2     | SAM's lemma, sam.in, sam.hyp.in | [GOBS69, MOW76, LM92]  | - | 28 | 1.6 | -  | 79%  |
| -3     | SAM's lemma                     | [GOBS69, McC88]  | - | 27 | 1.3 | -  | 100% |
| -4     | Test Problem 12, SAM's lemma    | [McC88, Wos88]   | - | 44 | 2.1 | -  | 24%  |
| -5     | SAMslemma.ver1.in               | [GOBS69, MOW76]  | - | 50 | 2.1 | -  | 21%  |
| -6     | Test Problem 12, SAM's lemma    | [Wos88]  |   |    |     |    |      |

### Domain LCL (256 abstract problems, 278 problems)

|        |                 |  |   |   |     |   |   |
|--------|-----------------|--|---|---|-----|---|---|
| LCL001 | WR_CAM          | The Whitehead-Russell system $\Rightarrow$ the Meredith axiom<br>[Mer53, MW92, McC92b] | - | 6 | 1.3 | - | - |
| -1     | AN-50           |  |   |   |     |   |   |
| LCL002 | CAM_AN1         | AN-CAMerideth $\Rightarrow$ AN-1<br>[Mer53, MW92, McC92b]                              | - | 3 | 1.7 | - | - |
| -1     | AN-51           |  |   |   |     |   |   |
| LCL003 | CAM_AN2         | AN-CAMerideth $\Rightarrow$ AN-2<br>[Mer53, MW92, McC92b]                              | - | 3 | 1.7 | - | - |
| -1     | AN-52           |  |   |   |     |   |   |
| LCL004 | CAM_AN3         | AN-CAMerideth $\Rightarrow$ AN-3<br>[Mer53, MW92, McC92b]                              | - | 3 | 1.7 | - | - |
| -1     | AN-53           |  |   |   |     |   |   |
| LCL005 | CAM_AN4         | AN-CAMerideth $\Rightarrow$ AN-4<br>[Mer53, MW92, McC92b]                              | - | 3 | 1.7 | - | - |
| -1     | AN-54           |  |   |   |     |   |   |
| LCL006 | Wj_EC1          | EC-1 depends on the Wajsberg system<br>[MW92, McC92b]                                  | - | 4 | 1.5 | - | - |
| -1     | EC-69           |  |   |   |     |   |   |
| LCL007 | Wj_EC2          | EC-2 depends on the Wajsberg system<br>[MW92, McC92b]                                  | - | 4 | 1.5 | - | - |
| -1     | EC-70           |  |   |   |     |   |   |
| LCL008 | YQL_EC4         | EC-4 depends on YQL<br>[MW92, McC92b]  | - | 3 | 1.7 | - | - |
| -1     | EC-71           |  |   |   |     |   |   |
| LCL009 | YQL_EC5         | EC-5 depends on YQL<br>[MW92, McC92b]  | - | 3 | 1.7 | - | - |
| -1     | EC-72           |  |   |   |     |   |   |
| LCL010 | YQF_YQL         | YQL depends on YQF<br>[MW92, McC92b]   | - | 3 | 1.7 | - | - |
| -1     | EC-73, ec_yq.in |  |   |   |     |   |   |
| LCL011 | YQJ_YQF         | YQF depends on YQJ<br>[MW92, McC92b]   | - | 3 | 1.7 | - | - |
| -1     | EC-74           |  |   |   |     |   |   |
| LCL012 | UM_YQJ          | YQJ depends on UM<br>[MW92, McC92b]  | - | 3 | 1.7 | - | - |
| -1     | EC-75           |  |   |   |     |   |   |
| LCL013 | XGF_UM          | UM depends on XGF<br>[MW92, McC92b]  | - | 3 | 1.7 | - | - |
| -1     | EC-76           |  |   |   |     |   |   |
| LCL014 | WN_XGF          | XGF depends on WN<br>[MW92, McC92b]  | - | 3 | 1.7 | - | - |
| -1     | EC-77           |  |   |   |     |   |   |
| LCL015 | YRM_WN          | WN depends on YRM<br>[MW92, McC92b]  | - | 3 | 1.7 | - | - |
| -1     | EC-78           |  |   |   |     |   |   |

| Syntactic name<br>V# | Semantic name<br>Other names                           | Description  | References                  | V | Cl | Av  | nH | Eq |
|----------------------|--|--|-----------------------------|---|----|-----|----|----|
| LCL016<br>-1         | YRO_YRM<br>EC-79                                       | YRM depends on YRO                                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL017<br>-1         | PYO_YRO<br>EC-80                                       | YRO depends on PYO                                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL018<br>-1         | PYM_PYO<br>EC-81                                       | PYO depends on PYM                                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL019<br>-1         | XGK_PYM<br>EC-82                                       | PYM depends on XGK                                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL020<br>-1         | XHK_XGK<br>EC-83                                       | XGK depends on XHK                                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL021<br>-1         | XHN_XHK<br>EC-84                                       | XHK depends on XHN                                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL022<br>-1         | YQL_EC1<br>ec.in part 1                                | EC-1 depends on YQL                                |                             | - | 3  | 1.7 | -  | -  |
| LCL023<br>-1         | YQL_EC2<br>ec.in part 2                                | EC-2 depends on YQL                                |                             | - | 3  | 1.7 | -  | -  |
| LCL024<br>-1         | XGK_PYO<br>Test Problem 16, CADE-11 Comp. 4, THEOREM 4 | PYO depends on XGK                                 | [Wos88, Ove90, Ove93, LM93] | - | 3  | 1.7 | -  | -  |
| LCL025<br>-1         | Ch_C01<br>C0-37  | C0-1 depends on the Church system                  | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL026<br>-1         | Ch_C03<br>C0-38  | C0-3 depends on the Church system                  | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL027<br>-1         | Ch_C04<br>C0-39  | C0-4 depends on the Church system                  | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL028<br>-1         | Ch_CAM<br>C0-40  | C0-CAMerideth depends on the Church system         | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL029<br>-1         | TB_C05<br>C0-41  | C0-5 depends on the Tarski-Bernays system          | [MW92, McC92b]              | - | 6  | 1.3 | -  | -  |
| LCL030<br>-1         | TB_C06<br>C0-42  | C0-6 depends on the Tarski-Bernays system          | [MW92, McC92b]              | - | 6  | 1.3 | -  | -  |
| LCL031<br>-1         | TB_CAM<br>C0-43  | C0-CAMerideth depends on the Tarski-Bernays system | [MW92, McC92b]              | - | 6  | 1.3 | -  | -  |
| LCL032<br>-1         | CAM_C01<br>C0-44                                       | C0-1 depends on the Merideth axiom                 | [Mer53, MW92, McC92b]       | - | 3  | 1.7 | -  | -  |
| LCL033<br>-1         | CAM_C02<br>C0-45                                       | C0-2 depends on the Merideth axiom                 | [Mer53, MW92, McC92b]       | - | 3  | 1.7 | -  | -  |
| LCL034<br>-1         | CAM_C03<br>C0-46                                       | C0-3 depends on the Merideth axiom                 | [Mer53, MW92, McC92b]       | - | 3  | 1.7 | -  | -  |
| LCL035<br>-1         | CAM_C04<br>C0-47                                       | C0-4 depends on the Merideth axiom                 | [Mer53, MW92, McC92b]       | - | 3  | 1.7 | -  | -  |
| LCL036<br>-1         | CAM_C05<br>C0-48                                       | C0-5 depends on the Merideth axiom                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL037<br>-1         | CAM_C06<br>C0-49                                       | C0-6 depends on the Merideth axiom                 | [MW92, McC92b]              | - | 3  | 1.7 | -  | -  |
| LCL038<br>-1         | Ov_C01<br>CADE-11 Comp. 5, THEOREM 5                   | C0-1 depends on a single axiom                     | [Ove90, Ove93, LM93]        | - | 3  | 1.7 | -  | -  |
| LCL039<br>-1         | Modal<br>Pelletier 69                                  | A theorem from Morgan                              | [Mor84, Pel86]              | - | 8  | 1.4 | -  | -  |
| LCL040<br>-1         | Fr_CN21<br>CN-1  | CN-21 depends on the rest of Frege's system        | [MW92, McC92b]              | - | 7  | 1.3 | -  | -  |
| LCL041<br>-1         | Hi_CN30<br>CN-2  | CN-30 depends on the rest of Hilbert's system      | [MW92, McC92b]              | - | 7  | 1.3 | -  | -  |
| LCL042<br>-1         | Hi_CN35<br>CN-3  | CN-35 depends on Hilbert's system                  | [MW92, McC92b]              | - | 7  | 1.3 | -  | -  |
| LCL043<br>-1         | Hi_CN39<br>CN-4  | CN-39 depends on Hilbert's system                  | [MW92, McC92b]              | - | 7  | 1.3 | -  | -  |
| LCL044<br>-1         | Hi_CN40<br>CN-5  | CN-40 depends on Hilbert's system                  | [MW92, McC92b]              | - | 7  | 1.3 | -  | -  |
| LCL045<br>-1         | Hi_CN46<br>CN-6  | CN-46 depends on Hilbert's system                  | [MW92, McC92b]              | - | 7  | 1.3 | -  | -  |
| LCL046<br>-1         | Lk_CN16<br>CN-7, cn.in part 1                          | CN-16 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL047<br>-1         | Lk_CN18<br>CN-8, cn.in part 2                          | CN-18 depends on the Lukasiewicz system            | [MW92, Wos92, McC92b]       | - | 5  | 1.4 | -  | -  |
| LCL048<br>-1         | Lk_CN19<br>CN-9, cn.in part 3                          | CN-19 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL049<br>-1         | Lk_CN20<br>CN-10                                       | CN-20 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL050<br>-1         | Lk_CN21<br>CN-11                                       | CN-21 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL051<br>-1         | Lk_CN22<br>CD-12, CN-12                                | CN-22 depends on the Lukasiewicz system            | [LM92, MW92, McC92b]        | - | 5  | 1.4 | -  | -  |
| LCL052<br>-1         | Lk_CN24<br>CD-13, CN-13                                | CN-24 depends on the Lukasiewicz system            | [LM92, MW92, McC92b]        | - | 5  | 1.4 | -  | -  |
| LCL053<br>-1         | Lk_CN30<br>CN-14                                       | CN-30 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL054<br>-1         | Lk_CN35<br>CN-15                                       | CN-35 depends on the Lukasiewicz system            | [MW92, Wos92, McC92b]       | - | 5  | 1.4 | -  | -  |
| LCL055<br>-1         | Lk_CN37<br>CN-16                                       | CN-37 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL056<br>-1         | Lk_CN39<br>CN-17                                       | CN-39 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |
| LCL057<br>-1         | Lk_CN40<br>CN-18                                       | CN-40 depends on the Lukasiewicz system            | [MW92, McC92b]              | - | 5  | 1.4 | -  | -  |

| Syntactic name<br>V# | Semantic name<br>Other names  | Description           | References   | V | Cl | Av  | nH | Eq |
|----------------------|---|-----------------------|--|---|----|-----|----|----|
| LCL058               | -1 Lk_CN46<br>CN-19, cn19.in  | CN-46 depends on the  | Lukasiewicz system<br>[MW92, McC92b]   | - | 5  | 1.4 | -  | -  |
| LCL059               | -1 Lk_CN49<br>CN-20   | CN-49 depends on the  | Lukasiewicz system<br>[MW92, Wos92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL060               | -1 Lk_CN54<br>CN-21   | CN-54 depends on the  | Lukasiewicz system<br>[MW92, McC92b]   | - | 5  | 1.4 | -  | -  |
| LCL061               | -1 Lk_CN59<br>CN-22   | CN-59 depends on the  | Lukasiewicz system<br>[MW92, McC92b]   | - | 5  | 1.4 | -  | -  |
| LCL062               | -1 Lk_CN60<br>CN-23   | CN-60 depends on the  | Lukasiewicz system<br>[MW92, McC92b]   | - | 5  | 1.4 | -  | -  |
| LCL063               | -1 Lk_CAM<br>CN-24  | CN-CAMerideth depends | on the Lukasiewicz system<br>[MW92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL064               | -1 Ch_CN1<br>CN-25<br>morgan.six.ver1.in  | CN-1 depends on the   | Church system<br>[MW92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL065               | -1 Ch_CN2<br>CN-26  | CN-2 depends on the   | Church system<br>[MW92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL066               | -1 Ch_CN3<br>CN-27  | CN-3 depends on the   | Church system<br>[MW92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL067               | -1 Lk2_CN1<br>CN-28   | CN-1 depends on the   | second Lukasiewicz system<br>[MW92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL068               | -1 Lk2_CN2<br>CN-29   | CN-2 depends on the   | second Lukasiewicz system<br>[MW92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL069               | -1 Lk2_CN3<br>CN-30   | CN-3 depends on the   | second Lukasiewicz system<br>[MW92, McC92b]  | - | 5  | 1.4 | -  | -  |
| LCL070               | -1 Ws_CN1<br>CN-31  | CN-1 depends on the   | Wos system<br>[MW92, McC92b]   | - | 5  | 1.4 | -  | -  |
| LCL071               | -1 Ws_CN2<br>CN-32  | CN-2 depends on the   | Wos system<br>[MW92, McC92b]   | - | 5  | 1.4 | -  | -  |
| LCL072               | -1 Ws_CN3<br>CN-33  | CN-3 depends on the   | Wos system<br>[MW92, McC92b]   | - | 5  | 1.4 | -  | -  |
| LCL073               | -1 CAM_CN1<br>CN-34   | CN-1 depends on the   | single Merideth axiom<br>[MW92, McC92b]  | - | 3  | 1.7 | -  | -  |
| LCL074               | -1 CAM_CN2<br>CN-35   | CN-2 depends on the   | single Merideth axiom<br>[MW92, McC92b]  | - | 3  | 1.7 | -  | -  |
| LCL075               | -1 CAM_CN3<br>CN-36   | CN-3 depends on the   | single Merideth axiom<br>[MW92, McC92b]  | - | 3  | 1.7 | -  | -  |
| LCL076               | -1 Ch_CN40<br>Pelletier 66<br>morgan.three.ver1.in, morgan.three.ver2.in<br>morgan.four.ver1.in | CN-40 depends on the  | Church system<br>[Mor84, Pel86]  | - | 5  | 1.4 | -  | -  |
| LCL077               | -1 Ch_CN39<br>Pelletier 67, morgan.five.ver1.in<br>morgan.two.ver1.in                           | CN-39 depends on the  | Church system<br>[Mor84, Pel86]<br>[Mor84]   | - | 5  | 1.4 | -  | -  |
| LCL078               | -1 Ch1_CN40<br>Pelletier 68, morgan.five.ver2.in  | CN-40 depends on      | CN-18 CN-35 CN-46<br>[Mor84, Pel86]  | - | 5  | 1.4 | -  | -  |
| LCL079               | -1 Ch_TR<br>morgan.one.ver2.in  | Transitivity can be   | derived from Church's system   | - | 7  | 1.3 | -  | -  |
| LCL080               | -1 TB_Lk1<br>IC-63  | The 1st Lukasiewicz   | axiom depends on Tarski-Bernays system<br>[Luk48, MW92, McC92b]<br>[Luk48, MW92]   | - | 5  | 1.4 | -  | -  |
| LCL081               | -1 Lk1_IC1<br>I1, IC-64, ls1  | IC-1 depends on the   | 1st Lukasiewicz axiom<br>[Luk48, Pfe88, MW92, McC92b]  | - | 3  | 1.7 | -  | -  |
| LCL082               | -1 Lk1_IC2<br>S1, IC-1.1, IC-65, ls2  | IC-2 depends on the   | 1st Lukasiewicz axiom<br>[Luk48, Pfe88, WWM <sup>+</sup> 90, MW92, McC92b]   | - | 3  | 1.7 | -  | -  |
| LCL083               | -1 Lk1_IC3<br>P1, IC-1.2, IC-66, ls3<br>IP1, ls4  | IC-3 depends on the   | 1st Lukasiewicz axiom<br>[Luk48, Pfe88, WWM <sup>+</sup> 90, MW92, McC92b]<br>[Luk48, Pfe88]                             | - | 3  | 1.7 | -  | -  |
| LCL084               | -1 Lk1_IC4<br>H1, IC-1.3, IC-67, Imp-4, ls5<br>IH1, ls6<br>IPH1, ls7                            | IC-4 depends on the   | 1st Lukasiewicz axiom<br>[Luk48, Pfe88, WWM <sup>+</sup> 90]<br>[LM92, MW92, McC92b]<br>[Luk48, Pfe88]<br>[Luk48, Pfe88] | - | 3  | 1.7 | -  | -  |
| LCL085               | -1 Lk1_IC5<br>IC-68   | IC-5 depends on the   | 1st Lukasiewicz axiom<br>[Luk48, MW92, McC92b]   | - | 3  | 1.7 | -  | -  |
| LCL086               | -1 Lk4_IC1  | IC-1 depends on the   | 4th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL087               | -1 Lk4_IC2  | IC-2 depends on the   | 4th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL088               | -1 Lk4_IC3  | IC-3 depends on the   | 4th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL089               | -1 Lk4_IC4  | IC-4 depends on the   | 4th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL090               | -1 Lk5_IC1  | IC-1 depends on the   | 5th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL091               | -1 Lk5_IC2  | IC-2 depends on the   | 5th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL092               | -1 Lk5_IC3  | IC-3 depends on the   | 5th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL093               | -1 Lk5_IC4  | IC-4 depends on the   | 5th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL094               | -1 Lk4_IC5  | IC-5 depends on the   | 4th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |
| LCL095               | -1 Lk5_IC5  | IC-5 depends on the   | 5th Lukasiewicz axiom<br>[Luk48, Pfe88]  | - | 3  | 1.7 | -  | -  |

| Syntactic name<br>V#                       | Semantic name<br>Other names  | Description                            | References   | V                          | Cl                              | Av                                     | nH                         | Eq                                      |
|--|---|--|--|----------------------------|---------------------------------|--|----------------------------|---|
| LCL096<br>-1                               | K1.LG1<br>LG-89   | LG-1 depends on LG-2,                  | LG-3, LG-4<br>[MW92, McC92a, McC92b]   | -                          | 5                               | 1.4                                    | -                          | -                                       |
| LCL097<br>-1                               | K1.LG4<br>CD-90, LG-90  | LG-4 depends on LG-2,                  | LG-3<br>[LM92, MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL098<br>-1                               | LG3.LG4<br>LG-91  | LG-4 depends on LG-3                   | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL099<br>-1                               | Mc1.LG5<br>LG-92  | LG-5 depends on the 1st McCune system  | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL100<br>-1                               | Mc2.LG3<br>LG-93  | LG-3 depends on the 2nd McCune system  | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL101<br>-1                               | Mc3.P1<br>LG-94   | P-1 depends on the 3rd McCune system   | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL102<br>-1                               | Mc4.P1<br>LG-95   | P-1 depends on the 4th McCune system   | [MW92, McC92a, McC92b]   | -                          | 5                               | 1.4                                    | -                          | -                                       |
| LCL103<br>-1                               | Mc5.LG2<br>LG-96  | LG-2 depends on the 5th McCune system  | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL104<br>-1                               | Mc6.P1<br>LG-97   | P-1 depends on the 6th McCune system   | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL105<br>-1                               | Mc7.LG2<br>LG-98  | LG-2 depends on the 7th McCune system  | [MW92, McC92a, McC92b]   | -                          | 5                               | 1.4                                    | -                          | -                                       |
| LCL106<br>-1                               | Q1Q4.Q2<br>LG-99  | Q-2 depends on Q-1, Q-4                | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL107<br>-1                               | McAx.P1<br>LG-100   | P-1 depends on the single McCune axiom | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL108<br>-1                               | McAx.Q3<br>LG-101   | Q-3 depends on the single McCune axiom | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL109<br>-1<br>-2<br>-3<br>-4<br>-5<br>-6 | CAM.MV4<br>MV-55, Luka5<br>CADE-11 Comp. Eq-5, Luka-5,<br>MV4, THEOREM EQ-5, PROBLEM 5<br>Lattice structure theorem 8<br>Lattice structure theorem 8<br>Lattice structure theorem 8 | MV-4 depends on the Merideth system    | [MW92, McC92b]<br>[Ove90, LM92, LW92]<br>[Ove93, LM93, Zha93]<br>[Bon91, MW92]<br>[FRT84, Bon91]<br>[FRT84, Bon91]<br>[FRT84, AB90, Bon91] | -<br>-<br>-<br>-<br>-<br>- | 6<br>11<br>21<br>21<br>29<br>24 | 1.3<br>1.5<br>1.4<br>1.8<br>1.7<br>1.4 | -<br>-<br>-<br>-<br>-<br>- | -<br>100%<br>100%<br>83%<br>71%<br>100% |
| LCL110<br>-1<br>-2                         | CAM.MV24<br>MV-56, mv.in part 1<br>MV1.1  | MV-24 depends on the Merideth system   | [MW92, McC92b]<br>[FRT84, MW92, LW92]  | -<br>-                     | 6<br>11                         | 1.3<br>1.5                             | -<br>-                     | -<br>100%                               |
| LCL111<br>-1<br>-2                         | CAM.MV25<br>CADE-11 Comp. 6, MV-57, THEOREM 6,<br>mv.in part 2, mv25.in, ovb6<br>Lemma 6, MV2   | MV-25 depends on the Merideth system   | [Ove90, MW92, McC92b, Ove93, LM93]<br>[FRT84, Bon91, MW92, LW92]   | -<br>-                     | 6<br>11                         | 1.3<br>1.5                             | -<br>-                     | -<br>100%                               |
| LCL112<br>-1<br>-2                         | CAM.MV29<br>MV-58, mv.in part 3<br>MV1.2  | MV-29 depends on the Merideth system   | [MW92, McC92b]<br>[FRT84, MW92, LW92, McC92b]  | -<br>-                     | 6<br>11                         | 1.3<br>1.5                             | -<br>-                     | -<br>100%                               |
| LCL113<br>-1<br>-2                         | CAM.MV33<br>MV-59   | MV-33 depends on the Merideth system   | [MW92, McC92b]<br>[FRT84, MW92]  | -<br>-                     | 6<br>11                         | 1.3<br>1.5                             | -<br>-                     | -<br>100%                               |
| LCL114<br>-1<br>-2                         | CAM.MV36<br>CADE-11 Comp. 7, MV-60, THEOREM 7<br>MV3  | MV-36 depends on the Merideth system   | [Ove90, MW92, McC92b, Ove93, LM93]<br>[FRT84, MW92, LW92]  | -<br>-                     | 6<br>11                         | 1.3<br>1.5                             | -<br>-                     | -<br>100%                               |
| LCL115<br>-1<br>-2                         | CAM.MV39<br>MV-61   | MV-39 depends on the Merideth system   | [MW92, McC92b]<br>[FRT84, MW92]  | -<br>-                     | 6<br>11                         | 1.3<br>1.5                             | -<br>-                     | -<br>100%                               |
| LCL116<br>-1<br>-2                         | CAM.MV50<br>MV-62   | MV-50 depends on the Merideth system   | [MW92, McC92b]<br>[FRT84, MW92]  | -<br>-                     | 6<br>11                         | 1.3<br>1.5                             | -<br>-                     | -<br>100%                               |
| LCL117<br>-1                               | YQM.QYF<br>R-85   | QYF depends on YQM                     | [MW92, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL118<br>-1                               | WO.YQM<br>R-86  | YQM depends on WO                      | [MW92, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL119<br>-1                               | XGJ.WO<br>RC-1, R-87  | WO depends on XGJ                      | [WWM <sup>+</sup> 90, MW92, McC92b]  | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL120<br>-1                               | QYF.XGJ<br>R-88   | XGJ depends on QYF                     | [MW92, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL121<br>-1                               | LG2.LG1<br>RG-102   | LG-1 depends on LG-2                   | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL122<br>-1                               | LG2.LG3<br>RG-103   | LG-3 depends on LG-2                   | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL123<br>-1                               | LG2.LG4<br>RG-104   | LG-4 depends on LG-2                   | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL124<br>-1                               | LG2.LG5<br>RG-105   | LG-5 depends on LG-2                   | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL125<br>-1                               | Mc1.LG2<br>RG-106   | LG-2 depends on the 1st McCune system  | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL126<br>-1                               | Mc2.LG2<br>RG-107   | Q-2 depends on the 2nd McCune system   | [MW92, McC92a, McC92b]   | -                          | 4                               | 1.5                                    | -                          | -                                       |
| LCL127<br>-1                               | LG2.S2<br>RG-108  | LG-2 depends on S-2                    | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL128<br>-1                               | LG2.S3<br>RG-109  | LG-2 depends on S-3                    | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL129<br>-1                               | LG2.S4<br>RG-110  | LG-2 depends on S-4                    | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |
| LCL130<br>-1                               | LG2.P4<br>RG-111  | LG-2 depends on P-4                    | [MW92, McC92a, McC92b]   | -                          | 3                               | 1.7                                    | -                          | -                                       |

| Syntactic name<br>V# | Semantic name<br>Other names                | Description<br>References   | V | Cl | Av  | nH | Eq   |
|----------------------|---|---|---|----|-----|----|------|
| LCL131<br>-1         | LG2_S6<br>RG-112                            | LG-2 depends on S-6<br>[MW92, McC92a, McC92b]                                       | - | 3  | 1.7 | -  | -    |
| LCL132<br>-1         | WjAlg1Eqn1<br>Lemma 1                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91]                                      | - | 11 | 1.5 | -  | 100% |
| LCL133<br>-1         | WjAlg1Eqn2<br>Lemma 2                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91]                                      | - | 12 | 1.5 | -  | 100% |
| LCL134<br>-1         | WjAlg1Eqn3<br>Lemma 3                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91]                                      | - | 11 | 1.5 | -  | 100% |
| LCL135<br>-1         | WjAlg1Eqn4<br>Lemma 4                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91, MW92]                                | - | 11 | 1.5 | -  | 100% |
| LCL136<br>-1         | WjAlg1Eqn5<br>Lemma 5                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91, MW92]                                | - | 12 | 1.5 | -  | 100% |
| LCL137<br>-1         | WjAlg1Eqn6                                  | A lemma in Wajsberg algebras<br>[FRT84, MW92]                                       | - | 11 | 1.5 | -  | 100% |
| LCL138<br>-1         | WjAlg1Eqn7<br>Lemma 7                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91]                                      | - | 11 | 1.5 | -  | 100% |
| LCL139<br>-1         | WjAlg1Eqn8<br>Lemma 8                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91]                                      | - | 11 | 1.5 | -  | 100% |
| LCL140<br>-1         | WjAlg1Eqn9<br>Lemma 9                       | A lemma in Wajsberg algebras<br>[FRT84, Bon91]                                      | - | 11 | 1.5 | -  | 100% |
| LCL141<br>-1         | WjAlg1Eqn10<br>Lemma 10                     | A lemma in Wajsberg algebras<br>[FRT84, Bon91, MW92]                                | - | 11 | 1.5 | -  | 100% |
| LCL142<br>-1         | WjLattEqn1<br>Lattice structure theorem 1   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 22 | 1.7 | -  | 78%  |
| LCL143<br>-1         | WjLattEqn2<br>Lattice structure theorem 2   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 22 | 1.7 | -  | 78%  |
| LCL144<br>-1         | WjLattEqn3<br>Lattice structure theorem 3   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 22 | 1.8 | 4% | 75%  |
| LCL145<br>-1         | WjLattEqn4<br>Lattice structure theorem 4   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL146<br>-1         | WjLattEqn5<br>Lattice structure theorem 5   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL147<br>-1         | WjLattEqn6<br>Lattice structure theorem 6   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL148<br>-1         | WjLattEqn7<br>Lattice structure theorem 7   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL149<br>-1         | WjLattEqn9<br>Lattice structure theorem 9   | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL150<br>-1         | WjLattEqn10<br>Lattice structure theorem 10 | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL151<br>-1         | WjLattEqn11<br>Lattice structure theorem 11 | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL152<br>-1         | WjLattEqn12<br>Lattice structure theorem 12 | A theorem in the lattice structure of Wajsberg algebras<br>[FRT84, Bon91]           | - | 21 | 1.8 | -  | 83%  |
| LCL153<br>-1         | WjAlg2Ax1<br>W' axiom 1                     | The 1st alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL154<br>-1         | WjAlg2Ax2<br>W' axiom 2                     | The 2nd alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL155<br>-1         | WjAlg2Ax3<br>W' axiom 3                     | The 3rd alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL156<br>-1         | WjAlg2Ax4<br>W' axiom 4                     | The 4th alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL157<br>-1         | WjAlg2Ax5<br>W' axiom 5                     | The 5th alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL158<br>-1         | WjAlg2Ax6<br>W' axiom 6                     | The 6th alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL159<br>-1         | WjAlg2Ax7<br>W' axiom 7                     | The 7th alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL160<br>-1         | WjAlg2Ax8<br>W' axiom 8                     | The 8th alternative Wajsberg algebra axiom<br>[FRT84, AB90, Bon91]                  | - | 31 | 1.5 | -  | 100% |
| LCL161<br>-1         | WjAlg1Ax1<br>W axiom 1                      | The 1st Wajsberg algebra axiom, from the alternative axioms<br>[FRT84, AB90, Bon91] | - | 24 | 1.4 | -  | 100% |
| LCL162<br>-1         | WjAlg1Ax2<br>W axiom 2                      | The 2nd Wajsberg algebra axiom, from the alternative axioms<br>[FRT84, AB90, Bon91] | - | 24 | 1.4 | -  | 100% |
| LCL163<br>-1         | WjAlg1Ax3<br>W axiom 3                      | The 3rd Wajsberg algebra axiom, from the alternative axioms<br>[FRT84, AB90, Bon91] | - | 24 | 1.4 | -  | 100% |
| LCL164<br>-1         | WjAlg1Ax4<br>W axiom 4                      | The 4th Wajsberg algebra axiom, from the alternative axioms<br>[FRT84, AB90, Bon91] | - | 24 | 1.4 | -  | 100% |
| LCL165<br>-1         | WjAlg1Eqn11<br>Third problem                | A theorem in Wajsberg algebras<br>[FRT84, AB90, Bon91]                              | - | 21 | 1.5 | -  | 100% |
| LCL166<br>-1         | XHN_UM<br>EC-1                              | UM depends on XHN<br>[WWM <sup>+</sup> 90, MW92]                                    | - | 3  | 1.7 | -  | -    |
| LCL167<br>-1         | XHK_YRO<br>EC-2                             | YRO depends on XHK<br>[WWM <sup>+</sup> 90, MW92]                                   | - | 3  | 1.7 | -  | -    |
| LCL168<br>-1         | XEHNotAx<br>RC-2                            | XEH is not a single axiom for the R-calculus<br>[WWM <sup>+</sup> 90, MW92]         | - | 6  | 1.3 | -  | -    |
| LCL169<br>-1         | PropEqn2.01<br>Problem 2.01                 | Principia Mathematica 2.01<br>[WR27, NSS63, O'R89, SE94]                            | - | 9  | 1.6 | -  | -    |
| LCL170<br>-1         | PropEqn2.02<br>Problem 2.02                 | Principia Mathematica 2.02<br>[WR27, NSS63, O'R89, SE94]                            | - | 9  | 1.6 | -  | -    |
| LCL171<br>-1         | PropEqn2.03<br>Problem 2.03                 | Principia Mathematica 2.03<br>[WR27, NSS63, O'R89, SE94]                            | - | 9  | 1.6 | -  | -    |
| LCL172<br>-1         | PropEqn2.04<br>Problem 2.04                 | Principia Mathematica 2.04<br>[WR27, NSS63, O'R89, SE94]                            | - | 9  | 1.6 | -  | -    |



| Syntactic name<br>V# | Semantic name<br>Other names               | Description<br>References  | V | Cl     | Av         | nH       | Eq     |
|----------------------|--|--|---|--------|------------|----------|--------|
| LCL173<br>-1         | PropEqn2.05<br>Problem 2.05                | Principia Mathematica 2.05<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL174<br>-1         | PropEqn2.06<br>Problem 2.06                | Principia Mathematica 2.06<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL175<br>-1         | PropEqn2.07<br>Problem 2.07                | Principia Mathematica 2.07<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL176<br>-1         | PropEqn2.1<br>Problem 2.1, Problem 2.08    | Principia Mathematica 2.1 and 2.08<br>[WR27, NSS63, O'R89, SE94]                 | - | 9      | 1.6        | -        | -      |
| LCL177<br>-1         | PropEqn2.11<br>Problem 2.11                | Principia Mathematica 2.11<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL178<br>-1         | PropEqn2.12<br>Problem 2.12                | Principia Mathematica 2.12<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL179<br>-1         | PropEqn2.13<br>Problem 2.13                | Principia Mathematica 2.13<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL180<br>-1         | PropEqn2.14<br>Problem 2.14                | Principia Mathematica 2.14<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL181<br>-1<br>-2   | PropEqn2.15<br>Problem 2.15<br>Pelletier 4 | Principia Mathematica 2.15<br>[WR27, NSS63, O'R89, SE94]<br>[WR27, SRM73, Pel86] | - | 9<br>4 | 1.6<br>1.5 | -<br>25% | -<br>- |
| LCL182<br>-1         | PropEqn2.16<br>Problem 2.16                | Principia Mathematica 2.16<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL183<br>-1         | PropEqn2.17<br>Problem 2.17                | Principia Mathematica 2.17<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL184<br>-1         | PropEqn2.18<br>Problem 2.18                | Principia Mathematica 2.18<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL185<br>-1         | PropEqn2.2<br>Problem 2.2                  | Principia Mathematica 2.2<br>[WR27, NSS63, O'R89, SE94]                          | - | 9      | 1.6        | -        | -      |
| LCL186<br>-1         | PropEqn2.21<br>Problem 2.21                | Principia Mathematica 2.21<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL187<br>-1         | PropEqn2.24<br>Problem 2.24                | Principia Mathematica 2.24<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL188<br>-1         | PropEqn2.25<br>Problem 2.25                | Principia Mathematica 2.25<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL189<br>-1         | PropEqn2.26<br>Problem 2.26, Problem 2.27  | Principia Mathematica 2.26 and 2.27<br>[WR27, NSS63, O'R89, SE94]                | - | 9      | 1.6        | -        | -      |
| LCL190<br>-1         | PropEqn2.3<br>Problem 2.3                  | Principia Mathematica 2.3<br>[WR27, NSS63, O'R89, SE94]                          | - | 9      | 1.6        | -        | -      |
| LCL191<br>-1         | PropEqn2.31<br>Problem 2.31                | Principia Mathematica 2.31<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL192<br>-1         | PropEqn2.32<br>Problem 2.32, Problem 2.33  | Principia Mathematica 2.32 and 2.33<br>[WR27, NSS63, O'R89, SE94]                | - | 9      | 1.6        | -        | -      |
| LCL193<br>-1         | PropEqn2.36<br>Problem 2.36                | Principia Mathematica 2.36<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL194<br>-1         | PropEqn2.37<br>Problem 2.37                | Principia Mathematica 2.37<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL195<br>-1         | PropEqn2.38<br>Problem 2.38                | Principia Mathematica 2.38<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL196<br>-1         | PropEqn2.4<br>Problem 2.4                  | Principia Mathematica 2.4<br>[WR27, NSS63, O'R89, SE94]                          | - | 9      | 1.6        | -        | -      |
| LCL197<br>-1         | PropEqn2.41<br>Problem 2.41                | Principia Mathematica 2.41<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL198<br>-1         | PropEqn2.42<br>Problem 2.42, Problem 2.43  | Principia Mathematica 2.42 and 2.43<br>[WR27, NSS63, O'R89, SE94]                | - | 9      | 1.6        | -        | -      |
| LCL199<br>-1         | PropEqn2.45<br>Problem 2.45                | Principia Mathematica 2.45<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL200<br>-1         | PropEqn2.46<br>Problem 2.46                | Principia Mathematica 2.46<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL201<br>-1         | PropEqn2.47<br>Problem 2.47                | Principia Mathematica 2.47<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL202<br>-1         | PropEqn2.48<br>Problem 2.48                | Principia Mathematica 2.48<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL203<br>-1         | PropEqn2.49<br>Problem 2.49                | Principia Mathematica 2.49<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL204<br>-1         | PropEqn2.5<br>Problem 2.5                  | Principia Mathematica 2.5<br>[WR27, NSS63, O'R89, SE94]                          | - | 9      | 1.6        | -        | -      |
| LCL205<br>-1         | PropEqn2.51<br>Problem 2.51                | Principia Mathematica 2.51<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL206<br>-1         | PropEqn2.52<br>Problem 2.52                | Principia Mathematica 2.52<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL207<br>-1         | PropEqn2.521<br>Problem 2.521              | Principia Mathematica 2.521<br>[WR27, NSS63, O'R89, SE94]                        | - | 9      | 1.6        | -        | -      |
| LCL208<br>-1         | PropEqn2.53<br>Problem 2.53                | Principia Mathematica 2.53<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL209<br>-1         | PropEqn2.54<br>Problem 2.54                | Principia Mathematica 2.54<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL210<br>-1         | PropEqn2.55<br>Problem 2.55                | Principia Mathematica 2.55<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL211<br>-1         | PropEqn2.56<br>Problem 2.56                | Principia Mathematica 2.56<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL212<br>-1         | PropEqn2.6<br>Problem 2.6                  | Principia Mathematica 2.6<br>[WR27, NSS63, O'R89, SE94]                          | - | 9      | 1.6        | -        | -      |
| LCL213<br>-1         | PropEqn2.61<br>Problem 2.61                | Principia Mathematica 2.61<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |
| LCL214<br>-1         | PropEqn2.61<br>Problem 2.61                | Principia Mathematica 2.61<br>[WR27, NSS63, O'R89, SE94]                         | - | 9      | 1.6        | -        | -      |

| Syntactic name<br>V# | Semantic name<br>Other names               | Description<br>References  | V      | Cl     | Av         | nH       | Eq     |
|----------------------|--|--|--------|--------|------------|----------|--------|
| LCL215<br>-1         | PropEqn2.62<br>Problem 2.62, Problem 2.63  | Principia Mathematica 2.62 and 2.63<br>[WR27, NSS63, O'R89, SE94]                | -      | 9      | 1.6        | -        | -      |
| LCL216<br>-1         | PropEqn2.64<br>Problem 2.64                | Principia Mathematica 2.64<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL217<br>-1         | PropEqn2.65<br>Problem 2.65                | Principia Mathematica 2.65<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL218<br>-1         | PropEqn2.67<br>Problem 2.67                | Principia Mathematica 2.67<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL219<br>-1         | PropEqn2.68<br>Problem 2.68                | Principia Mathematica 2.68<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL220<br>-1         | PropEqn2.69<br>Problem 2.69                | Principia Mathematica 2.69<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL221<br>-1         | PropEqn2.73<br>Problem 2.73                | Principia Mathematica 2.73<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL222<br>-1         | PropEqn2.74<br>Problem 2.74                | Principia Mathematica 2.74<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL223<br>-1         | PropEqn2.75<br>Problem 2.75                | Principia Mathematica 2.75<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL224<br>-1         | PropEqn2.76<br>Problem 2.76                | Principia Mathematica 2.76<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL225<br>-1         | PropEqn2.77<br>Problem 2.77                | Principia Mathematica 2.77<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL226<br>-1         | PropEqn2.8<br>Problem 2.8                  | Principia Mathematica 2.8<br>[WR27, NSS63, O'R89, SE94]                          | -      | 9      | 1.6        | -        | -      |
| LCL227<br>-1         | PropEqn2.81<br>Problem 2.81                | Principia Mathematica 2.81<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL228<br>-1         | PropEqn2.82<br>Problem 2.82                | Principia Mathematica 2.82<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL229<br>-1         | PropEqn2.83<br>Problem 2.83                | Principia Mathematica 2.83<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL230<br>-1<br>-2   | PropEqn2.85<br>Problem 2.85<br>Pelletier 5 | Principia Mathematica 2.85<br>[WR27, NSS63, O'R89, SE94]<br>[WR27, SRM73, Pel86] | -<br>- | 9<br>4 | 1.6<br>1.5 | -<br>25% | -<br>- |
| LCL231<br>-1         | PropEqn2.86<br>Problem 2.86                | Principia Mathematica 2.86<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL232<br>-1         | PropEqn3.1<br>Problem 3.1                  | Principia Mathematica 3.1<br>[WR27, NSS63, O'R89, SE94]                          | -      | 9      | 1.6        | -        | -      |
| LCL233<br>-1         | PropEqn3.11<br>Problem 3.11                | Principia Mathematica 3.11<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL234<br>-1         | PropEqn3.2<br>Problem 3.2, Problem 3.12    | Principia Mathematica 3.2 and 3.12<br>[WR27, NSS63, O'R89, SE94]                 | -      | 9      | 1.6        | -        | -      |
| LCL235<br>-1         | PropEqn3.13<br>Problem 3.13                | Principia Mathematica 3.13<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL236<br>-1         | PropEqn3.14<br>Problem 3.14                | Principia Mathematica 3.14<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL237<br>-1         | PropEqn3.21<br>Problem 3.21                | Principia Mathematica 3.21<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL238<br>-1         | PropEqn3.22<br>Problem 3.22                | Principia Mathematica 3.22<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL239<br>-1         | PropEqn3.24<br>Problem 3.24                | Principia Mathematica 3.24<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL240<br>-1         | PropEqn3.26<br>Problem 3.26                | Principia Mathematica 3.26<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL241<br>-1         | PropEqn3.27<br>Problem 3.27                | Principia Mathematica 3.27<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL242<br>-1         | PropEqn3.3<br>Problem 3.3                  | Principia Mathematica 3.3<br>[WR27, NSS63, O'R89, SE94]                          | -      | 9      | 1.6        | -        | -      |
| LCL243<br>-1         | PropEqn3.31<br>Problem 3.31                | Principia Mathematica 3.31<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL244<br>-1         | PropEqn3.33<br>Problem 3.33                | Principia Mathematica 3.33<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL245<br>-1         | PropEqn3.34<br>Problem 3.34                | Principia Mathematica 3.34<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL246<br>-1         | PropEqn3.35<br>Problem 3.35                | Principia Mathematica 3.35<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL247<br>-1         | PropEqn3.37<br>Problem 3.37                | Principia Mathematica 3.37<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL248<br>-1         | PropEqn3.4<br>Problem 3.4                  | Principia Mathematica 3.4<br>[WR27, NSS63, O'R89, SE94]                          | -      | 9      | 1.6        | -        | -      |
| LCL249<br>-1         | PropEqn3.41<br>Problem 3.41                | Principia Mathematica 3.41<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL250<br>-1         | PropEqn3.42<br>Problem 3.42                | Principia Mathematica 3.42<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL251<br>-1         | PropEqn3.43<br>Problem 3.43                | Principia Mathematica 3.43<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL252<br>-1         | PropEqn3.44<br>Problem 3.44                | Principia Mathematica 3.44<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL253<br>-1         | PropEqn3.45<br>Problem 3.45                | Principia Mathematica 3.45<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL254<br>-1         | PropEqn3.47<br>Problem 3.47                | Principia Mathematica 3.47<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL255<br>-1         | PropEqn3.48<br>Problem 3.48                | Principia Mathematica 3.48<br>[WR27, NSS63, O'R89, SE94]                         | -      | 9      | 1.6        | -        | -      |
| LCL256<br>-1         | Lk_NotNotImplies                           | A formula that can be derived from the Lukasiewicz system<br>[MW92]              | -      | 5      | 1.4        | -        | -      |

| Syntactic name<br>V#                           | Semantic name<br>Other names           | Description<br>References   | V           | Cl             | Av                | nH            | Eq                 |
|--|--|---|-------------|----------------|-------------------|---------------|--------------------|
| Domain LDA (14 abstract problems, 23 problems) |  |   |             |                |                   |               |                    |
| LDA001<br>-1                                   | LDAAlgEqn1<br>Problem 1                | Verify $3*2*U = UUU$ , where $U = 2*2$<br>[Jec93a]  | -           | 10             | 1.5               | -             | 100%               |
| LDA002<br>-1                                   | LDAAlgEqn2<br>Problem 2                | Verify $3*2(U2)(UU(UU)) = U1(U3)(UU(UU))$<br>[Jec93a]                                       | -           | 17             | 1.3               | -             | 100%               |
| LDA003<br>-1                                   | LeftSegEqn1<br>Problem 3               | Show that 3 is a left segment of $U = 2*2$<br>[Jec93a]                                      | -           | 14             | 1.8               | -             | 64%                |
| LDA004<br>-1                                   | LeftSegEqn2<br>Problem 4               | Show that $3*2(U2)$ is a left segment of $U1(U3)$<br>[Jec93a]                               | -           | 19             | 1.6               | -             | 70%                |
| LDA005<br>-1<br>-2                             | EmbdgAlgEqn1<br>Problem 5              | Let $g = cr(t)$ . Show that $tt(tsg) < t(tsg)$ (for any $s$ )<br>[Jec93a]<br>[Jec93a]       | -<br>-      | 25<br>25       | 1.7<br>1.6        | 8%<br>8%      | 61%<br>70%         |
| LDA006<br>-1<br>-2                             | EmbdgAlgEqn2<br>Problem 6              | Let $g = cr(t)$ . Show that $tsg$ is not in the range of $t$<br>[Jec93a]<br>[Jec93a]        | -<br>-      | 25<br>25       | 1.7<br>1.6        | 8%<br>8%      | 64%<br>72%         |
| LDA007<br>-1<br>-2<br>-3                       | EmbdgAlgEqn3<br>Problem 7<br>Problem 8 | Let $g = cr(t)$ . Show that $t(tsg) = tt(ts)(tg)$<br>[Jec93a]<br>[Jec93a]<br>[Jec93a]       | -<br>-<br>- | 27<br>27<br>12 | 1.6<br>1.6<br>1.4 | 7%<br>7%<br>- | 65%<br>73%<br>100% |
| LDA008<br>-1<br>-2                             | EmbdgAlgEqn4<br>Problem 9              | Let $g = cr(t) = cr(T)$ . If $Ta < Tsg$ , then $ta < tsg$<br>[Jec93a]<br>[Jec93a]           | -<br>-      | 26<br>27       | 1.7<br>1.6        | 7%<br>7%      | 60%<br>63%         |
| LDA009<br>-1<br>-2                             | EmbdgAlgEqn5<br>Problem 10             | Let $g = cr(t)$ . If $g < sg$ , then $st(ts)g < stt(sg)$<br>[Jec93a]<br>[Jec93a]            | -<br>-      | 28<br>28       | 1.6<br>1.5        | 7%<br>7%      | 62%<br>69%         |
| LDA010<br>-1<br>-2                             | EmbdgAlgEqn6<br>Problem 11             | Let $g = cr(t)$ . Show that $stts(sttt)(stts)g < stt(sg)$<br>[Jec93a]<br>[Jec93a]           | -<br>-      | 28<br>28       | 1.6<br>1.5        | 7%<br>7%      | 62%<br>69%         |
| LDA011<br>-1<br>-2                             | EmbdgAlgEqn7<br>Problem 12             | Let $g = cr(t)$ . Show that $stts(sttt)(stts)stts(sttt)g < stt(sg)$<br>[Jec93a]<br>[Jec93a] | -<br>-      | 28<br>28       | 1.6<br>1.5        | 7%<br>7%      | 62%<br>69%         |
| LDA012<br>-1<br>-2                             | EmbdgAlgEqn8<br>Problem 13             | Let $g = cr(t)$ . Show that $stts(sttt)g = g$<br>[Jec93a]<br>[Jec93a]                       | -<br>-      | 28<br>28       | 1.6<br>1.5        | 7%<br>7%      | 64%<br>72%         |
| LDA013<br>-1                                   | EmbdgAlgEqn9Base<br>Conjecture 1       | Let $g = cr(t)$ . Show that $aag \leq ag, t=a$<br>[Jec93a]                                  | -           | 21             | 1.8               | 9%            | 57%                |
| LDA014<br>-1                                   | EmbdgAlgEqn9Indn<br>Conjecture 1       | Let $g = cr(t)$ . Show that $aag \leq ag, t=a$<br>[Jec93a]                                  | -           | 33             | 1.5               | 6%            | 64%                |

### Domain MSC (9 abstract problems, 12 problems)

|                            |  |  |        |          |            |            |          |
|----------------------------|--|--|--------|----------|------------|------------|----------|
| MSC001<br>-1               | BHand1<br>APABHP, APABHP   | A Blind Hand Problem<br>[Pop70, MRS72, WM76]                           | -      | 18       | 2.0        | 5%         | -        |
| MSC002<br>-1<br>-2         | BHand2<br>DBABHP, DBABHP   | A Blind Hand Problem<br>[Pop70, MRS72, WM76]<br>[Pop70, MRS72]         | -<br>- | 14<br>10 | 2.1<br>2.0 | 7%<br>10%  | -<br>-   |
| MSC003<br>-1               | HasParts1<br>HASPARTS-T1, HASPARTS-T1  | Show that the boy, John, has 2 hands<br>[RRY+72, WM76]                 | -      | 8        | 2.0        | 12%        | -        |
| MSC004<br>-1               | HasParts2<br>HASPARTS-T2, HASPARTS-T2  | Show that the boy, John, has 10 fingers<br>[RRY+72, WM76]              | -      | 8        | 2.0        | 12%        | -        |
| MSC005<br>-1               | XOR<br>Problem 5.1   | The evaluation of XOR expressions<br>[Pla82]                           | -      | 7        | 2.1        | -          | -        |
| MSC006<br>-1               | NonObv<br>nonob.lop  | A "non-obvious" problem<br>[PR86]                                      | -      | 6        | 2.0        | 16%        | -        |
| MSC007<br>-1.005<br>-2.002 | Pigeon<br>Pelletier 72 (Size 4), pigeon.in (Size 4)<br>Pelletier 73 (Size 4) | Cook pigeon-hole problem<br>[CR79, Pel86]<br>[CR79, Pel86, Pel88]      | -<br>- | 45<br>16 | 2.2<br>2.3 | 11%<br>-   | -<br>41% |
| MSC008<br>-1.002<br>-2.002 | LatSq<br>LATINSQ   | The (in)constructability of Graeco-Latin Squares<br>[Rob63]<br>[Rob63] | -<br>- | 17<br>16 | 2.6<br>2.5 | 35%<br>43% | -<br>-   |
| MSC009<br>-1               | FamilyTBox<br>KL-ONE-example   | Definitions of a family structure<br>[FLTZ93]                          | -      | 28       | 2.5        | 14%        | -        |

### Domain NUM (285 abstract problems, 309 problems)

|              |   |  |   |     |     |     |     |
|--------------|---|--|---|-----|-----|-----|-----|
| NUM001<br>-1 | SumAssc<br>Chang-Lee-10a, ls28, ls28              | $(A + B) + C = A + (B + C)$<br>[Cha70, LS74, WM76] | - | 13  | 1.8 | -   | -   |
| NUM002<br>-1 | SumDiff1<br>Chang-Lee-10b, ls29, Problem 29, ls29 | $(X - Y) + Z = X + (Z - Y)$<br>[Cha70, LS74, WM76] | - | 13  | 1.8 | -   | -   |
| NUM003<br>-1 | SumDiff2<br>Chang-Lee-10c                         | $A + (B - C) = (A - C) + B$<br>[Cha70, LS74]       | - | 13  | 1.8 | -   | -   |
| NUM004<br>-1 | SumDiff3<br>Chang-Lee-10d, Problem 29             | $(A + B) - C = A + (B - C)$<br>[Cha70, LS74]       | - | 13  | 1.8 | -   | -   |
| NUM005<br>-1 | GCD<br>gcd, GCD                                   | Greatest Common Divisor<br>[Wan85, WB87]           | - | 40  | 2.2 | 5%  | 36% |
| NUM006<br>-1 | Goldbach<br>Problem 246-248                       | Goldbach conjecture<br>[BLM+86]                    | - | 408 | 2.6 | 14% | 39% |
| NUM007<br>-1 | LCM<br>lcm, LCM                                   | Least Common Multiple<br>[Wan85, WB87]             | - | 46  | 2.4 | 8%  | 33% |
| NUM008<br>-1 | Peano1<br>Problem 232                             | Peano axiom 0<br>[BLM+86]                          | - | 406 | 2.6 | 14% | 39% |
| NUM009<br>-1 | Peano2<br>Problem 233                             | Peano axiom 1<br>[BLM+86]                          | - | 406 | 2.6 | 14% | 39% |

| Syntactic name<br>V# | Semantic name<br>Other names  | Description  | References   | V      | Cl       | Av         | nH         | Eq       |
|----------------------|---|--|--|--------|----------|------------|------------|----------|
| NUM010<br>-1         | Peano3<br>Problem 234-235   | Peano axiom 2                                      | [BLM+ 86]  | -      | 407      | 2.6        | 14%        | 39%      |
| NUM011<br>-1         | Peano4<br>Problem 236-237   | Peano axiom 3                                      | [BLM+ 86]  | -      | 407      | 2.6        | 14%        | 39%      |
| NUM012<br>-1         | Peano5<br>Problem 238-241   | Peano axiom 4                                      | [BLM+ 86]  | -      | 409      | 2.6        | 14%        | 39%      |
| NUM013<br>-1         | Peano6<br>Problem 242-244   | Peano axiom 5                                      | [BLM+ 86]  | -      | 408      | 2.6        | 14%        | 39%      |
| NUM014<br>-1         | ValIsPrm<br>Example 6, Chang-Lee-7, NUM1, Example 2                       | If a is a prime and $a = b^2/c^2$ then a divides b | [Luc68, Cha70, RRY+ 72, LS74, FLSY74]              | -      | 7        | 1.9        | 14%        | -        |
| NUM015<br>-1         | PrmDivEx<br>Example 2, Example 3, Example 7,<br>Chang-Lee-8, PRIM         | Any number greater than 1 has a prime divisor      | [Luc68, Lov69, Cha70]<br>[RRY+ 72, CL73, FLSY74]   | -      | 9        | 2.1        | 33%        | -        |
| NUM016<br>-1<br>-2   | InfPrmEx<br>Example 8b, ls17, Problem 17, ls17<br>Example 8a, Chang-Lee-9 | There exist infinitely many primes                 | [Luc68, Cha70, LS74, WM76]<br>[Luc68, Cha70, CL73] | -<br>- | 12<br>8  | 1.8<br>1.9 | 25%<br>37% | -<br>-   |
| NUM017<br>-1<br>-2   | SqRtPrmIrr<br>Problem 26, wos26   | Square root of this prime is irrational            | [Rob63, Wosb, LS74, WM76]<br>[Rob63]               | -<br>- | 24<br>28 | 2.4<br>2.4 | -<br>-     | -<br>33% |
| NUM018<br>-1         | Inf2PrmEx<br>Problem 245  | There is an infinite number of twin prime numbers  | [BLM+ 86]  | -      | 406      | 2.6        | 14%        | 39%      |
| NUM019<br>-1         | EqSymm<br>ls41, Problem 41, ls41  | Symmetry of equality can be derived                | [LS74, WM76]                                       | -      | 11       | 1.4        | -          | -        |
| NUM020<br>-1         | SuccX<br>ls55, ls55   | $a + 1 = \text{successor}(a)$                      | [LS74, WM76]                                       | -      | 12       | 1.4        | -          | -        |
| NUM021<br>-1         | NotDiv<br>ls65, ls65  | If $a \leq b < c$ , then c cannot divide a         | [LS74, WM76]                                       | -      | 19       | 1.7        | 5%         | -        |
| NUM022<br>-1         | LtDiv<br>ls651  | Numerator divisible by smaller denominators        | [LS74, WM76]                                       | -      | 10       | 2.0        | 10%        | -        |
| NUM023<br>-1         | OLtX<br>ls68, ls68  | Zero is less than all successor numbers            | [LS74, WM76]                                       | -      | 15       | 1.6        | -          | -        |
| NUM024<br>-1         | XNNotLtX<br>ls75, ls75  | No number is less than itself                      | [LS74, WM76]                                       | -      | 16       | 1.6        | -          | -        |
| NUM025<br>-1<br>-2   | LtASym<br>ls76t1, ls76t1<br>Problem 76t1                                  | If $a < b$ then not $b < a$                        | [LS74, WM76]<br>[LS74]                             | -<br>- | 16<br>16 | 1.6<br>1.6 | -<br>12%   | -<br>-   |
| NUM026<br>-1         | LtMult<br>ls76t2, ls76t2  | Less preserved over multiplication by a number     | [LS74, WM76]                                       | -      | 17       | 1.5        | -          | -        |
| NUM027<br>-1         | Eqn1<br>ls87, ls87  | If $a > b$ and $b + c \leq a * c$ , then $c = 0$   | [LS74, WM76]                                       | -      | 21       | 1.7        | 9%         | -        |
| NUM028<br>-1         | SymnEqn1<br>SY1   | Symmetrization property 1                          | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM029<br>-1         | SymnEqn2<br>SY2   | Symmetrization property 2                          | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM030<br>-1         | SymnEqn3<br>SY3   | Symmetrization property 3                          | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM031<br>-1         | SymnEqn4<br>SY4   | Symmetrization property 4                          | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM032<br>-1         | SymnEqn5<br>SY5   | Symmetrization property 5                          | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM033<br>-1         | SymnEqn6<br>SY6   | Symmetrization property 6                          | [Qua92a]   | -      | 267      | 2.1        | 4%         | 44%      |
| NUM034<br>-1         | SymnIdem<br>SY7   | Symmetrization is idempotent                       | [Qua92a]   | -      | 265      | 2.1        | 4%         | 44%      |
| NUM035<br>-1         | DomEqRngSymn<br>SY8   | Domain equals range of symmetrization              | [Qua92a]   | -      | 265      | 2.1        | 4%         | 44%      |
| NUM036<br>-1         | SymnEqn7<br>SY9   | Symmetrization property 7                          | [Qua92a]   | -      | 265      | 2.1        | 4%         | 44%      |
| NUM037<br>-1         | SymnEqn8<br>SY10.1  | Symmetrization property 8                          | [Qua92a]   | -      | 265      | 2.1        | 4%         | 44%      |
| NUM038<br>-1         | SymnEqn9<br>SY10.2  | Symmetrization property 9                          | [Qua92a]   | -      | 265      | 2.1        | 4%         | 44%      |
| NUM039<br>-1         | IrreflClEqn1<br>IR1   | Irreflexive class property 1                       | [Qua92a]   | -      | 267      | 2.1        | 4%         | 44%      |
| NUM040<br>-1         | IrreflClEqn2<br>IR2   | Irreflexive class property 2                       | [Qua92a]   | -      | 267      | 2.1        | 4%         | 44%      |
| NUM041<br>-1         | IrreflClEqn3<br>IR3.1   | Irreflexive class property 3                       | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM042<br>-1         | IrreflClEqn4<br>IR3.2   | Irreflexive class property 4                       | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM043<br>-1         | IrreflClEqn5<br>IR4   | Irreflexive class property 5                       | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM044<br>-1         | IrreflClEqn6<br>IR5   | Irreflexive class property 6                       | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM045<br>-1         | IrreflClEqn7<br>IR6   | Irreflexive class property 7                       | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM046<br>-1         | ConnClEqn1<br>CR1   | Connected class property 1                         | [Qua92a]   | -      | 269      | 2.1        | 4%         | 44%      |
| NUM047<br>-1         | ConnClEqn2<br>CR2   | Connected class property 2                         | [Qua92a]   | -      | 267      | 2.1        | 4%         | 44%      |
| NUM048<br>-1         | ConnClEqn3<br>CR3   | Connected class property 3                         | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |
| NUM049<br>-1         | ConnClEqn4<br>CR4   | Connected class property 4                         | [Qua92a]   | -      | 266      | 2.1        | 4%         | 44%      |

| Syntactic name<br>V# | Semantic name<br>Other names        | Description<br>References   | V | Cl  | Av  | nH | Eq  |
|----------------------|-------------------------------------|---|---|-----|-----|----|-----|
| NUM050               | -1<br>ConnClEqn5<br>CR5             | [Qua92a]<br>Connected class property 5                            | - | 266 | 2.1 | 4% | 44% |
| NUM051               | -1<br>ConnNullCl<br>CR6             | [Qua92a]<br>Everything is connected to the null class             | - | 265 | 2.1 | 4% | 44% |
| NUM052               | -1<br>TransOrdEqn1<br>TO1           | [Qua92a]<br>Transitive ordering property 1                        | - | 270 | 2.1 | 4% | 44% |
| NUM053               | -1<br>TransOrdEqn2<br>TO2           | [Qua92a]<br>Transitive ordering property 2                        | - | 267 | 2.1 | 4% | 44% |
| NUM054               | -1<br>ASymClEqn1<br>AS1             | [Qua92a]<br>Asymmetric class property 1                           | - | 268 | 2.1 | 4% | 44% |
| NUM055               | -1<br>ASymClEqn2<br>AS2             | [Qua92a]<br>Asymmetric class property 2                           | - | 267 | 2.1 | 4% | 44% |
| NUM056               | -1<br>ASymClEqn3<br>AS3             | [Qua92a]<br>Asymmetric class property 3                           | - | 266 | 2.1 | 4% | 44% |
| NUM057               | -1<br>SegsEqn1<br>SG1               | [Qua92a]<br>Segments property 1                                   | - | 265 | 2.1 | 4% | 44% |
| NUM058               | -1<br>SegsEqn2<br>SG2               | [Qua92a]<br>Segments property 2                                   | - | 266 | 2.1 | 4% | 44% |
| NUM059               | -1<br>SegsEqn3<br>SG3               | [Qua92a]<br>Segments property 3                                   | - | 266 | 2.1 | 4% | 44% |
| NUM060               | -1<br>SegsEqn4<br>SG4.1             | [Qua92a]<br>Segments property 4                                   | - | 266 | 2.1 | 4% | 44% |
| NUM061               | -1<br>SegsEqn5<br>SG4.2             | [Qua92a]<br>Segments property 5                                   | - | 268 | 2.1 | 4% | 44% |
| NUM062               | -1<br>SegsEqn6<br>SG5               | [Qua92a]<br>Segments property 6                                   | - | 266 | 2.1 | 4% | 44% |
| NUM063               | -1<br>SegsEqn7<br>SG6               | [Qua92a]<br>Segments property 7                                   | - | 266 | 2.1 | 4% | 44% |
| NUM064               | -1<br>LeastUnq<br>WE1               | [Qua92a]<br>Least(xr,u) is unique                                 | - | 269 | 2.1 | 4% | 44% |
| NUM065               | -1<br>WellOrdEqn1<br>WE2.1          | [Qua92a]<br>Well ordering property 1                              | - | 269 | 2.1 | 4% | 44% |
| NUM066               | -1<br>WellOrdEqn1Cor<br>WE2.2 cor   | [Qua92a]<br>Corollary to well ordering property 1                 | - | 268 | 2.1 | 4% | 44% |
| NUM067               | -1<br>WellOrdEqn2<br>WE3.1          | [Qua92a]<br>Well ordering property 2                              | - | 268 | 2.1 | 4% | 44% |
| NUM068               | -1<br>WellOrdEqn3<br>WE3.2          | [Qua92a]<br>Well ordering property 3                              | - | 268 | 2.1 | 4% | 44% |
| NUM069               | -1<br>WellOrdEqn3Cor<br>WE3 cor.    | [Qua92a]<br>Corollary to well ordering property 3                 | - | 268 | 2.1 | 4% | 44% |
| NUM070               | -1<br>WellOrdASym<br>WE4.1          | [Qua92a]<br>A well-order is asymmetric                            | - | 266 | 2.1 | 4% | 44% |
| NUM071               | -1<br>WellOrdIrrefl<br>WE4.2        | [Qua92a]<br>Well ordering is irreflexive                          | - | 267 | 2.1 | 4% | 44% |
| NUM072               | -1<br>WellOrdEqn4<br>WE5            | [Qua92a]<br>Well ordering property 4                              | - | 270 | 2.1 | 4% | 44% |
| NUM073               | -1<br>WellOrdEqn4Cor<br>WE5 cor.    | [Qua92a]<br>Corollary to well ordering property 4                 | - | 270 | 2.1 | 4% | 44% |
| NUM074               | -1<br>WellOrdEqn5<br>WE6            | [Qua92a]<br>Well ordering property 5                              | - | 266 | 2.1 | 4% | 44% |
| NUM075               | -1<br>WellOrdEqn6<br>WE7            | [Qua92a]<br>Well ordering property 6                              | - | 267 | 2.1 | 4% | 44% |
| NUM076               | -1<br>WellOrdEqn7<br>WE8            | [Qua92a]<br>Well ordering property 7                              | - | 267 | 2.1 | 4% | 44% |
| NUM077               | -1<br>WellOrdEqn7Cor1<br>WE8 cor. 1 | [Qua92a]<br>Corollary 1 to well ordering property 7               | - | 267 | 2.1 | 4% | 44% |
| NUM078               | -1<br>WellOrdEqn7Cor2<br>WE8 cor. 2 | [Qua92a]<br>Corollary 2 to well ordering property 7               | - | 267 | 2.1 | 4% | 44% |
| NUM079               | -1<br>WellOrdEqn8<br>WE9.1          | [Qua92a]<br>Well ordering property 8                              | - | 266 | 2.1 | 4% | 44% |
| NUM080               | -1<br>WellOrdEqn9<br>WE9.2          | [Qua92a]<br>Well ordering property 9                              | - | 265 | 2.1 | 4% | 44% |
| NUM081               | -1<br>WellOrdEqn9Cor<br>WE9 cor.    | [Qua92a]<br>Corollary to well ordering property 9                 | - | 266 | 2.1 | 4% | 44% |
| NUM082               | -1<br>LeastUnqInSubS<br>WE10        | [Qua92a]<br>Uniqueness of the least element of a non-empty subset | - | 269 | 2.1 | 4% | 44% |
| NUM083               | -1<br>TransClEqn1<br>TR1            | [Qua92a]<br>Transitive class property 1                           | - | 267 | 2.1 | 4% | 44% |
| NUM084               | -1<br>AltTransClDef1<br>TR2         | [Qua92a]<br>Alternate transitive class definition, part 1         | - | 266 | 2.1 | 4% | 44% |
| NUM085               | -1<br>AltTransClDef2<br>TR3         | [Qua92a]<br>Alternate transitive class definition, part 2         | - | 266 | 2.1 | 4% | 44% |
| NUM086               | -1<br>TransClEqn2<br>TR4            | [Qua92a]<br>Transitive class property 2                           | - | 267 | 2.1 | 4% | 44% |
| NUM087               | -1<br>TransClEqn3<br>TR5            | [Qua92a]<br>Transitive class property 3                           | - | 267 | 2.1 | 4% | 44% |
| NUM088               | -1<br>TransClEqn4<br>TR6            | [Qua92a]<br>Transitive class property 4                           | - | 267 | 2.1 | 4% | 44% |
| NUM089               | -1<br>SectsEqn1<br>SE1              | [Qua92a]<br>Sections property 1                                   | - | 269 | 2.1 | 4% | 44% |
| NUM090               | -1<br>SectsEqn1Cor<br>SE1 cor       | [Qua92a]<br>Corollary to sections property 1                      | - | 268 | 2.1 | 4% | 44% |
| NUM091               | -1<br>SectsEqn2<br>SE2              | [Qua92a]<br>Sections property 2                                   | - | 267 | 2.1 | 4% | 44% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References                  | V   | Cl | Av | nH  | Eq  |    |     |
|----------------------|------------------------------|--|---|----|----|-----|-----|----|-----|
| NUM092               | -1                           | SectsEqn2Cor1<br>SE2 cor. 1 [Qua92a]       | Corollary 1 to sections property 2            |    | -  | 267 | 2.1 | 4% | 44% |
| NUM093               | -1                           | SectsEqn2Cor2<br>SE2 cor. 2 [Qua92a]       | Corollary 2 to sections property 2            |    | -  | 267 | 2.1 | 4% | 44% |
| NUM094               | -1                           | SectsEqn3<br>SE3.1 [Qua92a]                | Sections property 3                           |    | -  | 268 | 2.1 | 4% | 44% |
| NUM095               | -1                           | SectsEqn4<br>SE3.2 [Qua92a]                | Sections property 4                           |    | -  | 268 | 2.1 | 4% | 44% |
| NUM096               | -1                           | SectsEqn5<br>SE4 [Qua92a]                  | Sections property 5                           |    | -  | 268 | 2.1 | 4% | 44% |
| NUM097               | -1                           | SectsEqn5Cor<br>SE4 cor. [Qua92a]          | Corollary to sections property 5              |    | -  | 268 | 2.1 | 4% | 44% |
| NUM098               | -1                           | OrdIEqn1<br>ORD1 [Qua92a]                  | Ordinal property 1                            |    | -  | 265 | 2.1 | 4% | 44% |
| NUM099               | -1                           | OrdIEqn1Cor<br>ORD1 cor [Qua92a]           | Corollary to ordinal property 1               |    | -  | 265 | 2.1 | 4% | 44% |
| NUM100               | -1                           | OrdIEqn2<br>ORD2 [Qua92a]                  | Ordinal property 2                            |    | -  | 265 | 2.1 | 4% | 44% |
| NUM101               | -1                           | OrdIEqn3<br>ORD5.1 [Qua92a]                | Ordinal property 3                            |    | -  | 269 | 2.1 | 4% | 44% |
| NUM102               | -1                           | OrdIEqn4<br>ORD5.2 [Qua92a]                | Ordinal property 4                            |    | -  | 268 | 2.1 | 4% | 44% |
| NUM103               | -1                           | OrdIEqn4Cor<br>ORD5 cor [Qua92a]           | Corollary to ordinal property 4               |    | -  | 268 | 2.1 | 4% | 44% |
| NUM104               | -1                           | OrdIEqn5<br>ORD6 [Qua92a]                  | Ordinal property 5                            |    | -  | 269 | 2.1 | 4% | 44% |
| NUM105               | -1                           | OrdIEqn6<br>ORD7.1 [Qua92a]                | Ordinal property 6                            |    | -  | 266 | 2.1 | 4% | 44% |
| NUM106               | -1                           | OrdIEqn7<br>ORD7.2 [Qua92a]                | Ordinal property 7                            |    | -  | 267 | 2.1 | 4% | 44% |
| NUM107               | -1                           | OrdIEqn8<br>ORD8.1 [Qua92a]                | Ordinal property 8                            |    | -  | 266 | 2.1 | 4% | 44% |
| NUM108               | -1                           | OrdIEqn9<br>ORD8.2 [Qua92a]                | Ordinal property 9                            |    | -  | 269 | 2.1 | 4% | 44% |
| NUM109               | -1                           | OrdIEqn10<br>ORD9 [Qua92a]                 | Ordinal property 10                           |    | -  | 269 | 2.1 | 4% | 44% |
| NUM110               | -1                           | OrdIEqn10Cor<br>ORD9 cor [Qua92a]          | Corollary to ordinal property 10              |    | -  | 265 | 2.1 | 4% | 44% |
| NUM111               | -1                           | OrdIEqn11<br>ORD11 [Qua92a]                | Ordinal property 11                           |    | -  | 267 | 2.1 | 4% | 44% |
| NUM112               | -1                           | OrdIEqn12<br>ORD12 [Qua92a]                | Ordinal property 12                           |    | -  | 265 | 2.1 | 4% | 44% |
| NUM113               | -1                           | OrdIEqn13<br>ORD13 [Qua92a]                | Ordinal property 13                           |    | -  | 269 | 2.1 | 4% | 43% |
| NUM114               | -1                           | OrdIEqn13Cor<br>ORD13 cor. [Qua92a]        | Corollary to ordinal property 13              |    | -  | 266 | 2.1 | 4% | 44% |
| NUM115               | -1                           | OrdCINotSet<br>ORD14 [Qua92a]              | The class of ordinals is not a set.           |    | -  | 265 | 2.1 | 4% | 44% |
| NUM116               | -1                           | OrdCINotSetCor<br>ORD14 cor [Qua92a]       | Corollary to the class of ordinals is not set |    | -  | 265 | 2.1 | 4% | 44% |
| NUM117               | -1                           | OrdCINumCor<br>ORD15 [Qua92a]              | Corollary to ordinal class and numbers        |    | -  | 270 | 2.1 | 4% | 43% |
| NUM118               | -1                           | OrdIEqn14<br>ORD16 [Qua92a]                | Ordinal property 14                           |    | -  | 268 | 2.1 | 4% | 44% |
| NUM119               | -1                           | TransCIEqn4Cor<br>ORD17 [Qua92a]           | Corollary to transitive class property 4      |    | -  | 266 | 2.1 | 4% | 44% |
| NUM120               | -1                           | TrnsfIndn1<br>ORD18.1 [Qua92a]             | Transfinite induction, part 1                 |    | -  | 266 | 2.1 | 4% | 44% |
| NUM121               | -1                           | TrnsfIndn2<br>ORD18.2 [Qua92a]             | Transfinite induction, part 2                 |    | -  | 266 | 2.1 | 4% | 44% |
| NUM122               | -1                           | TrnsfIndn3<br>ORD18.3 [Qua92a]             | Transfinite induction, part 3                 |    | -  | 266 | 2.1 | 4% | 44% |
| NUM123               | -1                           | AltTrnsfIndn3<br>ORD18.4 [Qua92a]          | Alternate transfinite induction 3             |    | -  | 266 | 2.1 | 4% | 44% |
| NUM124               | -1                           | SmTrnsfInd<br>ORD18.5 [Qua92a]             | Condensed statement of transfinite induction  |    | -  | 266 | 2.1 | 4% | 44% |
| NUM125               | -1                           | CmpltIndnOmega<br>ORD18.6 [Qua92a]         | Complete induction upto omega                 |    | -  | 266 | 2.1 | 4% | 44% |
| NUM126               | -1                           | Alt1TrnsfInd1<br>ORD18-5.1 [Qua92a]        | Alternate 1 for transfinite induction, part 1 |    | -  | 266 | 2.1 | 4% | 44% |
| NUM127               | -1                           | Alt1TrnsfInd2<br>ORD18-5.2 [Qua92a]        | Alternate 1 for transfinite induction, part 2 |    | -  | 266 | 2.1 | 4% | 44% |
| NUM128               | -1                           | Alt1TrnsfInd3<br>ORD18-5.3 [Qua92a]        | Alternate 1 for transfinite induction, part 3 |    | -  | 266 | 2.1 | 4% | 44% |
| NUM129               | -1                           | Alt2TrnsfInd1<br>ORD18-6.1 [Qua92a]        | Alternate 2 for transfinite induction, part 1 |    | -  | 267 | 2.1 | 4% | 44% |
| NUM130               | -1                           | Alt2TrnsfInd2<br>ORD18-6.2 [Qua92a]        | Alternate 2 for transfinite induction, part 2 |    | -  | 267 | 2.1 | 4% | 44% |
| NUM131               | -1                           | Alt2TrnsfInd3<br>ORD18-6.3 [Qua92a]        | Alternate 2 for transfinite induction, part 3 |    | -  | 267 | 2.1 | 4% | 44% |
| NUM132               | -1                           | UnionSuccRelOrd1<br>ORD20 [Qua92a]         | Union of successor relation ordinal           |    | -  | 266 | 2.1 | 4% | 44% |
| NUM133               | -1                           | UnionSuccRelOrd1Cor<br>ORD20 cor. [Qua92a] | Corollary to union of successor ordinal       |    | -  | 268 | 2.1 | 4% | 44% |

| Syntactic name<br>V# | Semantic name<br>Other names               | Description<br>References                                  | V | Cl  | Av  | nH | Eq  |
|----------------------|--|--|---|-----|-----|----|-----|
| NUM134               | -1<br>SuccRelOrd1<br>ORD21 [Qua92a]        | Successor relation of an ordinal is an ordinal             | - | 266 | 2.1 | 4% | 44% |
| NUM135               | -1<br>NullClsmOrd1<br>ORD22 [Qua92a]       | The null class is the smallest ordinal                     | - | 265 | 2.1 | 4% | 44% |
| NUM136               | -1<br>Ord1Trans<br>ORD23 [Qua92a]          | Transitivity of ordinals                                   | - | 268 | 2.1 | 4% | 44% |
| NUM137               | -1<br>Cond1CmpltIndn<br>ORD24.1 [Qua92a]   | Condition 1 for complete induction                         | - | 268 | 2.1 | 4% | 44% |
| NUM138               | -1<br>Cond2CmpltIndn<br>ORD24.2 [Qua92a]   | Condition 2 for complete induction                         | - | 266 | 2.1 | 4% | 44% |
| NUM139               | -1<br>Cond3CmpltIndn<br>ORD24.3 [Qua92a]   | Condition 3 for complete induction                         | - | 266 | 2.1 | 4% | 44% |
| NUM140               | -1<br>SuccSet1<br>SUC1.1 [Qua92a]          | The successor of a set is a set, part 1                    | - | 266 | 2.1 | 4% | 44% |
| NUM141               | -1<br>SuccSet2<br>SUC1.2 [Qua92a]          | The successor of a set is a set, part 2                    | - | 266 | 2.1 | 4% | 44% |
| NUM142               | -1<br>SuccSet3<br>SUC1.3 [Qua92a]          | The successor of a set is a set, part 3                    | - | 265 | 2.1 | 4% | 44% |
| NUM143               | -1<br>SuccSetCor<br>SUC1 cor. [Qua92a]     | Corollary to the successor of a set being a set            | - | 265 | 2.1 | 4% | 44% |
| NUM144               | -1<br>SuccPprCl<br>SUC2 [Qua92a]           | The successor of a proper class is a class                 | - | 266 | 2.1 | 4% | 44% |
| NUM145               | -1<br>SuccPprClCor<br>SUC2 cor. [Qua92a]   | Corollary to the successor of a proper class being a class | - | 266 | 2.1 | 4% | 44% |
| NUM146               | -1<br>SuccTransSet<br>SUC3 [Qua92a]        | The successor of a transitive set is transitive            | - | 266 | 2.1 | 4% | 44% |
| NUM147               | -1<br>SuccOrd1<br>SUC4 [Qua92a]            | The successor of an ordinal is an ordinal                  | - | 266 | 2.1 | 4% | 44% |
| NUM148               | -1<br>PredOrd1<br>SUC5 [Qua92a]            | The predecessor of an ordinal is an ordinal                | - | 266 | 2.1 | 4% | 44% |
| NUM149               | -1<br>SuccEqn1<br>SUC6 [Qua92a]            | Successor property 1                                       | - | 265 | 2.1 | 4% | 44% |
| NUM150               | -1<br>SuccEqn1Cor1<br>SUC6 cor. 1 [Qua92a] | Corollary 1 to successor property 1                        | - | 265 | 2.1 | 4% | 44% |
| NUM151               | -1<br>SuccEqn1Cor2<br>SUC6 cor. 2 [Qua92a] | Corollary 2 to successor property 1                        | - | 266 | 2.1 | 4% | 44% |
| NUM152               | -1<br>SuccEqn1Cor3<br>SUC6 cor. 3 [Qua92a] | Corollary 3 to successor property 1                        | - | 266 | 2.1 | 4% | 44% |
| NUM153               | -1<br>SuccEqn1Cor4<br>SUC6 cor. 4 [Qua92a] | Corollary 4 to successor property 1                        | - | 266 | 2.1 | 4% | 44% |
| NUM154               | -1<br>SuccEqn1Cor5<br>SUC6 cor. 5 [Qua92a] | Corollary 5 to successor property 1                        | - | 265 | 2.1 | 4% | 44% |
| NUM155               | -1<br>NoOrd1Btwn<br>SUC7 [Qua92a]          | There is no ordinal between $x$ and $x + 1$                | - | 268 | 2.1 | 4% | 44% |
| NUM156               | -1<br>Cond1K1Ord1<br>SUC9.1 [Qua92a]       | Membership condition 1 for kind 1 ordinals                 | - | 265 | 2.1 | 4% | 44% |
| NUM157               | -1<br>Cond2K1Ord1<br>SUC9.2 [Qua92a]       | Membership condition 2 for kind 1 ordinals                 | - | 266 | 2.1 | 4% | 44% |
| NUM158               | -1<br>Cond3K1Ord1<br>SUC9.3 [Qua92a]       | Membership condition 3 for kind 1 ordinals                 | - | 267 | 2.1 | 4% | 44% |
| NUM159               | -1<br>Cond4K1Ord1<br>SUC9.4 [Qua92a]       | Membership condition 4 for kind 1 ordinals                 | - | 265 | 2.1 | 4% | 44% |
| NUM160               | -1<br>K1Ord1Cl<br>SUC10 [Qua92a]           | Kind 1 ordinals is a class of ordinals                     | - | 265 | 2.1 | 4% | 44% |
| NUM161               | -1<br>K1Ord1ClCor<br>SUC10 cor. [Qua92a]   | Corollary to kind 1 ordinals being a class of ordinals     | - | 265 | 2.1 | 4% | 44% |
| NUM162               | -1<br>SuccEqn2<br>SUC11 [Qua92a]           | Successor property 2                                       | - | 265 | 2.1 | 4% | 44% |
| NUM163               | -1<br>IndvClsdUnion<br>SUC12.1 [Qua92a]    | Inductive is closed under union                            | - | 267 | 2.1 | 4% | 44% |
| NUM164               | -1<br>IndvClsdIntsc<br>SUC12.2 [Qua92a]    | Inductive is closed under intersection                     | - | 267 | 2.1 | 4% | 44% |
| NUM165               | -1<br>OmegaDefCor1<br>SUC13.1 [Qua92a]     | Corollary to omega definition, part 1                      | - | 266 | 2.1 | 4% | 44% |
| NUM166               | -1<br>OmegaDefCor2<br>SUC13.2 [Qua92a]     | Corollary to omega definition, part 2                      | - | 265 | 2.1 | 4% | 44% |
| NUM167               | -1<br>SuccEqn3<br>SUC14 [Qua92a]           | Successor property 3                                       | - | 265 | 2.1 | 4% | 44% |
| NUM168               | -1<br>SuccEqn3Cor<br>SUC14 cor. [Qua92a]   | Corollary to successor property 3                          | - | 265 | 2.1 | 4% | 44% |
| NUM169               | -1<br>SuccEqn4<br>SUC15.1 [Qua92a]         | Successor property 4                                       | - | 266 | 2.1 | 4% | 44% |
| NUM170               | -1<br>SuccEqn5<br>SUC15.2 [Qua92a]         | Successor property 5                                       | - | 267 | 2.1 | 4% | 44% |
| NUM171               | -1<br>SuccEqn6<br>SUC15.3 [Qua92a]         | Successor property 6                                       | - | 265 | 2.1 | 4% | 44% |
| NUM172               | -1<br>SuccRelSet<br>SUC16 [Qua92a]         | The successor relation of a set is different from the set  | - | 266 | 2.1 | 4% | 44% |
| NUM173               | -1<br>SuccEqn7<br>SUC17 [Qua92a]           | Successor property 7                                       | - | 266 | 2.1 | 4% | 44% |
| NUM174               | -1<br>SuccEqn8<br>SUC18 [Qua92a]           | Successor property 8                                       | - | 265 | 2.1 | 4% | 44% |
| NUM175               | -1<br>SuccEqn9<br>SUC19 [Qua92a]           | Successor property 9                                       | - | 265 | 2.1 | 4% | 44% |

| Syntactic name<br>V# | Semantic name<br>Other names  | Description<br>References   | V | Cl  | Av  | nH | Eq  |
|----------------------|-------------------------------|---|---|-----|-----|----|-----|
| NUM176<br>-1         | SuccEqn10<br>SUC20            | Successor property 10<br>[Qua92a]   | - | 266 | 2.1 | 4% | 44% |
| NUM177<br>-1         | Cond1IndvCl<br>SUC21.1        | Condition 1 for a class to be inductive<br>[Qua92a]                                 | - | 267 | 2.1 | 4% | 44% |
| NUM178<br>-1         | Cond2IndvCl<br>SUC21.2        | Condition 2 for a class to be inductive<br>[Qua92a]                                 | - | 266 | 2.1 | 4% | 44% |
| NUM179<br>-1         | Cond3IndvCl<br>SUC21.3        | Condition 3 for a class to be inductive<br>[Qua92a]                                 | - | 266 | 2.1 | 4% | 44% |
| NUM180<br>-1         | LmtOrd1<br>LIM2.1             | Limit ordinals are ordinals<br>[Qua92a]   | - | 265 | 2.1 | 4% | 44% |
| NUM181<br>-1         | NullClInNotLmt<br>LIM2.2      | The null class is not a limit ordinal<br>[Qua92a]                                   | - | 265 | 2.1 | 4% | 44% |
| NUM182<br>-1         | LmtOrd1EqSucc<br>LIM2.3       | Only limit ordinals equal their successors<br>[Qua92a]                              | - | 266 | 2.1 | 4% | 44% |
| NUM183<br>-1         | OrdIK1OrLmt<br>LIM2.4         | Ordinals are either kind 1 or limit<br>[Qua92a]                                     | - | 267 | 2.1 | 4% | 44% |
| NUM184<br>-1         | OrdIK1OrLmtCor<br>LIM2.4 cor. | Corollary to ordinals are either kind 1 or limit<br>[Qua92a]                        | - | 265 | 2.1 | 4% | 44% |
| NUM185<br>-1         | LmtOrd1NotMemb<br>LIM3        | Limit ordinals are not members<br>[Qua92a]  | - | 265 | 2.1 | 4% | 44% |
| NUM186<br>-1         | OmegaEqn1<br>OM1              | Omega property 1<br>[Qua92a]  | - | 265 | 2.1 | 4% | 44% |
| NUM187<br>-1         | SuccEqn8Lem<br>OM2            | Lemma for successor property 8<br>[Qua92a]  | - | 267 | 2.1 | 4% | 44% |
| NUM188<br>-1         | OmegaTrans<br>OM3             | Omega is transitive<br>[Qua92a]   | - | 265 | 2.1 | 4% | 44% |
| NUM189<br>-1         | OmegaOrd1<br>OM4              | Omega is an ordinal<br>[Qua92a]   | - | 265 | 2.1 | 4% | 44% |
| NUM190<br>-1         | OmegaNotNullCl<br>OM5         | Omega is not the null class<br>[Qua92a]   | - | 265 | 2.1 | 4% | 44% |
| NUM191<br>-1         | OmegaLmtOrd1<br>OM6           | Omega is a limit ordinal<br>[Qua92a]  | - | 265 | 2.1 | 4% | 44% |
| NUM192<br>-1         | OmegaSmLmtOrd1<br>OM7         | Omega is the smallest limit ordinal<br>[Qua92a]                                     | - | 266 | 2.1 | 4% | 44% |
| NUM193<br>-1         | SumOrdls<br>LUB1              | The sum of ordinals is an ordinal<br>[Qua92a]                                       | - | 265 | 2.1 | 4% | 44% |
| NUM194<br>-1         | UnionClOrdls<br>LUB2          | The union of a class of ordinals is a class of ordinals<br>[Qua92a]                 | - | 266 | 2.1 | 4% | 44% |
| NUM195<br>-1         | UnionClOrdlsTrans<br>LUB3     | The union of a class of ordinals is transitive<br>[Qua92a]                          | - | 266 | 2.1 | 4% | 44% |
| NUM196<br>-1         | UnionSetOrdls<br>LUB4         | The union of a set of ordinals is an ordinal<br>[Qua92a]                            | - | 267 | 2.1 | 4% | 44% |
| NUM197<br>-1         | UnionPprClOrdls<br>LUB4-5     | The union of a proper class of ordinals is the class of ordinals<br>[Qua92a]        | - | 267 | 2.1 | 4% | 44% |
| NUM198<br>-1         | UnionSetOrdlsGt<br>LUB5.1     | The union of a set of ordinals is $\geq$ each ordinal in the set<br>[Qua92a]        | - | 269 | 2.1 | 4% | 44% |
| NUM199<br>-1         | LubEqn1<br>LUB5.2             | Least upper bound property 1<br>[Qua92a]  | - | 267 | 2.1 | 4% | 44% |
| NUM200<br>-1         | LubEqn2<br>LUB6               | If every element of $x$ is $\leq y$ , then $\text{sum class}(x) \leq y$<br>[Qua92a] | - | 267 | 2.1 | 4% | 44% |
| NUM201<br>-1         | LubEqn3<br>LUB7               | Least upper bound property 3<br>[Qua92a]  | - | 268 | 2.1 | 4% | 44% |
| NUM202<br>-1         | LubSuccRel<br>LUB8            | If the lub of a set of ordinals is a successor, it's in the set<br>[Qua92a]         | - | 268 | 2.1 | 4% | 44% |
| NUM203<br>-1         | LubSuccRelCor<br>LUB8 cor.    | Corollary to least upper bound being a successor relation<br>[Qua92a]               | - | 269 | 2.1 | 4% | 44% |
| NUM204<br>-1         | LubEqn5<br>LUB9               | Least upper bound property 5<br>[Qua92a]  | - | 266 | 2.1 | 4% | 44% |
| NUM205<br>-1         | LubEqn5Cor1<br>LUB9 cor. 1    | Corollary 1 to least upper bound property 5<br>[Qua92a]                             | - | 266 | 2.1 | 4% | 44% |
| NUM206<br>-1         | LubEqn5Cor2<br>LUB9 cor. 2    | Corollary 2 to least upper bound property 5<br>[Qua92a]                             | - | 266 | 2.1 | 4% | 44% |
| NUM207<br>-1         | LubEqn6<br>LUB10              | Least upper bound property 6<br>[Qua92a]  | - | 267 | 2.1 | 4% | 44% |
| NUM208<br>-1         | LubEqn7<br>LUB11              | Least upper bound property 7<br>[Qua92a]  | - | 266 | 2.1 | 4% | 44% |
| NUM209<br>-1         | LubEqn7Cor<br>LUB11 cor.      | Corollary to least upper bound property 7<br>[Qua92a]                               | - | 267 | 2.1 | 4% | 44% |
| NUM210<br>-1         | LubEqn8Lem1<br>LUB12.1        | Lemma 1 for least upper bound property 8<br>[Qua92a]                                | - | 267 | 2.1 | 4% | 44% |
| NUM211<br>-1         | LubEqn8Lem2<br>LUB12.2        | Lemma 2 for least upper bound property 8<br>[Qua92a]                                | - | 267 | 2.1 | 4% | 44% |
| NUM212<br>-1         | LubEqn8Lem3<br>LUB12.3        | Lemma 3 for least upper bound property 8<br>[Qua92a]                                | - | 267 | 2.1 | 4% | 44% |
| NUM213<br>-1         | Alt3TrnsfInd<br>LUB13         | Alternate 3 for transfinite induction<br>[Qua92a]                                   | - | 268 | 2.1 | 4% | 44% |
| NUM214<br>-1         | IndnY<br>LUB14                | Induction up to $y$<br>[Qua92a]   | - | 269 | 2.1 | 4% | 44% |
| NUM215<br>-1         | IndnYCor<br>LUB14 cor.        | Corollary to induction upto $y$<br>[Qua92a]   | - | 267 | 2.1 | 4% | 44% |
| NUM216<br>-1         | RestDefCor1<br>TRECDEF1 cor.1 | Corollary 1 to rest definition<br>[Qua92a]  | - | 266 | 2.1 | 4% | 44% |
| NUM217<br>-1         | RestDefCor2<br>TRECDEF1 cor.2 | Corollary 2 to rest definition<br>[Qua92a]  | - | 265 | 2.1 | 4% | 44% |



| Syntactic name<br>V# | Semantic name<br>Other names           | Description<br>References   | V      | Cl         | Av         | nH       | Eq         |
|----------------------|--|---|--------|------------|------------|----------|------------|
| NUM218<br>-1         | RestFunc<br>TREC2                      | Rest of is a function<br>[Qua92a]                                       | -      | 265        | 2.1        | 4%       | 44%        |
| NUM219<br>-1         | DomRestOfEqDom<br>TREC3                | The domain of rest_of(X) is the domain of X<br>[Qua92a]                 | -      | 265        | 2.1        | 4%       | 44%        |
| NUM220<br>-1         | DomRestOfEqDomCor<br>TREC3 cor.        | Corollary to the domain of rest_of(X) being the domain of X<br>[Qua92a] | -      | 265        | 2.1        | 4%       | 44%        |
| NUM221<br>-1         | RestOfEqn1<br>TREC3-5                  | Rest_of property 1<br>[Qua92a]  | -      | 266        | 2.1        | 4%       | 44%        |
| NUM222<br>-1         | RestOfMono<br>TREC3-7                  | Rest_of is monotonic.<br>[Qua92a]                                       | -      | 266        | 2.1        | 4%       | 44%        |
| NUM223<br>-1         | RestRelFunc<br>TREC3-9.1               | Rest relation is a function<br>[Qua92a]                                 | -      | 265        | 2.1        | 4%       | 44%        |
| NUM224<br>-1         | RestRelEqn1<br>TREC3-9.2               | Rest relation property 1<br>[Qua92a]                                    | -      | 265        | 2.1        | 4%       | 44%        |
| NUM225<br>-1         | RestRelEqn2<br>TREC3-9.3               | Rest relation property 2<br>[Qua92a]                                    | -      | 265        | 2.1        | 4%       | 44%        |
| NUM226<br>-1         | RestRelEqn3<br>TREC3-9.4               | Rest relation property 3<br>[Qua92a]                                    | -      | 266        | 2.1        | 4%       | 44%        |
| NUM227<br>-1         | RestRelEqn4<br>TREC3-9.5               | Rest relation property 4<br>[Qua92a]                                    | -      | 265        | 2.1        | 4%       | 44%        |
| NUM228<br>-1         | RecrEqnFuncDefCor<br>TRECDEF4 cor.     | Corollary to recursion equation functions definition<br>[Qua92a]        | -      | 266        | 2.1        | 4%       | 44%        |
| NUM229<br>-1         | TrnsfRecrLem0<br>TREC.LEMMA0           | Transfinite recursion lemma 0<br>[Qua92a]                               | -      | 267        | 2.1        | 4%       | 44%        |
| NUM230<br>-1         | TrnsfRecrLem1<br>TREC.LEMMA1           | Transfinite recursion lemma 1<br>[Qua92a]                               | -      | 269        | 2.1        | 4%       | 44%        |
| NUM231<br>-1         | TrnsfRecrLem2<br>TREC.LEMMA2           | Transfinite recursion lemma 2<br>[Qua92a]                               | -      | 270        | 2.1        | 4%       | 44%        |
| NUM232<br>-1         | TrnsfRecrLem3<br>TREC.LEMMA3           | Transfinite recursion lemma 3<br>[Qua92a]                               | -      | 268        | 2.1        | 4%       | 44%        |
| NUM233<br>-1         | TrnsfRecrLem4<br>TREC.LEMMA4           | Transfinite recursion lemma 4<br>[Qua92a]                               | -      | 269        | 2.1        | 4%       | 44%        |
| NUM234<br>-1         | TrnsfRecrLem5<br>TREC.LEMMA5           | Transfinite recursion lemma 5<br>[Qua92a]                               | -      | 269        | 2.1        | 4%       | 44%        |
| NUM235<br>-1         | TrnsfRecrLem6<br>TREC.LEMMA6           | Transfinite recursion lemma 6<br>[Qua92a]                               | -      | 268        | 2.1        | 4%       | 44%        |
| NUM236<br>-1         | TrnsfRecrLem6Cor1<br>TREC.LEMMA6 cor.1 | Corollary 1 to transfinite recursion lemma 6<br>[Qua92a]                | -      | 267        | 2.1        | 4%       | 44%        |
| NUM237<br>-1         | TrnsfRecrLem6Cor2<br>TREC.LEMMA6 cor.2 | Corollary 2 to transfinite recursion lemma 6<br>[Qua92a]                | -      | 267        | 2.1        | 4%       | 44%        |
| NUM238<br>-1         | TrnsfRecrLem7<br>TREC.LEMMA7           | Transfinite recursion lemma 7<br>[Qua92a]                               | -      | 269        | 2.1        | 4%       | 44%        |
| NUM239<br>-1         | TrnsfRecrLem8<br>TREC.LEMMA8           | Transfinite recursion lemma 8<br>[Qua92a]                               | -      | 268        | 2.1        | 4%       | 44%        |
| NUM240<br>-1         | TrnsfRecrLem9_1<br>TREC.LEMMA9.1       | Transfinite recursion lemma 9.1<br>[Qua92a]                             | -      | 266        | 2.1        | 4%       | 44%        |
| NUM241<br>-1         | TrnsfRecrLem9_2<br>TREC.LEMMA9.2       | Transfinite recursion lemma 9.2<br>[Qua92a]                             | -      | 265        | 2.1        | 4%       | 44%        |
| NUM242<br>-1         | TrnsfRecrLem9_3<br>TREC.LEMMA9.3       | Transfinite recursion lemma 9.3<br>[Qua92a]                             | -      | 270        | 2.1        | 4%       | 44%        |
| NUM243<br>-1         | TrnsfRecrLem10<br>TREC.LEMMA10         | Transfinite recursion lemma 10<br>[Qua92a]                              | -      | 269        | 2.1        | 4%       | 44%        |
| NUM244<br>-1         | TrnsfRecrLem11<br>TREC.LEMMA11         | Transfinite recursion lemma 11<br>[Qua92a]                              | -      | 269        | 2.1        | 4%       | 44%        |
| NUM245<br>-1<br>-2   | TrnsfRecrEqn1<br>TREC5.1               | Transfinite recursion property 1<br>[Qua92a]<br>[Qua92a]                | -<br>- | 267<br>283 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM246<br>-1<br>-2   | TrnsfRecrEqn2<br>TREC5.2               | Transfinite recursion property 2<br>[Qua92a]<br>[Qua92a]                | -<br>- | 270<br>286 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM247<br>-1<br>-2   | TrnsfRecrEqn3<br>TREC6                 | Transfinite recursion property 3<br>[Qua92a]<br>[Qua92a]                | -<br>- | 265<br>281 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM248<br>-1<br>-2   | TrnsfRecrEqn4<br>TREC7                 | Transfinite recursion property 4<br>[Qua92a]<br>[Qua92a]                | -<br>- | 265<br>281 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM249<br>-1<br>-2   | TrnsfRecrEqn5<br>TREC7-5               | Transfinite recursion property 5<br>[Qua92a]<br>[Qua92a]                | -<br>- | 265<br>281 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM250<br>-1<br>-2   | TrnsfRecrEqn6<br>TREC8                 | Transfinite recursion property 6<br>[Qua92a]<br>[Qua92a]                | -<br>- | 265<br>281 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM251<br>-1<br>-2   | TrnsfRecrEqn7<br>TREC9                 | Transfinite recursion property 7<br>[Qua92a]<br>[Qua92a]                | -<br>- | 265<br>281 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM252<br>-1<br>-2   | TrnsfRecrEqn8<br>TREC10                | Transfinite recursion property 8<br>[Qua92a]<br>[Qua92a]                | -<br>- | 266<br>282 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM253<br>-1<br>-2   | TrnsfRecrEqn9<br>TREC11                | Transfinite recursion property 9<br>[Qua92a]<br>[Qua92a]                | -<br>- | 266<br>282 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |
| NUM254<br>-1<br>-2   | TrnsfRecrEqn10<br>TREC12               | Transfinite recursion property 10<br>[Qua92a]<br>[Qua92a]               | -<br>- | 266<br>282 | 2.1<br>2.2 | 4%<br>6% | 44%<br>42% |

| Syntactic name<br>V# | Semantic name<br>Other names   | Description<br>References   | V | Cl  | Av  | nH  | Eq  |
|----------------------|--------------------------------|---|---|-----|-----|-----|-----|
| NUM255<br>-1<br>-2   | TrnsfRecrEqn11<br>TREC13       | Transfinite recursion property 11<br>[Qua92a]<br>[Qua92a]                               | - | 266 | 2.1 | 4%  | 44% |
| NUM256<br>-1<br>-2   | TrnsfRecrEqn12<br>TREC14       | Transfinite recursion property 12<br>[Qua92a]<br>[Qua92a]                               | - | 267 | 2.1 | 4%  | 44% |
| NUM257<br>-1<br>-2   | TrnsfRecrEqn13<br>TREC15       | Transfinite recursion property 13<br>[Qua92a]<br>[Qua92a]                               | - | 266 | 2.1 | 4%  | 44% |
| NUM258<br>-1<br>-2   | TrnsfRecrEqn14<br>TREC16       | Transfinite recursion property 14<br>[Qua92a]<br>[Qua92a]                               | - | 266 | 2.1 | 4%  | 44% |
| NUM259<br>-1<br>-2   | TrndfRecrFuncUnq<br>TREC17     | The uniqueness of the function defined by transfinite recursion<br>[Qua92a]<br>[Qua92a] | - | 268 | 2.1 | 4%  | 44% |
| NUM260<br>-1<br>-2   | Alt4TrnsfIndn1<br>TREC18.1     | Alternate 4 for transfinite induction, part 1<br>[Qua92a]<br>[Qua92a]                   | - | 265 | 2.1 | 4%  | 44% |
| NUM261<br>-1<br>-2   | Alt4TrnsfIndn2<br>TREC18.2     | Alternate 4 for transfinite induction, part 2<br>[Qua92a]<br>[Qua92a]                   | - | 265 | 2.1 | 4%  | 44% |
| NUM262<br>-1<br>-2   | Alt4TrnsfIndn3<br>TREC18.3     | Alternate 4 for transfinite induction, part 3<br>[Qua92a]<br>[Qua92a]                   | - | 265 | 2.1 | 4%  | 44% |
| NUM263<br>-1<br>-2   | Alt4TrnsfIndn4<br>TREC18.4     | Alternate 4 for transfinite induction, part 4<br>[Qua92a]<br>[Qua92a]                   | - | 266 | 2.1 | 4%  | 44% |
| NUM264<br>-1<br>-2   | Alt4TrnsfIndn5<br>TREC18.5     | Alternate 4 for transfinite induction, part 5<br>[Qua92a]<br>[Qua92a]                   | - | 266 | 2.1 | 4%  | 44% |
| NUM265<br>-1         | Ord1AddEqn1<br>OA6.1           | Ordinal addition property 1<br>[Qua92a]   | - | 265 | 2.1 | 4%  | 44% |
| NUM266<br>-1         | Ord1AddEqn2<br>OA6.2           | Ordinal addition property 2<br>[Qua92a]   | - | 266 | 2.1 | 4%  | 44% |
| NUM267<br>-1         | Ord1AddEqn3<br>OA6.3           | Ordinal addition property 3<br>[Qua92a]   | - | 266 | 2.1 | 4%  | 44% |
| NUM268<br>-1         | Ord1AddEqn4<br>OA6.4           | Ordinal addition property 4<br>[Qua92a]   | - | 266 | 2.1 | 4%  | 44% |
| NUM269<br>-1         | Ord1AddEqn5<br>OA7             | Ordinal addition property 5<br>[Qua92a]   | - | 267 | 2.1 | 4%  | 44% |
| NUM270<br>-1         | Ord1AddEqn6<br>OA8             | Ordinal addition property 6<br>[Qua92a]   | - | 265 | 2.1 | 4%  | 44% |
| NUM271<br>-1         | Ord1AddEqn7Lem1<br>OA9 lemma 1 | Lemma 1 for ordinal addition property 7<br>[Qua92a]                                     | - | 268 | 2.1 | 4%  | 44% |
| NUM272<br>-1         | Ord1AddEqn7Lem2<br>OA9 lemma 2 | Lemma 2 for ordinal addition property 7<br>[Qua92a]                                     | - | 268 | 2.1 | 4%  | 44% |
| NUM273<br>-1         | Ord1AddEqn7Lem3<br>OA9 lemma 3 | Lemma 3 for ordinal addition property 7<br>[Qua92a]                                     | - | 268 | 2.1 | 4%  | 44% |
| NUM274<br>-1         | Ord1AddEqn7Lem4<br>OA9 lemma 4 | Lemma 4 for ordinal addition property 7<br>[Qua92a]                                     | - | 268 | 2.1 | 4%  | 44% |
| NUM275<br>-1         | Ord1AddEqn7Lem5<br>OA9 lemma 5 | Lemma 5 for ordinal addition property 7<br>[Qua92a]                                     | - | 268 | 2.1 | 4%  | 44% |
| NUM276<br>-1         | Ord1AddEqn7Lem6<br>OA9 lemma 6 | Lemma 6 for ordinal addition property 7<br>[Qua92a]                                     | - | 268 | 2.1 | 4%  | 44% |
| NUM277<br>-1<br>-2   | Ord1AddEqn7_1<br>OA9.1<br>OA10 | Ordinal addition property 7_1<br>[Qua92a]<br>[Qua92a]                                   | - | 268 | 2.1 | 4%  | 44% |
| NUM278<br>-1         | Ord1AddEqn7_2<br>OA9.2         | Ordinal addition property 7_2<br>[Qua92a]   | - | 266 | 2.1 | 4%  | 44% |
| NUM279<br>-1         | Ord1AddEqn8<br>[Qua92a]        | Ordinal addition property 8   | - | 265 | 2.1 | 4%  | 44% |
| NUM280<br>-1         | Ord1MultEqn1<br>OM2.1          | Ordinal multiplication property 1<br>[Qua92a]   | - | 265 | 2.1 | 4%  | 44% |
| NUM281<br>-1         | Ord1MultEqn2<br>OM2.2          | Ordinal multiplication property 2<br>[Qua92a]   | - | 266 | 2.1 | 4%  | 44% |
| NUM282<br>-1         | Ord1MultEqn3<br>OM2.3          | Ordinal multiplication property 3<br>[Qua92a]   | - | 266 | 2.1 | 4%  | 44% |
| NUM283<br>-1.005     | Factorial<br>facX.lop (Size X) | Calculation of factorial  | - | 7   | 1.7 | -   | -   |
| NUM284<br>-1.010     | Fibonacci<br>fibX.lop (Size X) | Calculation of fibonacci numbers  | - | 6   | 2.0 | -   | -   |
| NUM285<br>-1         | BiCond                         | $a_0 + \dots + a_5 = b_1 + \dots + b_5$ , expression in logic                           | - | 54  | 2.7 | 57% | -   |

### Domain PLA (23 abstract problems, 30 problems)

|                    |                      |   |   |    |     |    |   |
|--------------------|----------------------|---|---|----|-----|----|---|
| PLA001<br>-1       | Bread                | Cheyenne to DesMoines, buying a loaf of bread on the way<br>[Pla81] | - | 16 | 1.4 | -  | - |
| PLA002<br>-1<br>-2 | Going<br>Problem 5.7 | Getting from here to there, in all weather<br>[Pla82]<br>[Pla82]    | - | 17 | 2.1 | 5% | - |
| PLA003<br>-1       | Monkey               | Monkey and Bananas Problem  | - | 11 | 1.8 | -  | - |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References                                  | V | Cl | Av  | nH | Eq |
|----------------------|------------------------------|--|---|----|-----|----|----|
| PLA004<br>-1<br>-2   | Blocks_CBA                   | Block C on B on A<br>[G.J73, SE94]<br>[G.J73, SE94]        | - | 31 | 1.7 | -  | -  |
| PLA005<br>-1<br>-2   | Blocks_CA_DB                 | Block C on A and D on B<br>[G.J73, SE94]<br>[G.J73, SE94]  | - | 31 | 1.7 | -  | -  |
| PLA006<br>-1         | Blocks_CTable                | Block C on Table<br>[G.J73, SE94]                          | - | 31 | 1.7 | -  | -  |
| PLA007<br>-1         | Blocks_AD                    | Block A on D<br>[G.J73, SE94]                              | - | 31 | 1.7 | -  | -  |
| PLA008<br>-1         | Blocks_BD_AC                 | Block B on D and A on C<br>[G.J73, SE94]                   | - | 31 | 1.7 | -  | -  |
| PLA009<br>-1<br>-2   | Blocks_AB_D                  | Block A on B and D clear<br>[G.J73, SE94]<br>[G.J73, SE94] | - | 31 | 1.7 | -  | -  |
| PLA010<br>-1         | Blocks_ADB                   | Block A on D on B<br>[G.J73, SE94]                         | - | 31 | 1.7 | -  | -  |
| PLA011<br>-1<br>-2   | Blocks_DCB                   | Block D on C on B<br>[G.J73, SE94]<br>[G.J73, SE94]        | - | 31 | 1.7 | -  | -  |
| PLA012<br>-1         | Blocks_DBC                   | Block D on B on C<br>[G.J73, SE94]                         | - | 31 | 1.7 | -  | -  |
| PLA013<br>-1         | Blocks_ACB                   | Block A on C on B<br>[G.J73, SE94]                         | - | 31 | 1.7 | -  | -  |
| PLA014<br>-1<br>-2   | Blocks_ABC                   | Block A on B on C<br>[G.J73, SE94]<br>[G.J73, SE94]        | - | 31 | 1.7 | -  | -  |
| PLA015<br>-1         | Blocks_ABD                   | Block A on B on D<br>[G.J73, SE94]                         | - | 31 | 1.7 | -  | -  |
| PLA016<br>-1         | Blocks_DA                    | Block D on A<br>[G.J73, SE94]                              | - | 31 | 1.7 | -  | -  |
| PLA017<br>-1         | Blocks_AC                    | Block A on C<br>[G.J73, SE94]                              | - | 31 | 1.7 | -  | -  |
| PLA018<br>-1         | Blocks_AB_DC                 | Block A on B and D on C<br>[G.J73, SE94]                   | - | 31 | 1.7 | -  | -  |
| PLA019<br>-1         | Blocks_DC                    | Block D on C<br>[G.J73, SE94]                              | - | 31 | 1.7 | -  | -  |
| PLA020<br>-1         | Blocks_D                     | Block D clear<br>[G.J73, SE94]                             | - | 31 | 1.7 | -  | -  |
| PLA021<br>-1         | Blocks_BD_CA                 | Block B on D and C on A<br>[G.J73, SE94]                   | - | 31 | 1.7 | -  | -  |
| PLA022<br>-1<br>-2   | Blocks_ACD                   | Block A on C on D<br>[G.J73, SE94]<br>[G.J73, SE94]        | - | 31 | 1.7 | -  | -  |
| PLA023<br>-1         | Blocks_DAC                   | Block D on A on C<br>[G.J73, SE94]                         | - | 31 | 1.7 | -  | -  |

Domain PRV (9 abstract problems, 9 problems)

|              |                                  |   |   |    |     |     |     |
|--------------|----------------------------------|---|---|----|-----|-----|-----|
| PRV001<br>-1 | Unknown<br>PV1                   | PV1<br>[MOW76]  | - | 14 | 2.6 | 14% | -   |
| PRV002<br>-1 | Unknown<br>E1, v1.lop            | E1<br>[MOW76]   | - | 29 | 1.8 | 6%  | 39% |
| PRV003<br>-1 | Unknown<br>E2, v2.lop            | E2<br>[MOW76]   | - | 27 | 1.9 | 7%  | 41% |
| PRV004<br>-1 | Unknown<br>E3, v3.lop            | E3<br>[MOW76]   | - | 29 | 1.8 | 6%  | 39% |
| PRV005<br>-1 | Unknown<br>E4, v4.lop            | E4<br>[MOW76]   | - | 27 | 1.9 | 7%  | 41% |
| PRV006<br>-1 | Unknown<br>E5, v5.lop            | E5<br>[MOW76]   | - | 26 | 1.9 | 7%  | 42% |
| PRV007<br>-1 | Unknown<br>E6, v6.lop            | E6<br>[MOW76]   | - | 29 | 1.8 | 6%  | 41% |
| PRV008<br>-1 | Unknown<br>E7, v7.lop            | E7<br>[MOW76]   | - | 23 | 2.0 | 8%  | 46% |
| PRV009<br>-1 | FIND<br>Hoares FIND, Problem 5.5 | A condition from Hoare's FIND program<br>[Ble77, Pla82] | - | 9  | 2.2 | 11% | -   |

Domain PUZ (34 abstract problems, 45 problems)

|                          |                               |   |   |    |     |     |     |
|--------------------------|-------------------------------|---|---|----|-----|-----|-----|
| PUZ001<br>-1<br>-2<br>-3 | Agatha<br>Pelletier 55        | Dreadbury Mansion<br>[Pel86, MB88]<br>[Pel86, Pel88]<br>[Pel86, MB88] | - | 12 | 1.8 | 16% | -   |
| PUZ002<br>-1             | Animals<br>animals.ver1.in    | The Animals Puzzle<br>[Car86]   | - | 12 | 1.8 | 8%  | -   |
| PUZ003<br>-1             | Barber<br>barber.ver1.in      | The Barber Puzzle   | - | 8  | 1.6 | -   | -   |
| PUZ004<br>-1             | Letters<br>letters.ver1.in    | The Letters Puzzle<br>[Car86]   | - | 12 | 1.8 | 8%  | -   |
| PUZ005<br>-1             | LionU<br>Lion and the Unicorn | Lions and Unicorns<br>[Smu78b, OSS85]                                 | - | 51 | 2.2 | 11% | -   |
| PUZ006<br>-1             | MarsVenus1<br>mars_venus.in   | Determine sex and race on Mars and Venus                              | - | 42 | 2.3 | 9%  | 18% |
| PUZ007<br>-1             | MarsVenus2<br>mars_venus2.in  | Mixed couples on Mars and Venus                                       | - | 41 | 2.3 | 17% | 21% |

| Syntactic name<br>V#           | Semantic name<br>Other names   | Description  | References                      | V | Cl  | Av  | nH  | Eq  |
|--------------------------------|--|--|---------------------------------|---|-----|-----|-----|-----|
| PUZ008<br>-1<br>-2<br>-3       | MissCann<br>mission.ver1.in<br>mission.ver2.in                       | Missionaries and Cannibals                                 | [WOLB92, Rap95]<br>[Rap95]      | - | 16  | 1.6 | -   | -   |
| PUZ009<br>-1                   | Oona<br>oona.in  | Looking for Oona   | [Smu87]                         | - | 18  | 2.2 | 33% | -   |
| PUZ010<br>-1                   | Zebra<br>jobs  | Who owns the zebra?  | [SS86, LP92, Lee92]             | - | 128 | 2.5 | 4%  | -   |
| PUZ011<br>-1                   | Borders1<br>Problem 5.6  | An ocean that borders on an African and an Asian country   | [Pla82]                         | - | 27  | 1.1 | -   | -   |
| PUZ012<br>-1                   | Boxes<br>Boxes-of-fruit, Boxes-of-fruit, boxes.ver1.in               | The Mislabeled Boxes                                       | [WOLB92, Wos88]                 | - | 18  | 1.6 | 11% | -   |
| PUZ013<br>-1                   | Boys1<br>boys.ver1.in  | The School Boys : Prove some monitors are awake            | [Car86]                         | - | 20  | 2.5 | 40% | -   |
| PUZ014<br>-1                   | Boys2<br>School Boys   | The School Boys : Prove that all monitors are awake        | [LO85a, Car86]                  | - | 20  | 2.5 | 40% | -   |
| PUZ015<br>-1<br>-2.003         | Checkers1<br>chekndom.ver1.in  | Checkerboard and Dominoes : Opposing corners removed       | [Sti93]                         | - | 37  | 1.7 | -   | 65% |
| PUZ016<br>-1<br>-2.003         | Checkers2<br>chekndom.ver2.in  | Checkerboard and Dominoes : Row 1, columns 2 and 3 removed | [Sti93]                         | - | 37  | 1.7 | -   | 65% |
| PUZ017<br>-1                   | Houses<br>houses.ver1.in   | The Houses   |                                 | - | 148 | 2.2 | 11% | -   |
| PUZ018<br>-1<br>-2             | Interns<br>interns.ver1.in   | The Interns  | [Rap95]<br>[Rap95]              | - | 48  | 1.5 | 4%  | -   |
| PUZ019<br>-1                   | Jobs<br>jobs.ver1.in   | The Jobs Puzzles   | [WOLB92]                        | - | 63  | 1.7 | 6%  | -   |
| PUZ020<br>-1                   | KKnave1<br>knightknave.in  | A knights & knaves problem, if he's a knight, so is she    | [Rap95]                         | - | 29  | 2.3 | 10% | 26% |
| PUZ021<br>-1                   | KKnave2<br>Problem 95, How to Win a Bride                            | How to Win a Bride   | [Smu78b, Ohl85]                 | - | 13  | 2.4 | 30% | -   |
| PUZ022<br>-1                   | Borders2   | An ocean that borders on two adjacent Australian states    | [Pla82]                         | - | 33  | 1.2 | -   | -   |
| PUZ023<br>-1                   | KKnave27<br>Problem 27, tandl27.ver1.in                              | Knights and Knaves #27                                     | [Smu78b]                        | - | 22  | 3.0 | 27% | -   |
| PUZ024<br>-1                   | KKnave31<br>Problem 31, tandl31.ver1.in                              | Knights and Knaves #31                                     | [Smu78b]                        | - | 20  | 3.0 | 30% | -   |
| PUZ025<br>-1                   | KKnave35<br>Problem 35, tandl35.ver1.in                              | Knights and Knaves #35                                     | [Smu78b]                        | - | 24  | 2.5 | 25% | -   |
| PUZ026<br>-1                   | KKnave39<br>Problem 39, tandl39.ver1.in                              | Knights and Knaves #39                                     | [Smu78b]                        | - | 23  | 2.3 | 17% | -   |
| PUZ027<br>-1                   | KKnave42<br>Problem 42, tandl42.ver1.in                              | Knights and Knaves #42                                     | [Smu78b]                        | - | 32  | 2.8 | 28% | -   |
| PUZ028<br>-1<br>-2<br>-3<br>-4 | Party<br>ramsey1.lop<br>ramsey3.lop<br>ramsey3a.lop                  | People at a party  | [ICO92]                         | - | 15  | 1.7 | 6%  | -   |
| PUZ029<br>-1                   | Pigs<br>pigs.ver1.in   | The pigs and balloons puzzle                               | [Car86]                         | - | 15  | 2.4 | 26% | -   |
| PUZ030<br>-1<br>-2             | SaltM<br>Salt and Mustard Problem,<br>salt.in                        | Salt and Mustard Problem                                   | [LO85a, Car86, MB88]<br>[Car86] | - | 43  | 2.5 | 30% | -   |
| PUZ031<br>-1                   | SteamR<br>Pelletier 47, steamroller.ver1.in, steam.in, SST           | Schubert's Steamroller                                     | [Sti86, Pel86, WB87, MB88]      | - | 26  | 2.4 | 3%  | -   |
| PUZ032<br>-1                   | KKnave26<br>Problem 26, Truth-tellers and the Liars, tandl.ver1.in   | Knights and Knaves #26                                     | [Smu78b, LO85a]                 | - | 10  | 2.0 | 20% | -   |
| PUZ033<br>-1                   | Winds<br>winds.ver1.in   | The Winds and the Windows Puzzle                           | [Car86]                         | - | 13  | 2.5 | 15% | -   |
| PUZ034<br>-1.003               | NQueens<br>q1-2.lop (Size 8), q1-9.lop (Size 9), q1-10.lop (Size 10) | N queens problem   |                                 | - | 18  | 2.2 | 11% | -   |

### Domain RNG (40 abstract problems, 100 problems)

|                                      |   |   |  |   |    |     |   |     |
|--------------------------------------|---|---|--|---|----|-----|---|-----|
| RNG001<br>-1<br>-2<br>-3<br>-4<br>-5 | XTimesAId<br>R1, zero.ver1.in<br>ls37, ls37<br>Example 6a, EX6-T?, ex6.lop, FEX6T1, FEX6T2<br>R1<br>Problem 21, wos21 | $X.additive\_identity = additive\_identity$ for any X | [MOW76]<br>[LS74, WM76]<br>[FLSY74, WM76]<br>[MOW76]<br>[Wosb, FLSY74, WM76] | - | 32 | 2.7 | - | 28% |
| RNG002<br>-1                         | AddRCanc<br>Established lemma,  | Right cancellation for addition                       | [MOW76, OMW76]   | - | 34 | 2.6 | - | 28% |
| RNG003<br>-1                         | AddLCanc<br>Established lemma,  | Left cancellation for addition                        | [MOW76, OMW76]   | - | 34 | 2.6 | - | 28% |
| RNG004<br>-1<br>-2<br>-3             | ProdInv<br>R2, minuses.ver1.in<br>R2<br>Problem 22, wos22   | $X*Y = -X*-Y$   | [MOW76]<br>[MOW76]<br>[Wosb, WM76]   | - | 34 | 2.6 | - | 28% |
| RNG005<br>-1<br>-2                   | SumEqAId<br>Problem 23<br>Problem 23, wos23   | $(-X*Y) + (X*Y) = additive\_identity$                 | [Wosb, MOW76]<br>[Wosb, WM76]  | - | 34 | 2.6 | - | 27% |

| Syntactic name<br>V# | Semantic name<br>Other names                     | Description   | References                        | V | Cl | Av  | nH | Eq   |
|----------------------|--|---|-----------------------------------|---|----|-----|----|------|
| RNG006               | Eqn1   | $X*(Y+Z) = (X*Y) + -(X*Z)$  |                                   | - | 39 | 2.4 | -  | 25%  |
| -1                   | Problem 25                                       |   | [Wosb, MOW76]                     | - | 36 | 2.4 | -  | -    |
| -2                   | Problem 25, wos25                                |   | [Wosb, WM76]                      | - | 36 | 2.5 | -  | 27%  |
| -3                   | Problem 25                                       |   | [Wosb]                            | - | 36 | 2.5 | -  | 27%  |
| RNG007               | BoolInv  | In Boolean rings, X is its own inverse                            |                                   | - | 33 | 2.6 | -  | 27%  |
| -1                   | lemma.ver3.in, lemma.ver4.in                     |   | [MOW76]                           | - | 24 | 1.3 | -  | 100% |
| -4                   | lemma.ver2.in                                    |   | [PS81]                            | - | 39 | 2.4 | -  | 27%  |
| -5                   | lemma.ver1.in                                    |   | [MOW76, PS81]                     | - | 39 | 2.4 | -  | 27%  |
| RNG008               | BoolComm   | Boolean rings are commutative                                     |                                   | - | 34 | 2.6 | -  | 27%  |
| -1                   | Test Problem 8, commute.ver3.in, commute.ver4.in |   | [MOW76, Wos88]                    | - | 36 | 2.6 | -  | 28%  |
| -2                   | R3, Theorem 2                                    |   | [MOW76, OMW76]                    | - | 27 | 1.3 | -  | 100% |
| -3                   | commute.ver2.in                                  |   | [MOW76, PS81]                     | - | 25 | 1.3 | -  | 100% |
| -4                   |  |   | [MOW76, PS81]                     | - | 40 | 2.3 | -  | 25%  |
| -5                   | commute.ver1.in                                  |   | [MOW76, PS81]                     | - | 36 | 2.5 | -  | 27%  |
| -6                   | CADE-11 Comp. 3, THEOREM 3                       |   | [MOW76, Ove90, Ove93, LM93]       | - | 20 | 1.4 | -  | 100% |
| -7                   | Problem 3, Test Problem 8, RT1                   |   | [LO85b, Wos88, LW91]              | - | 20 | 1.4 | -  | 100% |
| RNG009               | CubeComm   | If $X*X*X = X$ then the ring is commutative                       |                                   | - | 17 | 1.5 | -  | 100% |
| -5                   | CADE-11 Comp. Eq-7, EQ-7, PROBLEM 7              |   | [PS81, Ove90, Ove93, LM93, Zha93] | - | 20 | 1.4 | -  | 100% |
| -7                   | Problem 6, RT2                                   |   | [LO85b, LW91]                     | - | 20 | 1.4 | -  | 100% |
| RNG010               | AuxSkewSymm                                      | Skew symmetry of the auxilliary function                          |                                   | - | 32 | 1.4 | -  | 100% |
| -1                   |  |   | [AH90]                            | - | 35 | 1.4 | -  | 100% |
| -2                   | PROOF VI   |   | [AH90]                            | - | 44 | 1.4 | -  | 100% |
| -5                   | CADE-11 Comp. Eq-9, THEOREM EQ-9, PROBLEM 9      |   | [Ove90, Ove93, LM93, Zha93]       | - | 36 | 1.5 | -  | 100% |
| -6                   |  |   | [Ste87]                           | - | 43 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87]                           | - | 43 | 1.4 | -  | 100% |
| RNG011               | RAltEqn  | In a right alternative ring $((X,X,Y)*X)*(X,X,Y) = \text{Add Id}$ |                                   | - | 35 | 1.4 | -  | 100% |
| -5                   | CADE-11 Comp. Eq-10, EQ-10, PROBLEM 10           |   | [Ove90, Ove93, LM93, Zha93]       | - | 35 | 1.4 | -  | 100% |
| RNG012               | ProdInv  | Product of inverses equal product                                 |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c15  |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| RNG013               | InvProd1   | $-X*Y = -(X*Y)$   |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c16  |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| RNG014               | InvProd2   | $-X*Y = -(X*Y)$   |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c17  |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| RNG015               | DiffDist1  | $X*(Y+Z) = (X*Y) + -(X*Z)$  |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c18  |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| RNG016               | DiffDist2  | $(X+Y)*Z = (X*Z) + -(Y*Z)$  |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c19  |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| RNG017               | DiffDist3  | $-X*(Y+Z) = -(X*Y) + -(X*Z)$                                      |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c20  |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| RNG018               | DiffDist4  | $(X+Y)*-Z = -(X*Z) + -(Y*Z)$                                      |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c21  |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| RNG019               | LinAssr1   | First part of the linearised form of the associator               |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c24  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| RNG020               | LinAssr2   | Second part of the linearised form of the associator              |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c25  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| RNG021               | LinAssr3   | Third part of the linearised form of the associator               |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | c26  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| RNG023               | LAlt   | Left alternative  |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   |  |   | [Ste87, Ste92]                    | - | 36 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87, Ste92]                    | - | 36 | 1.4 | -  | 100% |
| RNG024               | RAlt   | Right alternative   |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   |  |   | [Ste87, Ste92]                    | - | 36 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87, Ste92]                    | - | 36 | 1.4 | -  | 100% |
| RNG025               | FlexLaw  | Middle or Flexible Law  |                                   | - | 26 | 1.4 | -  | 100% |
| -1                   | PROOF I  |   | [AH90]                            | - | 29 | 1.4 | -  | 100% |
| -4                   |  |   | [Ste87, Ste92]                    | - | 36 | 1.4 | -  | 100% |
| -5                   |  |   | [Ste87, Ste92]                    | - | 29 | 1.4 | -  | 100% |
| -6                   |  |   | [Ste87, Ste92]                    | - | 36 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87, Ste92]                    | - | 31 | 1.4 | -  | 100% |
| -8                   |  |   | [Ste87]                           | - | 38 | 1.3 | -  | 100% |
| -9                   |  |   | [Ste87]                           | - | 38 | 1.3 | -  | 100% |
| RNG026               | TeichId  | Teichmuller Identity  |                                   | - | 29 | 1.4 | -  | 100% |
| -6                   | Teichmuller Identity                             |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| RNG027               | R Moufang  | Right Moufang identity  |                                   | - | 26 | 1.4 | -  | 100% |
| -1                   |  |   | [AH90]                            | - | 33 | 1.4 | -  | 100% |
| -2                   | PROOF IV   |   | [AH90]                            | - | 29 | 1.4 | -  | 100% |
| -5                   |  |   | [Ste87, Ste88]                    | - | 29 | 1.4 | -  | 100% |
| -6                   | m1   |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| -8                   | m1'  |   | [Ste87, Ste88]                    | - | 29 | 1.4 | -  | 100% |
| -9                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| RNG028               | L Moufang  | Left Moufang identity   |                                   | - | 26 | 1.4 | -  | 100% |
| -1                   |  |   | [AH90]                            | - | 33 | 1.4 | -  | 100% |
| -2                   | PROOF III  |   | [AH90]                            | - | 29 | 1.4 | -  | 100% |
| -5                   |  |   | [Ste87, Ste88]                    | - | 29 | 1.4 | -  | 100% |
| -6                   | m2   |   | [Ste87]                           | - | 29 | 1.4 | -  | 100% |
| -7                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |
| -8                   | m2'  |   | [Ste87, Ste88]                    | - | 29 | 1.4 | -  | 100% |
| -9                   |  |   | [Ste87]                           | - | 36 | 1.4 | -  | 100% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description                                     | References          | V | Cl | Av  | nH | Eq   |
|----------------------|------------------------------|---|---------------------|---|----|-----|----|------|
| RNG029               | M Moufang                    | Middle Moufang identity                         |                     | - | 26 | 1.4 | -  | 100% |
| -1                   |                              |   | [AH90]              | - | 33 | 1.4 | -  | 100% |
| -2                   | PROOF V                      |   | [Ste87, Ste88]      | - | 29 | 1.4 | -  | 100% |
| -5                   |                              |   | [Ste87]             | - | 29 | 1.4 | -  | 100% |
| -6                   | m3                           |   | [Ste87]             | - | 36 | 1.4 | -  | 100% |
| -7                   |                              |   | [Ste87]             | - | 36 | 1.4 | -  | 100% |
| RNG030               | AssrEqn2                     | $2*assr(X,X,Y)^3 =$ additive identity           |                     | - | 28 | 1.5 | -  | 100% |
| -6                   | Conjecture 1                 |   | [Ste87]             | - | 35 | 1.4 | -  | 100% |
| -7                   | Conjecture 1                 |   | [Ste87]             | - | 35 | 1.4 | -  | 100% |
| RNG031               | AssrEqn3                     | $(W*W)*X*(W*W) =$ additive identity             |                     | - | 28 | 1.5 | -  | 100% |
| -6                   | Conjecture 2                 |   | [Ste87]             | - | 35 | 1.4 | -  | 100% |
| -7                   | Conjecture 2                 |   | [Ste87]             | - | 35 | 1.4 | -  | 100% |
| RNG032               | AssrEqn4                     | $6*assr(X,X,Y)^6 =$ additive identity           |                     | - | 28 | 1.5 | -  | 100% |
| -6                   | Conjecture 3                 |   | [Ste87]             | - | 35 | 1.4 | -  | 100% |
| -7                   | Conjecture 3                 |   | [Ste87]             | - | 35 | 1.4 | -  | 100% |
| RNG033               | AssrEqn5                     | A fairly complex equation with associators      |                     | - | 29 | 1.4 | -  | 100% |
| -6                   | ch                           |   | [Ste87]             | - | 36 | 1.4 | -  | 100% |
| -7                   |                              |   | [Ste87]             | - | 30 | 1.4 | -  | 100% |
| -8                   |                              |   | [Ste87]             | - | 37 | 1.4 | -  | 100% |
| -9                   |                              |   | [Ste87]             | - | 37 | 1.4 | -  | 100% |
| RNG034               | AssrSkewSymm                 | A skew symmetry relation of the associator      |                     | - | 30 | 1.4 | -  | 100% |
| -1                   | PROOF II                     |   | [AH90]              | - | 30 | 1.4 | -  | 100% |
| RNG035               | FourthComm                   | If $X*X*X*X = X$ then the ring is commutative   |                     | - | 20 | 1.4 | -  | 100% |
| -7                   | RT3                          |   | [LW91]              | - | 20 | 1.4 | -  | 100% |
| RNG036               | FifthComm                    | If $X*X*X*X*X = X$ then the ring is commutative |                     | - | 20 | 1.4 | -  | 100% |
| -7                   | RT4                          |   | [LW91]              | - | 20 | 1.4 | -  | 100% |
| RNG037               | SumEqAId2                    | $(X* -Y) + (X*Y) =$ additive identity           |                     | - | 34 | 2.6 | -  | 27%  |
| -1                   | Problem 24                   |   | [Wosb, MOW76]       | - | 29 | 2.7 | -  | -    |
| -2                   | Problem 24, wos24            |   | [Wosb, WM76]        | - | 29 | 2.7 | -  | -    |
| RNG038               | RngEqn1                      | Ring property 1                                 |                     | - | 37 | 2.5 | -  | 33%  |
| -1                   | Problem 27                   |   | [Wosb, MOW76]       | - | 30 | 2.6 | -  | -    |
| -2                   | Problem 27, wos27            |   | [Wosb, WM76]        | - | 30 | 2.6 | -  | -    |
| RNG039               | RngEqn2                      | Ring property 2                                 |                     | - | 74 | 1.7 | -  | 23%  |
| -1                   | Problem 28                   |   | [Wosb, MOW76]       | - | 74 | 1.7 | -  | -    |
| -2                   | Problem 28, wos28            |   | [Wosb, WM76]        | - | 74 | 1.7 | -  | -    |
| RNG040               | RngEqn3                      | Ring property 4                                 |                     | - | 42 | 2.4 | 4% | 28%  |
| -1                   | Problem 29                   |   | [Wosb, MOW76]       | - | 40 | 2.2 | 5% | 31%  |
| -2                   | Problem 29, wos29            |   | [Wosb, MOW76, WM76] | - | 40 | 2.2 | 5% | 31%  |
| RNG041               | RngEqn4                      | Unknown   |                     | - | 41 | 2.4 | 4% | 30%  |
| -1                   | Problem 30, wos30            |   | [Wosb, MOW76, WM76] | - | 41 | 2.4 | 4% | 30%  |

### Domain ROB (27 abstract problems, 36 problems)

|        |   |  |                             |   |    |     |   |      |
|--------|---|--|-----------------------------|---|----|-----|---|------|
| ROB001 | RobBool   | Is every Robbins algebra Boolean?  |                             | - | 10 | 1.6 | - | 100% |
| -1     |   |  | [HMT71, Win90]              | - | 10 | 1.6 | - | 100% |
| ROB002 | RobBool1  | $--X = X \Rightarrow$ Boolean  |                             | - | 11 | 1.5 | - | 100% |
| -1     | Lemma 2.1   |  | [HMT71, Win90]              | - | 11 | 1.5 | - | 100% |
| ROB003 | RobBool2  | $X + c=c \Rightarrow$ Boolean  |                             | - | 11 | 1.5 | - | 100% |
| -1     | Lemma 2.2, RA1, robbins.in  |  | [HMT71, Win90, LW92]        | - | 11 | 1.5 | - | 100% |
| ROB004 | RobBool3  | $c = -d, c + d=d,$ and $c + c=c \Rightarrow$ Boolean                     |                             | - | 13 | 1.5 | - | 100% |
| -1     | Lemma 2.3   |  | [HMT71, Win90]              | - | 13 | 1.5 | - | 100% |
| ROB005 | RobBool4  | $c + c=c \Rightarrow$ Boolean  |                             | - | 11 | 1.5 | - | 100% |
| -1     | CADE-11 Comp. Eq-2, Lemma 2.4, RA3, THEOREM EQ-2, PROBLEM 2, robbins.occ.in |  | [HMT71, Win90, Ove90, LW92] | - | 11 | 1.5 | - | 100% |
| ROB006 | RobBool5  | $c + d=d \Rightarrow$ Boolean  |                             | - | 11 | 1.5 | - | 100% |
| -1     | Theorem 1.1, RA4  |  | [HMT71, Win90, Wos92, LW92] | - | 11 | 1.5 | - | 100% |
| -2     | Theorem 1.1   |  | [HMT71, Win90, Wos92]       | - | 11 | 1.5 | - | 100% |
| -3     | Theorem 1.1   |  | [HMT71, Win90, Wos92]       | - | 23 | 1.7 | - | 82%  |
| ROB007 | RobBool6  | $-(a + b) = -b \Rightarrow$ Boolean                                      |                             | - | 11 | 1.5 | - | 100% |
| -1     | Theorem 1.2, RA5  |  | [HMT71, Win90, LW92]        | - | 13 | 1.5 | - | 100% |
| -2     | Theorem 1.2   |  | [HMT71, Win90]              | - | 22 | 1.7 | - | 83%  |
| -3     | Theorem 1.2   |  | [HMT71, Win90]              | - | 24 | 1.6 | - | 84%  |
| -4     | Theorem 1.2   |  | [HMT71, Win90]              | - | 24 | 1.6 | - | 84%  |
| ROB008 | Eqn1  | If $-(a + -(b + c)) = -(a + b + -c)$ then $a+b=a$                        |                             | - | 11 | 1.5 | - | 100% |
| -1     | Lemma 3.1   |  | [Win90]                     | - | 11 | 1.5 | - | 100% |
| ROB009 | Eqn2  | If $-(a + -(b + c)) = -(b + -(a + c))$ then $a = b$                      |                             | - | 11 | 1.5 | - | 100% |
| -1     | Lemma 3.2   |  | [Win90]                     | - | 11 | 1.5 | - | 100% |
| ROB010 | Eqn3  | If $-(a + -b) = c$ then $-(c + -(b + a)) = a$                            |                             | - | 11 | 1.5 | - | 100% |
| -1     | Lemma 3.3, RA2  |  | [Win90, LW92]               | - | 11 | 1.5 | - | 100% |
| ROB011 | Eqn3Base  | If $-(a + -b) = c$ then $-(a + -(b + k(a + c))) = c, k=1$                |                             | - | 19 | 1.7 | - | 81%  |
| -1     | Lemma 3.4   |  | [Win90]                     | - | 19 | 1.7 | - | 81%  |
| ROB012 | Eqn3Indn  | If $-(a + -b) = c$ then $-(a + -(b + k(a + c))) = c, k=k + 1$            |                             | - | 21 | 1.6 | - | 79%  |
| -1     | Lemma 3.4   |  | [Win90]                     | - | 22 | 1.6 | - | 80%  |
| -2     | Lemma 3.4   |  | [Win90]                     | - | 22 | 1.6 | - | 80%  |
| ROB013 | Eqn4  | If $-(a + b) = c$ then $-(c + -(b + a)) = a$                             |                             | - | 11 | 1.5 | - | 100% |
| -1     | Lemma 3.5   |  | [Win90]                     | - | 11 | 1.5 | - | 100% |
| ROB014 | Eqn5Base  | If $-(-e + -(d + -e)) = d$ then $-(e + k(d + -(d + -e))) = -e, k=1$      |                             | - | 19 | 1.7 | - | 81%  |
| -1     | Lemma 3.6   |  | [Win90]                     | - | 21 | 1.8 | - | 81%  |
| -2     | Lemma 3.6   |  | [Win90]                     | - | 21 | 1.8 | - | 81%  |
| ROB015 | Eqn5Indn  | If $-(-e + -(d + -e)) = d$ then $-(e + k(d + -(d + -e))) = -e, k=k+1$    |                             | - | 21 | 1.6 | - | 79%  |
| -1     | Lemma 3.6   |  | [Win90]                     | - | 23 | 1.7 | - | 79%  |
| -2     | Lemma 3.6   |  | [Win90]                     | - | 23 | 1.7 | - | 79%  |
| ROB016 | Eqn6  | If $-(d + e) = -e$ then $-(e + k(d + -(d + -e))) = -e, \text{ for } k>0$ |                             | - | 21 | 1.7 | - | 77%  |
| -1     | Corollary 3.7   |  | [Win90]                     | - | 21 | 1.7 | - | 77%  |
| ROB017 | Absb1   | If $-(2f + h) = -(3f + h) = -h$ then $2f + h = 3f + h$                   |                             | - | 13 | 1.5 | - | 100% |
| -1     | Lemma 3.8   |  | [Win90]                     | - | 13 | 1.5 | - | 100% |

| Syntactic name<br>V# | Semantic name<br>Other names                 | Description<br>References  | V | Cl | Av  | nH | Eq   |
|----------------------|--|--|---|----|-----|----|------|
| ROB018<br>-1         | Absb2<br>Corollary 3.9                       | If $-(d + e) = -e$ then $e + 2(d + -(d + -e))$ absorbs $d + -(d + -e)$<br>[Win90]            | - | 19 | 1.7 | -  | 81%  |
| ROB019<br>-1         | Absb3<br>Corollary 3.9                       | A complex absorption condition<br>[Win90]  | - | 19 | 1.7 | -  | 81%  |
| ROB020<br>-1<br>-2   | RobBool7<br>Corollary 3.10<br>Corollary 3.10 | $-(a + -b) = b \Rightarrow$ Boolean<br>[HMT71, Win90]<br>[HMT71, Win90]                      | - | 11 | 1.5 | -  | 100% |
| ROB021<br>-1         | RobBool8                                     | $(-X = -Y) \Rightarrow (X = Y) \Rightarrow$ Boolean<br>[HMT71, Win90, McC92b]                | - | 11 | 1.6 | -  | 100% |
| ROB022<br>-1         | RobBool9                                     | $c + -c = c \Rightarrow$ Boolean<br>[HMT71, Win90, McC92b]                                   | - | 11 | 1.5 | -  | 100% |
| ROB023<br>-1         | RobBool10<br>Robbins                         | $X + X = X \Rightarrow$ Boolean<br>[HMT71, Win90, LM92, McC92b]                              | - | 11 | 1.5 | -  | 100% |
| ROB024<br>-1         | RobBool11<br>RA-1                            | $-(a + (a + b)) + -(a + -b) = a \Rightarrow$ Boolean<br>[Win90, WWM <sup>+</sup> 90]         | - | 11 | 1.5 | -  | 100% |
| ROB025<br>-1         | RobBool12<br>RA-2                            | $-(X + Y) = \text{intersection}(-X, -Y) \Rightarrow$ Boolean<br>[Win90, WWM <sup>+</sup> 90] | - | 11 | 1.5 | -  | -    |
| ROB026<br>-1         | RobBool13                                    | $c + d = c \Rightarrow$ Boolean<br>[HMT71, Win90, Wos94b]                                    | - | 11 | 1.5 | -  | 100% |
| ROB027<br>-1         | RobBool14                                    | $-(-c) = c \Rightarrow$ Boolean<br>[HMT71, Win90, Wos94b]                                    | - | 11 | 1.5 | -  | 100% |

Domain SET (562 abstract problems, 695 problems)

|                                      |   |  |   |     |     |     |     |
|--------------------------------------|---|--|---|-----|-----|-----|-----|
| SET001<br>-1                         | SupSE1<br>ls100, ls100                                      | Set members are superset members<br>[LS74, WM76]   | - | 9   | 1.9 | 11% | -   |
| SET002<br>-1                         | UnionEqS<br>ls103, ls103                                    | A set union itself is itself<br>[LS74, WM76]   | - | 14  | 2.6 | 21% | -   |
| SET003<br>-1                         | SubSUnion1<br>ls105, ls105                                  | A set is a subset of the union of itself with itself<br>[LS74, WM76]   | - | 14  | 2.6 | 21% | -   |
| SET004<br>-1                         | SubSUnion2<br>ls106, ls106                                  | A set is a subset of the union of itself and another set<br>[LS74, WM76]   | - | 14  | 2.6 | 21% | -   |
| SET005<br>-1                         | IntscAssc<br>ls108, ls108                                   | Associativity of set intersection<br>[LS74, WM76]  | - | 16  | 2.4 | 18% | -   |
| SET006<br>-1                         | IntscSubS<br>ls111, ls111                                   | Intersection is a subset<br>[LS74, WM76]   | - | 14  | 2.6 | 21% | -   |
| SET007<br>-1                         | IntscUnion<br>ls112, ls112                                  | Intersection distributes over union<br>[LS74, WM76]  | - | 23  | 2.6 | 21% | -   |
| SET008<br>-1                         | DiffE1<br>ls115, ls115                                      | Difference contains no operand elements<br>[LS74, WM76]  | - | 21  | 2.7 | 33% | -   |
| SET009<br>-1                         | SubSEqn<br>ls116, ls116                                     | If $d$ is a subset of $a$ , then $b-a$ is a subset of $b-d$<br>[LS74, WM76]  | - | 16  | 2.4 | 31% | -   |
| SET010<br>-1                         | UnionEqn<br>ls118, ls118                                    | $c-a$ union $c-b$ equals $c$ -(the intersection of $a$ and $b$ )<br>[LS74, WM76]   | - | 29  | 2.7 | 31% | -   |
| SET011<br>-1                         | DiffIntsc<br>ls121, ls121                                   | A property of difference and intersection<br>[LS74, WM76]  | - | 21  | 2.7 | 33% | -   |
| SET012<br>-1<br>-2<br>-3<br>-4       | CpmtIvln<br>S1, EST-S1<br>compl.ver1.in<br>compl.ver2.in    | Complement is an involution<br>[MOW76, WB87]<br>[MOW76]<br>[BLM <sup>+</sup> 86]<br>[BLM <sup>+</sup> 86]                                    | - | 33  | 2.2 | 9%  | -   |
| SET013<br>-1<br>-2<br>-3<br>-4       | IntscComm<br>S2, EST-S2<br>inters.ver1.in<br>inters.ver2.in | The intersection of sets is commutative<br>[MOW76, WB87]<br>[MOW76]<br>[BLM <sup>+</sup> 86]<br>[BLM <sup>+</sup> 86]                        | - | 33  | 2.2 | 9%  | -   |
| SET014<br>-2<br>-3<br>-4             | UnionOfSubS<br>S4, subset.ver1.in, EST-S4<br>subset.ver2.in | Union of subsets is a subset<br>[MOW76, WB87]<br>[BLM <sup>+</sup> 86]<br>[BLM <sup>+</sup> 86]  | - | 35  | 2.1 | 8%  | -   |
| SET015<br>-1<br>-2<br>-3<br>-4       | UnionComm<br>S3, EST-S3<br>union.ver1.in<br>union.ver2.in   | The union of sets is commutative<br>[MOW76, WB87]<br>[MOW76]<br>[BLM <sup>+</sup> 86]<br>[BLM <sup>+</sup> 86]                               | - | 33  | 2.2 | 9%  | -   |
| SET016<br>-1<br>-3<br>-6<br>-7       | 1stCpntsEq<br>NU3.1<br>Lemma 1<br>OP4, OP10                 | First components of equal ordered pairs are equal<br>[LW91, LW92]<br>[BLM <sup>+</sup> 86]<br>[Qua92a]<br>[Qua92a]                           | - | 18  | 1.8 | 5%  | 72% |
| SET017<br>-3<br>-4<br>-6<br>-7       | UOrdPrLCanc<br>Lemma 2<br>Lemma 2<br>UP4                    | Left cancellation for non-ordered pairs<br>[BLM <sup>+</sup> 86]<br>[BLM <sup>+</sup> 86]<br>[Qua92a]<br>[Qua92a]                            | - | 271 | 2.4 | 7%  | 43% |
| SET018<br>-1<br>-3<br>-4<br>-6<br>-7 | 2ndCpntsEq<br>NU3.2<br>Lemma 3<br>Lemma 3<br>OP5, OP11      | Second components of equal ordered pairs are equal<br>[LW91, LW92]<br>[BLM <sup>+</sup> 86]<br>[BLM <sup>+</sup> 86]<br>[Qua92a]<br>[Qua92a] | - | 18  | 1.8 | 5%  | 72% |
| SET019<br>-3<br>-4                   | SetsEq<br>Lemma 4<br>Lemma 4                                | Two sets that contain one another are equal<br>[BLM <sup>+</sup> 86]<br>[BLM <sup>+</sup> 86]  | - | 272 | 2.4 | 7%  | 43% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References                                | V | Cl  | Av  | nH  | Eq  |
|----------------------|------------------------------|--|---|-----|-----|-----|-----|
| SET020               | 1stUnq                       | 1st is unique when x is an ordered pair of sets          |   |     |     |     |     |
| -3                   | Lemma 5                      | [BLM <sup>+</sup> 86]                                    | - | 273 | 2.4 | 7%  | 43% |
| -4                   | Lemma 5                      | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| -6                   |                              | [Qua92a]   | - | 161 | 2.1 | 4%  | 48% |
| -7                   | OP7.1                        | [Qua92a]   | - | 229 | 2.1 | 13% | 47% |
| SET021               | 2ndUnq                       | 2nd is unique when x is an ordered pair of sets          |   |     |     |     |     |
| -3                   | Lemma 6                      | [BLM <sup>+</sup> 86]                                    | - | 274 | 2.4 | 7%  | 43% |
| -4                   | Lemma 6                      | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| -6                   |                              | [Qua92a]   | - | 161 | 2.1 | 4%  | 48% |
| -7                   | OP7.2                        | [Qua92a]   | - | 229 | 2.1 | 13% | 47% |
| SET022               | 1stCpntSet                   | The first component of an ordered pair is a little set   |   |     |     |     |     |
| -3                   | Lemma 7                      | [BLM <sup>+</sup> 86]                                    | - | 274 | 2.4 | 7%  | 43% |
| -4                   | Lemma 7                      | [BLM <sup>+</sup> 86]                                    | - | 268 | 2.4 | 7%  | 43% |
| SET023               | 2ndCpntSet                   | The second component of an ordered pair is a little set  |   |     |     |     |     |
| -3                   | Lemma 8                      | [BLM <sup>+</sup> 86]                                    | - | 275 | 2.4 | 7%  | 43% |
| -4                   | Lemma 8                      | [BLM <sup>+</sup> 86]                                    | - | 268 | 2.4 | 7%  | 43% |
| SET024               | SetInSgtn                    | A set belongs to its singleton                           |   |     |     |     |     |
| -3                   | Lemma 9                      | [BLM <sup>+</sup> 86]                                    | - | 276 | 2.4 | 7%  | 42% |
| -4                   | Lemma 9                      | [BLM <sup>+</sup> 86]                                    | - | 268 | 2.4 | 7%  | 43% |
| -6                   |                              | [Qua92a]   | - | 161 | 2.1 | 4%  | 47% |
| -7                   | SS2                          | [Qua92a]   | - | 191 | 2.1 | 7%  | 45% |
| SET025               | OrdPrSet                     | Ordered pairs are little sets                            |   |     |     |     |     |
| -3                   | Lemma 10                     | [BLM <sup>+</sup> 86]                                    | - | 276 | 2.4 | 7%  | 42% |
| -4                   | Lemma 10                     | [BLM <sup>+</sup> 86]                                    | - | 267 | 2.4 | 7%  | 43% |
| -6                   |                              | [Qua92a]   | - | 160 | 2.1 | 5%  | 48% |
| -7                   | OP1                          | [Qua92a]   | - | 215 | 2.1 | 11% | 47% |
| -8                   | Lemma 11                     | [BLM <sup>+</sup> 86]                                    | - | 278 | 2.4 | 7%  | 42% |
| -9                   | Lemma 11                     | [BLM <sup>+</sup> 86]                                    | - | 268 | 2.4 | 7%  | 43% |
| SET027               | SubSTrans                    | Transitivity of subset                                   |   |     |     |     |     |
| -3                   | Lemma 12                     | [BLM <sup>+</sup> 86]                                    | - | 280 | 2.4 | 7%  | 42% |
| -4                   | Lemma 12                     | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| -6                   |                              | [Qua92a]   | - | 162 | 2.1 | 4%  | 47% |
| -7                   | PO3                          | [Qua92a]   | - | 167 | 2.1 | 4%  | 46% |
| SET028               | Apply_Img1                   | Relationship between apply and image, part 1 of 2        |   |     |     |     |     |
| -3                   | Lemma 13                     | [BLM <sup>+</sup> 86]                                    | - | 279 | 2.4 | 7%  | 42% |
| -4                   | Lemma 13                     | [BLM <sup>+</sup> 86]                                    | - | 267 | 2.4 | 7%  | 43% |
| SET029               | Apply_Img2                   | Relationship between apply and image, part 2 of 2        |   |     |     |     |     |
| -3                   | Lemma 14                     | [BLM <sup>+</sup> 86]                                    | - | 280 | 2.4 | 7%  | 42% |
| -4                   | Lemma 14                     | [BLM <sup>+</sup> 86]                                    | - | 267 | 2.4 | 7%  | 43% |
| SET030               | FuncValSet                   | Function values are little sets                          |   |     |     |     |     |
| -3                   | Lemma 15                     | [BLM <sup>+</sup> 86]                                    | - | 282 | 2.4 | 7%  | 42% |
| -4                   | Lemma 15                     | [BLM <sup>+</sup> 86]                                    | - | 268 | 2.4 | 7%  | 43% |
| -6                   | AP8                          | [Qua92a]   | - | 189 | 2.1 | 4%  | 46% |
| SET031               | CpsnRel                      | The composition of two sets is a relation                |   |     |     |     |     |
| -3                   | Lemma 16                     | [BLM <sup>+</sup> 86]                                    | - | 282 | 2.4 | 7%  | 42% |
| -4                   | Lemma 16                     | [BLM <sup>+</sup> 86]                                    | - | 267 | 2.4 | 7%  | 43% |
| SET032               | RngCpsn                      | Range of composition                                     |   |     |     |     |     |
| -3                   | Lemma 17                     | [BLM <sup>+</sup> 86]                                    | - | 283 | 2.4 | 7%  | 42% |
| -4                   | Lemma 17                     | [BLM <sup>+</sup> 86]                                    | - | 267 | 2.4 | 7%  | 43% |
| -6                   | CO6.3                        | [Qua92a]   | - | 188 | 2.1 | 4%  | 46% |
| SET033               | DomCpsn                      | Domain of composition                                    |   |     |     |     |     |
| -3                   | Lemma 18                     | [BLM <sup>+</sup> 86]                                    | - | 285 | 2.4 | 7%  | 42% |
| -4                   | Lemma 18                     | [BLM <sup>+</sup> 86]                                    | - | 268 | 2.4 | 7%  | 43% |
| -6                   | CO9                          | [Qua92a]   | - | 189 | 2.1 | 4%  | 46% |
| SET034               | CpsnFuncs                    | The composition of functions is a function               |   |     |     |     |     |
| -3                   | Lemma 19                     | [BLM <sup>+</sup> 86]                                    | - | 287 | 2.4 | 6%  | 41% |
| -4                   | Lemma 19                     | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| -6                   | FU6                          | [Qua92a]   | - | 190 | 2.0 | 4%  | 46% |
| SET035               | MapCpsn                      | Maps for composition                                     |   |     |     |     |     |
| -3                   | Lemma 20                     | [BLM <sup>+</sup> 86]                                    | - | 288 | 2.4 | 6%  | 41% |
| -4                   | Lemma 20                     | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| -6                   | MA1                          | [Qua92a]   | - | 190 | 2.0 | 4%  | 46% |
| SET036               | ApplyFunc1                   | Properties of apply for functions, part 1 of 3           |   |     |     |     |     |
| -3                   | Lemma 21                     | [BLM <sup>+</sup> 86]                                    | - | 291 | 2.3 | 6%  | 41% |
| -4                   | Lemma 21                     | [BLM <sup>+</sup> 86]                                    | - | 271 | 2.3 | 7%  | 43% |
| -6                   | AP9                          | [Qua92a]   | - | 191 | 2.0 | 4%  | 46% |
| SET037               | ApplyFunc2                   | Properties of apply for functions, part 2 of 3           |   |     |     |     |     |
| -3                   | Lemma 22                     | [BLM <sup>+</sup> 86]                                    | - | 291 | 2.4 | 6%  | 41% |
| -4                   | Lemma 22                     | [BLM <sup>+</sup> 86]                                    | - | 270 | 2.3 | 7%  | 43% |
| -6                   | AP10                         | [Qua92a]   | - | 190 | 2.0 | 4%  | 46% |
| SET038               | ApplyFunc3                   | Properties of apply for functions, part 3 of 3           |   |     |     |     |     |
| -3                   | Lemma 23                     | [BLM <sup>+</sup> 86]                                    | - | 291 | 2.4 | 6%  | 41% |
| -4                   | Lemma 23                     | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| -6                   | MA2                          | [Qua92a]   | - | 190 | 2.0 | 4%  | 46% |
| SET039               | ApplyCpsn1                   | Properties of apply for composition of functions, 1 of 3 |   |     |     |     |     |
| -3                   | Lemma 24                     | [BLM <sup>+</sup> 86]                                    | - | 292 | 2.4 | 6%  | 41% |
| -4                   | Lemma 24                     | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| SET040               | ApplyCpsn2                   | Properties of apply for composition of functions, 2 of 3 |   |     |     |     |     |
| -3                   | Lemma 25                     | [BLM <sup>+</sup> 86]                                    | - | 292 | 2.4 | 6%  | 41% |
| -4                   | Lemma 25                     | [BLM <sup>+</sup> 86]                                    | - | 268 | 2.4 | 7%  | 43% |
| -6                   | AP12                         | [Qua92a]   | - | 189 | 2.1 | 4%  | 46% |
| SET041               | ApplyCpsn3                   | Properties of apply for composition of functions, 3 of 3 |   |     |     |     |     |
| -3                   | Lemma 26                     | [BLM <sup>+</sup> 86]                                    | - | 294 | 2.4 | 6%  | 41% |
| -4                   | Lemma 26                     | [BLM <sup>+</sup> 86]                                    | - | 269 | 2.3 | 7%  | 43% |
| -6                   | AP11                         | [Qua92a]   | - | 190 | 2.0 | 4%  | 46% |



| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References                                   | V | Cl  | Av  | nH  | Eq  |
|----------------------|------------------------------|---|---|-----|-----|-----|-----|
| SET042               | OrdPrXProd                   | Ordered pairs are in cross products                         | - | 295 | 2.4 | 6%  | 40% |
| -3                   | Lemma 27                     | [BLM <sup>+</sup> 86]                                       | - | 269 | 2.3 | 7%  | 43% |
| -4                   | Lemma 27                     | [BLM <sup>+</sup> 86]                                       |   |     |     |     |     |
| SET043               | Russell                      | Russell's Paradox   | - | 2   | 2.0 | 50% | -   |
| -5                   | Pelletier 39, p39.in         | [Pel86]   |   |     |     |     |     |
| SET044               | ARussellSet                  | Anti-Russell Sets   | - | 4   | 2.0 | 25% | -   |
| -5                   | Pelletier 40, p40.in         | [Pel86, Pel88]  |   |     |     |     |     |
| SET045               | NotUnivSet                   | No Universal Set  | - | 4   | 2.0 | 25% | -   |
| -5                   | Pelletier 41, p41.in         | [Pel86]   |   |     |     |     |     |
| SET046               | NotCirc                      | No set of non-circular sets                                 | - | 3   | 2.3 | 66% | -   |
| -5                   | Pelletier 42, p42.in         | [Pel86]   |   |     |     |     |     |
| SET047               | EqSymm                       | Set equality is symmetric                                   | - | 6   | 2.7 | 33% | -   |
| -5                   | Pelletier 43, p43.in         | [Cha79, Pel86]  |   |     |     |     |     |
| SET050               | UnOrdPrAxCor1                | Corollary to Unordered pair axiom                           | - | 161 | 2.1 | 4%  | 47% |
| -6                   |                              | [Qua92a]  |   |     |     |     |     |
| SET051               | UnOrdPrAxCor2                | Corollary to Unordered pair axiom                           | - | 161 | 2.1 | 4%  | 47% |
| -6                   |                              | [Qua92a]  |   |     |     |     |     |
| SET052               | XProdAxCor1                  | Corollary to Cartesian product axiom                        | - | 161 | 2.1 | 4%  | 47% |
| -6                   |                              | [Qua92a]  |   |     |     |     |     |
| SET053               | XProdAxCor2                  | Corollary to Cartesian product axiom                        | - | 161 | 2.1 | 4%  | 47% |
| -6                   |                              | [Qua92a]  |   |     |     |     |     |
| SET054               | SubCRef1                     | Subclass is reflexive                                       | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 164 | 2.1 | 4%  | 46% |
| -7                   | PO1                          | [Qua92a]  |   |     |     |     |     |
| SET055               | EqRef1                       | Equality is reflexive                                       | - | 159 | 2.1 | 5%  | -   |
| -6                   |                              | [Qua92a]  | - | 165 | 2.1 | 4%  | -   |
| -7                   | EQ1                          | [Qua92a]  |   |     |     |     |     |
| SET056               | EqDef1                       | Expanded equality definition                                | - | 162 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 168 | 2.1 | 4%  | 46% |
| -7                   | EQ2.1                        | [Qua92a]  |   |     |     |     |     |
| SET057               | EqDef2                       | Expanded equality definition                                | - | 162 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 168 | 2.1 | 4%  | 46% |
| -7                   | EQ2.2                        | [Qua92a]  |   |     |     |     |     |
| SET058               | EqDef3                       | Expanded equality definition                                | - | 162 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 168 | 2.1 | 4%  | 46% |
| -7                   | EQ2.3                        | [Qua92a]  |   |     |     |     |     |
| SET059               | EqDef4                       | Expanded equality definition                                | - | 162 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 168 | 2.1 | 4%  | 46% |
| -7                   | EQ2.4                        | [Qua92a]  |   |     |     |     |     |
| SET060               | IntscEmpty                   | Nothing in the intersection of a set and its complement     | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 170 | 2.1 | 6%  | 45% |
| -7                   | SP1                          | [Qua92a]  |   |     |     |     |     |
| SET061               | NullCIEx                     | Existence of the null class                                 | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 171 | 2.1 | 6%  | 45% |
| -7                   | SP2                          | [Qua92a]  |   |     |     |     |     |
| SET062               | NullCISubC1                  | The null class is a subclass of every class                 | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 172 | 2.1 | 6%  | 45% |
| -7                   | SP3                          | [Qua92a]  |   |     |     |     |     |
| SET063               | NullCISubCICor1              | Corollary to the null class being a subclass of every class | - | 161 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 174 | 2.1 | 6%  | 45% |
| -7                   | SP3 cor.                     | [Qua92a]  |   |     |     |     |     |
| SET064               | NullCIUnq                    | The null class is unique                                    | - | 161 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 175 | 2.1 | 6%  | 45% |
| -7                   | SP4                          | [Qua92a]  |   |     |     |     |     |
| SET065               | NullCISet                    | The null class is a set                                     | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 175 | 2.1 | 6%  | 45% |
| -7                   | SP5                          | [Qua92a]  |   |     |     |     |     |
| SET066               | UOrdPrComm                   | Unordered pair is commutative                               | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 176 | 2.1 | 6%  | 45% |
| -7                   | UP1                          | [Qua92a]  |   |     |     |     |     |
| SET067               | UOrdPrArg1                   | Proper class in an unordered pair, part 1                   | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 177 | 2.1 | 6%  | 45% |
| -7                   | UP2.1                        | [Qua92a]  |   |     |     |     |     |
| SET068               | UOrdPrArg2                   | Proper class in an unordered pair, part 2                   | - | 160 | 2.1 | 5%  | 48% |
| -6                   |                              | [Qua92a]  | - | 177 | 2.1 | 6%  | 45% |
| -7                   | UP2.2                        | [Qua92a]  |   |     |     |     |     |
| SET069               | UOrdPrArg3                   | Proper class in an unordered pair, part 3                   | - | 161 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 178 | 2.1 | 6%  | 45% |
| -7                   | UP2.3                        | [Qua92a]  |   |     |     |     |     |
| SET070               | UOrdPrArg4                   | Proper class in an unordered pair, part 4                   | - | 161 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 178 | 2.1 | 6%  | 45% |
| -7                   | UP2.4                        | [Qua92a]  |   |     |     |     |     |
| SET071               | NullUOrdPr                   | Null unordered pair   | - | 162 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 183 | 2.0 | 7%  | 45% |
| -7                   | UP3                          | [Qua92a]  |   |     |     |     |     |
| SET072               | UOrdPrRCanc                  | Right cancellation for unordered pairs                      | - | 162 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 185 | 2.1 | 8%  | 45% |
| -7                   | UP5                          | [Qua92a]  |   |     |     |     |     |
| SET073               | UnOrdPrAxCor3                | Corollary to unordered pair axiom                           | - | 161 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 185 | 2.1 | 8%  | 45% |
| -7                   | UP6.1                        | [Qua92a]  |   |     |     |     |     |
| SET074               | UnOrdPrAxCor4                | Corollary to unordered pair axiom                           | - | 161 | 2.1 | 4%  | 48% |
| -6                   |                              | [Qua92a]  | - | 185 | 2.1 | 8%  | 45% |
| -7                   | UP6.2                        | [Qua92a]  |   |     |     |     |     |

| Syntactic name<br>V# | Semantic name<br>Other names           | Description<br>References   | V | Cl  | Av  | nH | Eq  |
|----------------------|--|---|---|-----|-----|----|-----|
| SET075<br>-6<br>-7   | UnOrdPrAxCor5<br>UP6 cor.              | Corollary to unordered pair axiom<br>[Qua92a]<br>[Qua92a]                           | - | 161 | 2.1 | 4% | 48% |
| SET076<br>-6<br>-7   | UOrdPrSubS<br>UP7                      | Unorderd pair is a subset<br>[Qua92a]<br>[Qua92a]                                   | - | 162 | 2.1 | 4% | 47% |
| SET077<br>-6<br>-7   | SgtnSet<br>SS1                         | Every singleton is a set<br>[Qua92a]<br>[Qua92a]                                    | - | 160 | 2.1 | 5% | 48% |
| SET078<br>-6<br>-7   | SgtnSetCor1<br>SS1 cor.                | Corollary to every singleton is a set<br>[Qua92a]<br>[Qua92a]                       | - | 160 | 2.1 | 5% | 48% |
| SET079<br>-6<br>-7   | SetInSgtnCor1<br>SS2 cor.<br>SS2 cor.1 | Corollary to a set belongs to its singleton<br>[Qua92a]<br>[Qua92a]                 | - | 161 | 2.1 | 4% | 48% |
| SET080<br>-6<br>-7   | SetInSgtnCor2<br>SS2 cor.2             | Corollary to a set belongs to its singleton<br>[Qua92a]<br>[Qua92a]                 | - | 160 | 2.1 | 5% | 48% |
| SET081<br>-6<br>-7   | EIOFSgtn<br>SS3                        | Only the element can belong to its singleton<br>[Qua92a]<br>[Qua92a]                | - | 161 | 2.1 | 4% | 48% |
| SET082<br>-6<br>-7   | SngtOfNonSet<br>SS4                    | The singleton of a non-set is the null class<br>[Qua92a]<br>[Qua92a]                | - | 161 | 2.1 | 4% | 48% |
| SET083<br>-6<br>-7   | SgtnDepE11<br>SS5.1                    | A singleton set depends on its element, part 1<br>[Qua92a]<br>[Qua92a]              | - | 162 | 2.1 | 4% | 48% |
| SET084<br>-6<br>-7   | SgtnDepE12<br>SS5.2                    | A singleton set depends on its element, part 2<br>[Qua92a]<br>[Qua92a]              | - | 162 | 2.1 | 4% | 48% |
| SET085<br>-6<br>-7   | UOrdPrSgtn<br>SS5.5                    | Unordered pair that is a singleton<br>[Qua92a]<br>[Qua92a]                          | - | 163 | 2.1 | 4% | 48% |
| SET086<br>-6<br>-7   | SgtnE11<br>SS6.1                       | A singleton set has a member, part 1<br>[Qua92a]<br>[Qua92a]                        | - | 162 | 2.1 | 4% | 48% |
| SET087<br>-6<br>-7   | SgtnE12<br>SS6.2                       | A singleton set has a member, part 2<br>[Qua92a]<br>[Qua92a]                        | - | 162 | 2.1 | 4% | 48% |
| SET088<br>-6<br>-7   | SgtnE13<br>SS6.3                       | A singleton set has a member, part 3<br>[Qua92a]<br>[Qua92a]                        | - | 162 | 2.1 | 4% | 48% |
| SET089<br>-6<br>-7   | SgtnE14<br>SS6.4                       | A singleton set has a member, part 4<br>[Qua92a]<br>[Qua92a]                        | - | 162 | 2.1 | 4% | 48% |
| SET090<br>-6<br>-7   | SgtnE1Unq<br>SS7                       | The member of a singleton set is unique<br>[Qua92a]<br>[Qua92a]                     | - | 162 | 2.1 | 4% | 48% |
| SET091<br>-6<br>-7   | MembUnq1<br>SS8.1                      | Member_of(X) is unique if X is not a singleton, part 1<br>[Qua92a]<br>[Qua92a]      | - | 163 | 2.1 | 4% | 48% |
| SET092<br>-6<br>-7   | MembUnq2<br>SS8.2                      | Member_of(X) is unique if X is not a singleton, part 2<br>[Qua92a]<br>[Qua92a]      | - | 163 | 2.1 | 4% | 49% |
| SET093<br>-6<br>-7   | SgtnSetCor2<br>SS9                     | Corollary to every singleton is a set<br>[Qua92a]<br>[Qua92a]                       | - | 162 | 2.1 | 4% | 48% |
| SET094<br>-6<br>-7   | SgtnEqn1<br>SS10<br>SS10               | Property 1 of singleton sets<br>[Qua92a]<br>[Qua92a]                                | - | 163 | 2.1 | 4% | 48% |
| SET095<br>-6<br>-7   | SgtnEqn2<br>SS11<br>SS11               | Property 2 of singleton sets<br>[Qua92a]<br>[Qua92a]                                | - | 161 | 2.1 | 4% | 47% |
| SET096<br>-6<br>-7   | SubSOFSgtn<br>SS12<br>SS12             | There are at most two subsets of a singleton set<br>[Qua92a]<br>[Qua92a]            | - | 162 | 2.1 | 4% | 48% |
| SET097<br>-6<br>-7   | ClElEx<br>SS13<br>SS13                 | A class contains 0, 1, or at least 2 members<br>[Qua92a]<br>[Qua92a]                | - | 162 | 2.1 | 4% | 48% |
| SET098<br>-6<br>-7   | ClElExCor1<br>SS13 cor.<br>SS13 cor.1  | Corollary 1 to a class contains 0, 1, or at least 2 members<br>[Qua92a]<br>[Qua92a] | - | 162 | 2.1 | 4% | 48% |
| SET099<br>-6<br>-7   | ClElExCor2<br>SS13<br>SS13 cor.2       | Corollary 2 to a class contains 0, 1, or at least 2 members<br>[Qua92a]<br>[Qua92a] | - | 162 | 2.1 | 4% | 48% |
| SET100<br>-6<br>-7   | SgtnOrdPr<br>SS14                      | The relationship of singleton sets to ordered pairs<br>[Qua92a]<br>[Qua92a]         | - | 160 | 2.1 | 5% | 48% |
| SET101<br>-6<br>-7   | SgtnElOrdPr<br>OP2.1                   | Singleton of the first is a member of an ordered pair<br>[Qua92a]<br>[Qua92a]       | - | 160 | 2.1 | 5% | 48% |
| SET102<br>-6<br>-7   | OrdPrElOrdPr<br>OP2.2                  | Ordered pair member of ordered pair<br>[Qua92a]<br>[Qua92a]                         | - | 160 | 2.1 | 5% | 48% |

| Syntactic name | Semantic name    | Description  | V | Cl  | Av  | nH  | Eq  |
|----------------|------------------|--|---|-----|-----|-----|-----|
| V#             | Other names      | References   |   |     |     |     |     |
| SET103         | OrdPrE11         | Special member 1 of an ordered pair                          | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 219 | 2.1 | 11% | 47% |
| -7             | OP3.1            | [Qua92a]   |   |     |     |     |     |
| SET104         | OrdPrE12         | Special member 2 of an ordered pair                          | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 219 | 2.1 | 11% | 47% |
| -7             | OP3.2            | [Qua92a]   |   |     |     |     |     |
| SET105         | OrdPrE13         | Special member 3 of an ordered pair                          | - | 162 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 220 | 2.1 | 11% | 46% |
| -7             | OP3.3            | [Qua92a]   |   |     |     |     |     |
| SET108         | 1st2ndOrdPr      | 1st and 2nd make the ordered pair                            | - | 161 | 2.1 | 4%  | 47% |
| -6             |                  | [Qua92a, Qua92b]   | - | 224 | 2.1 | 12% | 46% |
| -7             | OP6.1            | [Qua92a, Qua92b]   |   |     |     |     |     |
| SET109         | 1stOrdPr1        | 1st is the ordered pair, first condition                     | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 224 | 2.1 | 12% | 47% |
| -7             | OP6.2            | [Qua92a]   |   |     |     |     |     |
| SET110         | 2ndOrdPr1        | 2nd is the ordered pair, first condition                     | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 224 | 2.1 | 12% | 47% |
| -7             | OP6.3            | [Qua92a]   |   |     |     |     |     |
| SET111         | 1stOrdPr2        | 1st is the ordered pair, second condition                    | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 224 | 2.1 | 12% | 47% |
| -7             | OP6.4            | [Qua92a]   |   |     |     |     |     |
| SET112         | 2ndOrdPr2        | 2nd is the ordered pair, second condition                    | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 224 | 2.1 | 12% | 47% |
| -7             | OP6.5            | [Qua92a]   |   |     |     |     |     |
| SET113         | 1stUnq1          | 1st is unique if x is not an ordered pair of sets, part 1    | - | 163 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 233 | 2.1 | 13% | 47% |
| -7             | OP8.1            | [Qua92a]   |   |     |     |     |     |
| SET114         | 2ndUnq1          | 2nd is unique if x is not an ordered pair of sets, part 1    | - | 163 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 233 | 2.1 | 13% | 47% |
| -7             | OP8.2            | [Qua92a]   |   |     |     |     |     |
| SET115         | 1stUnq2          | 1st is unique if x is not an ordered pair of sets, part 2    | - | 163 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   | - | 233 | 2.1 | 13% | 48% |
| -7             | OP8.3            | [Qua92a]   |   |     |     |     |     |
| SET116         | 2ndUnq2          | 2nd is unique if x is not an ordered pair of sets, part 2    | - | 163 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   | - | 233 | 2.1 | 13% | 48% |
| -7             | OP8.4            | [Qua92a]   |   |     |     |     |     |
| SET117         | OrdPrSetCor1     | Corollary 1 to every ordered pair being a set                | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 237 | 2.1 | 15% | 48% |
| -7             | OP9.1            | [Qua92a]   |   |     |     |     |     |
| SET118         | OrdPrSetCor2     | Corollary 2 to every ordered pair being a set                | - | 161 | 2.1 | 4%  | 47% |
| -6             |                  | [Qua92a]   | - | 237 | 2.1 | 15% | 48% |
| -7             | OP9.2            | [Qua92a]   |   |     |     |     |     |
| SET119         | OrdPrCpntsEqCor1 | Corollary 1 to components of equal ordered pairs being equal | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 239 | 2.1 | 15% | 48% |
| -7             | OP10 cor.1       | [Qua92a]   |   |     |     |     |     |
| SET120         | OrdPrCpntsEqCor2 | Corollary 2 to components of equal ordered pairs being equal | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 239 | 2.1 | 15% | 48% |
| -7             | OP10 cor.2       | [Qua92a]   |   |     |     |     |     |
| SET121         | OrdPrCpntsEqCor3 | Corollary 3 to components of equal ordered pairs being equal | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 241 | 2.1 | 15% | 48% |
| -7             | OP11 cor.1       | [Qua92a]   |   |     |     |     |     |
| SET122         | OrdPrCpntsEqCor4 | Corollary 4 to components of equal ordered pairs being equal | - | 161 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   | - | 241 | 2.1 | 15% | 48% |
| -7             | OP11 cor.2       | [Qua92a]   |   |     |     |     |     |
| SET123         | SetBAltDef1      | Alternative definition of set builder, part 1                | - | 165 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET124         | SetBAltDef2      | Alternative definition of set builder, part 2                | - | 164 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET125         | SetBAltDef3      | Alternative definition of set builder, part 3                | - | 164 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET126         | SetB_Sgtn        | Relation to singleton  | - | 163 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET127         | SetB_UOrdPr      | Relation to unordered pair                                   | - | 163 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET128         | SetB3            | Building a triple  | - | 163 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET129         | SetB3E1          | Membership in a built unordered triple                       | - | 166 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET130         | SetB3E11         | Membership in unordered triple, part 1                       | - | 164 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET131         | SetB3E12         | Membership in unordered triple, part 2                       | - | 164 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET132         | SetB3E13         | Membership in unordered triple, part 3                       | - | 164 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET133         | SetB3Cor1        | Corollary 1 to membership in unordered triple                | - | 166 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET134         | SetB3Cor2        | Corollary 2 to membership in unordered triple                | - | 164 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET135         | SetB3Cor3        | Corollary 3 to membership in unordered triple                | - | 164 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET136         | SetB3Cor4        | Corollary 4 to membership in unordered triple                | - | 164 | 2.1 | 4%  | 49% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |
| SET137         | SetB3Fix1        | Kludge 1 to instantiate variables in unordered triples       | - | 166 | 2.1 | 4%  | 48% |
| -6             |                  | [Qua92a]   |   |     |     |     |     |

| Syntactic name<br>V# | Semantic name<br>Other names        | Description<br>References                              | V | Cl  | Av  | nH | Eq  |
|----------------------|-------------------------------------|--|---|-----|-----|----|-----|
| SET138<br>-6         | SetB3Fix2<br>SB5.11<br>[Qua92a]     | Kludge 2 to instantiate variables in unordered triples | - | 166 | 2.1 | 4% | 48% |
| SET139<br>-6         | SetB3Rdcn1<br>SB6.1<br>[Qua92a]     | Triple reduction 1                                     | - | 163 | 2.1 | 4% | 49% |
| SET140<br>-6         | SetB3Rdcn2<br>SB6.2<br>[Qua92a]     | Triple reduction 2                                     | - | 163 | 2.1 | 4% | 49% |
| SET141<br>-6         | SetB3Rdcn3<br>SB6.3<br>[Qua92a]     | Triple reduction 3                                     | - | 163 | 2.1 | 4% | 49% |
| SET142<br>-6         | SetBOrd<br>SB7<br>[Qua92a]          | Lexical ordering in unordered triples is irrelevant    | - | 163 | 2.1 | 4% | 49% |
| SET143<br>-6         | IntscAssc<br>I1<br>[Qua92a]         | Associativity of intersection                          | - | 188 | 2.1 | 4% | 47% |
| SET144<br>-6         | IntscComm1<br>I2<br>[Qua92a]        | Commutativity of intersection                          | - | 188 | 2.1 | 4% | 47% |
| SET145<br>-6         | IntscComm2<br>I3<br>[Qua92a]        | Commutativity outside intersection                     | - | 188 | 2.1 | 4% | 47% |
| SET146<br>-6         | IntscNull<br>I4<br>[Qua92a]         | Intersection with null class                           | - | 188 | 2.1 | 4% | 47% |
| SET147<br>-6         | IntscId<br>I5<br>[Qua92a]           | Universal class is identity for intersection           | - | 188 | 2.1 | 4% | 47% |
| SET148<br>-6         | IntscIdem<br>I6<br>[Qua92a]         | Idempotency of intersection                            | - | 188 | 2.1 | 4% | 47% |
| SET149<br>-6         | IntscIdemCor<br>I6 cor.<br>[Qua92a] | Corollary to idempotency of intersection               | - | 188 | 2.1 | 4% | 47% |
| SET150<br>-6         | CpmtIvln<br>C1<br>[Qua92a]          | Complement is an involution                            | - | 188 | 2.1 | 4% | 47% |
| SET151<br>-6         | CpmtNull<br>C2.1<br>[Qua92a]        | Complement of null class is universal class            | - | 188 | 2.1 | 4% | 47% |
| SET152<br>-6         | CpmtUniv<br>C2.2<br>[Qua92a]        | Complement of universal class is null class            | - | 188 | 2.1 | 4% | 47% |
| SET153<br>-6         | IntscCpmt<br>C3.1<br>[Qua92a]       | Intersection with complement is null class             | - | 188 | 2.1 | 4% | 47% |
| SET154<br>-6         | UnionCpmt<br>C3.2<br>[Qua92a]       | Union with complement is universal class               | - | 188 | 2.1 | 4% | 47% |
| SET155<br>-6         | DeMorgan1<br>C4.1<br>[Qua92a]       | De Morgans law 1                                       | - | 188 | 2.1 | 4% | 47% |
| SET156<br>-6         | DeMorgan2<br>C4.2<br>[Qua92a]       | De Morgans law 2                                       | - | 188 | 2.1 | 4% | 47% |
| SET157<br>-6         | CpmtUnq<br>C5<br>[Qua92a]           | Complement is unique                                   | - | 190 | 2.0 | 4% | 47% |
| SET158<br>-6         | CpmtAxCor<br>C6<br>[Qua92a]         | Corollary to complement axiom                          | - | 190 | 2.0 | 4% | 46% |
| SET159<br>-6         | UnionAssc<br>U1<br>[Qua92a]         | Associativity of union                                 | - | 188 | 2.1 | 4% | 47% |
| SET160<br>-6         | UnionComm1<br>U2<br>[Qua92a]        | Commutativity of union                                 | - | 188 | 2.1 | 4% | 47% |
| SET161<br>-6         | UnionComm2<br>U3<br>[Qua92a]        | Commutativity outside union                            | - | 188 | 2.1 | 4% | 47% |
| SET162<br>-6         | UnionId<br>U4<br>[Qua92a]           | Null class is identity for union                       | - | 188 | 2.1 | 4% | 47% |
| SET163<br>-6         | UnionUniv<br>U5<br>[Qua92a]         | Union with universal class                             | - | 188 | 2.1 | 4% | 47% |
| SET164<br>-6         | UnionIdem<br>U6<br>[Qua92a]         | Idempotency of union                                   | - | 188 | 2.1 | 4% | 47% |
| SET165<br>-6         | UnionIdemCor<br>U6 cor.<br>[Qua92a] | Corollary to idempotency of union                      | - | 188 | 2.1 | 4% | 47% |
| SET166<br>-6         | UnionE11<br>U7.1<br>[Qua92a]        | Members of union 1                                     | - | 190 | 2.0 | 4% | 46% |
| SET167<br>-6         | UnionE12<br>U7.2<br>[Qua92a]        | Members of union 2                                     | - | 189 | 2.1 | 4% | 46% |
| SET168<br>-6         | UnionE13<br>U7.3<br>[Qua92a]        | Members of union 3                                     | - | 189 | 2.1 | 4% | 46% |
| SET169<br>-6         | IntscUnion1<br>D1.1<br>[Qua92a]     | Distribution of intersection over union 1              | - | 188 | 2.1 | 4% | 47% |
| SET170<br>-6         | IntscUnion2<br>D1.2<br>[Qua92a]     | Distribution of intersection over union 2              | - | 188 | 2.1 | 4% | 47% |
| SET171<br>-6         | UnionIntsc1<br>D2.1<br>[Qua92a]     | Distribution of union over intersection 1              | - | 188 | 2.1 | 4% | 47% |
| SET172<br>-6         | UnionIntsc2<br>D2.2<br>[Qua92a]     | Distribution of union over intersection 2              | - | 188 | 2.1 | 4% | 47% |
| SET173<br>-6         | IntscAbsb<br>D3<br>[Qua92a]         | Absorbtion for intersection                            | - | 188 | 2.1 | 4% | 47% |
| SET174<br>-6         | IntscAbsbCor<br>D3 cor.<br>[Qua92a] | Corollary to absorbtion for intersection               | - | 188 | 2.1 | 4% | 47% |
| SET175<br>-6         | UnionAbsb<br>D4<br>[Qua92a]         | Absorbtion for union                                   | - | 188 | 2.1 | 4% | 47% |
| SET176<br>-6         | UnionAbsbCor<br>D4 cor.<br>[Qua92a] | Corollary to absorbtion for union                      | - | 188 | 2.1 | 4% | 47% |
| SET177<br>-6         | DistEqn1<br>D5<br>[Qua92a]          | Distribution property 1                                | - | 188 | 2.1 | 4% | 47% |
| SET178<br>-6         | DistEqn1Cor1<br>D5 cor.<br>[Qua92a] | Corollary 1 to distribution property 1                 | - | 188 | 2.1 | 4% | 47% |
| SET179<br>-6         | DistEqn1Cor2<br>D5 cor.<br>[Qua92a] | Corollary 2 to distribution property 1                 | - | 188 | 2.1 | 4% | 47% |

| Syntactic name<br>V# | Semantic name<br>Other names     | Description<br>References                                     | V | Cl  | Av  | nH | Eq  |
|----------------------|----------------------------------|---|---|-----|-----|----|-----|
| SET180               | -6<br>DistEqn2<br>D6             | Distribution property 2<br>[Qua92a]                           | - | 188 | 2.1 | 4% | 47% |
| SET181               | -6<br>DistEqn2Cor<br>D6 cor.     | Corollary to distribution property 2<br>[Qua92a]              | - | 188 | 2.1 | 4% | 47% |
| SET182               | -6<br>DistEqn3<br>D7             | Distribution property 3<br>[Qua92a]                           | - | 188 | 2.1 | 4% | 47% |
| SET183               | -6<br>SubCEqn1<br>SU1            | Subclass property 1<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET184               | -6<br>SubCEqn2<br>SU2            | Subclass property 2<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET185               | -6<br>SubCEqn3<br>SU3            | Subclass property 3<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET186               | -6<br>SubCEqn4<br>SU4            | Subclass property 4<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET187               | -6<br>SubCEqn5<br>SU5            | Subclass property 5<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET188               | -6<br>SubCEqn6<br>SU6            | Subclass property 6<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET189               | -6<br>SubCEqn6Cor<br>SU6 cor.    | Corollary to subclass property 6<br>[Qua92a]                  | - | 190 | 2.0 | 4% | 47% |
| SET190               | -6<br>SubCEqn7<br>SU7            | Subclass property 7<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET191               | -6<br>SubCEqn8<br>SU8            | Subclass property 8<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET192               | -6<br>SubCEqn9<br>SU9            | Subclass property 9<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET193               | -6<br>SubCEqn10<br>SU10          | Subclass property 10<br>[Qua92a]                              | - | 189 | 2.1 | 4% | 46% |
| SET194               | -6<br>LattUpBnd1<br>LA1.1        | Lattice upper bound 1<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET195               | -6<br>LattUpBnd2<br>LA1.2        | Lattice upper bound 2<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET196               | -6<br>LattLowBnd1<br>LA1.3       | Lattice lower bound 1<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET197               | -6<br>LattLowBnd2<br>LA1.4       | Lattice lower bound 2<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET198               | -6<br>MinUpBnd<br>LA2.1          | Least upper bound<br>[Qua92a]                                 | - | 190 | 2.0 | 4% | 46% |
| SET199               | -6<br>MaxLowBnd<br>LA2.2         | Greatest lower bound<br>[Qua92a]                              | - | 190 | 2.0 | 4% | 46% |
| SET200               | -6<br>UnionMono<br>LA3.1         | Union is monotonic<br>[Qua92a]                                | - | 190 | 2.0 | 4% | 46% |
| SET201               | -6<br>IntscMono<br>LA3.2         | Intersection is monotonic<br>[Qua92a]                         | - | 190 | 2.0 | 4% | 46% |
| SET202               | -6<br>XProdEqn1<br>CP1           | Cross product property 1<br>[Qua92a]                          | - | 188 | 2.1 | 4% | 46% |
| SET203               | -6<br>XProdEqn1Cor<br>CP1 cor.   | Corollary to cross product property 1<br>[Qua92a]             | - | 190 | 2.0 | 4% | 46% |
| SET204               | -6<br>XProdEqn2<br>CP2           | Cross product property 2<br>[Qua92a]                          | - | 189 | 2.1 | 4% | 46% |
| SET205               | -6<br>XProdNull1<br>CP3.1        | Cross product with null class 1<br>[Qua92a]                   | - | 188 | 2.1 | 4% | 47% |
| SET206               | -6<br>XProdNull2<br>CP3.2        | Cross product with null class 2<br>[Qua92a]                   | - | 188 | 2.1 | 4% | 47% |
| SET207               | -6<br>XProdEqn3<br>CP4           | Cross product property 3<br>[Qua92a]                          | - | 188 | 2.1 | 4% | 46% |
| SET208               | -6<br>XProdMono1<br>CP5.1        | Cross product is monotonic 1<br>[Qua92a]                      | - | 189 | 2.1 | 4% | 46% |
| SET209               | -6<br>XProdMono2<br>CP5.2        | Cross product is monotonic 2<br>[Qua92a]                      | - | 189 | 2.1 | 4% | 46% |
| SET210               | -6<br>XProdMonoCor1<br>CP5 cor.1 | Corollary 1 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET211               | -6<br>XProdMonoCor2<br>CP5 cor.2 | Corollary 2 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET212               | -6<br>XProdMonoCor3<br>CP5 cor.3 | Corollary 3 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET213               | -6<br>XProdMonoCor4<br>CP5 cor.4 | Corollary 4 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET214               | -6<br>XProdMonoCor5<br>CP5 cor.5 | Corollary 5 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET215               | -6<br>XProdMonoCor6<br>CP5 cor.6 | Corollary 6 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET216               | -6<br>XProdMonoCor7<br>CP5 cor.7 | Corollary 7 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET217               | -6<br>XProdMonoCor8<br>CP5 cor.8 | Corollary 8 to cross product product monotonicity<br>[Qua92a] | - | 188 | 2.1 | 4% | 46% |
| SET218               | -6<br>XProdUnion1<br>CP6.1       | Cross product distributes over union 1<br>[Qua92a]            | - | 188 | 2.1 | 4% | 47% |
| SET219               | -6<br>XProdUnion2<br>CP6.2       | Cross product distributes over union 2<br>[Qua92a]            | - | 188 | 2.1 | 4% | 47% |
| SET220               | -6<br>XProdIntsc1<br>CP7.1       | Cross product distributes over intersection 1<br>[Qua92a]     | - | 188 | 2.1 | 4% | 47% |
| SET221               | -6<br>XProdIntsc2<br>CP7.2       | Cross product distributes over intersection 2<br>[Qua92a]     | - | 188 | 2.1 | 4% | 47% |

| Syntactic name | Semantic name | Description                         | V | Cl  | Av  | nH | Eq  |
|----------------|---------------|-------------------------------------|---|-----|-----|----|-----|
| V#             | Other names   | References                          |   |     |     |    |     |
| SET222         | -6            | XProdEqn4<br>CP8 [Qua92a]           | - | 188 | 2.1 | 4% | 46% |
| SET223         | -6            | XProdEqn5<br>CP8 [Qua92a]           | - | 188 | 2.1 | 4% | 46% |
| SET224         | -6            | XProd2Dist<br>CP9 [Qua92a]          | - | 188 | 2.1 | 4% | 47% |
| SET225         | -6            | InvSqrXProd<br>CP10 [Qua92a]        | - | 188 | 2.1 | 4% | 47% |
| SET226         | -6            | XProdLCanc1<br>CP11.1 [Qua92a]      | - | 190 | 2.0 | 4% | 47% |
| SET227         | -6            | XProdLCanc2<br>CP11.2 [Qua92a]      | - | 190 | 2.0 | 4% | 47% |
| SET228         | -6            | XProdRCanc1<br>CP12.1 [Qua92a]      | - | 190 | 2.0 | 4% | 47% |
| SET229         | -6            | XProdRCanc2<br>CP12.2 [Qua92a]      | - | 190 | 2.0 | 4% | 47% |
| SET230         | -6            | XProdCancCor<br>CP13 [Qua92a]       | - | 189 | 2.1 | 4% | 47% |
| SET231         | -6            | XProdEqn6<br>CP14.1 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET232         | -6            | XProdEqn7<br>CP14.2 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET233         | -6            | XProdEqn8<br>CP14.3 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET234         | -6            | XProdEqn9<br>CP14.4 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET235         | -6            | XProdEqn10<br>CP15.1 [Qua92a]       | - | 190 | 2.0 | 4% | 46% |
| SET236         | -6            | XProdEqn11<br>CP15.2 [Qua92a]       | - | 190 | 2.0 | 4% | 46% |
| SET237         | -6            | RstnAltDef1<br>RS0 [Qua92a]         | - | 188 | 2.1 | 4% | 46% |
| SET238         | -6            | RstnAltDef1Cor<br>RS0 cor. [Qua92a] | - | 189 | 2.1 | 4% | 46% |
| SET239         | -6            | RstnAltDef2<br>RS1 [Qua92a]         | - | 189 | 2.1 | 4% | 46% |
| SET240         | -6            | RstnAltDef3<br>RS2 [Qua92a]         | - | 189 | 2.1 | 4% | 46% |
| SET241         | -6            | RstnAltDef4<br>RS3 [Qua92a]         | - | 189 | 2.1 | 4% | 46% |
| SET242         | -6            | RstnAltDef5<br>RS4 [Qua92a]         | - | 190 | 2.0 | 4% | 46% |
| SET243         | -6            | RstnEqn1<br>RS5 [Qua92a]            | - | 188 | 2.1 | 4% | 47% |
| SET244         | -6            | RstnUnivC1<br>RS6.1 [Qua92a]        | - | 188 | 2.1 | 4% | 47% |
| SET245         | -6            | RstnNullC11<br>RS6.2 [Qua92a]       | - | 188 | 2.1 | 4% | 47% |
| SET246         | -6            | RstnNullC12<br>RS6.3 [Qua92a]       | - | 188 | 2.1 | 4% | 47% |
| SET247         | -6            | RstnNullC13<br>RS6.4 [Qua92a]       | - | 188 | 2.1 | 4% | 47% |
| SET248         | -6            | RstnIntsc<br>RS7 [Qua92a]           | - | 188 | 2.1 | 4% | 47% |
| SET249         | -6            | RstnEqn2<br>RS8 [Qua92a]            | - | 188 | 2.1 | 4% | 47% |
| SET250         | -6            | RstnEqn2Cor<br>RS8 cor. [Qua92a]    | - | 188 | 2.1 | 4% | 47% |
| SET251         | -6            | RstdElRel1<br>RS9.1 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET252         | -6            | RstnEqn3<br>RS10.1 [Qua92a]         | - | 188 | 2.1 | 4% | 46% |
| SET253         | -6            | RstnEqn4<br>RS10.2 [Qua92a]         | - | 188 | 2.1 | 4% | 46% |
| SET254         | -6            | RstnMono1<br>RS11.1 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET255         | -6            | RstnMono2<br>RS11.2 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET256         | -6            | RstnMono3<br>RS11.3 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET257         | -6            | RstnEqn5<br>RS12 [Qua92a]           | - | 188 | 2.1 | 4% | 47% |
| SET258         | -6            | DomAltDef1<br>DO1.1 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET259         | -6            | DomAltDef2<br>DO1.2 [Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET260         | -6            | DomAltDef3<br>DO1.3 [Qua92a]        | - | 190 | 2.0 | 4% | 46% |
| SET261         | -6            | DomOfNullC1<br>DO2.1 [Qua92a]       | - | 188 | 2.1 | 4% | 47% |
| SET262         | -6            | DomOfUnivC1<br>DO2.2 [Qua92a]       | - | 188 | 2.1 | 4% | 47% |
| SET263         | -6            | DomUnion<br>DO3 [Qua92a]            | - | 188 | 2.1 | 4% | 47% |

| Syntactic name<br>V# | Semantic name<br>Other names   | Description<br>References                                     | V | Cl  | Av  | nH | Eq  |
|----------------------|--------------------------------|---|---|-----|-----|----|-----|
| SET264               | -6<br>DomMono1<br>DO3 cor.1    | Domain is monotonic 1<br>[Qua92a]                             | - | 189 | 2.1 | 4% | 46% |
| SET265               | -6<br>DomMono2<br>DO3 cor.2    | Domain is monotonic 2<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET266               | -6<br>DomMono3<br>DO3 cor.3    | Domain is monotonic 3<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET267               | -6<br>DomMono4<br>DO3 cor.4    | Domain is monotonic 4<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET268               | -6<br>DomEqn1<br>DO4           | Domain property 1<br>[Qua92a]                                 | - | 188 | 2.1 | 4% | 46% |
| SET269               | -6<br>DomPrs<br>DO5            | Domain only considers ordered pairs<br>[Qua92a]               | - | 188 | 2.1 | 4% | 47% |
| SET270               | -6<br>DomEqn2<br>DO6           | Domain property 2<br>[Qua92a]                                 | - | 189 | 2.1 | 4% | 47% |
| SET271               | -6<br>DomEqn2Cor<br>DO6 cor.   | Corollary to domain property 2<br>[Qua92a]                    | - | 188 | 2.1 | 4% | 47% |
| SET272               | -6<br>DomEqn3<br>DO7           | Domain property 3<br>[Qua92a]                                 | - | 188 | 2.1 | 4% | 47% |
| SET273               | -6<br>DomEqn3Cor<br>DO7 cor.   | Corollary to domain property 3<br>[Qua92a]                    | - | 188 | 2.1 | 4% | 47% |
| SET274               | -6<br>DomEqn4<br>DO8           | Domain property 4<br>[Qua92a]                                 | - | 188 | 2.1 | 4% | 47% |
| SET275               | -6<br>DomEqn4Cor1<br>DO8 cor.1 | Corollary 1 to domain property 4<br>[Qua92a]                  | - | 188 | 2.1 | 4% | 46% |
| SET276               | -6<br>DomEqn4Cor2<br>DO8 cor.2 | Corollary 2 to domain property 4<br>[Qua92a]                  | - | 188 | 2.1 | 4% | 46% |
| SET277               | -6<br>DomEqn4Cor3<br>DO8 cor.3 | Corollary 3 to domain property 4<br>[Qua92a]                  | - | 188 | 2.1 | 4% | 46% |
| SET278               | -6<br>DomEqn4Cor4<br>DO8 cor.4 | Corollary 4 to domain property 4<br>[Qua92a]                  | - | 188 | 2.1 | 4% | 46% |
| SET279               | -6<br>DomEqn5<br>DO9           | Domain property 5<br>[Qua92a]                                 | - | 190 | 2.0 | 4% | 46% |
| SET280               | -6<br>DomEqn6<br>DO10          | Domain property 6<br>[Qua92a]                                 | - | 190 | 2.0 | 4% | 47% |
| SET281               | -6<br>DomRelFunc<br>DO12       | Domain relation is a function<br>[Qua92a]                     | - | 188 | 2.1 | 4% | 46% |
| SET282               | -6<br>DomOfDomRel<br>DO13      | Domain of domain relation<br>[Qua92a]                         | - | 188 | 2.1 | 4% | 47% |
| SET283               | -6<br>ApplyDomRel<br>DO14      | Apply domain relation<br>[Qua92a]                             | - | 189 | 2.1 | 4% | 46% |
| SET284               | -6<br>ImgOfDomRel<br>DO15      | Image of domain relation<br>[Qua92a]                          | - | 188 | 2.1 | 4% | 47% |
| SET285               | -6<br>DomEqn7<br>DO16          | Domain property 7<br>[Qua92a]                                 | - | 189 | 2.1 | 4% | 46% |
| SET286               | -6<br>DomEqn7Cor<br>DO16 cor.  | Corollary to domain property 7<br>[Qua92a]                    | - | 189 | 2.1 | 4% | 46% |
| SET287               | -6<br>DomEqn8<br>DO17          | Domain property 8<br>[Qua92a]                                 | - | 189 | 2.1 | 4% | 46% |
| SET288               | -6<br>DomEqn9<br>DO18          | Domain property 9<br>[Qua92a]                                 | - | 190 | 2.0 | 4% | 46% |
| SET289               | -6<br>GodelAx1<br>IN1          | Proof of Goedel's axiom B6, part 1<br>[Qua92a]                | - | 188 | 2.1 | 4% | 46% |
| SET290               | -6<br>GodelAx2<br>IN2          | Proof of Goedel's axiom B6, part 2<br>[Qua92a]                | - | 189 | 2.1 | 4% | 46% |
| SET291               | -6<br>GodelAx3<br>IN3          | Proof of Goedel's axiom B6, part 3<br>[Qua92a]                | - | 190 | 2.0 | 4% | 46% |
| SET292               | -6<br>InvNullCl<br>IN4.1       | Inverse of null class is the null class<br>[Qua92a]           | - | 188 | 2.1 | 4% | 47% |
| SET293               | -6<br>InvUnivCl<br>IN4.2       | Inverse of universal class is the universal class<br>[Qua92a] | - | 188 | 2.1 | 4% | 47% |
| SET294               | -6<br>InvUnion<br>IN5.1        | Inverse distributes over union<br>[Qua92a]                    | - | 188 | 2.1 | 4% | 47% |
| SET295               | -6<br>InvIntsc<br>IN5.2        | Inverse distributes over intersection<br>[Qua92a]             | - | 188 | 2.1 | 4% | 47% |
| SET296               | -6<br>DomOfInv<br>IN6.1        | Domain of inverse<br>[Qua92a, Ale95]                          | - | 188 | 2.1 | 4% | 47% |
| SET297               | -6<br>RngOfInv<br>IN6.2        | Range of inverse<br>[Qua92a]                                  | - | 188 | 2.1 | 4% | 47% |
| SET298               | -6<br>InvOfCpmt<br>IN7         | Inverse of complement<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 47% |
| SET299               | -6<br>InvOfProd<br>IN8         | Inverse of product<br>[Qua92a]                                | - | 188 | 2.1 | 4% | 47% |
| SET300               | -6<br>InvOfInv<br>IN9          | Inverse of inverse<br>[Qua92a]                                | - | 188 | 2.1 | 4% | 47% |
| SET301               | -6<br>IncRstn<br>IN10          | Inverse commutes with restriction<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 47% |
| SET302               | -6<br>RngAltDef1<br>RA1.1      | Range alternate definition 1<br>[Qua92a]                      | - | 189 | 2.1 | 4% | 46% |
| SET303               | -6<br>RngAltDef2<br>RA1.2      | Range alternate definition 2<br>[Qua92a]                      | - | 189 | 2.1 | 4% | 46% |
| SET304               | -6<br>RngAltDef3<br>RA1.3      | Range alternate definition 3<br>[Qua92a]                      | - | 190 | 2.0 | 4% | 46% |
| SET305               | -6<br>RngOfNullCl<br>RA2.1     | Range of null class is the null class<br>[Qua92a]             | - | 188 | 2.1 | 4% | 47% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References                                   | V | Cl  | Av  | nH | Eq  |
|----------------------|------------------------------|---|---|-----|-----|----|-----|
| SET306<br>-6         | RngOfUnivCl<br>RA2.2         | Range of universal class is the universal class<br>[Qua92a] | - | 188 | 2.1 | 4% | 47% |
| SET307<br>-6         | RngUnion<br>RA3              | Range preserves union<br>[Qua92a]                           | - | 188 | 2.1 | 4% | 47% |
| SET308<br>-6         | RngMono1<br>RA3 cor.1        | Monotonicity of range 1<br>[Qua92a]                         | - | 189 | 2.1 | 4% | 46% |
| SET309<br>-6         | RngMono2<br>RA3 cor.2        | Monotonicity of range 2<br>[Qua92a]                         | - | 188 | 2.1 | 4% | 46% |
| SET310<br>-6         | RngMono3<br>RA3 cor.3        | Monotonicity of range 3<br>[Qua92a]                         | - | 188 | 2.1 | 4% | 46% |
| SET311<br>-6         | RngEqn1<br>RA4               | Range property 1<br>[Qua92a]                                | - | 188 | 2.1 | 4% | 46% |
| SET312<br>-6         | RngOrdPrs<br>RA5             | Range only considers ordered pairs<br>[Qua92a]              | - | 188 | 2.1 | 4% | 47% |
| SET313<br>-6         | RngEqn2<br>RA6               | Range property 2<br>[Qua92a]                                | - | 189 | 2.1 | 4% | 47% |
| SET314<br>-6         | RngEqn3<br>RA7               | Range property 3<br>[Qua92a]                                | - | 188 | 2.1 | 4% | 47% |
| SET315<br>-6         | RngEqn3Cor<br>RA7 cor.       | Corollary to range property 3<br>[Qua92a]                   | - | 188 | 2.1 | 4% | 47% |
| SET316<br>-6         | RngEqn4<br>RA8               | Range property 4<br>[Qua92a]                                | - | 188 | 2.1 | 4% | 47% |
| SET317<br>-6         | RngEqn4Cor1<br>RA8 cor.1     | Corollary 1 to range property 4<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 46% |
| SET318<br>-6         | RngEqn4Cor2<br>RA8 cor.2     | Corollary 2 to range property 4<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 46% |
| SET319<br>-6         | RngEqn4Cor3<br>RA8 cor.3     | Corollary 3 to range property 4<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 46% |
| SET320<br>-6         | RngEqn4Cor4<br>RA8 cor.4     | Corollary 4 to range property 4<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 46% |
| SET321<br>-6         | RngEqn5<br>RA9.1             | Range property 5<br>[Qua92a]                                | - | 189 | 2.1 | 4% | 46% |
| SET322<br>-6         | RngEqn6<br>RA9.2             | Range property 6<br>[Qua92a]                                | - | 189 | 2.1 | 4% | 46% |
| SET323<br>-6         | RngEqn7<br>RA10              | Range property 7<br>[Qua92a]                                | - | 190 | 2.0 | 4% | 47% |
| SET324<br>-6         | ImgAltDef1<br>IM3            | Image alternate definition 1<br>[Qua92a]                    | - | 189 | 2.1 | 4% | 46% |
| SET325<br>-6         | ImgAltDef2<br>IM4            | Image alternate definition 2<br>[Qua92a]                    | - | 189 | 2.1 | 4% | 46% |
| SET326<br>-6         | ImgAltDef2Cor<br>IM4 cor.    | Corollary to image alternate definition 2<br>[Qua92a]       | - | 189 | 2.1 | 4% | 46% |
| SET327<br>-6         | ImgAltDef3<br>IM1            | Image alternate definition 3<br>[Qua92a]                    | - | 189 | 2.1 | 4% | 46% |
| SET328<br>-6         | ImgAltDef3Cor<br>IM1 cor.    | Corollary to image alternate definition 3<br>[Qua92a]       | - | 190 | 2.0 | 4% | 46% |
| SET329<br>-6         | ImgAltDef4<br>IM2            | Image alternate definition 4<br>[Qua92a]                    | - | 191 | 2.0 | 4% | 46% |
| SET330<br>-6         | ImgAltDef4Cor<br>IM2 cor.    | Corollary to image alternate definition 4<br>[Qua92a]       | - | 190 | 2.0 | 4% | 46% |
| SET331<br>-6         | RngImgDom<br>IM5             | Range is image of the domain<br>[Qua92a]                    | - | 188 | 2.1 | 4% | 47% |
| SET332<br>-6         | RngImgDomCor<br>IM5 cor.     | Corollary to range is image of domain<br>[Qua92a]           | - | 188 | 2.1 | 4% | 47% |
| SET333<br>-6         | ImgMono1<br>IM6.1            | Monotonicity of image 1<br>[Qua92a]                         | - | 189 | 2.1 | 4% | 46% |
| SET334<br>-6         | ImgMono2<br>IM6.2            | Monotonicity of image 2<br>[Qua92a]                         | - | 189 | 2.1 | 4% | 46% |
| SET335<br>-6         | ImgEqn1<br>IM7               | Image property 1<br>[Qua92a]                                | - | 189 | 2.1 | 4% | 47% |
| SET336<br>-6         | ImgEqn1Cor1<br>IM7 cor.1     | Corollary 1 image property 1<br>[Qua92a]                    | - | 188 | 2.1 | 4% | 47% |
| SET337<br>-6         | ImgEqn1Cor2<br>IM7 cor.2     | Corollary 2 image property 1<br>[Qua92a]                    | - | 188 | 2.1 | 4% | 47% |
| SET338<br>-6         | ImgEqn1Cor3<br>IM7 cor.3     | Corollary 3 image property 1<br>[Qua92a]                    | - | 189 | 2.1 | 4% | 46% |
| SET339<br>-6         | SubCAltDef1<br>IM8           | Subclass alternate definition 1<br>[Qua92a]                 | - | 189 | 2.1 | 4% | 46% |
| SET340<br>-6         | SubCAltDef2<br>IM9           | Subclass alternate definition 2<br>[Qua92a]                 | - | 190 | 2.0 | 4% | 46% |
| SET341<br>-6         | ImgUnivCl<br>IM10            | Image under universal class<br>[Qua92a]                     | - | 189 | 2.1 | 4% | 47% |
| SET342<br>-6         | ImgOfUnion<br>IM11           | Image of union<br>[Qua92a]                                  | - | 188 | 2.1 | 4% | 46% |
| SET343<br>-6         | ImgOfIntsc<br>IM12           | Image of intersection<br>[Qua92a]                           | - | 188 | 2.1 | 4% | 47% |
| SET344<br>-6         | SumCAltDef1<br>SC1.1         | Sum class alternate definition 1<br>[Qua92a]                | - | 189 | 2.1 | 4% | 46% |
| SET345<br>-6         | SumCAltDef2<br>SC1.2         | Sum class alternate definition 2<br>[Qua92a]                | - | 189 | 2.1 | 4% | 46% |
| SET346<br>-6         | SumCAltDef3<br>SC2           | Sum class alternate definition 3<br>[Qua92a]                | - | 190 | 2.0 | 4% | 46% |
| SET347<br>-6         | SumCOfNullCl<br>SC3.1        | Sum class of null class is null class<br>[Qua92a]           | - | 188 | 2.1 | 4% | 47% |



| Syntactic name<br>V# | Semantic name<br>Other names            | Description<br>References                         | V | Cl  | Av  | nH | Eq  |
|----------------------|---|---|---|-----|-----|----|-----|
| SET348<br>-6         | SumClOfUnivCl<br>SC3.2<br>[Qua92a]      | Sum class of universal class is universal class   | - | 188 | 2.1 | 4% | 47% |
| SET349<br>-6         | SumClOfSgtnNull1<br>SC3.3<br>[Qua92a]   | Sum class of singleton null is null class 1       | - | 188 | 2.1 | 4% | 47% |
| SET350<br>-6         | SumClOfSgtnNull2<br>SC3.4<br>[Qua92a]   | Sum class of singleton null is null class 2       | - | 190 | 2.0 | 4% | 47% |
| SET351<br>-6         | SumClSgtn<br>SC4<br>[Qua92a]            | Sum of singleton                                  | - | 189 | 2.1 | 4% | 46% |
| SET352<br>-6         | SumClPr<br>SC5<br>[Qua92a]              | Sum of pair                                       | - | 189 | 2.1 | 4% | 46% |
| SET353<br>-6         | SumClPrCor<br>SC5 cor.<br>[Qua92a]      | Corollary to sum of pair                          | - | 189 | 2.1 | 4% | 46% |
| SET354<br>-6         | SumClOrdPr<br>SC6<br>[Qua92a]           | Sum of ordered pair                               | - | 189 | 2.1 | 4% | 46% |
| SET355<br>-6         | SubCUnion<br>SC7<br>[Qua92a]            | An element of a class is a subclass of union      | - | 189 | 2.1 | 4% | 46% |
| SET356<br>-6         | SubCUnionCor<br>SC7 cor.<br>[Qua92a]    | Corollary to subclass of union                    | - | 188 | 2.1 | 4% | 46% |
| SET357<br>-6         | SumClAltDef4<br>SC8<br>[Qua92a]         | Sum class alternate definition 4                  | - | 188 | 2.1 | 4% | 47% |
| SET358<br>-6         | SumClUnion<br>SC9<br>[Qua92a]           | Sum distributes over union                        | - | 188 | 2.1 | 4% | 47% |
| SET359<br>-6         | SumClEqn1<br>SC10<br>[Qua92a]           | Sum class property 1                              | - | 188 | 2.1 | 4% | 46% |
| SET360<br>-6         | DomSumClSqr<br>SC11.1<br>[Qua92a]       | Domain is sum squared                             | - | 188 | 2.1 | 4% | 46% |
| SET361<br>-6         | RngSumClSqr<br>SC11.2<br>[Qua92a]       | Range is sum squared                              | - | 188 | 2.1 | 4% | 46% |
| SET362<br>-6         | SumClMono<br>SC12<br>[Qua92a]           | Monotonicity of sum                               | - | 189 | 2.1 | 4% | 46% |
| SET363<br>-6         | PwrClAltDef1<br>PC1<br>[Qua92a]         | Power class alternative definition 1              | - | 189 | 2.1 | 4% | 46% |
| SET364<br>-6         | PwrClAltDef2<br>PC2<br>[Qua92a]         | Power class alternative definition 2              | - | 190 | 2.0 | 4% | 46% |
| SET365<br>-6         | PwrClMono<br>PC3<br>[Qua92a]            | Monotonicity of power                             | - | 189 | 2.1 | 4% | 46% |
| SET366<br>-6         | NullClEIPrCl<br>PC4.1<br>[Qua92a]       | Null class in power class                         | - | 188 | 2.1 | 4% | 46% |
| SET367<br>-6         | PwrClNotNull<br>PC4.2<br>[Qua92a]       | Power class not in null class                     | - | 188 | 2.1 | 4% | 47% |
| SET368<br>-6         | PwrClOfUnivCl<br>PC4.3<br>[Qua92a]      | Power class of universal class is universal class | - | 188 | 2.1 | 4% | 47% |
| SET369<br>-6         | PwrClOfSet<br>PC5<br>[Qua92a]           | Power class of set                                | - | 189 | 2.1 | 4% | 46% |
| SET370<br>-6         | PwrClEqn1<br>PC6<br>[Qua92a]            | Power class property 1                            | - | 188 | 2.1 | 4% | 46% |
| SET371<br>-6         | PwrClEqn2<br>PC7<br>[Qua92a]            | Power class property 2                            | - | 188 | 2.1 | 4% | 46% |
| SET372<br>-6         | PwrClEqn3<br>PC8<br>[Qua92a]            | Power class property 3                            | - | 188 | 2.1 | 4% | 47% |
| SET373<br>-6         | PwrClEqn4<br>PC9<br>[Qua92a]            | Power class property 4                            | - | 188 | 2.1 | 4% | 47% |
| SET374<br>-6         | PwrClClsdUnion<br>PC10<br>[Qua92a]      | Power class is closed under union                 | - | 190 | 2.0 | 4% | 46% |
| SET375<br>-6         | PwrClClsdIntsc<br>PC11<br>[Qua92a]      | Power class is closed under intersection          | - | 190 | 2.0 | 4% | 46% |
| SET376<br>-6         | PwrClSetB<br>PC12<br>[Qua92a]           | Power class set builder                           | - | 190 | 2.0 | 4% | 46% |
| SET377<br>-6         | PwrClSetBCor1<br>PC12 cor.1<br>[Qua92a] | Corollary 1 to power class set builder            | - | 189 | 2.1 | 4% | 46% |
| SET378<br>-6         | PwrClSetBCor2<br>PC12 cor.2<br>[Qua92a] | Corollary 2 to power class set builder            | - | 188 | 2.1 | 4% | 46% |
| SET379<br>-6         | PwrClSetBCor3<br>PC12 cor.3<br>[Qua92a] | Corollary 3 to power class set builder            | - | 189 | 2.1 | 4% | 46% |
| SET380<br>-6         | RelEqn1<br>RL1<br>[Qua92a]              | Relation property 1                               | - | 188 | 2.1 | 4% | 46% |
| SET381<br>-6         | RelEqn2<br>RL2<br>[Qua92a]              | Relation property 2                               | - | 189 | 2.1 | 4% | 46% |
| SET382<br>-6         | RelEqn2Cor1<br>RL2 cor.2<br>[Qua92a]    | Corollary 1 to relation property 2                | - | 189 | 2.1 | 4% | 46% |
| SET383<br>-6         | RelEqn2Cor2<br>RL2 cor.2<br>[Qua92a]    | Corollary 2 to relation property 2                | - | 188 | 2.1 | 4% | 46% |
| SET384<br>-6         | RelEqn3Cor1<br>RL3 cor.1<br>[Qua92a]    | Corollary 1 to relation property 3                | - | 188 | 2.1 | 4% | 47% |
| SET385<br>-6         | RelEqn3Cor2<br>RL3 cor.2<br>[Qua92a]    | Corollary 2 to relation property 3                | - | 188 | 2.1 | 4% | 47% |
| SET386<br>-6         | RelEqn4<br>RL4<br>[Qua92a]              | Relation property 4                               | - | 189 | 2.1 | 4% | 46% |
| SET387<br>-6         | CmpsnAltDef1<br>CO1.1<br>[Qua92a]       | Composition alternate definition 1                | - | 189 | 2.1 | 4% | 46% |
| SET388<br>-6         | CmpsnAltDef2<br>CO1.2<br>[Qua92a]       | Composition alternate definition 2                | - | 189 | 2.1 | 4% | 46% |
| SET389<br>-6         | CmpsnAltDef3<br>CO1.3<br>[Qua92a]       | Composition alternate definition 3                | - | 189 | 2.1 | 4% | 46% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References   | V | Cl  | Av  | nH | Eq  |
|----------------------|------------------------------|---|---|-----|-----|----|-----|
| SET390<br>-6         | CmpsnAltDef4<br>CO1.4        | Composition alternate definition 4<br>[Qua92a]                        | - | 189 | 2.1 | 4% | 46% |
| SET391<br>-6         | CmpsnEqn1<br>CO2             | Composition property 1<br>[Qua92a]                                    | - | 192 | 2.0 | 4% | 46% |
| SET392<br>-6         | CmpsnRId<br>CO3.1            | Right identity for composition<br>[Qua92a]                            | - | 188 | 2.1 | 4% | 47% |
| SET393<br>-6         | CmpsnLId<br>CO3.2            | Left identity for composition<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 47% |
| SET394<br>-6         | CmpsnEqn2<br>CO4             | Composition property 2<br>[Qua92a]                                    | - | 188 | 2.1 | 4% | 46% |
| SET395<br>-6         | CmpsnImg<br>CO5              | Composition relates to image<br>[Qua92a]                              | - | 188 | 2.1 | 4% | 47% |
| SET396<br>-6         | DomOfCmpsn1<br>CO6.1         | Domain of composition 1<br>[Qua92a]                                   | - | 188 | 2.1 | 4% | 46% |
| SET397<br>-6         | RngOfCmpsn<br>CO6.2          | Range of composition<br>[Qua92a]                                      | - | 188 | 2.1 | 4% | 46% |
| SET398<br>-6         | CmpsnAssc<br>CO7             | Associativity of composition<br>[Qua92a]                              | - | 188 | 2.1 | 4% | 47% |
| SET399<br>-6         | LCmpsnNullCl<br>CO8.1        | Left compose with null class<br>[Qua92a]                              | - | 188 | 2.1 | 4% | 47% |
| SET400<br>-6         | RCmpsnNullCl<br>CO8.2        | Right compose with null class<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 47% |
| SET401<br>-6         | LCmpsnUnicCl<br>CO8.3        | Left compose with universal class<br>[Qua92a]                         | - | 188 | 2.1 | 4% | 47% |
| SET402<br>-6         | RCmpsnUnicCl<br>CO8.4        | Right compose with universal class<br>[Qua92a]                        | - | 188 | 2.1 | 4% | 47% |
| SET403<br>-6         | DomOfCmpsn2<br>CO10          | Domain of composition 2<br>[Qua92a]                                   | - | 189 | 2.1 | 4% | 46% |
| SET404<br>-6         | CmpsnMono1<br>CO11.1         | Monotonicity of composition 1<br>[Qua92a]                             | - | 189 | 2.1 | 4% | 46% |
| SET405<br>-6         | CmpsnMono2<br>CO11.2         | Monotonicity of composition 2<br>[Qua92a]                             | - | 189 | 2.1 | 4% | 46% |
| SET406<br>-6         | CmpsnMonoCor1<br>CO11 cor.1  | Corollary 1 monotonicity of composition<br>[Qua92a]                   | - | 189 | 2.1 | 4% | 46% |
| SET407<br>-6         | CmpsnMonoCor2<br>CO11 cor.2  | Corollary 2 monotonicity of composition<br>[Qua92a]                   | - | 189 | 2.1 | 4% | 46% |
| SET408<br>-6         | InvCmpsn<br>CO12             | Inverse of composition<br>[Qua92a]                                    | - | 188 | 2.1 | 4% | 47% |
| SET409<br>-6         | CmpsnElRel1<br>CO13.1        | Composition of element relation 1<br>[Qua92a]                         | - | 189 | 2.1 | 4% | 46% |
| SET410<br>-6         | CmpsnElRel2<br>CO13.2        | Composition of element relation 2<br>[Qua92a]                         | - | 190 | 2.0 | 4% | 46% |
| SET411<br>-6         | CmpsnSgtnE11<br>CO15         | Compose condition for singleton membership 1<br>[Qua92a]              | - | 189 | 2.1 | 4% | 46% |
| SET412<br>-6         | CmpsnSgtnE12<br>CO16         | Compose condition for singleton membership 2<br>[Qua92a]              | - | 189 | 2.1 | 4% | 46% |
| SET413<br>-6         | CmpsnSgtnE13<br>CO17         | Compose condition for singleton membership 3<br>[Qua92a]              | - | 190 | 2.0 | 4% | 46% |
| SET414<br>-6         | CmpsnUnion<br>CO18           | Composition distributes over union<br>[Qua92a]                        | - | 188 | 2.1 | 4% | 47% |
| SET415<br>-6         | CmpsnSgtnFunc1<br>CO19.1     | Composition with singleton function 1<br>[Qua92a]                     | - | 189 | 2.1 | 4% | 46% |
| SET416<br>-6         | CmpsnSgtnFunc2<br>CO19.2     | Composition with singleton function 2<br>[Qua92a]                     | - | 189 | 2.1 | 4% | 46% |
| SET417<br>-6         | CmpsnEqn1<br>CO21            | Composition property 1<br>[Qua92a]                                    | - | 188 | 2.1 | 4% | 46% |
| SET418<br>-6         | CmpsnEqn2<br>CO22            | Composition property 2<br>[Qua92a]                                    | - | 188 | 2.1 | 4% | 46% |
| SET419<br>-6         | CmpsnEqn3<br>CO23            | Composition property 3<br>[Qua92a]                                    | - | 189 | 2.1 | 4% | 46% |
| SET420<br>-6         | CmpsnEqn4<br>CO24            | Composition property 4<br>[Qua92a]                                    | - | 189 | 2.1 | 4% | 46% |
| SET421<br>-6         | CmpsnClFunc<br>CO26          | Compose class is a function<br>[Qua92a]                               | - | 188 | 2.1 | 4% | 46% |
| SET422<br>-6         | CmpsnClApply<br>CO27         | Compose class and apply<br>[Qua92a]                                   | - | 189 | 2.1 | 4% | 46% |
| SET423<br>-6         | SumCmpsnCl<br>CO28           | Sum compose class<br>[Qua92a]   | - | 188 | 2.1 | 4% | 47% |
| SET424<br>-6         | CmpsnClCmpsn<br>CO29         | Compose class and composition function are related<br>[Qua92a]        | - | 189 | 2.1 | 4% | 46% |
| SET425<br>-6         | SVCIAltDef1<br>SV1           | Single valued class alternate definition 1<br>[Qua92a]                | - | 193 | 2.0 | 4% | 46% |
| SET426<br>-6         | SVCIAltDef2<br>SV3.1         | Single valued class alternate definition 2<br>[Qua92a]                | - | 189 | 2.1 | 4% | 46% |
| SET427<br>-6         | SVCIAltDef3<br>SV3.2         | Single valued class alternate definition 3<br>[Qua92a]                | - | 189 | 2.1 | 4% | 46% |
| SET428<br>-6         | SVCIAltDef4<br>SV3.3         | Single valued class alternate definition 4<br>[Qua92a]                | - | 189 | 2.1 | 4% | 46% |
| SET429<br>-6         | SubClSVC1<br>SV4             | A subclass of a single-valued class is single-valued<br>[Qua92a]      | - | 189 | 2.1 | 4% | 46% |
| SET430<br>-6         | SVC1Img<br>SV5               | In a single-valued class, each image is a singleton<br>[Qua92a]       | - | 191 | 2.0 | 4% | 47% |
| SET431<br>-6         | CmpsnSVC1s<br>SV6            | The composition of single-valued classes is single-valued<br>[Qua92a] | - | 190 | 2.0 | 4% | 46% |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References  | V | Cl  | Av  | nH | Eq  |
|----------------------|------------------------------|--|---|-----|-----|----|-----|
| SET432<br>-6         | FuncAltDef1<br>FU1           | Function alternate definition 1<br>[Qua92a]                                | - | 191 | 2.0 | 4% | 46% |
| SET433<br>-6         | FuncAltDef2<br>FU3.1         | Function alternate definition 2<br>[Qua92a]                                | - | 190 | 2.0 | 4% | 46% |
| SET434<br>-6         | FuncAltDef3<br>FU3.2         | Function alternate definition 3<br>[Qua92a]                                | - | 190 | 2.0 | 4% | 46% |
| SET435<br>-6         | FuncAltDef4<br>FU3.3         | Function alternate definition 4<br>[Qua92a]                                | - | 190 | 2.0 | 4% | 46% |
| SET436<br>-6         | SubClOfFunc1<br>FU4.1        | Subclass of function is a function, part 1<br>[Qua92a]                     | - | 189 | 2.1 | 4% | 46% |
| SET437<br>-6         | SubClOfFunc2<br>FU4.2        | Subclass of function is a function, part 2<br>[Qua92a]                     | - | 189 | 2.1 | 4% | 46% |
| SET438<br>-6         | FuncImg<br>FU5               | In a function, the image of each domain element is a singleton<br>[Qua92a] | - | 191 | 2.0 | 4% | 47% |
| SET439<br>-6         | NullClFunc<br>FU7            | Null class is a function<br>[Qua92a]                                       | - | 188 | 2.1 | 4% | 46% |
| SET440<br>-6         | RstnFuncs<br>FU1, FU8        | The restriction of function is function<br>[Qua92a]                        | - | 189 | 2.1 | 4% | 46% |
| SET441<br>-6         | IntscFuncs<br>FU2, FU9       | The intersection of functions is a function<br>[Qua92a]                    | - | 190 | 2.0 | 4% | 46% |
| SET442<br>-6         | RstnFunc<br>FU4, FU10        | Restriction of function<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET443<br>-6         | DiffFuncs<br>FU11            | Difference of functions is a function<br>[Qua92a]                          | - | 190 | 2.0 | 4% | 46% |
| SET444<br>-6         | FuncEqn1<br>FU12             | Function property 1<br>[Qua92a]  | - | 191 | 2.0 | 4% | 46% |
| SET445<br>-6         | FuncEqn2<br>FU12 cor.        | Corollary to function property 1<br>[Qua92a]                               | - | 190 | 2.0 | 4% | 46% |
| SET446<br>-6         | FuncEqn2Cor<br>FU13          | Function property 2<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET447<br>-6         | FuncEqn3<br>FU14             | Function property 3<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET448<br>-6         | FuncEqn4<br>FU15             | Function property 4<br>[Qua92a]  | - | 191 | 2.0 | 4% | 46% |
| SET449<br>-6         | FuncSubS1<br>FU16.1          | Condition 1 for one function to be a subset of another<br>[Qua92a]         | - | 193 | 2.0 | 4% | 47% |
| SET450<br>-6         | FuncSubS2<br>FU16.2          | Condition 2 for one function to be a subset of another<br>[Qua92a]         | - | 193 | 2.0 | 4% | 47% |
| SET451<br>-6         | SubSRelAltDef1<br>SR1        | Subset relation alternate definition 1<br>[Qua92a]                         | - | 188 | 2.1 | 4% | 46% |
| SET452<br>-6         | SubSRelAltDef2<br>SR2        | Subset relation alternate definition 2<br>[Qua92a]                         | - | 189 | 2.1 | 4% | 46% |
| SET453<br>-6         | SubSRelAltDef3<br>SR3        | Subset relation alternate definition 3<br>[Qua92a]                         | - | 190 | 2.0 | 4% | 46% |
| SET454<br>-6         | IdAltDef1<br>ID1             | Identity alternate definition 1<br>[Qua92a]                                | - | 188 | 2.1 | 4% | 46% |
| SET455<br>-6         | IdAltDef2<br>ID2             | Identity alternate definition 2<br>[Qua92a]                                | - | 189 | 2.1 | 4% | 46% |
| SET456<br>-6         | IdAltDef3<br>ID3             | Identity alternate definition 3<br>[Qua92a]                                | - | 190 | 2.0 | 4% | 46% |
| SET457<br>-6         | IdFunc<br>ID4                | Identity is a function<br>[Qua92a]   | - | 188 | 2.1 | 4% | 46% |
| SET458<br>-6         | IdFuncCor<br>ID4 cor.        | Corollary to identity is a function<br>[Qua92a]                            | - | 188 | 2.1 | 4% | 46% |
| SET459<br>-6         | IdDom<br>ID5.1               | Domain of identity is the universal class<br>[Qua92a]                      | - | 188 | 2.1 | 4% | 47% |
| SET460<br>-6         | IdRng<br>ID5.2               | Range of identity<br>[Qua92a]  | - | 188 | 2.1 | 4% | 47% |
| SET461<br>-6         | RstdIdDom<br>ID5.3           | Domain of restricted identity<br>[Qua92a]                                  | - | 188 | 2.1 | 4% | 47% |
| SET462<br>-6         | RstdIdRng<br>ID5.4           | Range of restricted identity<br>[Qua92a]                                   | - | 188 | 2.1 | 4% | 47% |
| SET463<br>-6         | IdDomRngCor<br>ID5 cor.      | Corollary to domain and range of identity<br>[Qua92a]                      | - | 188 | 2.1 | 4% | 47% |
| SET464<br>-6         | ClImgId<br>ID6               | Class image under identity<br>[Qua92a]                                     | - | 188 | 2.1 | 4% | 47% |
| SET465<br>-6         | Id1to1<br>ID7                | Identity is one-to-one<br>[Qua92a]   | - | 188 | 2.1 | 4% | 46% |
| SET466<br>-6         | InvId<br>ID8                 | Inverse of identity is identity<br>[Qua92a]                                | - | 188 | 2.1 | 4% | 47% |
| SET467<br>-6         | Set1E11<br>ID9.1             | Sets with at most one member 1<br>[Qua92a]                                 | - | 190 | 2.0 | 4% | 47% |
| SET468<br>-6         | Set1E12<br>ID9.2             | Sets with at most one member 2<br>[Qua92a]                                 | - | 189 | 2.1 | 4% | 46% |
| SET469<br>-6         | Set1E13<br>ID9.3             | Sets with at most one member 3<br>[Qua92a]                                 | - | 190 | 2.1 | 4% | 47% |
| SET470<br>-6         | Set1E1Cor<br>ID9 cor.        | Corollary to sets with one member<br>[Qua92a]                              | - | 191 | 2.0 | 4% | 47% |
| SET471<br>-6         | SetNE11<br>ID10.1            | Sets with more than one member 1<br>[Qua92a]                               | - | 190 | 2.0 | 4% | 46% |
| SET472<br>-6         | SetNE12<br>ID10.2            | Sets with more than one member 2<br>[Qua92a]                               | - | 190 | 2.0 | 4% | 46% |
| SET473<br>-6         | RstdDomLem1<br>ID11.1        | Lemma 1 to restricted domain<br>[Qua92a]                                   | - | 189 | 2.1 | 4% | 47% |

| Syntactic name<br>V# | Semantic name<br>Other names  | Description<br>References   | V | Cl  | Av  | nH | Eq  |
|----------------------|-------------------------------|---|---|-----|-----|----|-----|
| SET474<br>-6         | RstdDomLem2<br>ID11.2         | Lemma 2 to restricted domain<br>[Qua92a]                                    | - | 190 | 2.0 | 4% | 46% |
| SET475<br>-6         | RstdDom<br>ID11.3             | Restricted domain<br>[Qua92a]   | - | 191 | 2.0 | 4% | 47% |
| SET476<br>-6         | IntescCl<br>ID11.4, ID12      | Intersection subclass<br>[Qua92a]   | - | 188 | 2.1 | 4% | 46% |
| SET477<br>-6         | AxOfSubs1<br>RP1.1            | Axiom of subsets 1<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET478<br>-6         | AxOfSubs2<br>RP1.2            | Axiom of subsets 2<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET479<br>-6         | RplmtEqn1<br>RP2.1            | Replacement property 1<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET480<br>-6         | RplmtEqn2<br>RP2.2            | Replacement property 2<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET481<br>-6         | RplmtEqn3<br>RP3              | Replacement property 3<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET482<br>-6         | RplmtEqn4<br>RP4              | Replacement property 4<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET483<br>-6         | RplmtEqn5<br>RP5              | Replacement property 5<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET484<br>-6         | RplmtEqn6<br>RP6              | Replacement property 6<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET485<br>-6         | RplmtEqn7<br>RP7              | Replacement property 7<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET486<br>-6         | RplmtEqn8<br>RP8              | Replacement property 8<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET487<br>-6         | RplmtEqn9<br>RP9              | Replacement property 9<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET488<br>-6         | RplmtEqn10<br>RP10            | Replacement property 10<br>[Qua92a]   | - | 189 | 2.1 | 4% | 46% |
| SET489<br>-6         | RplmtEqn11<br>RP11.1          | Replacement property 11<br>[Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET490<br>-6         | RplmtEqn12<br>RP11.2          | Replacement property 12<br>[Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET491<br>-6         | DiagnLem1<br>DI1.1            | Diagonalization lemma 1<br>[Qua92a]   | - | 189 | 2.1 | 4% | 46% |
| SET492<br>-6         | DiagnLem2<br>DI1.2            | Diagonalization lemma 2<br>[Qua92a]   | - | 189 | 2.1 | 4% | 46% |
| SET493<br>-6         | DiagnCor<br>DI1 cor.          | Diagonalization corollary<br>[Qua92a]                                       | - | 190 | 2.0 | 4% | 46% |
| SET494<br>-6         | DiagnAltDef1<br>DI2           | Diagonalization alternate definition 1<br>[Qua92a]                          | - | 188 | 2.1 | 4% | 47% |
| SET495<br>-6         | DiagnAltDef2<br>DI3           | Diagonalization alternate definition 2<br>[Qua92a]                          | - | 189 | 2.1 | 4% | 46% |
| SET496<br>-6         | DiagnAltDef3<br>DI4           | Diagonalization alternate definition 3<br>[Qua92a]                          | - | 190 | 2.0 | 4% | 46% |
| SET497<br>-6         | RussellC11<br>DI5             | Special case of the Russell class, without the regularity axiom<br>[Qua92a] | - | 189 | 2.1 | 4% | 46% |
| SET498<br>-6         | RussellC12<br>DI6             | Special case of the Russell class, without the regularity axiom<br>[Qua92a] | - | 190 | 2.0 | 4% | 46% |
| SET499<br>-6         | RussellCINotSet<br>DI7        | The Russell class not a set<br>[Qua92a]                                     | - | 188 | 2.1 | 4% | 46% |
| SET500<br>-6         | DiagnEqn1<br>DI8              | Diagonalization property 1<br>[Qua92a]                                      | - | 188 | 2.1 | 4% | 47% |
| SET501<br>-6         | DiagnEqn2<br>DI9.1            | Diagonalization property 2<br>[Qua92a]                                      | - | 188 | 2.1 | 4% | 47% |
| SET502<br>-6         | DiagnEqn3<br>DI9.2            | Diagonalization property 3<br>[Qua92a]                                      | - | 188 | 2.1 | 4% | 47% |
| SET503<br>-6         | UnivCINotSet<br>SP6           | The universal class not set<br>[Qua92a]                                     | - | 188 | 2.1 | 4% | 46% |
| SET504<br>-6         | UnivCINotSetCor1<br>SP6 cor.1 | Corollary 1 to universal class not set<br>[Qua92a]                          | - | 188 | 2.1 | 4% | 46% |
| SET505<br>-6         | UnivCINotSetCor2<br>SP6 cor.2 | Corollary 2 to universal class not set<br>[Qua92a]                          | - | 188 | 2.1 | 4% | 46% |
| SET506<br>-6         | UnivCINotNullC1<br>SP7.1      | Universal class not null class<br>[Qua92a]                                  | - | 188 | 2.1 | 4% | 47% |
| SET507<br>-6         | UnivCINotNullSubC1<br>SP7.2   | Universal class not subclass of null class<br>[Qua92a]                      | - | 188 | 2.1 | 4% | 46% |
| SET508<br>-6         | SgtnUOrdPrAxCor1<br>SP8.1     | Corollary 1 to singleton in unordered pair axiom<br>[Qua92a]                | - | 188 | 2.1 | 4% | 47% |
| SET509<br>-6         | SgtnUOrdPrAxCor2<br>SP8.2     | Corollary 2 to singleton in unordered pair axiom<br>[Qua92a]                | - | 188 | 2.1 | 4% | 47% |
| SET510<br>-6         | SgtnNullCICor<br>SP9          | Corollary to singleton is null class<br>[Qua92a]                            | - | 188 | 2.1 | 4% | 47% |
| SET511<br>-6         | OrdPrElCor1<br>SP10.1         | Corollary 1 to special members of ordered pairs<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 47% |
| SET512<br>-6         | OrdPrElCor2<br>SP10.2         | Corollary 2 to special members of ordered pairs<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 47% |
| SET513<br>-6         | OrdPrElCor3<br>SP10.3         | Corollary 3 to special members of ordered pairs<br>[Qua92a]                 | - | 188 | 2.1 | 4% | 47% |
| SET514<br>-6         | OrdPrCINotSet<br>SP11         | Class of ordered pairs is not a set<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 46% |
| SET515<br>-6         | CINotCIE1<br>RE1              | No class belongs to itself<br>[Qua92a]                                      | - | 188 | 2.1 | 4% | 46% |

| Syntactic name<br>V# | Semantic name<br>Other names       | Description<br>References  | V | Cl  | Av  | nH | Eq  |
|----------------------|------------------------------------|--|---|-----|-----|----|-----|
| SET516               | -6<br>CINotCIEICor<br>RE2          | Corollary to no class belongs to itself<br>[Qua92a]                          | - | 188 | 2.1 | 4% | 47% |
| SET517               | -6<br>XE1XNotSgtn<br>RE3           | If member of X is X then X is not a singleton of a set<br>[Qua92a]           | - | 190 | 2.1 | 4% | 47% |
| SET518               | -6<br>No2Cycle<br>RE4              | There are no cycles of length 2<br>[Qua92a]                                  | - | 189 | 2.1 | 4% | 46% |
| SET519               | -6<br>No2CycleCor1<br>RE5.1        | Corollary 1 to no cycles of length 2<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 47% |
| SET520               | -6<br>No2CycleCor2<br>RE5.2        | Corollary 2 to no cycles of length 2<br>[Qua92a]                             | - | 188 | 2.1 | 4% | 47% |
| SET521               | -6<br>OrdPrCmpts1<br>RE6.1         | Ordered pair determines components 1<br>[Qua92a]                             | - | 189 | 2.1 | 4% | 46% |
| SET522               | -6<br>OrdPrCmpts2<br>RE6.2         | Ordered pair determines components 2<br>[Qua92a]                             | - | 189 | 2.1 | 4% | 46% |
| SET523               | -6<br>ElCpmtNotSet<br>RE7          | Element and complement can't both be sets<br>[Qua92a]                        | - | 189 | 2.1 | 4% | 46% |
| SET524               | -6<br>NotOrdPr1<br>RE8.1           | Equivalent condition 1 for x not to be an ordered pair<br>[Qua92a]           | - | 189 | 2.1 | 4% | 47% |
| SET525               | -6<br>NotOrdPr2<br>RE8.2           | Equivalent condition 2 for x not to be an ordered pair<br>[Qua92a]           | - | 189 | 2.1 | 4% | 47% |
| SET526               | -6<br>OrdPrCmptSet1<br>RE9.1       | Ordered pair components are sets 1<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET527               | -6<br>OrdPrCmptSet2<br>RE9.2       | Ordered pair components are sets 2<br>[Qua92a]                               | - | 189 | 2.1 | 4% | 46% |
| SET528               | -6<br>OrdPrCmptSetCor1<br>RE9 cor. | Corollary 1 to ordered pair components are sets<br>[Qua92a]                  | - | 189 | 2.1 | 4% | 46% |
| SET529               | -6<br>OrdPrCmptSetCor2<br>RE10.1   | Corollary 2 to ordered pair components are sets<br>[Qua92a]                  | - | 189 | 2.1 | 4% | 46% |
| SET530               | -6<br>OrdPrCmptSetCor3<br>RE10.2   | Corollary 3 to ordered pair components are sets<br>[Qua92a]                  | - | 189 | 2.1 | 4% | 46% |
| SET531               | -6<br>AppnEqn1<br>AP1.1            | Application property 1<br>[Qua92a]   | - | 191 | 2.0 | 4% | 47% |
| SET532               | -6<br>AppnEqn2<br>AP1.2            | Application property 2<br>[Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET533               | -6<br>RngClAppn1<br>AP2            | The range of Z is the class of applications of Z to Z's domain 1<br>[Qua92a] | - | 190 | 2.0 | 4% | 46% |
| SET534               | -6<br>RngClAppn2<br>AP3            | The range of Z is the class of applications of Z to Z's domain 2<br>[Qua92a] | - | 190 | 2.0 | 4% | 46% |
| SET535               | -6<br>AppnEqn3<br>AP4              | Application property 3<br>[Qua92a]   | - | 189 | 2.1 | 4% | 46% |
| SET536               | -6<br>AppnEqn3Cor1<br>AP4 cor.1    | Corollary 1 to application property 3<br>[Qua92a]                            | - | 188 | 2.1 | 4% | 46% |
| SET537               | -6<br>AppnEqn3Cor2<br>AP4 cor.2    | Corollary 2 to application property 3<br>[Qua92a]                            | - | 190 | 2.0 | 4% | 46% |
| SET538               | -6<br>AppnEqn4<br>AP5              | Application property 4<br>[Qua92a]   | - | 188 | 2.1 | 4% | 47% |
| SET539               | -6<br>AppnEqn5<br>AP6.1            | Application property 5<br>[Qua92a]   | - | 189 | 2.1 | 4% | 46% |
| SET540               | -6<br>AppnEqn6<br>AP6.2            | Application property 6<br>[Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET541               | -6<br>AppnEqn7<br>AP7, AP12        | Application property 7<br>[Qua92a]   | - | 189 | 2.1 | 4% | 46% |
| SET542               | -6<br>AppnEqn9Cor<br>AP9 cor.      | Corollary to application property 9<br>[Qua92a]                              | - | 190 | 2.0 | 4% | 46% |
| SET543               | -6<br>AppnEqn10Cor<br>AP10 cor.    | Corollary to application property 10<br>[Qua92a]                             | - | 191 | 2.0 | 4% | 46% |
| SET544               | -6<br>AppnEqn11Cor<br>AP11 cor.    | Corollary to application property 11<br>[Qua92a]                             | - | 190 | 2.0 | 4% | 46% |
| SET545               | -6<br>AppnEqn13<br>AP14.1, AP13.1  | Application special case 1<br>[Qua92a]                                       | - | 189 | 2.1 | 4% | 46% |
| SET546               | -6<br>AppnEqn14<br>AP14.2, AP13.2  | Application special case 2<br>[Qua92a]                                       | - | 189 | 2.1 | 4% | 46% |
| SET547               | -6<br>AppnEqn15<br>AP14.3, AP13.3  | Application special case 3<br>[Qua92a]                                       | - | 188 | 2.1 | 4% | 47% |
| SET548               | -6<br>AppnEqn16<br>AP14            | Application property 16<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET549               | -6<br>AppnEqn17<br>AP16            | Application property 17<br>[Qua92a]  | - | 188 | 2.1 | 4% | 46% |
| SET550               | -6<br>AppnEqn18<br>AP17            | Application property 18<br>[Qua92a]  | - | 188 | 2.1 | 4% | 46% |
| SET551               | -6<br>AppnEqn19<br>AP18            | Application property 19<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET552               | -6<br>AppnEqn20<br>AP19            | Application property 20<br>[Qua92a]  | - | 190 | 2.0 | 4% | 46% |
| SET553               | -6<br>CantorAltDef1<br>CA1         | Cantor class alternate definition 1<br>[Qua92a]                              | - | 188 | 2.1 | 4% | 46% |
| SET554               | -6<br>CantorAltDef2<br>CA2         | Cantor class alternate definition 2<br>[Qua92a]                              | - | 189 | 2.1 | 4% | 46% |
| SET555               | -6<br>CantorAltDef3<br>CA3         | Cantor class alternate definition 3<br>[Qua92a]                              | - | 190 | 2.0 | 4% | 46% |
| SET556               | -6<br>CantorEqn1<br>CA2            | Cantor class property 1<br>[Qua92a]  | - | 189 | 2.1 | 4% | 46% |
| SET557               | -6<br>CantorThm<br>CA4             | Cantor's theorem<br>[Qua92a]   | - | 190 | 2.0 | 4% | 46% |

| Syntactic name<br>V# | Semantic name<br>Other names   | Description                                   | References | V | Cl  | Av  | nH | Eq  |
|----------------------|--------------------------------|---|------------|---|-----|-----|----|-----|
| SET558<br>-6         | CmpblFuncAltDef1<br>CF1        | Compatible functions alternate definition 1   | [Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET559<br>-6         | CmpblFuncAltDef2<br>CF2        | Compatible functions alternate definition 2   | [Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET560<br>-6         | CmpblFuncAltDef3<br>CF3        | Compatible functions alternate definition 3   | [Qua92a]   | - | 191 | 2.0 | 4% | 46% |
| SET561<br>-6         | CmpblFuncEqn1<br>CF4           | Compatible function property 1                | [Qua92a]   | - | 191 | 2.0 | 4% | 46% |
| SET562<br>-6         | CmpblFuncEqn2<br>CF5           | Compatible function property 2                | [Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET563<br>-6         | CmpblFuncEqn3<br>CF6           | Compatible function property 3                | [Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET564<br>-6         | CmpblFuncEqn3Cor1<br>CF6 cor.1 | Corollary 1 to compatible function property 3 | [Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET565<br>-6         | CmpblFuncEqn3Cor2<br>CF6 cor.2 | Corollary 2 to compatible function property 3 | [Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET566<br>-6         | CmpblFuncEqn4<br>CF7           | Compatible function property 4                | [Qua92a]   | - | 190 | 2.0 | 4% | 46% |
| SET567<br>-6         | CmpblFunc1<br>CF8              | Compatible function special case              | [Qua92a]   | - | 188 | 2.1 | 4% | 46% |

### Domain SYN (340 abstract problems, 350 problems)

|                                |  |  |  |                  |                        |                          |                          |                  |
|--------------------------------|--|--|--|------------------|------------------------|--------------------------|--------------------------|------------------|
| SYN001<br>-1.005               | Allways<br>ls5 (Size 2), Pelletier 2, 6, 7, 8, 11 (Size 1),<br>Pelletier 9, 14 (Size 2), Pelletier 12 (Size 3) | All signed combinations of some propositions.                | [NS72, LS74, WM76, Pel86]  | -                | 32                     | 5.0                      | 81%                      | -                |
| SYN002<br>-1.007:008           | OddEven<br>ederX-Y.lop (Size X:Y)  | Odd and Even Problem   | [SA92]   | -                | 2                      | 2.0                      | 50%                      | -                |
| SYN003<br>-1.006               | Implies1<br>Problem 5.2  | Implications that form a contradiction                       | [Pla82]  | -                | 24                     | 2.3                      | -                        | -                |
| SYN004<br>-1.007               | Implies2<br>Problem 5.3  | Implications that form a contradiction                       | [Pla82]  | -                | 15                     | 2.7                      | -                        | -                |
| SYN005<br>-1.010               | Or1<br>Problem 5.4   | Disjunctions that form a contradiction                       | [Pla82]  | -                | 11                     | 1.8                      | -                        | -                |
| SYN006<br>-1                   | Splits<br>Problem 5.8  | A problem to demonstrate controlling splits                  | [Pla82]  | -                | 7                      | 1.7                      | 28%                      | -                |
| SYN007<br>-1.002               | FPell71<br>Pelletier 71  | Pelletier Problem 71   | [Pel86, Urq87]   | -                | 8                      | 3.0                      | 62%                      | -                |
| SYN008<br>-1                   | Relev1<br>Figure 3   | A problem to demonstrate the usefulness of relevancy testing | [WL89]   | -                | 6                      | 2.2                      | 50%                      | -                |
| SYN009<br>-1                   | Relev2<br>Figure 8   | A problem to demonstrate the usefulness of relevancy testing | [WL89]   | -                | 7                      | 1.7                      | 14%                      | -                |
| SYN010<br>-1.005:005           | Letz<br>Example 5.1  | Example for Proposition 5.2 in [Letz, et al., 1994]          | [LMG94]  | -                | 27                     | 4.9                      | -                        | -                |
| SYN011<br>-1                   | CRdcn<br>Problem for C Reduction   | A problem to demonstrate C-reduction                         | [Sho76]  | -                | 8                      | 2.1                      | 25%                      | -                |
| SYN012<br>-1                   | ModelElim<br>Example   | A problem to demonstrate Model Elimination                   | [Lov68]  | -                | 7                      | 2.4                      | 28%                      | -                |
| SYN013<br>-1                   | Quant1<br>ExQ1, EXQ1, wos31, exq1.ver1.in,<br>exq1.ver2.in, wang1.in   | A problem in quantification theory                           | [Wan65, Wosb, MOW76, WM76]   | -                | 23                     | 2.8                      | 47%                      | 61%              |
| SYN014<br>-1<br>-2             | Quant2<br>ExQ2, EXQ2, exq2.ver1.in, exq2.ver2.in<br>Problem 32, wos32  | A problem in quantification theory                           | [Wan65, MOW76]<br>[Wosb, Wan65, WM76]  | -<br>-           | 24<br>26               | 3.0<br>2.7               | 58%<br>50%               | 62%<br>-         |
| SYN015<br>-1<br>-2             | Quant3<br>ExQ3, EXQ3, exq3.ver1.in, exq3.ver2.in<br>Problem 33, wos33  | A problem in quantification theory                           | [Wan65, MOW76]<br>[Wosb, Wan65, WM76]  | -<br>-           | 23<br>26               | 3.0<br>2.7               | 56%<br>50%               | 60%<br>-         |
| SYN028<br>-1                   | EW1<br>EW1, EW1  | EW1  | [MRS72, WM76]  | -                | 6                      | 2.0                      | 16%                      | -                |
| SYN029<br>-1                   | EW2<br>EW2, EW2  | EW2  | [MRS72, WM76]  | -                | 5                      | 2.0                      | 20%                      | -                |
| SYN030<br>-1                   | EW3<br>EW3, EW3  | EW3  | [MRS72, WM76]  | -                | 9                      | 2.4                      | 11%                      | -                |
| SYN031<br>-1                   | MQW<br>MQW, MQW  | MQW  | [MRS72, WM76]  | -                | 5                      | 2.0                      | 40%                      | -                |
| SYN032<br>-1                   | Ances<br>ANCES2  | Ances  | [RRY <sup>+</sup> 72]  | -                | 7                      | 2.4                      | 42%                      | -                |
| SYN033<br>-1                   | DM<br>DM, DM   | DM   | [MRS72, WM76]  | -                | 4                      | 1.8                      | -                        | -                |
| SYN034<br>-1                   | QW<br>QW, QW   | QW   | [MRS72, WM76]  | -                | 3                      | 2.3                      | 66%                      | -                |
| SYN035<br>-1                   | ROB1<br>ROB1, ROB1   | ROB1   | [MRS72, WM76]  | -                | 3                      | 2.7                      | -                        | -                |
| SYN036<br>-1<br>-2<br>-3<br>-4 | PAndrews<br>Pelletier 34, andrews.in<br>Problem 9<br>Theorem A   | Andrews Challenge Problem                                    | [Cha79, Pel86, Pel88]<br>[Cha79, Pel86, And86, Pel88]<br>[Cha79, Pel86, AZ89]<br>[Cha79, Pel86, AZ89, Qua90] | -<br>-<br>-<br>- | 128<br>128<br>36<br>32 | 8.0<br>8.0<br>2.9<br>5.3 | 99%<br>99%<br>30%<br>78% | -<br>-<br>-<br>- |
| SYN037<br>-1<br>-2             | PAndrews2<br>Problem 1<br>Theorem P  | Andrews Challenge Problem Variant                            | [Cha79, Pel86, AZ89]<br>[Cha79, Pel86, AZ89, Qua90]  | -<br>-           | 36<br>22               | 2.9<br>3.5               | 30%<br>59%               | -<br>-           |
| SYN038<br>-1                   | SFleisig4<br>Example 4, EX4-T?, ex4.lop, FEX4T1, FEX4T2  | Syntactic formula  | [Fri63, FLSY74, WM76]  | -                | 7                      | 2.4                      | 28%                      | -                |
| SYN039<br>-1                   | VLifsch<br>lifsch.in   | A challenge to resolution programs                           | [Lif89]  | -                | 27                     | 3.0                      | 40%                      | -                |

| Syntactic name<br>V#     | Semantic name<br>Other names              | Description<br>References                              | V           | Cl             | Av                | nH                | Eq          |
|--------------------------|---|--|-------------|----------------|-------------------|-------------------|-------------|
| SYN040<br>-1             | FPell01<br>Pelletier 1                    | Pelletier Problem 1<br>[NSS63, Pel86]                  | -           | 4              | 1.5               | -                 | -           |
| SYN041<br>-1             | FPell03<br>Pelletier 3, Pelletier 16      | Pelletier Problem 3, 16<br>[SRM73, Pel86]              | -           | 4              | 1.0               | -                 | -           |
| SYN044<br>-1             | FPell10<br>Pelletier 10                   | Pelletier Problem 10<br>[Pel86]                        | -           | 6              | 2.2               | 33%               | -           |
| SYN045<br>-1             | FPell13<br>Pelletier 13                   | Pelletier Problem 13<br>[Pel86]                        | -           | 4              | 1.8               | 50%               | -           |
| SYN046<br>-1             | FPell15<br>Pelletier 15                   | Pelletier Problem 15<br>[Pel86, Pel88]                 | -           | 3              | 1.3               | -                 | -           |
| SYN047<br>-1             | FPell17<br>Pelletier 17                   | Pelletier Problem 17<br>[BBN72, Pel82, Pel86]          | -           | 5              | 2.0               | 20%               | -           |
| SYN048<br>-1             | FPell18<br>Pelletier 18                   | Pelletier Problem 18<br>[Pel86]                        | -           | 2              | 1.0               | -                 | -           |
| SYN049<br>-1             | FPell19<br>Pelletier 19                   | Pelletier Problem 19<br>[Pel86]                        | -           | 3              | 1.3               | -                 | -           |
| SYN050<br>-1             | FPell20<br>Pelletier 20                   | Pelletier Problem 20<br>[Pel86]                        | -           | 5              | 1.8               | -                 | -           |
| SYN051<br>-1             | FPell21<br>Pelletier 21                   | Pelletier Problem 21<br>[Pel86]                        | -           | 4              | 2.0               | 25%               | -           |
| SYN052<br>-1             | FPell22<br>Pelletier 22                   | Pelletier Problem 22<br>[Pel86]                        | -           | 5              | 2.0               | 20%               | -           |
| SYN053<br>-1             | FPell23<br>Pelletier 23                   | Pelletier Problem 23<br>[Pel86]                        | -           | 5              | 2.4               | 60%               | -           |
| SYN054<br>-1             | FPell24<br>Pelletier 24                   | Pelletier Problem 24<br>[KM64, Pel86]                  | -           | 6              | 2.2               | 33%               | -           |
| SYN055<br>-1             | FPell25<br>Pelletier 25                   | Pelletier Problem 25<br>[KM64, Pel86]                  | -           | 7              | 2.3               | 28%               | -           |
| SYN056<br>-1             | FPell26<br>Pelletier 26                   | Pelletier Problem 26<br>[KM64, Pel86]                  | -           | 13             | 2.8               | 30%               | -           |
| SYN057<br>-1             | FPell27<br>Pelletier 27                   | Pelletier Problem 27<br>[KM64, Pel86]                  | -           | 7              | 1.9               | -                 | -           |
| SYN058<br>-1             | FPell28<br>Pelletier 28                   | Pelletier Problem 28<br>[KM64, Pel86, Pel88]           | -           | 9              | 1.8               | -                 | -           |
| SYN059<br>-1             | FPell29<br>Pelletier 29                   | Pelletier Problem 29<br>[KM64, Pel86]                  | -           | 32             | 3.8               | 68%               | -           |
| SYN060<br>-1             | FPell30<br>Pelletier 30                   | Pelletier Problem 30<br>[KM64, Pel86]                  | -           | 7              | 1.9               | 57%               | -           |
| SYN061<br>-1             | FPell31<br>Pelletier 31                   | Pelletier Problem 31<br>[KM64, Pel86]                  | -           | 6              | 1.7               | 16%               | -           |
| SYN062<br>-1             | FPell32<br>Pelletier 32                   | Pelletier Problem 32<br>[KM64, Pel86]                  | -           | 7              | 2.0               | -                 | -           |
| SYN063<br>-1<br>-2       | FPell33<br>Pelletier 33                   | Pelletier Problem 33<br>[KM64, Pel86]<br>[KM64, Pel86] | -<br>-      | 7<br>3         | 3.1<br>1.3        | 42%<br>-          | -<br>-      |
| SYN064<br>-1             | FPell35<br>Pelletier 35, p35.in           | Pelletier Problem 35<br>[KM64, Pel86]                  | -           | 2              | 1.0               | -                 | -           |
| SYN065<br>-1             | FPell36<br>Pelletier 36, p36.in           | Pelletier Problem 36<br>[Pel86]                        | -           | 7              | 2.1               | -                 | -           |
| SYN066<br>-1             | FPell37<br>Pelletier 37, p37.in           | Pelletier Problem 37<br>[Pel86]                        | -           | 6              | 1.7               | 16%               | -           |
| SYN067<br>-1<br>-2<br>-3 | FPell38<br>Pelletier 38, p38a.in, p38b.in | Pelletier Problem 38<br>[Pel86]<br>[Pel86]<br>[Pel86]  | -<br>-<br>- | 84<br>55<br>46 | 6.0<br>5.3<br>5.6 | 82%<br>80%<br>86% | -<br>-<br>- |
| SYN068<br>-1             | FPell44<br>Pelletier 44, p44.in           | Pelletier Problem 44<br>[KM64, Pel86]                  | -           | 7              | 1.9               | -                 | -           |
| SYN069<br>-1             | FPell45<br>Pelletier 45, p45.in           | Pelletier Problem 45<br>[KM64, Pel86]                  | -           | 9              | 3.0               | 22%               | -           |
| SYN070<br>-1             | FPell46<br>Pelletier 46, p46.in           | Pelletier Problem 46<br>[KM64, Pel86]                  | -           | 9              | 2.9               | 44%               | -           |
| SYN071<br>-1             | FPell48<br>Pelletier 48                   | Pelletier Problem 48<br>[Pel86, Rud93]                 | -           | 7              | 1.7               | 28%               | 100%        |
| SYN072<br>-1             | FPell49<br>Pelletier 49                   | Pelletier Problem 49<br>[Pel86]                        | -           | 9              | 1.7               | 11%               | 66%         |
| SYN073<br>-1             | FPell50<br>Pelletier 50                   | Pelletier Problem 50<br>[Pel86]                        | -           | 8              | 2.1               | 12%               | 58%         |
| SYN074<br>-1             | FPell51<br>Pelletier 51                   | Pelletier Problem 51<br>[Pel86]                        | -           | 20             | 2.8               | 25%               | 65%         |
| SYN075<br>-1             | FPell52<br>Pelletier 52                   | Pelletier Problem 52<br>[Pel86]                        | -           | 19             | 2.7               | 21%               | 64%         |
| SYN076<br>-1             | FPell53<br>Pelletier 53                   | Pelletier Problem 53<br>[Pel86]                        | -           | 53             | 4.4               | 60%               | 71%         |
| SYN077<br>-1             | FPell54<br>Pelletier 54                   | Pelletier Problem 54<br>[Mon55, Pel86, Pel88]          | -           | 18             | 2.4               | 16%               | 51%         |
| SYN078<br>-1             | FPell56<br>Pelletier 56                   | Pelletier Problem 56<br>[Pel86, Pel88]                 | -           | 17             | 2.7               | 35%               | 34%         |
| SYN079<br>-1             | FPell57<br>Pelletier 57                   | Pelletier Problem 57<br>[Pel86]                        | -           | 4              | 1.5               | -                 | -           |
| SYN080<br>-1             | FPell58<br>Pelletier 58                   | Pelletier Problem 58<br>[Pel86]                        | -           | 7              | 1.7               | -                 | 100%        |
| SYN081<br>-1             | FPell59<br>Pelletier 59                   | Pelletier Problem 59<br>[Pel86]                        | -           | 3              | 2.0               | 33%               | -           |
| SYN082<br>-1             | FPell60<br>Pelletier 60                   | Pelletier Problem 60<br>[Pel86, Pel88]                 | -           | 8              | 3.1               | 50%               | -           |

| Syntactic name<br>V# | Semantic name<br>Other names            | Description<br>References                                      | V      | Cl      | Av         | nH         | Eq     |
|----------------------|---|--|--------|---------|------------|------------|--------|
| SYN083<br>-1         | FPell61<br>Pelletier 61                 | [Pel86] Pelletier Problem 61                                   | -      | 7       | 1.7        | -          | 100%   |
| SYN084<br>-1<br>-2   | FPell62<br>Pelletier 62<br>Pelletier 62 | [Pel86, Pel88, Pel95]<br>[Pel86, Pel88, Häh94, Pel95]          | -<br>- | 13<br>7 | 3.8<br>2.7 | 61%<br>28% | -<br>- |
| SYN085<br>-1.010     | DAPs1<br>S1n                            | [Pla94] Plaisted problem s(1,10)                               | -      | 12      | 1.8        | -          | -      |
| SYN086<br>-1.003     | DAPs2<br>S2n                            | [Pla94] Plaisted problem s(2,3)                                | -      | 19      | 2.6        | -          | -      |
| SYN087<br>-1.003     | DAPs3<br>S3n                            | [Pla94] Plaisted problem s(3,3)                                | -      | 21      | 2.8        | -          | -      |
| SYN088<br>-1.010     | DAPs4<br>S4n                            | [Pla94] Plaisted problem s(4,10)                               | -      | 22      | 1.5        | -          | -      |
| SYN089<br>-1.002     | DAPt2<br>T2n                            | [Pla94] Plaisted problem t(2,2)                                | -      | 13      | 1.9        | -          | -      |
| SYN090<br>-1.008     | DAPt3<br>T3n                            | [Pla94] Plaisted problem t(3,8)                                | -      | 65      | 2.8        | -          | -      |
| SYN091<br>-1.003     | DAPsyms2<br>Sym(S2n)                    | [Pla94] Plaisted problem sym(s(2,3))                           | -      | 38      | 2.6        | 31%        | -      |
| SYN092<br>-1.003     | DAPsyms3<br>Sym(S3n)                    | [Pla94] Plaisted problem sym(s(3,3))                           | -      | 42      | 2.8        | 40%        | -      |
| SYN093<br>-1.002     | DAPut2<br>U(T2n)                        | [Pla94] Plaisted problem u(t(2,2))                             | -      | 26      | 2.4        | 46%        | -      |
| SYN094<br>-1.005     | DAPut3<br>U(T3n)                        | [Pla94] Plaisted problem u(t(3,5))                             | -      | 82      | 2.8        | 48%        | -      |
| SYN095<br>-1.002     | DAPmt2<br>M(T2n)                        | [Pla94] Plaisted problem m(t(2,2))                             | -      | 13      | 1.9        | -          | -      |
| SYN096<br>-1.008     | DAPmt3<br>M(T3n)                        | [Pla94] Plaisted problem m(t(3,8))                             | -      | 65      | 2.8        | -          | -      |
| SYN097<br>-1.002     | DAPsymt2<br>Sym(U(T2n))                 | [Pla94] Plaisted problem sym(u(t(2,2)))                        | -      | 52      | 2.4        | 30%        | -      |
| SYN098<br>-1.002     | DAPsymt3<br>Sym(U(T3n))                 | [Pla94] Plaisted problem sym(u(t(3,2)))                        | -      | 68      | 2.6        | 36%        | -      |
| SYN099<br>-1.003     | DAPsymmt2<br>Sym(M(T2n))                | [Pla94] Plaisted problem sym(m(t(2,3)))                        | -      | 50      | 2.2        | 24%        | -      |
| SYN100<br>-1.005     | DAPsymmt3<br>Sym(M(T3n))                | [Pla94] Plaisted problem sym(m(t(3,5)))                        | -      | 82      | 2.7        | 40%        | -      |
| SYN101<br>-1.002:002 | DAPnt2<br>N(T2n))                       | [Pla94] Plaisted problem n(t(2,2),2)                           | -      | 17      | 2.2        | -          | -      |
| SYN102<br>-1.007:007 | DAPnt3<br>N(T3n))                       | [Pla94] Plaisted problem n(t(3,7),7)                           | -      | 71      | 2.8        | -          | -      |
| SYN103<br>-1         | RPT63_QU_1                              | [SE94] RPT63 synthetic problem 1 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN104<br>-1         | RPT63_QU_2                              | [SE94] RPT63 synthetic problem 2 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN105<br>-1         | RPT63_QU_3                              | [SE94] RPT63 synthetic problem 3 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN106<br>-1         | RPT63_QU_4                              | [SE94] RPT63 synthetic problem 4 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN107<br>-1         | RPT63_QU_5                              | [SE94] RPT63 synthetic problem 5 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN108<br>-1         | RPT63_QU_6                              | [SE94] RPT63 synthetic problem 6 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN109<br>-1         | RPT63_QU_7                              | [SE94] RPT63 synthetic problem 7 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN110<br>-1         | RPT63_QU_8                              | [SE94] RPT63 synthetic problem 8 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN111<br>-1         | RPT63_QU_9                              | [SE94] RPT63 synthetic problem 9 (quasi-uniform distribution)  | -      | 369     | 2.9        | -          | -      |
| SYN112<br>-1         | RPT63_QU_10                             | [SE94] RPT63 synthetic problem 10 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN113<br>-1         | RPT63_QU_11                             | [SE94] RPT63 synthetic problem 11 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN114<br>-1         | RPT63_QU_12                             | [SE94] RPT63 synthetic problem 12 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN115<br>-1         | RPT63_QU_13                             | [SE94] RPT63 synthetic problem 13 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN116<br>-1         | RPT63_QU_14                             | [SE94] RPT63 synthetic problem 14 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN117<br>-1         | RPT63_QU_15                             | [SE94] RPT63 synthetic problem 15 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN118<br>-1         | RPT63_QU_16                             | [SE94] RPT63 synthetic problem 16 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN119<br>-1         | RPT63_QU_17                             | [SE94] RPT63 synthetic problem 17 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN120<br>-1         | RPT63_QU_18                             | [SE94] RPT63 synthetic problem 18 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN121<br>-1         | RPT63_QU_19                             | [SE94] RPT63 synthetic problem 19 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN122<br>-1         | RPT63_QU_20                             | [SE94] RPT63 synthetic problem 20 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN123<br>-1         | RPT63_QU_21                             | [SE94] RPT63 synthetic problem 21 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |
| SYN124<br>-1         | RPT63_QU_22                             | [SE94] RPT63 synthetic problem 22 (quasi-uniform distribution) | -      | 369     | 2.9        | -          | -      |





| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References  | V | Cl  | Av  | nH | Eq |
|----------------------|------------------------------|--|---|-----|-----|----|----|
| SYN167               | -1                           | RPT63_QU_65 [SE94] RPT63 synthetic problem 65 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN168               | -1                           | RPT63_QU_66 [SE94] RPT63 synthetic problem 66 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN169               | -1                           | RPT63_QU_67 [SE94] RPT63 synthetic problem 67 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN170               | -1                           | RPT63_QU_68 [SE94] RPT63 synthetic problem 68 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN171               | -1                           | RPT63_QU_69 [SE94] RPT63 synthetic problem 69 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN172               | -1                           | RPT63_QU_70 [SE94] RPT63 synthetic problem 70 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN173               | -1                           | RPT63_QU_71 [SE94] RPT63 synthetic problem 71 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN174               | -1                           | RPT63_QU_72 [SE94] RPT63 synthetic problem 72 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN175               | -1                           | RPT63_QU_73 [SE94] RPT63 synthetic problem 73 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN176               | -1                           | RPT63_QU_74 [SE94] RPT63 synthetic problem 74 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN177               | -1                           | RPT63_QU_75 [SE94] RPT63 synthetic problem 75 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN178               | -1                           | RPT63_QU_76 [SE94] RPT63 synthetic problem 76 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN179               | -1                           | RPT63_QU_77 [SE94] RPT63 synthetic problem 77 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN180               | -1                           | RPT63_QU_78 [SE94] RPT63 synthetic problem 78 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN181               | -1                           | RPT63_QU_79 [SE94] RPT63 synthetic problem 79 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN182               | -1                           | RPT63_QU_80 [SE94] RPT63 synthetic problem 80 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN183               | -1                           | RPT63_QU_81 [SE94] RPT63 synthetic problem 81 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN184               | -1                           | RPT63_QU_82 [SE94] RPT63 synthetic problem 82 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN185               | -1                           | RPT63_QU_83 [SE94] RPT63 synthetic problem 83 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN186               | -1                           | RPT63_QU_84 [SE94] RPT63 synthetic problem 84 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN187               | -1                           | RPT63_QU_85 [SE94] RPT63 synthetic problem 85 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN188               | -1                           | RPT63_QU_86 [SE94] RPT63 synthetic problem 86 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN189               | -1                           | RPT63_QU_87 [SE94] RPT63 synthetic problem 87 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN190               | -1                           | RPT63_QU_88 [SE94] RPT63 synthetic problem 88 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN191               | -1                           | RPT63_QU_89 [SE94] RPT63 synthetic problem 89 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN192               | -1                           | RPT63_QU_90 [SE94] RPT63 synthetic problem 90 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN193               | -1                           | RPT63_QU_91 [SE94] RPT63 synthetic problem 91 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN194               | -1                           | RPT63_QU_92 [SE94] RPT63 synthetic problem 92 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN195               | -1                           | RPT63_QU_93 [SE94] RPT63 synthetic problem 93 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN196               | -1                           | RPT63_QU_94 [SE94] RPT63 synthetic problem 94 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN197               | -1                           | RPT63_QU_95 [SE94] RPT63 synthetic problem 95 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN198               | -1                           | RPT63_QU_96 [SE94] RPT63 synthetic problem 96 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN199               | -1                           | RPT63_QU_97 [SE94] RPT63 synthetic problem 97 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN200               | -1                           | RPT63_QU_98 [SE94] RPT63 synthetic problem 98 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN201               | -1                           | RPT63_QU_99 [SE94] RPT63 synthetic problem 99 (quasi-uniform distribution)   | - | 369 | 2.9 | -  | -  |
| SYN202               | -1                           | RPT63_QU_100 [SE94] RPT63 synthetic problem 100 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN203               | -1                           | RPT63_QU_101 [SE94] RPT63 synthetic problem 101 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN204               | -1                           | RPT63_QU_102 [SE94] RPT63 synthetic problem 102 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN205               | -1                           | RPT63_QU_103 [SE94] RPT63 synthetic problem 103 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN206               | -1                           | RPT63_QU_104 [SE94] RPT63 synthetic problem 104 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN207               | -1                           | RPT63_QU_105 [SE94] RPT63 synthetic problem 105 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN208               | -1                           | RPT63_QU_106 [SE94] RPT63 synthetic problem 106 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References  | V | Cl  | Av  | nH | Eq |
|----------------------|------------------------------|--|---|-----|-----|----|----|
| SYN209               | -1                           | RPT63_QU_107 [SE94] RPT63 synthetic problem 107 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN210               | -1                           | RPT63_QU_108 [SE94] RPT63 synthetic problem 108 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN211               | -1                           | RPT63_QU_109 [SE94] RPT63 synthetic problem 109 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN212               | -1                           | RPT63_QU_110 [SE94] RPT63 synthetic problem 110 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN213               | -1                           | RPT63_QU_111 [SE94] RPT63 synthetic problem 111 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN214               | -1                           | RPT63_QU_112 [SE94] RPT63 synthetic problem 112 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN215               | -1                           | RPT63_QU_113 [SE94] RPT63 synthetic problem 113 (quasi-uniform distribution) | - | 369 | 2.9 | -  | -  |
| SYN216               | -1                           | RPT63_SK_1 [SE94] RPT63 synthetic problem 1 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN217               | -1                           | RPT63_SK_2 [SE94] RPT63 synthetic problem 2 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN218               | -1                           | RPT63_SK_3 [SE94] RPT63 synthetic problem 3 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN219               | -1                           | RPT63_SK_4 [SE94] RPT63 synthetic problem 4 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN220               | -1                           | RPT63_SK_5 [SE94] RPT63 synthetic problem 5 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN221               | -1                           | RPT63_SK_6 [SE94] RPT63 synthetic problem 6 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN222               | -1                           | RPT63_SK_7 [SE94] RPT63 synthetic problem 7 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN223               | -1                           | RPT63_SK_8 [SE94] RPT63 synthetic problem 8 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN224               | -1                           | RPT63_SK_9 [SE94] RPT63 synthetic problem 9 (skewed distribution)            | - | 369 | 2.9 | -  | -  |
| SYN225               | -1                           | RPT63_SK_10 [SE94] RPT63 synthetic problem 10 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN226               | -1                           | RPT63_SK_11 [SE94] RPT63 synthetic problem 11 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN227               | -1                           | RPT63_SK_12 [SE94] RPT63 synthetic problem 12 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN228               | -1                           | RPT63_SK_13 [SE94] RPT63 synthetic problem 13 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN229               | -1                           | RPT63_SK_14 [SE94] RPT63 synthetic problem 14 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN230               | -1                           | RPT63_SK_15 [SE94] RPT63 synthetic problem 15 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN231               | -1                           | RPT63_SK_16 [SE94] RPT63 synthetic problem 16 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN232               | -1                           | RPT63_SK_17 [SE94] RPT63 synthetic problem 17 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN233               | -1                           | RPT63_SK_18 [SE94] RPT63 synthetic problem 18 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN234               | -1                           | RPT63_SK_19 [SE94] RPT63 synthetic problem 19 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN235               | -1                           | RPT63_SK_20 [SE94] RPT63 synthetic problem 20 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN236               | -1                           | RPT63_SK_21 [SE94] RPT63 synthetic problem 21 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN237               | -1                           | RPT63_SK_22 [SE94] RPT63 synthetic problem 22 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN238               | -1                           | RPT63_SK_23 [SE94] RPT63 synthetic problem 23 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN239               | -1                           | RPT63_SK_24 [SE94] RPT63 synthetic problem 24 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN240               | -1                           | RPT63_SK_25 [SE94] RPT63 synthetic problem 25 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN241               | -1                           | RPT63_SK_26 [SE94] RPT63 synthetic problem 26 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN242               | -1                           | RPT63_SK_27 [SE94] RPT63 synthetic problem 27 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN243               | -1                           | RPT63_SK_28 [SE94] RPT63 synthetic problem 28 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN244               | -1                           | RPT63_SK_29 [SE94] RPT63 synthetic problem 29 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN245               | -1                           | RPT63_SK_30 [SE94] RPT63 synthetic problem 30 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN246               | -1                           | RPT63_SK_31 [SE94] RPT63 synthetic problem 31 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN247               | -1                           | RPT63_SK_32 [SE94] RPT63 synthetic problem 32 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN248               | -1                           | RPT63_SK_33 [SE94] RPT63 synthetic problem 33 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN249               | -1                           | RPT63_SK_34 [SE94] RPT63 synthetic problem 34 (skewed distribution)          | - | 369 | 2.9 | -  | -  |
| SYN250               | -1                           | RPT63_SK_35 [SE94] RPT63 synthetic problem 35 (skewed distribution)          | - | 369 | 2.9 | -  | -  |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References   | V | Cl  | Av  | nH | Eq |
|----------------------|------------------------------|---|---|-----|-----|----|----|
| SYN251               | -1                           | RPT63_SK_36 [SE94] RPT63 synthetic problem 36 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN252               | -1                           | RPT63_SK_37 [SE94] RPT63 synthetic problem 37 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN253               | -1                           | RPT63_SK_38 [SE94] RPT63 synthetic problem 38 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN254               | -1                           | RPT63_SK_39 [SE94] RPT63 synthetic problem 39 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN255               | -1                           | RPT63_SK_40 [SE94] RPT63 synthetic problem 40 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN256               | -1                           | RPT63_SK_41 [SE94] RPT63 synthetic problem 41 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN257               | -1                           | RPT63_SK_42 [SE94] RPT63 synthetic problem 42 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN258               | -1                           | RPT63_SK_43 [SE94] RPT63 synthetic problem 43 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN259               | -1                           | RPT63_SK_44 [SE94] RPT63 synthetic problem 44 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN260               | -1                           | RPT63_SK_45 [SE94] RPT63 synthetic problem 45 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN261               | -1                           | RPT63_SK_46 [SE94] RPT63 synthetic problem 46 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN262               | -1                           | RPT63_SK_47 [SE94] RPT63 synthetic problem 47 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN263               | -1                           | RPT63_SK_48 [SE94] RPT63 synthetic problem 48 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN264               | -1                           | RPT63_SK_49 [SE94] RPT63 synthetic problem 49 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN265               | -1                           | RPT63_SK_50 [SE94] RPT63 synthetic problem 50 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN266               | -1                           | RPT63_SK_51 [SE94] RPT63 synthetic problem 51 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN267               | -1                           | RPT63_SK_52 [SE94] RPT63 synthetic problem 52 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN268               | -1                           | RPT63_SK_53 [SE94] RPT63 synthetic problem 53 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN269               | -1                           | RPT63_SK_54 [SE94] RPT63 synthetic problem 54 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN270               | -1                           | RPT63_SK_55 [SE94] RPT63 synthetic problem 55 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN271               | -1                           | RPT63_SK_56 [SE94] RPT63 synthetic problem 56 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN272               | -1                           | RPT63_SK_57 [SE94] RPT63 synthetic problem 57 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN273               | -1                           | RPT63_SK_58 [SE94] RPT63 synthetic problem 58 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN274               | -1                           | RPT63_SK_59 [SE94] RPT63 synthetic problem 59 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN275               | -1                           | RPT63_SK_60 [SE94] RPT63 synthetic problem 60 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN276               | -1                           | RPT63_SK_61 [SE94] RPT63 synthetic problem 61 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN277               | -1                           | RPT63_SK_62 [SE94] RPT63 synthetic problem 62 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN278               | -1                           | RPT63_SK_63 [SE94] RPT63 synthetic problem 63 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN279               | -1                           | RPT63_SK_64 [SE94] RPT63 synthetic problem 64 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN280               | -1                           | RPT63_SK_65 [SE94] RPT63 synthetic problem 65 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN281               | -1                           | RPT63_SK_66 [SE94] RPT63 synthetic problem 66 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN282               | -1                           | RPT63_SK_67 [SE94] RPT63 synthetic problem 67 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN283               | -1                           | RPT63_SK_68 [SE94] RPT63 synthetic problem 68 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN284               | -1                           | RPT63_SK_69 [SE94] RPT63 synthetic problem 69 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN285               | -1                           | RPT63_SK_70 [SE94] RPT63 synthetic problem 70 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN286               | -1                           | RPT63_SK_71 [SE94] RPT63 synthetic problem 71 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN287               | -1                           | RPT63_SK_72 [SE94] RPT63 synthetic problem 72 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN288               | -1                           | RPT63_SK_73 [SE94] RPT63 synthetic problem 73 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN289               | -1                           | RPT63_SK_74 [SE94] RPT63 synthetic problem 74 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN290               | -1                           | RPT63_SK_75 [SE94] RPT63 synthetic problem 75 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN291               | -1                           | RPT63_SK_76 [SE94] RPT63 synthetic problem 76 (skewed distribution) | - | 369 | 2.9 | -  | -  |
| SYN292               | -1                           | RPT63_SK_77 [SE94] RPT63 synthetic problem 77 (skewed distribution) | - | 369 | 2.9 | -  | -  |

| Syntactic name<br>V# | Semantic name<br>Other names      | Description<br>References                                  | V | Cl  | Av  | nH  | Eq   |
|----------------------|-----------------------------------|--|---|-----|-----|-----|------|
| SYN293<br>-1         | RPT63_SK_78                       | RPT63 synthetic problem 78 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN294<br>-1         | RPT63_SK_79                       | RPT63 synthetic problem 79 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN295<br>-1         | RPT63_SK_80                       | RPT63 synthetic problem 80 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN296<br>-1         | RPT63_SK_81                       | RPT63 synthetic problem 81 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN297<br>-1         | RPT63_SK_82                       | RPT63 synthetic problem 82 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN298<br>-1         | RPT63_SK_83                       | RPT63 synthetic problem 83 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN299<br>-1         | RPT63_SK_84                       | RPT63 synthetic problem 84 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN300<br>-1         | RPT63_SK_85                       | RPT63 synthetic problem 85 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN301<br>-1         | RPT63_SK_86                       | RPT63 synthetic problem 86 (skewed distribution)<br>[SE94] | - | 369 | 2.9 | -   | -    |
| SYN302<br>-1.003     | DAPa<br>An                        | Plaisted problem a(3)<br>[Pla94]                           | - | 72  | 3.0 | -   | -    |
| SYN303<br>-1         | Decide1<br>Example 1              | Problem for testing satisfiability<br>[BCP94]              | - | 5   | 1.6 | -   | -    |
| SYN304<br>-1         | Decide2<br>Example 2, EXAMPLE 7.8 | Problem for testing satisfiability<br>[BCP94, FLTZ93]      | - | 8   | 1.3 | 12% | -    |
| SYN305<br>-1         | Decide3<br>Example 3              | Problem for testing satisfiability<br>[BCP94]              | - | 9   | 1.7 | -   | 100% |
| SYN306<br>-1         | Decide4<br>EXAMPLE 3.2.2          | Problem for testing satisfiability<br>[FLTZ93]             | - | 6   | 1.7 | 16% | -    |
| SYN307<br>-1         | Decide5<br>EXAMPLE 3.2.3          | Problem for testing satisfiability<br>[FLTZ93]             | - | 4   | 2.0 | 25% | -    |
| SYN308<br>-1         | Decide6<br>EXAMPLE 4.11           | Problem for testing satisfiability<br>[FLTZ93]             | - | 4   | 2.3 | 75% | -    |
| SYN309<br>-1         | Decide7<br>EXAMPLE 7.1            | Problem for testing satisfiability<br>[FLTZ93]             | - | 6   | 1.8 | 50% | -    |
| SYN310<br>-1         | Decide8<br>H1                     | Problem for testing satisfiability<br>[FLTZ93]             | - | 6   | 1.7 | -   | -    |
| SYN311<br>-1         | Decide9<br>H2                     | Problem for testing satisfiability<br>[FLTZ93]             | - | 6   | 1.7 | -   | -    |
| SYN312<br>-1         | Decide10<br>H3                    | Problem for testing satisfiability<br>[FLTZ93]             | - | 8   | 1.8 | 12% | -    |
| SYN313<br>-1.001:002 | Decide11                          | Problem for testing satisfiability<br>[Fer94]              | - | 2   | 2.5 | 50% | -    |
| SYN314<br>-1.002:001 | Decide12                          | Problem for testing satisfiability<br>[Fer94]              | - | 2   | 2.5 | 50% | -    |
| SYN315<br>-1         | Church46_2_1<br>Ch2N1             | Church problem 46.2 (1)<br>[Chu56, FLTZ93, Tam94]          | - | 4   | 2.0 | 25% | -    |
| SYN316<br>-1         | Church46_2_2<br>Ch2N2             | Church problem 46.2 (2)<br>[Chu56, FLTZ93, Tam94]          | - | 2   | 2.0 | 50% | -    |
| SYN317<br>-1         | Church46_2_3<br>Ch2N3             | Church problem 46.2 (3)<br>[Chu56, FLTZ93, Tam94]          | - | 3   | 2.0 | 33% | -    |
| SYN318<br>-1         | Church46_2_4<br>Ch2N4             | Church problem 46.2 (4)<br>[Chu56, FLTZ93, Tam94]          | - | 4   | 1.5 | -   | -    |
| SYN319<br>-1         | Church46_2_5<br>Ch2N5             | Church problem 46.2 (5)<br>[Chu56, FLTZ93, Tam94]          | - | 7   | 1.9 | 14% | -    |
| SYN320<br>-1         | Church46_3_1<br>Ch3N1             | Church problem 46.3 (1)<br>[Chu56, FLTZ93, Tam94]          | - | 3   | 1.3 | 33% | -    |
| SYN321<br>-1         | Church46_3_2<br>Ch3N2             | Church problem 46.3 (2)<br>[Chu56, FLTZ93, Tam94]          | - | 4   | 2.0 | 25% | -    |
| SYN322<br>-1         | Church46_4_1<br>Ch4N1             | Church problem 46.4 (1)<br>[Chu56, FLTZ93, Tam94]          | - | 2   | 2.0 | -   | -    |
| SYN323<br>-1         | Church46_4_2<br>Ch4N2             | Church problem 46.4 (2)<br>[Chu56, FLTZ93, Tam94]          | - | 4   | 2.0 | 25% | -    |
| SYN324<br>-1         | Church46_9_1<br>Ch9N1             | Church problem 46.9 (1)<br>[Chu56, FLTZ93, Tam94]          | - | 4   | 2.0 | 25% | -    |
| SYN325<br>-1         | Church46_9_2<br>Ch9N2             | Church problem 46.9 (2)<br>[Chu56, FLTZ93, Tam94]          | - | 5   | 1.8 | 40% | -    |
| SYN326<br>-1         | Church46_12_1<br>Ch12N1           | Church problem 46.12 (1)<br>[Chu56, FLTZ93, Tam94]         | - | 7   | 1.7 | 42% | -    |
| SYN327<br>-1         | Church46_12_2<br>Ch12N2           | Church problem 46.12 (2)<br>[Chu56, FLTZ93, Tam94]         | - | 6   | 2.3 | 33% | -    |
| SYN328<br>-1         | Church46_12_3<br>Ch12N3           | Church problem 46.12 (3)<br>[Chu56, FLTZ93, Tam94]         | - | 11  | 2.5 | 36% | -    |
| SYN329<br>-1         | Church46_14_1<br>Ch14N1           | Church problem 46.14 (1)<br>[Chu56, FLTZ93, Tam94]         | - | 4   | 1.0 | -   | -    |
| SYN330<br>-1         | Church46_14_2<br>Ch14N2           | Church problem 46.14 (2)<br>[Chu56, FLTZ93, Tam94]         | - | 8   | 2.0 | 12% | -    |
| SYN331<br>-1         | Church46_14_3<br>Ch14N3           | Church problem 46.14 (3)<br>[Chu56, FLTZ93, Tam94]         | - | 7   | 1.4 | 14% | -    |
| SYN332<br>-1         | Church46_14_4<br>Ch14N4           | Church problem 46.14 (4)<br>[Chu56, FLTZ93, Tam94]         | - | 14  | 2.4 | 42% | -    |
| SYN333<br>-1         | Church46_14_5<br>Ch14N5           | Church problem 46.14 (5)<br>[Chu56, FLTZ93, Tam94]         | - | 3   | 2.7 | -   | -    |
| SYN334<br>-1         | Church46_14_6<br>Ch14N6           | Church problem 46.14 (6)<br>[Chu56, FLTZ93, Tam94]         | - | 7   | 2.4 | 28% | -    |

| Syntactic name<br>V# | Semantic name<br>Other names | Description<br>References                          | V | Cl | Av  | nH  | Eq |
|----------------------|------------------------------|--|---|----|-----|-----|----|
| SYN335<br>-1         | Church46_14_7<br>Ch14N7      | Church problem 46.14 (7)<br>[Chu56, FLTZ93, Tam94] | - | 12 | 2.2 | 33% | -  |
| SYN336<br>-1         | Church46_15_1<br>Ch15N1      | Church problem 46.15 (1)<br>[Chu56, FLTZ93, Tam94] | - | 5  | 1.0 | -   | -  |
| SYN337<br>-1         | Church46_15_2<br>Ch15N2      | Church problem 46.15 (2)<br>[Chu56, FLTZ93, Tam94] | - | 5  | 1.0 | -   | -  |
| SYN338<br>-1         | Church46_15_3<br>Ch15N3      | Church problem 46.15 (3)<br>[Chu56, FLTZ93, Tam94] | - | 3  | 1.0 | -   | -  |
| SYN339<br>-1         | Church46_15_4<br>Ch15N4      | Church problem 46.15 (4)<br>[Chu56, FLTZ93, Tam94] | - | 2  | 1.0 | -   | -  |
| SYN340<br>-1         | Church46_15_5<br>Ch15N5      | Church problem 46.15 (5)<br>[Chu56, FLTZ93, Tam94] | - | 2  | 1.0 | -   | -  |
| SYN341<br>-1         | Church46_15_6<br>Ch15N6      | Church problem 46.15 (6)<br>[Chu56, FLTZ93, Tam94] | - | 2  | 1.0 | -   | -  |
| SYN342<br>-1         | Church46_15_7<br>Ch15N7      | Church problem 46.15 (7)<br>[Chu56, FLTZ93, Tam94] | - | 2  | 1.0 | -   | -  |
| SYN343<br>-1         | Church46_16_2<br>Ch16N2      | Church problem 46.16 (2)<br>[Chu56, FLTZ93, Tam94] | - | 3  | 2.0 | 33% | -  |
| SYN344<br>-1         | Church46_16_3<br>Ch16N3      | Church problem 46.16 (3)<br>[Chu56, FLTZ93, Tam94] | - | 5  | 2.0 | 40% | -  |
| SYN345<br>-1         | Church46_16_4<br>Ch16N4      | Church problem 46.16 (4)<br>[Chu56, FLTZ93, Tam94] | - | 8  | 3.0 | 50% | -  |
| SYN346<br>-1         | Church46_17_2<br>Ch17N2      | Church problem 46.17 (2)<br>[Chu56, FLTZ93, Tam94] | - | 4  | 1.5 | -   | -  |
| SYN347<br>-1         | Church46_17_3<br>Ch17N3      | Church problem 46.17 (3)<br>[Chu56, FLTZ93, Tam94] | - | 6  | 2.7 | 50% | -  |
| SYN348<br>-1         | Church46_17_4<br>Ch17N4      | Church problem 46.17 (4)<br>[Chu56, FLTZ93, Tam94] | - | 16 | 6.0 | 93% | -  |
| SYN349<br>-1         | Church46_17_5<br>Ch17N5      | Church problem 46.17 (5)<br>[Chu56, FLTZ93, Tam94] | - | 10 | 3.6 | 70% | -  |
| SYN350<br>-1         | Church46_18_2<br>Ch18N2      | Church problem 46.18 (2)<br>[Chu56, FLTZ93, Tam94] | - | 6  | 2.7 | 33% | -  |
| SYN351<br>-1         | Church46_18_3<br>Ch18N3      | Church problem 46.18 (3)<br>[Chu56, FLTZ93, Tam94] | - | 7  | 2.0 | 42% | -  |
| SYN352<br>-1         | Church46_18_4<br>Ch18N4      | Church problem 46.18 (4)<br>[Chu56, FLTZ93, Tam94] | - | 7  | 2.6 | 57% | -  |
| SYN353<br>-1         | Church46_18_5<br>Ch18N5      | Church problem 46.18 (5)<br>[Chu56, FLTZ93, Tam94] | - | 17 | 2.8 | 47% | -  |
| SYN354<br>-1         | Church46_20_1<br>Ch20N1      | Church problem 46.20 (1)<br>[Chu56, FLTZ93, Tam94] | - | 7  | 2.4 | 14% | -  |

Domain TOP (19 abstract problems, 24 problems)

|                    |  |   |        |           |            |            |        |
|--------------------|--|---|--------|-----------|------------|------------|--------|
| TOP001<br>-1<br>-2 | BasisTpltgLem1<br>Lemma 1a<br>Lemma 1a | Topology generated by a basis forms a topological space, part 1<br>[WM89]<br>[WM89] | -<br>- | 111<br>13 | 3.0<br>2.1 | 20%<br>7%  | -<br>- |
| TOP002<br>-1<br>-2 | BasisTpltgLem2<br>Lemma 1b<br>Lemma 1b | Topology generated by a basis forms a topological space, part 2<br>[WM89]<br>[WM89] | -<br>- | 111<br>3  | 3.0<br>1.3 | 20%<br>33% | -<br>- |
| TOP003<br>-1<br>-2 | BasisTpltgLem3<br>Lemma 1c<br>Lemma 1c | Topology generated by a basis forms a topological space, part 3<br>[WM89]<br>[WM89] | -<br>- | 111<br>11 | 3.0<br>2.0 | 20%<br>9%  | -<br>- |
| TOP004<br>-1<br>-2 | BasisTpltgLem4<br>Lemma 1d<br>Lemma 1d | Topology generated by a basis forms a topological space, part 4<br>[WM89]<br>[WM89] | -<br>- | 113<br>21 | 3.0<br>2.8 | 20%<br>4%  | -<br>- |
| TOP005<br>-1<br>-2 | BasisTpltgLem5<br>Lemma 1e<br>Lemma 1e | Topology generated by a basis forms a topological space, part 5<br>[WM89]<br>[WM89] | -<br>- | 112<br>12 | 3.0<br>2.5 | 20%<br>16% | -<br>- |
| TOP006<br>-1       | BasisTpltg<br>Problem 1                | Topology generated by a basis forms a topological space<br>[WM89]                   | -      | 111       | 3.0        | 20%        | -      |
| TOP007<br>-1       | TpltgEqn1<br>Problem 2                 | Property 1 of topological spaces<br>[WM89]  | -      | 114       | 3.0        | 20%        | -      |
| TOP008<br>-1       | SubSpTpltg<br>Problem 3                | The subspace topology gives rise to a topological space<br>[WM89]                   | -      | 112       | 3.0        | 20%        | -      |
| TOP009<br>-1       | OpenTrans<br>Problem 4                 | If Y is open in X, and A is open in Y, then A is open in X<br>[WM89]                | -      | 112       | 3.0        | 20%        | -      |
| TOP010<br>-1       | FinerSubSp<br>Problem 5                | A finer topology induces a finer subspace topology<br>[WM89]                        | -      | 112       | 3.0        | 20%        | -      |
| TOP011<br>-1       | TopBasisAltDef<br>Problem 6            | An alternative definition of top_of_basis<br>[WM89]                                 | -      | 112       | 3.1        | 22%        | -      |
| TOP012<br>-1       | UnionIntscClsd<br>Problem 7            | Intersections and finite unions of closed sets are closed<br>[WM89]                 | -      | 119       | 3.2        | 22%        | -      |
| TOP013<br>-1       | IntrSubSClsr<br>Problem 8              | Properties of interior and closure<br>[WM89]  | -      | 112       | 3.0        | 20%        | -      |
| TOP014<br>-1       | OpenIntrClsdClsr<br>Problem 9          | Properties of open & interior and closed & closure<br>[WM89]                        | -      | 115       | 3.1        | 22%        | -      |
| TOP015<br>-1       | IntrBndy<br>Problem 10                 | The interior and the boundary of a set are disjoint<br>[WM89]                       | -      | 112       | 3.0        | 20%        | -      |
| TOP016<br>-1       | UnionIntrBndy<br>Problem 11            | The union of the interior and the boundary is the closure<br>[WM89]                 | -      | 112       | 3.0        | 20%        | -      |
| TOP017<br>-1       | BndyEmpty<br>Problem 12                | If the boundary of A is empty, A is both open and closed<br>[WM89]                  | -      | 114       | 3.0        | 21%        | -      |
| TOP018<br>-1       | LmtPtConnSet<br>Problem 13             | Propoerty of limits points and connected sets<br>[WM89]                             | -      | 112       | 3.0        | 20%        | -      |

| Syntactic name | Semantic name          | Description   | V | Cl  | Av  | nH  | Eq |
|----------------|------------------------|---|---|-----|-----|-----|----|
| V#             | Other names            | References  |   |     |     |     |    |
| TOP019<br>-1   | ClsrConn<br>Problem 14 | The closure of a connected set is connected<br>[WM89] | - | 111 | 3.0 | 20% | -  |

# 9 Appendix

## 9.1 Abbreviation List

|       |                            |        |                         |
|-------|----------------------------|--------|-------------------------|
| Acc   | : Account                  | Hi     | : High                  |
| Aff   | : Affect                   | IN     | : Index N               |
| AId   | : Additive Identity        | Id     | : Identity              |
| ASym  | : Anti-symmetric           | Idem   | : Idempotent            |
| Abn   | : Abelian                  | Img    | : Image                 |
| Abs   | : Absolute                 | Inc    | : Increase              |
| Absb  | : Absorption               | Indp   | : Independent           |
| Add   | : Addition/Additive        | Indisc | : Indiscernibles        |
| Alt   | : Alternative              | Indn   | : Induction step        |
| Apply | : Apply                    | Indv   | : Inductive             |
| Appn  | : Application              | Iia    | : Inertia               |
| Assc  | : Associative              | Inf    | : Infinite              |
| Assr  | : Associator               | Inr    | : Inner                 |
| Ax    | : Axiom                    | Insr   | : Insertion             |
| B3Alg | : Ternary Boolean Algebra  | Intchg | : Interchange           |
| Base  | : Base step                | Intmed | : Intermediate          |
| Bnd   | : Bound                    | Intr   | : Interior              |
| Bndy  | : Boundary                 | Intsc  | : Intersection          |
| Bool  | : Boolean                  | Inv    | : Inverse               |
| Btwn  | : Betweenness              | Invar  | : Invariant             |
| Canc  | : Cancellation             | Irr    | : Irrational            |
| Circ  | : Circular                 | Irrefl | : Irreflexive           |
| Cl    | : Class                    | Is El  | : Element               |
| Clsd  | : Closed                   | Isos   | : Isosceles             |
| Clsr  | : Closure                  | Ivln   | : Involution            |
| Cmbtr | : Combinator               | L      | : Left                  |
| Cmpbl | : Compatible               | Lrg    | : Large                 |
| Cmplt | : Complete                 | Latt   | : Lattice               |
| Cmx   | : Complex                  | LOG    | : Lattice Ordered Group |
| Cmps  | : Compose                  | Law    | : Law                   |
| Cmpsn | : Composition              | Leq    | : Less than or equal to |
| Cmpt  | : Component                | Lin    | : Linearised            |
| Cmtr  | : Commutator               | Lmt    | : Limit                 |
| Comm  | : Commute                  | Ln     | : Line                  |
| Cod   | : Codomain                 | Log    | : Logic                 |
| Coll  | : Collinearity             | Low    | : Lower                 |
| Comm  | : Commutative              | Lt     | : Less than             |
| Cond  | : Condition                | Lub    | : Least Upper Bound     |
| Cong  | : Congruent                | M      | : Middle                |
| Conj  | : Conjugate                | MId    | : Multiplicative Id     |
| Conn  | : Connected                | Max    | : Maximum               |
| Conn  | : Connectivity             | Memb   | : Member (of)           |
| Cons  | : Construction             | Min    | : Minimum               |
| Cont  | : Continuous               | Minus  | : Subtraction operator  |
| Cor   | : Corollary                | Mono   | : Monotonic             |
| Cpmt  | : Complement               | Mult M | : Multiplication/M'tive |
| Crit  | : Critical                 | Neg    | : Negative              |
| Cube  | : Cubed                    | Nrml   | : Normal                |
| Dbl   | : Double                   | Null   | : Null (segment)        |
| Dth   | : Death                    | ON     | : Order N               |
| Dec   | : Decrease                 | Obj    | : Object                |
| Def   | : Defined                  | Op     | : Operation             |
| Def   | : Definition               | Opp    | : Opposite              |
| Dep   | : Depends on               | Ord    | : Ordered               |
| Diagn | : Diagonalization          | Ordl   | : Ordinal               |
| Diff  | : Difference               | Org    | : Organisation          |
| Dsbg  | : Disbanding rate          | Orth   | : Orthogonal(ity)       |
| Dist  | : Distributive             | Out    | : Outer                 |
| Div   | : Division operator        | Pln    | : Plane                 |
| Dom   | : Domain                   | Plus   | : Addition operator     |
| EP    | : Efficient producers      | Pop    | : Population            |
| El    | : Element                  | Pos    | : Positive              |
| Elim  | : Elimination              | Ppr    | : Proper                |
| Embdg | : Embedding                | Ppty   | : Property              |
| Empty | : Empty                    | Pr(s)  | : Pair(s)               |
| Env   | : Environment              | Pred   | : Predecessor           |
| Eq    | : Equality                 | Prm    | : Prime                 |
| Eq    | : Equals                   | Prod   | : Product               |
| Eqid  | : Equidistance             | Prop   | : Propositional         |
| Eqn   | : Equation                 | Pt(s)  | : Point(s)              |
| Est   | : Estimate                 | PwrCl  | : Power Class           |
| Ex    | : Exists                   | Quant  | : Quantification        |
| Ext   | : Lengthen                 | Quot   | : Quotient              |
| Extn  | : Extension                | R      | : Right                 |
| Fact  | : Factor                   | Rdcn   | : Reduction             |
| FM    | : First movers             | Recr   | : Recursion             |
| Flex  | : Flexible                 | Refl   | : Reflexive             |
| Func  | : Function                 | Refc   | : Reflection            |
| Fxd   | : Fixed                    | Rel    | : Relation              |
| Gen   | : General                  | Reli   | : Reliable              |
| Geq   | : Greater than or equal to | Repr   | : Reproduce             |
| Gt    | : Greater than             | Rsce   | : Resource              |
| Grp   | : Group                    | Rng    | : Range                 |
| Gth   | : Growth                   | Rob    | : Robbins               |



Rplmt : Replacement  
Rstd : Restricted  
Rstn : Restriction  
Rev : Reverse  
SV : Single Valued  
Sat : Satisfiable  
Sect : Section  
Seg : Segment  
Sel : Selection  
SemiG : Semigroups  
Set : Set  
SetB : Set Builder  
Sgtn : Singleton  
Sim : Similar  
Sz : Size  
Sm : Small (set)  
Soln : Solution  
Sqr : Square(d)  
Stb : Stable  
StSp : State Space  
Strong : Strong  
Struc : Structure  
SubCl : Sub(class)  
SubG : Subgroups  
SubS : Sub(Set)  
SubSp : Sub(space)  
Subs : Substitution  
Succ : Successor  
SupS : Super(Set)  
Symm : Symmetric  
Symn : Symmetrization  
Thm : Theorem  
Tm : Time  
Times : Multiplication operator  
Tplg : Topology  
Trans : Transitive  
Tri : Triangle  
Trnsf : Transfinite  
Un : UnXXX  
Union : Union  
Univ : Universal  
Unq : Unique  
Up : Upper  
Val : Value  
Wk : Weak  
XProd : Cross product  
Xm : Xmorphism

## 9.2 Reverse Name Index

|                 |           |              |                |          |              |
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| AM8             | [WB87]    | : AHA001-1.p | Axiom 3.5.2    | [McC93]  | : GRP077-1.p |
| An              | [Pla94]   | : SYN302-1.g | Axiom 3.5.3    | [McC93]  | : GRP078-1.p |
| AN-50           | [MW92]    | : LCL001-1.p | Axiom 3.5.4    | [McC93]  | : GRP079-1.p |
| AN-51           | [MW92]    | : LCL002-1.p | Axiom 3.5.5    | [McC93]  | : GRP080-1.p |
| AN-52           | [MW92]    | : LCL003-1.p | Axiom 3.6.1    | [McC93]  | : GRP082-1.p |
| AN-53           | [MW92]    | : LCL004-1.p | Axiom 3.6.2    | [McC93]  | : GRP083-1.p |
| AN-54           | [MW92]    | : LCL005-1.p | Axiom 3.7.1    | [McC93]  | : GRP085-1.p |
| ANCES2          | [RRY+ 72] | : SYN032-1.p | Axiom 3.7.2    | [McC93]  | : GRP086-1.p |
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| AP3             | [Qua92a]  | : SET534-6.p | Axiom 3.9.1    | [McC93]  | : GRP093-1.p |
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| AP5             | [Qua92a]  | : SET538-6.p | ax_antisymb    | [Sch95]  | : GRP137-1.p |
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| Axiom 3.10.2    | [McC93]   | : GRP097-1.p | B7             | [MOW76]  | : B00011-1.p |
| Axiom 3.10.3    | [McC93]   | : GRP098-1.p | B7             | [Qua89b] | : EEO045-3.p |
| Axiom 3.11.1    | [McC93]   | : GRP099-1.p | B8             | [MOW76]  | : B00012-1.p |
| Axiom 3.11.2    | [McC93]   | : GRP100-1.p | B8             | [MOW76]  | : B00012-3.p |
| Axiom 3.11.3    | [McC93]   | : GRP101-1.p | B8             | [Qua89b] | : EEO046-3.p |
| Axiom 3.11.4    | [McC93]   | : GRP102-1.p | B9             | [MOW76]  | : B00013-1.p |
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| Axiom 3.12.1    | [McC93]   | : GRP104-1.p | B9             | [Qua89b] | : EEO047-3.p |
| Axiom 3.12.2    | [McC93]   | : GRP105-1.p | B10            | [MOW76]  | : B00014-3.p |
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| axiom 3.12.4    | [McC93]   | : GRP107-1.p | B11            | [Qua89b] | : EEO049-3.p |
| Axiom 3.12.5    | [McC93]   | : GRP108-1.p | B12            | [Qua89b] | : EEO050-3.p |
| Axiom 3.12.6    | [McC93]   | : GRP109-1.p | B13            | [Qua89b] | : EEO051-3.p |
| Axiom 3.12.7    | [McC93]   | : GRP110-1.p | B14            | [Qua89b] | : EEO052-3.p |
| Axiom 3.12.8    | [McC93]   | : GRP111-1.p | B15            | [Qua89b] | : EEO053-3.p |
| Axiom 3.2.1     | [McC93]   | : GRP064-1.p | barber.ver1.in | [ANL]    | : PUZ003-1.p |
| Axiom 3.2.2     | [McC93]   | : GRP065-1.p | Bennett QG1    | [TPTP]   | : GRP123-1.g |
| Axiom 3.2.3     | [McC93]   | : GRP060-1.p | Bennett QG2    | [TPTP]   | : GRP124-1.g |
| Axiom 3.3.1     | [McC93]   | : GRP066-1.p | Bennett QG3    | [TPTP]   | : GRP125-1.g |
| Axiom 3.3.2     | [McC93]   | : GRP067-1.p | Bennett QG4    | [TPTP]   | : GRP126-1.g |
| Axiom 3.3.3     | [McC93]   | : GRP068-1.p | Bennett QG5    | [TPTP]   | : GRP127-1.g |
| Axiom 3.3.4     | [McC93]   | : GRP069-1.p | Bennett QG6    | [TPTP]   | : GRP128-1.g |
| Axiom 3.4.1     | [McC93]   | : GRP070-1.p | Bennett QG7    | [TPTP]   | : GRP129-1.g |
| Axiom 3.4.2     | [McC93]   | : GRP071-1.p | Bennett QG8    | [TPTP]   | : GRP130-1.g |
| Axiom 3.4.3     | [McC93]   | : GRP072-1.p | bird1.ver1.in  | [ANL]    | : COL050-1.p |
| Axiom 3.4.4     | [McC93]   | : GRP073-1.p | bird2.ver1.in  | [ANL]    | : COL051-1.p |

|                            |           |              |                           |           |              |
|----------------------------|-----------|--------------|---------------------------|-----------|--------------|
| bird4.ver1.in              | [ANL]     | : COL052-1.p | CADE-11 Competition Eq-1  | [Ove90]   | : GRP002-3.p |
| bird4.ver2.in              | [ANL]     | : COL052-2.p | CADE-11 Competition Eq-10 | [Ove90]   | : RIG011-5.p |
| bird5.ver1.in              | [ANL]     | : COL053-1.p | CADE-11 Competition Eq-2  | [Ove90]   | : ROB005-1.p |
| bird6.ver1.in              | [ANL]     | : COL054-1.p | CADE-11 Competition Eq-3  | [Ove90]   | : B00002-1.p |
| bird7.ver1.in              | [ANL]     | : COL055-1.p | CADE-11 Competition Eq-4  | [Ove90]   | : GRP014-1.p |
| bird8.ver1.in              | [ANL]     | : COL056-1.p | CADE-11 Competition Eq-5  | [Ove90]   | : LCL009-2.p |
| Bisecting Diagonal Theorem | [Wos88]   | : GE0073-1.p | CADE-11 Competition Eq-6  | [Ove90]   | : COL049-1.p |
| BL1                        | [MOW76]   | : ANA003-2.p | CADE-11 Competition Eq-7  | [Ove90]   | : RIG009-5.p |
| BL2                        | [MOW76]   | : ANA004-2.p | CADE-11 Competition Eq-8  | [Ove90]   | : COL003-1.p |
| BL3                        | [MOW76]   | : ANA005-1.p | CADE-11 Competition Eq-9  | [Ove90]   | : RIG010-5.p |
| Bledsoe-P1                 | [LM92]    | : ANA003-4.p | CD-12                     | [LM92]    | : LCL051-1.p |
| bool.in                    | [OTT]     | : B00008-3.p | CD-13                     | [LM92]    | : LCL052-1.p |
| Boolean Rings              | [Wos88]   | : RIG008-1.p | CD-90                     | [LM92]    | : LCL097-1.p |
| Boolean Rings              | [Wos88]   | : RIG008-7.p | CF1                       | [Qua92a]  | : SET558-6.p |
| bool_ass.in                | [OTT]     | : B00008-3.p | CF2                       | [Qua92a]  | : SET559-6.p |
| Boxes-of-fruit             | [Wos88]   | : PUZ012-1.p | CF3                       | [Qua92a]  | : SET560-6.p |
| Boxes-of-fruit             | [WOLB92]  | : PUZ012-1.p | CF4                       | [Qua92a]  | : SET561-6.p |
| boxes.ver1.in              | [ANL]     | : PUZ012-1.p | CF5                       | [Qua92a]  | : SET562-6.p |
| boys.ver1.in               | [ANL]     | : PUZ013-1.p | CF6                       | [Qua92a]  | : SET563-6.p |
| BURSTALL                   | [RRY+ 72] | : COM002-1.p | CF6 cor.1                 | [Qua92a]  | : SET564-6.p |
| BURSTALL                   | [WM76]    | : COM002-1.p | CF6 cor.2                 | [Qua92a]  | : SET565-6.p |
| C0-37                      | [MW92]    | : LCL025-1.p | CF7                       | [Qua92a]  | : SET566-6.p |
| C0-38                      | [MW92]    | : LCL026-1.p | CF8                       | [Qua92d]  | : SET567-6.p |
| C0-39                      | [MW92]    | : LCL027-1.p | ch                        | [Ste87]   | : RIG033-6.p |
| C0-40                      | [MW92]    | : LCL028-1.p | Ch2N1                     | [Tam94]   | : SYN315-1.p |
| C0-41                      | [MW92]    | : LCL029-1.p | Ch2N2                     | [Tam94]   | : SYN316-1.p |
| C0-42                      | [MW92]    | : LCL030-1.p | Ch2N3                     | [Tam94]   | : SYN317-1.p |
| C0-43                      | [MW92]    | : LCL031-1.p | Ch2N4                     | [Tam94]   | : SYN318-1.p |
| C0-44                      | [MW92]    | : LCL032-1.p | Ch2N5                     | [Tam94]   | : SYN319-1.p |
| C0-45                      | [MW92]    | : LCL033-1.p | Ch3N1                     | [Tam94]   | : SYN320-1.p |
| C0-46                      | [MW92]    | : LCL034-1.p | Ch3N2                     | [Tam94]   | : SYN321-1.p |
| C0-47                      | [MW92]    | : LCL035-1.p | Ch4N1                     | [Tam94]   | : SYN322-1.p |
| C0-48                      | [MW92]    | : LCL036-1.p | Ch4N2                     | [Tam94]   | : SYN323-1.p |
| C0-49                      | [MW92]    | : LCL037-1.p | Ch9N1                     | [Tam94]   | : SYN324-1.p |
| C1                         | [Kun92]   | : GRP049-1.p | Ch9N2                     | [Tam94]   | : SYN325-1.p |
| C1                         | [MOW76]   | : CAT001-1.p | Ch12N1                    | [Tam94]   | : SYN326-1.p |
| C1                         | [Qua92a]  | : SET150-6.p | Ch12N2                    | [Tam94]   | : SYN327-1.p |
| C1                         | [WM88a]   | : COL001-1.p | Ch12N3                    | [Tam94]   | : SYN328-1.p |
| C1.1                       | [WM88a]   | : COL002-1.p | Ch14N1                    | [Tam94]   | : SYN329-1.p |
| C2                         | [MOW76]   | : CAT002-1.p | Ch14N2                    | [Tam94]   | : SYN330-1.p |
| C2                         | [WM88a]   | : COL003-1.p | Ch14N3                    | [Tam94]   | : SYN331-1.p |
| C2.1                       | [Qua89b]  | : GE0064-3.p | Ch14N4                    | [Tam94]   | : SYN332-1.p |
| C2.1                       | [Qua92a]  | : SET151-6.p | Ch14N5                    | [Tam94]   | : SYN333-1.p |
| C2.2                       | [Qua89b]  | : GE0065-3.p | Ch14N6                    | [Tam94]   | : SYN334-1.p |
| C2.2                       | [Qua92a]  | : SET152-6.p | Ch14N7                    | [Tam94]   | : SYN335-1.p |
| C2.3                       | [Qua89b]  | : GE0066-3.p | Ch15N1                    | [Tam94]   | : SYN336-1.p |
| C3                         | [Kun92]   | : GRP051-1.p | Ch15N2                    | [Tam94]   | : SYN337-1.p |
| C3                         | [MOW76]   | : CAT003-1.p | Ch15N3                    | [Tam94]   | : SYN338-1.p |
| C3                         | [Qua89b]  | : GE0067-3.p | Ch15N4                    | [Tam94]   | : SYN339-1.p |
| C3.1                       | [Qua92a]  | : SET153-6.p | Ch15N5                    | [Tam94]   | : SYN340-1.p |
| C3.2                       | [Qua92a]  | : SET154-6.p | Ch15N6                    | [Tam94]   | : SYN341-1.p |
| C4                         | [Kun92]   | : GRP052-1.p | Ch15N7                    | [Tam94]   | : SYN342-1.p |
| C4                         | [MOW76]   | : CAT004-1.p | Ch16N2                    | [Tam94]   | : SYN343-1.p |
| C4                         | [Qua89b]  | : GE0068-3.p | Ch16N3                    | [Tam94]   | : SYN344-1.p |
| C4                         | [WM88a]   | : COL004-1.p | Ch16N4                    | [Tam94]   | : SYN345-1.p |
| C4.1                       | [Qua92a]  | : SET155-6.p | Ch17N2                    | [Tam94]   | : SYN346-1.p |
| C4.2                       | [Qua92a]  | : SET156-6.p | Ch17N3                    | [Tam94]   | : SYN347-1.p |
| C5                         | [Kun92]   | : GRP053-1.p | Ch17N4                    | [Tam94]   | : SYN348-1.p |
| C5                         | [MOW76]   | : CAT005-1.p | Ch17N5                    | [Tam94]   | : SYN349-1.p |
| C5                         | [Qua89b]  | : GE0069-3.p | Ch18N2                    | [Tam94]   | : SYN350-1.p |
| C5                         | [Qua92a]  | : SET157-6.p | Ch18N3                    | [Tam94]   | : SYN351-1.p |
| C5                         | [WM88a]   | : COL005-1.p | Ch18N4                    | [Tam94]   | : SYN352-1.p |
| C6                         | [Kun92]   | : GRP054-1.p | Ch18N5                    | [Tam94]   | : SYN353-1.p |
| C6                         | [MOW76]   | : CAT006-1.p | Ch20N1                    | [Tam94]   | : SYN354-1.p |
| C6                         | [Qua92d]  | : SET158-6.p | Chang-Lee-1               | [Cha70]   | : GRP028-1.p |
| C6                         | [WM88a]   | : COL006-1.p | Chang-Lee-2               | [Cha70]   | : GRP001-5.p |
| C7                         | [Kun92]   | : GRP055-1.p | Chang-Lee-3               | [Cha70]   | : GRP003-1.p |
| C7                         | [MOW76]   | : CAT007-1.p | Chang-Lee-4               | [Cha70]   | : GRP004-1.p |
| C8                         | [Kun92]   | : GRP056-1.p | Chang-Lee-5               | [Cha70]   | : GRP005-1.p |
| C8                         | [MOW76]   | : CAT008-1.p | Chang-Lee-6               | [Cha70]   | : GRP006-1.p |
| c15                        | [Ste87]   | : RIG012-6.p | Chang-Lee-7               | [Cha70]   | : NUM014-1.p |
| c16                        | [Ste87]   | : RIG013-6.p | Chang-Lee-8               | [Cha70]   | : NUM015-1.p |
| c17                        | [Ste87]   | : RIG014-6.p | Chang-Lee-9               | [Cha70]   | : NUM016-2.p |
| c18                        | [Ste87]   | : RIG015-6.p | Chang-Lee-10a             | [Cha70]   | : NUM001-1.p |
| c19                        | [Ste87]   | : RIG016-6.p | Chang-Lee-10b             | [Cha70]   | : NUM002-1.p |
| c20                        | [Ste87]   | : RIG017-6.p | Chang-Lee-10c             | [Cha70]   | : NUM003-1.p |
| c21                        | [Ste87]   | : RIG018-6.p | Chang-Lee-10d             | [Cha70]   | : NUM004-1.p |
| c24                        | [Ste87]   | : RIG019-6.p | chekndom.ver1.in          | [ANL]     | : PUZ015-1.p |
| c25                        | [Ste87]   | : RIG020-6.p | chekndom.ver2.in          | [ANL]     | : PUZ016-1.p |
| c26                        | [Ste87]   | : RIG021-6.p | CL1                       | [LW92]    | : COL049-1.p |
| CA1                        | [Qua92a]  | : SET553-6.p | CL2                       | [LW92]    | : COL003-1.p |
| CA2                        | [Qua92a]  | : SET554-6.p | CL3                       | [LW92]    | : COL044-1.p |
| CA2                        | [Qua92d]  | : SET556-6.p | CL4                       | [LW92]    | : COL043-1.p |
| CA3                        | [Qua92a]  | : SET555-6.p | CL5                       | [LW92]    | : COL057-1.p |
| CA4                        | [Qua92a]  | : SET557-6.p | CL-1                      | [WWM+ 90] | : COL060-1.p |
| CADE-11 Competition 1      | [Ove90]   | : GRP001-1.p | CL-2                      | [WWM+ 90] | : COL061-1.p |
| CADE-11 Competition 2      | [Ove90]   | : GRP002-1.p | CL-3                      | [WWM+ 90] | : COL062-1.p |
| CADE-11 Competition 3      | [Ove90]   | : RIG008-6.p | CL-4                      | [WWM+ 90] | : COL063-1.p |
| CADE-11 Competition 4      | [Ove90]   | : LCL024-1.p | CL-5                      | [WWM+ 90] | : COL064-1.p |
| CADE-11 Competition 5      | [Ove90]   | : LCL038-1.p | CL-6                      | [WWM+ 90] | : COL065-1.p |
| CADE-11 Competition 6      | [Ove90]   | : LCL111-1.p | CL-7                      | [WWM+ 90] | : COL066-1.p |
| CADE-11 Competition 7      | [Ove90]   | : LCL114-1.p |                           |           |              |

|                              |          |              |                 |          |              |
|------------------------------|----------|--------------|-----------------|----------|--------------|
| cn19.in                      | [OTT]    | : LCL058-1.p | Conjecture 1    | [Jec93a] | : LDA013-1.p |
| CN-1                         | [MW92]   | : LCL040-1.p | Conjecture 1    | [Jec93a] | : LDA014-1.p |
| CN-2                         | [MW92]   | : LCL041-1.p | Conjecture 1    | [Ste87]  | : RIG030-6.p |
| CN-3                         | [MW92]   | : LCL042-1.p | Conjecture 1    | [Ste87]  | : RIG030-7.p |
| CN-4                         | [MW92]   | : LCL043-1.p | Conjecture 2    | [Ste87]  | : RIG031-6.p |
| CN-5                         | [MW92]   | : LCL044-1.p | Conjecture 2    | [Ste87]  | : RIG031-7.p |
| CN-6                         | [MW92]   | : LCL045-1.p | Conjecture 3    | [Ste87]  | : RIG032-6.p |
| CN-7                         | [MW92]   | : LCL046-1.p | Conjecture 3    | [Ste87]  | : RIG032-7.p |
| CN-8                         | [MW92]   | : LCL047-1.p | Corollary 3.10  | [Win90]  | : ROB020-1.p |
| CN-9                         | [MW92]   | : LCL048-1.p | Corollary 3.10  | [Win90]  | : ROB020-2.p |
| CN-10                        | [MW92]   | : LCL049-1.p | Corollary 3.7   | [Win90]  | : ROB016-1.p |
| CN-11                        | [MW92]   | : LCL050-1.p | Corollary 3.9   | [Win90]  | : ROB018-1.p |
| CN-12                        | [MW92]   | : LCL051-1.p | Corollary 3.9   | [Win90]  | : ROB019-1.p |
| CN-13                        | [MW92]   | : LCL052-1.p | CP1             | [Qua92a] | : SET202-6.p |
| CN-14                        | [MW92]   | : LCL053-1.p | CP1 cor.        | [Qua92a] | : SET203-6.p |
| CN-15                        | [MW92]   | : LCL054-1.p | CP2             | [Qua92a] | : SET204-6.p |
| CN-16                        | [MW92]   | : LCL055-1.p | CP3.1           | [Qua92a] | : SET205-6.p |
| CN-17                        | [MW92]   | : LCL056-1.p | CP3.2           | [Qua92a] | : SET206-6.p |
| CN-18                        | [MW92]   | : LCL057-1.p | CP4             | [Qua92a] | : SET207-6.p |
| CN-19                        | [MW92]   | : LCL058-1.p | CP5.1           | [Qua92a] | : SET208-6.p |
| CN-20                        | [MW92]   | : LCL059-1.p | CP5.2           | [Qua92a] | : SET209-6.p |
| CN-21                        | [MW92]   | : LCL060-1.p | CP5 cor.1       | [Qua92a] | : SET210-6.p |
| CN-22                        | [MW92]   | : LCL061-1.p | CP5 cor.2       | [Qua92a] | : SET211-6.p |
| CN-23                        | [MW92]   | : LCL062-1.p | CP5 cor.3       | [Qua92a] | : SET212-6.p |
| CN-24                        | [MW92]   | : LCL063-1.p | CP5 cor.4       | [Qua92a] | : SET213-6.p |
| CN-25                        | [MW92]   | : LCL064-1.p | CP5 cor.5       | [Qua92a] | : SET214-6.p |
| CN-26                        | [MW92]   | : LCL065-1.p | CP5 cor.6       | [Qua92a] | : SET215-6.p |
| CN-27                        | [MW92]   | : LCL066-1.p | CP5 cor.7       | [Qua92a] | : SET216-6.p |
| CN-28                        | [MW92]   | : LCL067-1.p | CP5 cor.8       | [Qua92a] | : SET217-6.p |
| CN-29                        | [MW92]   | : LCL068-1.p | CP6.1           | [Qua92a] | : SET218-6.p |
| CN-30                        | [MW92]   | : LCL069-1.p | CP6.2           | [Qua92a] | : SET219-6.p |
| CN-31                        | [MW92]   | : LCL070-1.p | CP7.1           | [Qua92a] | : SET220-6.p |
| CN-32                        | [MW92]   | : LCL071-1.p | CP7.2           | [Qua92a] | : SET221-6.p |
| CN-33                        | [MW92]   | : LCL072-1.p | CP8             | [Qua92a] | : SET222-6.p |
| CN-34                        | [MW92]   | : LCL073-1.p | CP8             | [Qua92d] | : SET223-6.p |
| CN-35                        | [MW92]   | : LCL074-1.p | CP9             | [Qua92a] | : SET224-6.p |
| CN-36                        | [MW92]   | : LCL075-1.p | CP10            | [Qua92a] | : SET225-6.p |
| cn.in part 1                 | [OTT]    | : LCL046-1.p | CP11.1          | [Qua92a] | : SET226-6.p |
| cn.in part 2                 | [OTT]    | : LCL047-1.p | CP11.2          | [Qua92a] | : SET227-6.p |
| cn.in part 3                 | [OTT]    | : LCL048-1.p | CP12.1          | [Qua92a] | : SET228-6.p |
| CO1.1                        | [Qua92a] | : SET387-6.p | CP12.2          | [Qua92a] | : SET229-6.p |
| CO1.2                        | [Qua92a] | : SET388-6.p | CP13            | [Qua92a] | : SET230-6.p |
| CO1.3                        | [Qua92a] | : SET389-6.p | CP14.1          | [Qua92d] | : SET231-6.p |
| CO1.4                        | [Qua92a] | : SET390-6.p | CP14.2          | [Qua92d] | : SET232-6.p |
| CO2                          | [Qua92a] | : SET391-6.p | CP14.3          | [Qua92d] | : SET233-6.p |
| CO3.1                        | [Qua92a] | : SET392-6.p | CP14.4          | [Qua92d] | : SET234-6.p |
| CO3.2                        | [Qua92a] | : SET393-6.p | CP15.1          | [Qua92d] | : SET235-6.p |
| CO4                          | [Qua92a] | : SET394-6.p | CP15.2          | [Qua92d] | : SET236-6.p |
| CO5                          | [Qua92a] | : SET395-6.p | CR1             | [Qua92d] | : NUM046-1.p |
| CO6.1                        | [Qua92a] | : SET396-6.p | CR2             | [Qua92d] | : NUM047-1.p |
| CO6.2                        | [Qua92a] | : SET397-6.p | CR3             | [Qua92d] | : NUM048-1.p |
| CO6.3                        | [Qua92a] | : SET032-6.p | CR4             | [Qua92d] | : NUM049-1.p |
| CO7                          | [Qua92a] | : SET398-6.p | CR5             | [Qua92d] | : NUM050-1.p |
| CO8.1                        | [Qua92a] | : SET399-6.p | CR6             | [Qua92d] | : NUM051-1.p |
| CO8.2                        | [Qua92a] | : SET400-6.p | cyclic.ver3.in  | [ANL]    | : GRP027-2.p |
| CO8.3                        | [Qua92a] | : SET401-6.p | D1              | [Qua89b] | : GEO014-2.p |
| CO8.4                        | [Qua92a] | : SET402-6.p | D1.1            | [Qua92a] | : SET169-6.p |
| CO9                          | [Qua92a] | : SET033-6.p | D1.2            | [Qua92a] | : SET170-6.p |
| CO10                         | [Qua92a] | : SET403-6.p | D2              | [Qua89b] | : GEO015-3.p |
| CO11.1                       | [Qua92a] | : SET404-6.p | D2.1            | [Qua92a] | : SET171-6.p |
| CO11.2                       | [Qua92a] | : SET405-6.p | D2.2            | [Qua92a] | : SET172-6.p |
| CO11 cor.1                   | [Qua92a] | : SET406-6.p | D3              | [Qua89b] | : GEO016-3.p |
| CO11 cor.2                   | [Qua92a] | : SET407-6.p | D3              | [Qua92a] | : SET173-6.p |
| CO12                         | [Qua92a] | : SET408-6.p | D3 cor.         | [Qua92a] | : SET174-6.p |
| CO13.1                       | [Qua92a] | : SET409-6.p | D4              | [Qua92a] | : SET175-6.p |
| CO13.2                       | [Qua92a] | : SET410-6.p | D4.1            | [Qua89b] | : GEO017-3.p |
| CO15                         | [Qua92a] | : SET411-6.p | D4.2            | [Qua89b] | : GEO018-3.p |
| CO16                         | [Qua92a] | : SET412-6.p | D4.3            | [Qua89b] | : GEO019-3.p |
| CO17                         | [Qua92a] | : SET413-6.p | D4.4            | [Qua89b] | : GEO020-3.p |
| CO18                         | [Qua92d] | : SET414-6.p | D4.5            | [Qua89b] | : GEO021-3.p |
| CO19.1                       | [Qua92d] | : SET415-6.p | D4 cor.         | [Qua92a] | : SET176-6.p |
| CO19.2                       | [Qua92d] | : SET416-6.p | D5              | [Qua89b] | : GEO022-3.p |
| CO21                         | [Qua92d] | : SET417-6.p | D5              | [Qua92a] | : SET177-6.p |
| CO22                         | [Qua92d] | : SET418-6.p | D5 cor.         | [Qua92a] | : SET178-6.p |
| CO23                         | [Qua92d] | : SET419-6.p | D5 cor.         | [Qua92a] | : SET179-6.p |
| CO24                         | [Qua92d] | : SET420-6.p | D6              | [Qua92a] | : SET180-6.p |
| CO26                         | [Qua92d] | : SET421-6.p | D6 cor.         | [Qua92a] | : SET181-6.p |
| CO27                         | [Qua92d] | : SET422-6.p | D7              | [Qua89b] | : GEO024-3.p |
| CO28                         | [Qua92d] | : SET423-6.p | D7              | [Qua92a] | : SET182-6.p |
| CO29                         | [Qua92d] | : SET424-6.p | D8              | [Qua89b] | : GEO025-3.p |
| comm.in                      | [OTT]    | : GRP002-3.p | D9              | [Qua89b] | : GEO026-3.p |
| Commutator Theorem           | [Wos88]  | : GRP002-1.p | D10.1           | [Qua89b] | : GEO027-3.p |
| Commutator Theorem           | [Wos88]  | : GRP002-4.p | D10.2           | [Qua89b] | : GEO028-3.p |
| commutator.ver1.in           | [ANL]    | : GRP002-1.p | D10.3           | [Qua89b] | : GEO029-3.p |
| commutator.ver2.in           | [ANL]    | : GRP002-2.p | D11             | [Qua89b] | : GEO030-3.p |
| commute.ver1.in              | [ANL]    | : RIG008-5.p | D12             | [Qua89b] | : GEO031-3.p |
| commute.ver2.in              | [ANL]    | : RIG008-3.p | D13             | [Qua89b] | : GEO032-3.p |
| commute.ver3.in              | [ANL]    | : RIG008-1.p | D14             | [Qua89b] | : GEO033-3.p |
| commute.ver4.in              | [ANL]    | : RIG008-1.p | D15             | [Qua89b] | : GEO034-3.p |
| compl.ver1.in                | [ANL]    | : SET012-2.p | DBABHP          | [MRS72]  | : MSC002-1.p |
| compl.ver2.in                | [ANL]    | : SET012-4.p | DBABHP          | [WM76]   | : MSC002-1.p |
| Composition of Homomorphisms | [Wos88]  | : ALG001-2.p | DeMorgan's Laws | [Ver92]  | : B00015-1.p |

|                        |                       |              |                    |          |              |
|------------------------|-----------------------|--------------|--------------------|----------|--------------|
| design_or.ver1.clauses | [ANL]                 | : CID001-1.p | Established lemma  | [MOW76]  | : GRP022-2.p |
| DI1.1                  | [Qua92a]              | : SET491-6.p | Established lemma  | [MOW76]  | : GRP023-2.p |
| DI1.2                  | [Qua92a]              | : SET492-6.p | Established lemma  | [MOW76]  | : RIG002-1.p |
| DI1 cor.               | [Qua92d]              | : SET493-6.p | Established lemma  | [MOW76]  | : RIG003-1.p |
| DI2                    | [Qua92a]              | : SET494-6.p | EW1                | [MRS72]  | : SYN028-1.p |
| DI3                    | [Qua92a]              | : SET495-6.p | EW1                | [WM76]   | : SYN028-1.p |
| DI4                    | [Qua92a]              | : SET496-6.p | EW2                | [MRS72]  | : SYN029-1.p |
| DI5                    | [Qua92a]              | : SET497-6.p | EW2                | [WM76]   | : SYN029-1.p |
| DI6                    | [Qua92a]              | : SET498-6.p | EW3                | [MRS72]  | : SYN030-1.p |
| DI7                    | [Qua92a]              | : SET499-6.p | EW3                | [WM76]   | : SYN030-1.p |
| DI8                    | [Qua92a]              | : SET500-6.p | EX1                | [SPR]    | : GRP028-1.p |
| DI9.1                  | [Qua92a]              | : SET501-6.p | EX2                | [SPR]    | : GRP001-5.p |
| DI9.2                  | [Qua92a]              | : SET502-6.p | EX3                | [SPR]    | : GRP003-1.p |
| distrnu                | [Sch95]               | : GRP164-1.p | EX4                | [SPR]    | : GRP004-1.p |
| distrun                | [Sch95]               | : GRP164-2.p | EX4-T?             | [WM76]   | : SYN038-1.p |
| DM                     | [MRS72]               | : SYN033-1.p | ex4.lop            | [SET]    | : SYN038-1.p |
| DM                     | [WM76]                | : SYN033-1.p | EX5                | [SPR]    | : GRP005-1.p |
| DO1.1                  | [Qua92a]              | : SET258-6.p | EX5-T?             | [WM76]   | : ALG002-1.p |
| DO1.2                  | [Qua92a]              | : SET259-6.p | ex5.lop            | [SET]    | : ALG002-1.p |
| DO1.3                  | [Qua92a]              | : SET260-6.p | EX6                | [SPR]    | : GRP006-1.p |
| DO2.1                  | [Qua92a]              | : SET261-6.p | EX6-T?             | [WM76]   | : RIG001-3.p |
| DO2.2                  | [Qua92a]              | : SET262-6.p | ex6.lop            | [SET]    | : RIG001-3.p |
| DO3                    | [Qua92a]              | : SET263-6.p | Example            | [Lov68]  | : SYN012-1.p |
| DO3 cor.1              | [Qua92a]              | : SET264-6.p | Example 1          | [BCP94]  | : SYN303-1.p |
| DO3 cor.2              | [Qua92a]              | : SET265-6.p | Example 1          | [Lov69]  | : GRP001-5.p |
| DO3 cor.3              | [Qua92a]              | : SET266-6.p | Example 1          | [Luc68]  | : GRP028-3.p |
| DO3 cor.4              | [Qua92d]              | : SET267-6.p | Example 2          | [BCP94]  | : SYN304-1.p |
| DO4                    | [Qua92a]              | : SET268-6.p | Example 2          | [FLSY74] | : NUM014-1.p |
| DO5                    | [Qua92a]              | : SET269-6.p | Example 2          | [Lov69]  | : NUM015-1.p |
| DO6                    | [Qua92a]              | : SET270-6.p | Example 2          | [Luc68]  | : GRP003-1.p |
| DO6 cor.               | [Qua92a]              | : SET271-6.p | Example 3          | [BCP94]  | : SYN305-1.p |
| DO7                    | [Qua92a]              | : SET272-6.p | Example 3          | [FLSY74] | : NUM015-1.p |
| DO7 cor.               | [Qua92a]              | : SET273-6.p | Example 3          | [Luc68]  | : GRP004-1.p |
| DO8                    | [Qua92a]              | : SET274-6.p | EXAMPLE 3.2.2      | [FLTZ93] | : SYN306-1.p |
| DO8 cor.1              | [Qua92a]              | : SET275-6.p | EXAMPLE 3.2.3      | [FLTZ93] | : SYN307-1.p |
| DO8 cor.2              | [Qua92a]              | : SET276-6.p | Example 4          | [BCP94]  | : B00019-1.p |
| DO8 cor.3              | [Qua92a]              | : SET277-6.p | Example 4          | [FLSY74] | : SYN038-1.p |
| DO8 cor.4              | [Qua92a]              | : SET278-6.p | Example 4          | [Luc68]  | : GRP001-5.p |
| DO9                    | [Qua92d]              | : SET279-6.p | EXAMPLE 4.11       | [FLTZ93] | : SYN308-1.p |
| DO10                   | [Qua92d]              | : SET280-6.p | Example 5          | [FLSY74] | : ALG002-1.p |
| DO12                   | [Qua92d]              | : SET281-6.p | Example 5          | [Luc68]  | : GRP005-1.p |
| DO13                   | [Qua92d]              | : SET282-6.p | Example 5.1        | [LMG94]  | : SYN010-1.g |
| DO14                   | [Qua92d]              | : SET283-6.p | Example 6          | [Luc68]  | : NUM014-1.p |
| DO15                   | [Qua92d]              | : SET284-6.p | Example 6a         | [FLSY74] | : RIG001-3.p |
| DO16                   | [Qua92d]              | : SET285-6.p | Example 7          | [Luc68]  | : NUM015-1.p |
| DO16 cor.              | [Qua92d]              | : SET286-6.p | EXAMPLE 7.1        | [FLTZ93] | : SYN309-1.p |
| DO17                   | [Qua92d]              | : SET287-6.p | Example 8a         | [Luc68]  | : NUM016-2.p |
| DO18                   | [Qua92d]              | : SET288-6.p | Example 8b         | [Luc68]  | : NUM016-1.p |
| E1                     | [MOW76]               | : PRV002-1.p | EXQ1               | [MOW76]  | : SYN013-1.p |
| E1                     | [Qua89b]              | : GE0035-3.p | ExQ1               | [Wan65]  | : SYN013-1.p |
| E2                     | [MOW76]               | : PRV003-1.p | exq1.ver1.in       | [ANL]    | : SYN013-1.p |
| E2                     | [Qua89b]              | : GE0036-3.p | exq1.ver2.in       | [ANL]    | : SYN013-1.p |
| E3                     | [MOW76]               | : PRV004-1.p | EXQ2               | [MOW76]  | : SYN014-1.p |
| E3                     | [Qua89b]              | : GE0037-3.p | ExQ2               | [Wan65]  | : SYN014-1.p |
| E4                     | [MOW76]               | : PRV005-1.p | exq2.ver1.in       | [ANL]    | : SYN014-1.p |
| E5                     | [MOW76]               | : PRV006-1.p | exq2.ver2.in       | [ANL]    | : SYN014-1.p |
| E6                     | [MOW76]               | : PRV007-1.p | EXQ3               | [MOW76]  | : SYN015-1.p |
| E7                     | [MOW76]               | : PRV008-1.p | ExQ3               | [Wan65]  | : SYN015-1.p |
| EC-1                   | [WWM <sup>+</sup> 90] | : LCL166-1.p | exq3.ver1.in       | [ANL]    | : SYN015-1.p |
| EC-2                   | [WWM <sup>+</sup> 90] | : LCL167-1.p | exq3.ver2.in       | [ANL]    | : SYN015-1.p |
| EC-69                  | [MW92]                | : LCL006-1.p | fac2.lop (Size 2)  | [SET]    | : NUM283-1.g |
| EC-70                  | [MW92]                | : LCL007-1.p | fac3.lop (Size 3)  | [SET]    | : NUM283-1.g |
| EC-71                  | [MW92]                | : LCL008-1.p | fac4.lop (Size 4)  | [SET]    | : NUM283-1.g |
| EC-72                  | [MW92]                | : LCL009-1.p | fac5.lop (Size 5)  | [SET]    | : NUM283-1.g |
| EC-73                  | [MW92]                | : LCL010-1.p | fac6.lop (Size 7)  | [SET]    | : NUM283-1.g |
| EC-74                  | [MW92]                | : LCL011-1.p | fac7.lop (Size 7)  | [SET]    | : NUM283-1.g |
| EC-75                  | [MW92]                | : LCL012-1.p | FEX4T1             | [SPR]    | : SYN038-1.p |
| EC-76                  | [MW92]                | : LCL013-1.p | FEX4T2             | [SPR]    | : SYN038-1.p |
| EC-77                  | [MW92]                | : LCL014-1.p | FEX5               | [SPR]    | : ALG002-1.p |
| EC-78                  | [MW92]                | : LCL015-1.p | FEX6T1             | [SPR]    | : RIG001-3.p |
| EC-79                  | [MW92]                | : LCL016-1.p | FEX6T2             | [SPR]    | : RIG001-3.p |
| EC-80                  | [MW92]                | : LCL017-1.p | fib3.lop (Size 3)  | [SET]    | : NUM284-1.g |
| EC-81                  | [MW92]                | : LCL018-1.p | fib4.lop (Size 4)  | [SET]    | : NUM284-1.g |
| EC-82                  | [MW92]                | : LCL019-1.p | fib5.lop (Size 5)  | [SET]    | : NUM284-1.g |
| EC-83                  | [MW92]                | : LCL020-1.p | fib6.lop (Size 6)  | [SET]    | : NUM284-1.g |
| EC-84                  | [MW92]                | : LCL021-1.p | fib9.lop (Size 9)  | [SET]    | : NUM284-1.g |
| ec.in part 1           | [OTT]                 | : LCL022-1.p | Figure 3           | [WL89]   | : SYN008-1.p |
| ec.in part 2           | [OTT]                 | : LCL023-1.p | Figure 8           | [WL89]   | : SYN009-1.p |
| ec_yq.in               | [OTT]                 | : LCL010-1.p | Five Point Theorem | [Wos88]  | : GE0008-1.p |
| ederX-Y.lop (Size X:Y) | [TUM]                 | : SYN002-1.g | FU1                | [Qua92a] | : SET440-6.p |
| EQ1                    | [Qua92a]              | : SET055-7.p | FU1                | [Qua92d] | : SET432-6.p |
| EQ2.1                  | [Qua92a]              | : SET056-7.p | FU2                | [Qua92a] | : SET441-6.p |
| EQ2.2                  | [Qua92a]              | : SET057-7.p | FU3.1              | [Qua92d] | : SET433-6.p |
| EQ2.3                  | [Qua92a]              | : SET058-7.p | FU3.2              | [Qua92d] | : SET434-6.p |
| EQ2.4                  | [Qua92a]              | : SET059-7.p | FU3.3              | [Qua92d] | : SET435-6.p |
| EST-S1                 | [WB87]                | : SET012-1.p | FU4                | [Qua92a] | : SET442-6.p |
| EST-S2                 | [WB87]                | : SET013-1.p | FU4.1              | [Qua92d] | : SET436-6.p |
| EST-S3                 | [WB87]                | : SET015-1.p | FU4.2              | [Qua92d] | : SET437-6.p |
| EST-S4                 | [WB87]                | : SET014-2.p | FU5                | [Qua92d] | : SET438-6.p |
| Established lemma      | [MOW76]               | : B00007-1.p | FU6                | [Qua92a] | : SET034-6.p |
| Established lemma      | [MOW76]               | : B00016-1.p | FU7                | [Qua92d] | : SET439-6.p |
| Established lemma      | [MOW76]               | : B00017-1.p | FU8                | [Qua92d] | : SET440-6.p |

|                       |                 |              |                      |          |              |
|-----------------------|-----------------|--------------|----------------------|----------|--------------|
| FU9                   | [Qua92d]        | : SET441-6.p | hp6.ver1.in          | [ANL]    | : HEM006-7.p |
| FU10                  | [Qua92d]        | : SET442-6.p | hp6.ver2.in          | [ANL]    | : HEM006-6.p |
| FU11                  | [Qua92d]        | : SET443-6.p | hp6.ver3.in          | [ANL]    | : HEM006-5.p |
| FU12                  | [Qua92d]        | : SET444-6.p | HP7                  | [ANL]    | : HEM007-3.p |
| FU12 cor.             | [Qua92d]        | : SET445-6.p | hp7.ver1.in          | [ANL]    | : HEM007-6.p |
| FU13                  | [Qua92d]        | : SET446-6.p | hp7.ver2.in          | [ANL]    | : HEM007-4.p |
| FU14                  | [Qua92d]        | : SET447-6.p | hp7.ver3.in          | [ANL]    | : HEM007-5.p |
| FU15                  | [Qua92d]        | : SET448-6.p | HP8                  | [ANL]    | : HEM008-3.p |
| FU16.1                | [Qua92d]        | : SET449-6.p | hp8.ver1.in          | [ANL]    | : HEM008-1.p |
| FU16.2                | [Qua92d]        | : SET450-6.p | hp8.ver2.in          | [ANL]    | : HEM008-6.p |
| G1                    | [MOW76]         | : GRP001-1.p | hp8.ver3.in          | [ANL]    | : HEM008-5.p |
| G2                    | [MOW76]         | : GRP017-1.p | HP9                  | [ANL]    | : HEM009-3.p |
| G3                    | [MOW76]         | : GRP030-1.p | hp9.ver1.in          | [ANL]    | : HEM009-2.p |
| G4                    | [MOW76]         | : GRP031-1.p | hp9.ver2.in          | [ANL]    | : HEM009-6.p |
| G5                    | [MOW76]         | : GRP029-1.p | hp9.ver3.in          | [ANL]    | : HEM009-5.p |
| G5                    | [MOW76]         | : GRP029-2.p | HP10                 | [ANL]    | : HEM010-3.p |
| G6                    | [MOW76]         | : GRP002-1.p | hp10.ver1.in         | [ANL]    | : HEM010-7.p |
| G7                    | [MOW76]         | : GRP039-4.p | hp10.ver2.in         | [ANL]    | : HEM010-6.p |
| G8                    | [ANL]           | : GRP025-2.p | hp10.ver3.in         | [ANL]    | : HEM010-5.p |
| G8                    | [MOW76]         | : GRP025-1.p | HP11                 | [ANL]    | : HEM011-3.p |
| G9                    | [ANL]           | : GRP026-2.p | hp11.ver1.in         | [ANL]    | : HEM011-2.p |
| G9                    | [MOW76]         | : GRP026-1.p | hp11.ver2.in         | [ANL]    | : HEM011-4.p |
| G11A                  | [Ben92]         | : GE0077-4.p | hp11.ver3.in         | [ANL]    | : HEM011-5.p |
| G15                   | [Ben92]         | : GE0076-4.p | I1                   | [Pfe88]  | : LCL081-1.p |
| G16                   | [Ben92]         | : GE0078-5.p | I1                   | [Qua92a] | : SET143-6.p |
| GCD                   | [WB87]          | : NUM005-1.p | I2                   | [Qua89b] | : GE0061-3.p |
| gcd                   | [Wan85]         | : NUM005-1.p | I2                   | [Qua92a] | : SET144-6.p |
| GEOMETRY THEOREM      | [Sla67]         | : GE0079-1.p | I3                   | [Qua89b] | : GE0062-3.p |
| GP1                   | [MOW76]         | : GRP001-2.p | I3                   | [Qua92a] | : SET145-6.p |
| GP2                   | [MOW76]         | : GRP039-7.p | I4                   | [Qua89b] | : GE0063-3.p |
| GROUP1                | [RRY+72]        | : GRP028-1.p | I4                   | [Qua92a] | : SET146-6.p |
| GROUP1                | [WM76]          | : GRP028-1.p | I5                   | [Qua92a] | : SET147-6.p |
| GROUP2                | [RRY+72]        | : GRP001-5.p | I6                   | [Qua92a] | : SET148-6.p |
| GROUP2                | [WM76]          | : GRP001-5.p | I6 cor.              | [Qua92a] | : SET149-6.p |
| Groups of Order 4     | [Wos88]         | : GRP113-1.p | IC-1.1               | [WWM+90] | : LCL082-1.p |
| groups.exp3.in part 1 | [OTT]           | : GRP115-1.p | IC-1.2               | [WWM+90] | : LCL083-1.p |
| groups.exp3.in part 2 | [OTT]           | : GRP116-1.p | IC-1.3               | [WWM+90] | : LCL084-1.p |
| groups.exp3.in part 3 | [OTT]           | : GRP117-1.p | IC-63                | [MW92]   | : LCL080-1.p |
| groups.exp3.in part 4 | [OTT]           | : GRP118-1.p | IC-64                | [MW92]   | : LCL081-1.p |
| groups.exp4.in part 1 | [OTT]           | : GRP119-1.p | IC-65                | [MW92]   | : LCL082-1.p |
| groups.exp4.in part 2 | [OTT]           | : GRP120-1.p | IC-66                | [MW92]   | : LCL083-1.p |
| groups.exp4.in part 3 | [OTT]           | : GRP121-1.p | IC-67                | [MW92]   | : LCL084-1.p |
| groups.exp4.in part 4 | [OTT]           | : GRP122-1.p | IC-68                | [MW92]   | : LCL085-1.p |
| GT1                   | [LW92]          | : GRP001-2.p | ID1                  | [Qua92a] | : SET454-6.p |
| GT2                   | [LW92]          | : GRP112-1.p | ID2                  | [Qua92a] | : SET455-6.p |
| GT3                   | [LW92]          | : GRP002-4.p | ID3                  | [Qua92a] | : SET456-6.p |
| GT4                   | [LW92]          | : GRP058-1.p | ID4                  | [Qua92a] | : SET457-6.p |
| GT5                   | [LW92]          | : GRP085-1.p | ID4 cor.             | [Qua92a] | : SET458-6.p |
| GT6                   | [LW92]          | : GRP084-1.p | ID5.1                | [Qua92a] | : SET459-6.p |
| H1                    | [FLTZ93]        | : SYN310-1.p | ID5.2                | [Qua92a] | : SET460-6.p |
| H1                    | [MOW76]         | : HEN001-1.p | ID5.3                | [Qua92a] | : SET461-6.p |
| H1                    | [Pfe88]         | : LCL084-1.p | ID5.4                | [Qua92a] | : SET462-6.p |
| H2                    | [FLTZ93]        | : SYN311-1.p | ID5 cor.             | [Qua92a] | : SET463-6.p |
| H2                    | [MOW76]         | : HEN002-2.p | ID6                  | [Qua92a] | : SET464-6.p |
| H3                    | [FLTZ93]        | : SYN312-1.p | ID7                  | [Qua92a] | : SET465-6.p |
| H3                    | [MOW76]         | : HEN003-2.p | ID8                  | [Qua92a] | : SET466-6.p |
| H4                    | [MOW76]         | : HEN004-2.p | ID9.1                | [Qua92a] | : SET467-6.p |
| H5                    | [MOW76]         | : HEN005-2.p | ID9.2                | [Qua92a] | : SET468-6.p |
| H6                    | [MOW76]         | : HEN006-2.p | ID9.3                | [Qua92a] | : SET469-6.p |
| H7                    | [MOW76]         | : HEN007-2.p | ID9 cor.             | [Qua92d] | : SET470-6.p |
| H8                    | [MOW76]         | : HEN008-2.p | ID10.1               | [Qua92a] | : SET471-6.p |
| H9                    | [MOW76]         | : HEN009-2.p | ID10.2               | [Qua92a] | : SET472-6.p |
| H10                   | [MOW76]         | : HEN010-2.p | ID11.1               | [Qua92d] | : SET473-6.p |
| H11                   | [MOW76]         | : HEN011-2.p | ID11.2               | [Qua92d] | : SET474-6.p |
| HASPARTS-T1           | [RRY+72]        | : MSC003-1.p | ID11.3               | [Qua92d] | : SET475-6.p |
| HASPARTS-T1           | [WM76]          | : MSC003-1.p | ID11.4               | [Qua92a] | : SET476-6.p |
| HASPARTS-T2           | [RRY+72]        | : MSC004-1.p | ID12                 | [Qua92d] | : SET476-6.p |
| HASPARTS-T2           | [WM76]          | : MSC004-1.p | ident1.ver1.in       | [ANL]    | : GRP030-1.p |
| HO1                   | [Quaife, 1992a] | : ALG001-3.p | ident2.ver1.in       | [ANL]    | : GRP029-1.p |
| HO1                   | [Quaife, 1992b] | : ALG001-3.p | Identity established | [MOW76]  | : GRP018-1.p |
| Hoares FIND           | [Ble77]         | : PRV009-1.p | Identity established | [MOW76]  | : GRP019-1.p |
| houses.ver1.in        | [ANL]           | : PUZ017-1.p | Identity established | [MOW76]  | : GRP020-1.p |
| How to Win a Bride    | [Oh185]         | : PUZ021-1.p | Identity established | [MOW76]  | : GRP021-1.p |
| hp1.ver1.in           | [ANL]           | : HEN001-1.p | Identity established | [MOW76]  | : GRP022-1.p |
| hp1.ver2.in           | [ANL]           | : HEN001-3.p | Identity established | [MOW76]  | : GRP023-1.p |
| hp1.ver3.in           | [ANL]           | : HEN001-5.p | IH1                  | [Pfe88]  | : LCL084-2.p |
| hp2.ver1.in           | [ANL]           | : HEN002-1.p | IM1                  | [Qua92a] | : SET327-6.p |
| hp2.ver2.in           | [ANL]           | : HEN002-3.p | IM1 cor.             | [Qua92d] | : SET328-6.p |
| hp2.ver3.in           | [ANL]           | : HEN002-5.p | IM2                  | [Qua92a] | : SET329-6.p |
| HP3                   | [ANL]           | : HEN003-3.p | IM2 cor.             | [Qua92d] | : SET330-6.p |
| hp3.ver1.in           | [ANL]           | : HEN003-2.p | IM3                  | [Qua92a] | : SET324-6.p |
| hp3.ver2.in           | [ANL]           | : HEN003-4.p | IM4                  | [Qua92a] | : SET325-6.p |
| hp3.ver3.in           | [ANL]           | : HEN003-5.p | IM4 cor.             | [Qua92a] | : SET326-6.p |
| HP4                   | [ANL]           | : HEN004-3.p | IM5                  | [Qua92a] | : SET331-6.p |
| hp4.ver1.in           | [ANL]           | : HEN004-2.p | IM5 cor.             | [Qua92a] | : SET332-6.p |
| hp4.ver2.in           | [ANL]           | : HEN004-6.p | IM6.1                | [Qua92a] | : SET333-6.p |
| hp4.ver3.in           | [ANL]           | : HEN004-5.p | IM6.2                | [Qua92a] | : SET334-6.p |
| HP5                   | [ANL]           | : HEN005-3.p | IM7                  | [Qua92a] | : SET335-6.p |
| hp5.ver1.in           | [ANL]           | : HEN005-1.p | IM7 cor.1            | [Qua92a] | : SET336-6.p |
| hp5.ver2.in           | [ANL]           | : HEN005-6.p | IM7 cor.2            | [Qua92d] | : SET337-6.p |
| hp5.ver3.in           | [ANL]           | : HEN005-5.p | IM7 cor.3            | [Qua92a] | : SET338-6.p |
| HP6                   | [ANL]           | : HEN006-3.p | IM8                  | [Qua92a] | : SET339-6.p |

|                              |          |              |           |                        |              |
|------------------------------|----------|--------------|-----------|------------------------|--------------|
| IM9                          | [Qua92a] | : SET340-6.p | Lemma 1   | [Bon91]                | : LCL132-1.p |
| IM10                         | [Qua92a] | : SET341-6.p | Lemma 1   | [BL M <sup>+</sup> 86] | : SET016-3.p |
| IM11                         | [Qua92d] | : SET342-6.p | Lemma 1a  | [WM89]                 | : TOP001-1.p |
| IM12                         | [Qua92d] | : SET343-6.p | Lemma 1a  | [WM89]                 | : TOP001-2.p |
| Imp-4                        | [LM92]   | : LCL084-1.p | Lemma 1b  | [WM89]                 | : TOP002-1.p |
| IMV                          | [WB87]   | : ANA002-3.p | Lemma 1b  | [WM89]                 | : TOP002-2.p |
| IN1                          | [Qua92a] | : SET289-6.p | Lemma 1c  | [WM89]                 | : TOP003-1.p |
| IN2                          | [Qua92a] | : SET290-6.p | Lemma 1c  | [WM89]                 | : TOP003-2.p |
| IN3                          | [Qua92a] | : SET291-6.p | Lemma 1d  | [WM89]                 | : TOP004-1.p |
| IN4.1                        | [Qua92a] | : SET292-6.p | Lemma 1d  | [WM89]                 | : TOP004-2.p |
| IN4.2                        | [Qua92a] | : SET293-6.p | Lemma 1e  | [WM89]                 | : TOP005-1.p |
| IN5.1                        | [Qua92a] | : SET294-6.p | Lemma 1e  | [WM89]                 | : TOP005-2.p |
| IN5.2                        | [Qua92a] | : SET295-6.p | Lemma 2   | [Bon91]                | : LCL133-1.p |
| IN6.1                        | [Qua92a] | : SET296-6.p | Lemma 2   | [BL M <sup>+</sup> 86] | : SET017-3.p |
| IN6.2                        | [Qua92a] | : SET297-6.p | Lemma 2   | [BL M <sup>+</sup> 86] | : SET017-4.p |
| IN7                          | [Qua92a] | : SET298-6.p | Lemma 2.1 | [Win90]                | : ROB002-1.p |
| IN8                          | [Qua92a] | : SET299-6.p | Lemma 2.2 | [Win90]                | : ROB003-1.p |
| IN9                          | [Qua92a] | : SET300-6.p | Lemma 2.3 | [Win90]                | : ROB004-1.p |
| IN10                         | [Qua92a] | : SET301-6.p | Lemma 2.4 | [Win90]                | : ROB005-1.p |
| index.ver1.in                | [ANL]    | : GRP039-4.p | Lemma 3   | [Bon91]                | : LCL134-1.p |
| index.ver2.in                | [ANL]    | : GRP039-5.p | Lemma 3   | [BL M <sup>+</sup> 86] | : SET018-3.p |
| intchg_val.ver1.clauses      | [ANL]    | : CIV001-1.p | Lemma 3   | [BL M <sup>+</sup> 86] | : SET018-4.p |
| interchange.ver1.clauses     | [ANL]    | : CID002-1.p | Lemma 3.1 | [Win90]                | : ROB008-1.p |
| interns.ver1.in              | [ANL]    | : PUZ018-1.p | Lemma 3.2 | [Win90]                | : ROB009-1.p |
| inters.ver1.in               | [ANL]    | : SET013-2.p | Lemma 3.3 | [Win90]                | : ROB010-1.p |
| inters.ver2.in               | [ANL]    | : SET013-4.p | Lemma 3.4 | [Win90]                | : ROB011-1.p |
| invers1.ver1.in              | [ANL]    | : GRP017-1.p | Lemma 3.4 | [Win90]                | : ROB012-1.p |
| invers2.ver1.t               | [ANL]    | : GRP031-1.p | Lemma 3.4 | [Win90]                | : ROB012-2.p |
| IP1                          | [Pfe88]  | : LCL083-2.p | Lemma 3.5 | [Win90]                | : ROB013-1.p |
| IPH1                         | [Pfe88]  | : LCL084-3.p | Lemma 3.6 | [Win90]                | : ROB014-1.p |
| IR1                          | [Qua92d] | : NUM039-1.p | Lemma 3.6 | [Win90]                | : ROB014-2.p |
| IR2                          | [Qua92d] | : NUM040-1.p | Lemma 3.6 | [Win90]                | : ROB015-1.p |
| IR3.1                        | [Qua92d] | : NUM041-1.p | Lemma 3.6 | [Win90]                | : ROB015-2.p |
| IR3.2                        | [Qua92d] | : NUM042-1.p | Lemma 3.8 | [Win90]                | : ROB017-1.p |
| IR4                          | [Qua92d] | : NUM043-1.p | Lemma 4   | [Bon91]                | : LCL135-1.p |
| IR5                          | [Qua92d] | : NUM044-1.p | Lemma 4   | [BL M <sup>+</sup> 86] | : SET019-3.p |
| IR6                          | [Qua92d] | : NUM045-1.p | Lemma 4   | [BL M <sup>+</sup> 86] | : SET019-4.p |
| ivt.lop                      | [SET]    | : ANA002-4.p | Lemma 5   | [Bon91]                | : LCL136-1.p |
| jobs                         | [LP92]   | : PUZ010-1.p | Lemma 5   | [BL M <sup>+</sup> 86] | : SET020-3.p |
| jobs.ver1.in                 | [ANL]    | : PUZ019-1.p | Lemma 5   | [BL M <sup>+</sup> 86] | : SET020-4.p |
| KL-ONE-example               | [FLTZ93] | : MSC009-1.p | Lemma 6   | [Bon91]                | : LCL111-2.p |
| knightknav.in                | [ANL]    | : PUZ020-1.p | Lemma 6   | [BL M <sup>+</sup> 86] | : SET021-3.p |
| L1a                          | [McC88]  | : LAT001-1.p | Lemma 6   | [BL M <sup>+</sup> 86] | : SET021-4.p |
| L1b                          | [McC88]  | : LAT002-1.p | Lemma 7   | [Bon91]                | : LCL138-1.p |
| L2                           | [McC88]  | : LAT003-1.p | Lemma 7   | [BL M <sup>+</sup> 86] | : SET022-3.p |
| L3                           | [McC88]  | : LAT004-1.p | Lemma 7   | [BL M <sup>+</sup> 86] | : SET022-4.p |
| LA1.1                        | [Qua92a] | : SET194-6.p | Lemma 8   | [Bon91]                | : LCL139-1.p |
| LA1.2                        | [Qua92a] | : SET195-6.p | Lemma 8   | [BL M <sup>+</sup> 86] | : SET023-4.p |
| LA1.3                        | [Qua92a] | : SET196-6.p | Lemma 8   | [BL M <sup>+</sup> 86] | : SET023-3.p |
| LA1.4                        | [Qua92a] | : SET197-6.p | Lemma 9   | [Bon91]                | : LCL140-1.p |
| LA2.1                        | [Qua92a] | : SET198-6.p | Lemma 9   | [BL M <sup>+</sup> 86] | : SET024-4.p |
| LA2.2                        | [Qua92a] | : SET199-6.p | Lemma 9   | [BL M <sup>+</sup> 86] | : SET024-3.p |
| LA3.1                        | [Qua92a] | : SET200-6.p | Lemma 10  | [Bon91]                | : LCL141-1.p |
| LA3.2                        | [Qua92a] | : SET201-6.p | Lemma 10  | [BL M <sup>+</sup> 86] | : SET025-4.p |
| lat1a                        | [Sch95]  | : GRP165-1.p | Lemma 10  | [BL M <sup>+</sup> 86] | : SET025-3.p |
| lat1b                        | [Sch95]  | : GRP165-2.p | Lemma 11  | [BL M <sup>+</sup> 86] | : SET025-8.p |
| lat2a                        | [Sch95]  | : GRP166-1.p | Lemma 11  | [BL M <sup>+</sup> 86] | : SET025-9.p |
| lat2b                        | [Sch95]  | : GRP166-2.p | Lemma 12  | [BL M <sup>+</sup> 86] | : SET027-3.p |
| lat3a                        | [Sch95]  | : GRP166-3.p | Lemma 12  | [BL M <sup>+</sup> 86] | : SET027-4.p |
| lat3b                        | [Sch95]  | : GRP166-4.p | Lemma 13  | [BL M <sup>+</sup> 86] | : SET028-3.p |
| lat4                         | [Sch95]  | : GRP167-2.p | Lemma 13  | [BL M <sup>+</sup> 86] | : SET028-4.p |
| Lattice structure theorem 1  | [Bon91]  | : LCL142-1.p | Lemma 14  | [BL M <sup>+</sup> 86] | : SET029-3.p |
| Lattice structure theorem 10 | [Bon91]  | : LCL150-1.p | Lemma 14  | [BL M <sup>+</sup> 86] | : SET029-4.p |
| Lattice structure theorem 11 | [Bon91]  | : LCL151-1.p | Lemma 15  | [BL M <sup>+</sup> 86] | : SET030-3.p |
| Lattice structure theorem 12 | [Bon91]  | : LCL152-1.p | Lemma 15  | [BL M <sup>+</sup> 86] | : SET030-4.p |
| Lattice structure theorem 2  | [Bon91]  | : LCL143-1.p | Lemma 16  | [BL M <sup>+</sup> 86] | : SET031-3.p |
| Lattice structure theorem 3  | [Bon91]  | : LCL144-1.p | Lemma 16  | [BL M <sup>+</sup> 86] | : SET031-4.p |
| Lattice structure theorem 4  | [Bon91]  | : LCL145-1.p | Lemma 17  | [BL M <sup>+</sup> 86] | : SET032-3.p |
| Lattice structure theorem 5  | [Bon91]  | : LCL146-1.p | Lemma 17  | [BL M <sup>+</sup> 86] | : SET032-4.p |
| Lattice structure theorem 6  | [Bon91]  | : LCL147-1.p | Lemma 18  | [BL M <sup>+</sup> 86] | : SET033-3.p |
| Lattice structure theorem 7  | [Bon91]  | : LCL148-1.p | Lemma 18  | [BL M <sup>+</sup> 86] | : SET033-4.p |
| Lattice structure theorem 8  | [Bon91]  | : LCL109-4.p | Lemma 19  | [BL M <sup>+</sup> 86] | : SET034-3.p |
| Lattice structure theorem 8  | [Bon91]  | : LCL109-5.p | Lemma 19  | [BL M <sup>+</sup> 86] | : SET034-4.p |
| Lattice structure theorem 8  | [Bon91]  | : LCL109-6.p | Lemma 20  | [BL M <sup>+</sup> 86] | : SET035-3.p |
| Lattice structure theorem 9  | [Bon91]  | : LCL149-1.p | Lemma 20  | [BL M <sup>+</sup> 86] | : SET035-4.p |
| LCM                          | [WB87]   | : NUM007-1.p | Lemma 21  | [BL M <sup>+</sup> 86] | : SET036-3.p |
| lcm                          | [Wan85]  | : NUM007-1.p | Lemma 21  | [BL M <sup>+</sup> 86] | : SET036-4.p |
| Lemma for Axiom Independence | [Wos88]  | : B00002-2.p | Lemma 22  | [BL M <sup>+</sup> 86] | : SET037-3.p |
| Lemma proved                 | [OMW76]  | : B00003-1.p | Lemma 22  | [BL M <sup>+</sup> 86] | : SET037-4.p |
| Lemma proved                 | [OMW76]  | : B00004-1.p | Lemma 23  | [BL M <sup>+</sup> 86] | : SET038-3.p |
| Lemma proved                 | [OMW76]  | : B00005-1.p | Lemma 23  | [BL M <sup>+</sup> 86] | : SET038-4.p |
| Lemma proved                 | [OMW76]  | : B00006-1.p | Lemma 24  | [BL M <sup>+</sup> 86] | : SET039-3.p |
| Lemma proved                 | [OMW76]  | : B00009-1.p | Lemma 24  | [BL M <sup>+</sup> 86] | : SET039-4.p |
| Lemma proved                 | [OMW76]  | : B00010-1.p | Lemma 25  | [BL M <sup>+</sup> 86] | : SET040-3.p |
| Lemma proved                 | [OMW76]  | : GRP018-1.p | Lemma 25  | [BL M <sup>+</sup> 86] | : SET040-4.p |
| Lemma proved                 | [OMW76]  | : GRP019-1.p | Lemma 26  | [BL M <sup>+</sup> 86] | : SET041-3.p |
| Lemma proved                 | [OMW76]  | : GRP020-1.p |           |                        |              |
| Lemma proved                 | [OMW76]  | : GRP021-1.p |           |                        |              |
| Lemma proved                 | [OMW76]  | : GRP022-1.p |           |                        |              |
| Lemma proved                 | [OMW76]  | : GRP023-1.p |           |                        |              |
| Lemma proved                 | [OMW76]  | : RIG002-1.p |           |                        |              |
| Lemma proved                 | [OMW76]  | : RIG003-1.p |           |                        |              |

|                      |                       |              |                      |                       |              |
|----------------------|-----------------------|--------------|----------------------|-----------------------|--------------|
| Lemma 26             | [BLM <sup>+</sup> 86] | : SET041-4.p | LUB1                 | [Qua92d]              | : NUM193-1.p |
| Lemma 27             | [BLM <sup>+</sup> 86] | : SET042-3.p | LUB2                 | [Qua92d]              | : NUM194-1.p |
| Lemma 27             | [BLM <sup>+</sup> 86] | : SET042-4.p | LUB3                 | [Qua92d]              | : NUM195-1.p |
| lemma.ver1.in        | [ANL]                 | : RIG007-5.p | LUB4                 | [Qua92d]              | : NUM196-1.p |
| lemma.ver2.in        | [ANL]                 | : RIG007-4.p | LUB4-5               | [Qua92d]              | : NUM197-1.p |
| lemma.ver3.in        | [ANL]                 | : RIG007-1.p | LUB5.1               | [Qua92d]              | : NUM198-1.p |
| lemma.ver4.in        | [ANL]                 | : RIG007-1.p | LUB5.2               | [Qua92d]              | : NUM199-1.p |
| letters.ver1.in      | [ANL]                 | : PUV004-1.p | LUB6                 | [Qua92d]              | : NUM200-1.p |
| LG-89                | [MW92]                | : LCL096-1.p | LUB7                 | [Qua92d]              | : NUM201-1.p |
| LG-90                | [MW92]                | : LCL097-1.p | LUB8                 | [Qua92d]              | : NUM202-1.p |
| LG-91                | [MW92]                | : LCL098-1.p | LUB8 cor.            | [Qua92d]              | : NUM203-1.p |
| LG-92                | [MW92]                | : LCL099-1.p | LUB9                 | [Qua92d]              | : NUM204-1.p |
| LG-93                | [MW92]                | : LCL100-1.p | LUB9 cor. 1          | [Qua92d]              | : NUM205-1.p |
| LG-94                | [MW92]                | : LCL101-1.p | LUB9 cor. 2          | [Qua92d]              | : NUM206-1.p |
| LG-95                | [MW92]                | : LCL102-1.p | LUB10                | [Qua92d]              | : NUM207-1.p |
| LG-96                | [MW92]                | : LCL103-1.p | LUB11                | [Qua92d]              | : NUM208-1.p |
| LG-97                | [MW92]                | : LCL104-1.p | LUB11 cor.           | [Qua92d]              | : NUM209-1.p |
| LG-98                | [MW92]                | : LCL105-1.p | LUB12.1              | [Qua92d]              | : NUM210-1.p |
| LG-99                | [MW92]                | : LCL106-1.p | LUB12.2              | [Qua92d]              | : NUM211-1.p |
| LG-100               | [MW92]                | : LCL107-1.p | LUB12.3              | [Qua92d]              | : NUM212-1.p |
| LG-101               | [MW92]                | : LCL108-1.p | LUB13                | [Qua92d]              | : NUM213-1.p |
| lifsch.in            | [OTT]                 | : SYN039-1.p | LUB14                | [Qua92d]              | : NUM214-1.p |
| LIM2.1               | [Qua92d]              | : NUM180-1.p | LUB14 cor.           | [Qua92d]              | : NUM215-1.p |
| LIM2.2               | [Qua92d]              | : NUM181-1.p | Luka5                | [ANL]                 | : LCL109-1.p |
| LIM2.3               | [Qua92d]              | : NUM182-1.p | Luka-5               | [LM92]                | : LCL109-2.p |
| LIM2.4               | [Qua92d]              | : NUM183-1.p | m1                   | [Ste87]               | : RIG027-6.p |
| LIM2.4 cor.          | [Qua92d]              | : NUM184-1.p | m1'                  | [Ste87]               | : RIG027-8.p |
| LIM3                 | [Qua92d]              | : NUM185-1.p | m2                   | [Ste87]               | : RIG028-6.p |
| LIM+                 | [Ble90]               | : AHA005-5.p | m2'                  | [Ste87]               | : RIG028-8.p |
| Lion and the Unicorn | [OSS85]               | : PUV005-1.p | m3                   | [Ste87]               | : RIG029-6.p |
| ls1                  | [SET]                 | : LCL081-1.p | M(T2n)               | [Pla94]               | : SYN095-1.g |
| ls2                  | [SET]                 | : LCL082-1.p | M(T3n)               | [Pla94]               | : SYN096-1.g |
| ls3                  | [SET]                 | : LCL083-1.p | MA 1                 | [Qua92d]              | : SET035-6.p |
| ls4                  | [SET]                 | : LCL083-2.p | MA 2                 | [Qua92d]              | : SET038-6.p |
| ls5                  | [SET]                 | : LCL084-1.p | mars_venus.in        | [ANL]                 | : PUV007-1.p |
| ls5 (Size 2)         | [LS74]                | : SYN001-1.g | mars_venus.in        | [ANL]                 | : PUV006-1.p |
| ls5 (Size 2)         | [WM76]                | : SYN001-1.g | minuses.ver1.in      | [ANL]                 | : RIG004-1.p |
| ls6                  | [SET]                 | : LCL084-2.p | mission.ver1.in      | [ANL]                 | : PUV008-1.p |
| ls7                  | [SET]                 | : LCL084-3.p | mission.ver2.in      | [ANL]                 | : PUV008-2.p |
| ls17                 | [LS74]                | : NUM016-1.p | morgan.five.ver1.in  | [ANL]                 | : LCL077-1.p |
| ls17                 | [WM76]                | : NUM016-1.p | morgan.five.ver2.in  | [ANL]                 | : LCL078-1.p |
| ls23                 | [LS74]                | : GRP031-2.p | morgan.four.ver1.in  | [ANL]                 | : LCL076-3.p |
| ls23                 | [WM76]                | : GRP031-2.p | morgan.one.ver2.in   | [ANL]                 | : LCL079-1.p |
| ls26                 | [LS74]                | : GRP034-4.p | morgan.six.ver1.in   | [ANL]                 | : LCL064-2.p |
| ls26                 | [WM76]                | : GRP034-4.p | morgan.three.ver1.in | [ANL]                 | : LCL076-2.p |
| ls28                 | [LS74]                | : NUM001-1.p | morgan.three.ver2.in | [ANL]                 | : LCL076-2.p |
| ls28                 | [WM76]                | : NUM001-1.p | morgan.two.ver1.in   | [ANL]                 | : LCL077-2.p |
| ls29                 | [LS74]                | : NUM002-1.p | MQW                  | [MRS72]               | : SYN031-1.p |
| ls29                 | [WM76]                | : NUM002-1.p | MQW                  | [WM76]                | : SYN031-1.p |
| ls36                 | [LS74]                | : GRP012-2.p | MV 1.1               | [LW92]                | : LCL110-2.p |
| ls36                 | [WM76]                | : GRP012-2.p | MV 1.2               | [LW92]                | : LCL112-2.p |
| ls37                 | [LS74]                | : RIG001-2.p | MV2                  | [LW92]                | : LCL111-2.p |
| ls37                 | [WM76]                | : RIG001-2.p | MV3                  | [LW92]                | : LCL114-2.p |
| ls41                 | [LS74]                | : NUM019-1.p | MV4                  | [LW92]                | : LCL109-2.p |
| ls41                 | [WM76]                | : NUM019-1.p | mv25.in              | [OTT]                 | : LCL111-1.p |
| ls55                 | [LS74]                | : NUM020-1.p | MV-55                | [MW92]                | : LCL109-1.p |
| ls55                 | [WM76]                | : NUM020-1.p | MV-56                | [MW92]                | : LCL110-1.p |
| ls65                 | [LS74]                | : NUM021-1.p | MV-57                | [MW92]                | : LCL111-1.p |
| ls65                 | [WM76]                | : NUM021-1.p | MV-58                | [MW92]                | : LCL112-1.p |
| ls68                 | [LS74]                | : NUM023-1.p | MV-59                | [MW92]                | : LCL113-1.p |
| ls68                 | [WM76]                | : NUM023-1.p | MV-60                | [MW92]                | : LCL114-1.p |
| ls75                 | [LS74]                | : NUM024-1.p | MV-61                | [MW92]                | : LCL115-1.p |
| ls75                 | [WM76]                | : NUM024-1.p | MV-62                | [MW92]                | : LCL116-1.p |
| ls76t1               | [LS74]                | : NUM025-1.p | mv.in part 1         | [OTT]                 | : LCL110-1.p |
| ls76t1               | [WM76]                | : NUM025-1.p | mv.in part 2         | [OTT]                 | : LCL111-1.p |
| ls76t2               | [LS74]                | : NUM026-1.p | mv.in part 3         | [OTT]                 | : LCL112-1.p |
| ls76t2               | [WM76]                | : NUM026-1.p | N(T2n))              | [Pla94]               | : SYN101-1.g |
| ls87                 | [LS74]                | : NUM027-1.p | N(T3n))              | [Pla94]               | : SYN102-1.g |
| ls87                 | [WM76]                | : NUM027-1.p | new.ver2.in          | [ANL]                 | : HEN012-3.p |
| ls100                | [LS74]                | : SET001-1.p | nonob.lop            | [SET]                 | : MSC006-1.p |
| ls100                | [WM76]                | : SET001-1.p | NU2                  | [LW92]                | : GRP039-2.p |
| ls103                | [LS74]                | : SET002-1.p | NU3.1                | [LW92]                | : SET016-1.p |
| ls103                | [WM76]                | : SET002-1.p | NU3.2                | [LW92]                | : SET018-1.p |
| ls105                | [LS74]                | : SET003-1.p | NUM1                 | [RRY <sup>+</sup> 72] | : NUM014-1.p |
| ls105                | [WM76]                | : SET003-1.p | OA 6.1               | [Qua92d]              | : NUM265-1.p |
| ls106                | [LS74]                | : SET004-1.p | OA 6.2               | [Qua92d]              | : NUM266-1.p |
| ls106                | [WM76]                | : SET004-1.p | OA 6.3               | [Qua92d]              | : NUM267-1.p |
| ls108                | [LS74]                | : SET005-1.p | OA 6.4               | [Qua92d]              | : NUM268-1.p |
| ls108                | [WM76]                | : SET005-1.p | OA7                  | [Qua92d]              | : NUM269-1.p |
| ls111                | [LS74]                | : SET006-1.p | OA8                  | [Qua92d]              | : NUM270-1.p |
| ls111                | [WM76]                | : SET006-1.p | OA9.1                | [Qua92d]              | : NUM277-1.p |
| ls112                | [LS74]                | : SET007-1.p | OA9.2                | [Qua92d]              | : NUM278-1.p |
| ls112                | [WM76]                | : SET007-1.p | OA9 lemma 1          | [Qua92d]              | : NUM271-1.p |
| ls115                | [LS74]                | : SET008-1.p | OA9 lemma 2          | [Qua92d]              | : NUM272-1.p |
| ls115                | [WM76]                | : SET008-1.p | OA9 lemma 3          | [Qua92d]              | : NUM273-1.p |
| ls116                | [LS74]                | : SET009-1.p | OA9 lemma 4          | [Qua92d]              | : NUM274-1.p |
| ls116                | [WM76]                | : SET009-1.p | OA9 lemma 5          | [Qua92d]              | : NUM275-1.p |
| ls118                | [LS74]                | : SET010-1.p | OA9 lemma 6          | [Qua92d]              | : NUM276-1.p |
| ls118                | [WM76]                | : SET010-1.p | OA 10                | [Qua92d]              | : NUM277-2.p |
| ls121                | [LS74]                | : SET011-1.p | OM1                  | [Qua92d]              | : NUM186-1.p |
| ls121                | [WM76]                | : SET011-1.p | OM2                  | [Qua92d]              | : NUM187-1.p |
| ls651                | [LS74]                | : NUM022-1.p | OM2.1                | [Qua92d]              | : NUM280-1.p |



|                |          |              |                 |         |              |
|----------------|----------|--------------|-----------------|---------|--------------|
| OM2.2          | [Qua92d] | : NUM281-1.p | p01b            | [Sch95] | : GRP168-2.p |
| OM2.3          | [Qua92d] | : NUM282-1.p | p2.lop          | [SET]   | : ANA004-4.p |
| OM3            | [Qua92d] | : NUM188-1.p | p2.ver1.in      | [ANL]   | : CAT002-1.p |
| OM4            | [Qua92d] | : NUM189-1.p | p2.ver2.in      | [ANL]   | : CAT002-2.p |
| OM5            | [Qua92d] | : NUM190-1.p | p2.ver3.in      | [ANL]   | : CAT002-3.p |
| OM6            | [Qua92d] | : NUM191-1.p | p02a            | [Sch95] | : GRP169-1.p |
| OM7            | [Qua92d] | : NUM192-1.p | p02b            | [Sch95] | : GRP169-2.p |
| oona.in        | [ANL]    | : PUZ009-1.p | p3.lop          | [SET]   | : ANA004-5.p |
| OP1            | [Qua92a] | : SET025-7.p | p3.ver1.in      | [ANL]   | : CAT003-1.p |
| OP2.1          | [Qua92a] | : SET101-7.p | p3.ver2.in      | [ANL]   | : CAT003-2.p |
| OP2.2          | [Qua92a] | : SET102-7.p | p3.ver3.in      | [ANL]   | : CAT003-3.p |
| OP3.1          | [Qua92a] | : SET103-7.p | p03a            | [Sch95] | : GRP170-1.p |
| OP3.2          | [Qua92a] | : SET104-7.p | p03b            | [Sch95] | : GRP170-2.p |
| OP3.3          | [Qua92a] | : SET105-7.p | p03c            | [Sch95] | : GRP170-3.p |
| OP4            | [Qua92a] | : SET016-7.p | p03d            | [Sch95] | : GRP170-4.p |
| OP5            | [Qua92a] | : SET018-7.p | p4.lop          | [SET]   | : ANA005-4.p |
| OP6.1          | [Qua92a] | : SET108-7.p | p4.ver1.in      | [ANL]   | : CAT004-1.p |
| OP6.2          | [Qua92a] | : SET109-7.p | p4.ver2.in      | [ANL]   | : CAT004-2.p |
| OP6.3          | [Qua92a] | : SET110-7.p | p4.ver3.in      | [ANL]   | : CAT004-3.p |
| OP6.4          | [Qua92a] | : SET111-7.p | p04a            | [Sch95] | : GRP171-1.p |
| OP6.5          | [Qua92a] | : SET112-7.p | p04b            | [Sch95] | : GRP172-1.p |
| OP7.1          | [Qua92a] | : SET020-7.p | p04c            | [Sch95] | : GRP171-2.p |
| OP7.2          | [Qua92a] | : SET021-7.p | p04d            | [Sch95] | : GRP172-2.p |
| OP8.1          | [Qua92a] | : SET113-7.p | p5.lop          | [SET]   | : ANA005-5.p |
| OP8.2          | [Qua92a] | : SET114-7.p | p5.ver1.in      | [ANL]   | : CAT005-1.p |
| OP8.3          | [Qua92a] | : SET115-7.p | p5.ver3.in      | [ANL]   | : CAT005-3.p |
| OP8.4          | [Qua92a] | : SET116-7.p | p05a            | [Sch95] | : GRP173-1.p |
| OP9.1          | [Qua92a] | : SET117-7.p | p05b            | [Sch95] | : GRP174-1.p |
| OP9.2          | [Qua92d] | : SET118-7.p | p6.ver1.in      | [ANL]   | : CAT006-1.p |
| OP10           | [Qua92a] | : SET016-7.p | p6.ver3.in      | [ANL]   | : CAT006-3.p |
| OP10 cor.      | [Qua92a] | : SET119-6.p | p06a            | [Sch95] | : GRP175-1.p |
| OP10 cor.      | [Qua92a] | : SET120-6.p | p06b            | [Sch95] | : GRP175-2.p |
| OP10 cor.1     | [Qua92a] | : SET119-7.p | p06c            | [Sch95] | : GRP175-3.p |
| OP10 cor.2     | [Qua92a] | : SET120-7.p | p06d            | [Sch95] | : GRP175-4.p |
| OP11           | [Qua92a] | : SET018-7.p | p07             | [Sch95] | : GRP176-2.p |
| OP11           | [Qua92a] | : SET121-6.p | p7.ver1.in      | [ANL]   | : CAT007-1.p |
| OP11 cor.      | [Qua92a] | : SET122-6.p | p7.ver3.in      | [ANL]   | : CAT007-3.p |
| OP11 cor.1     | [Qua92a] | : SET121-7.p | p8.ver1.in      | [ANL]   | : CAT008-1.p |
| OP11 cor.2     | [Qua92a] | : SET122-7.p | p08a            | [Sch95] | : GRP177-1.p |
| ORD1           | [Qua92d] | : NUM098-1.p | p08b            | [Sch95] | : GRP177-2.p |
| ORD1 cor       | [Qua92d] | : NUM099-1.p | p8_9a           | [Sch95] | : GRP193-1.p |
| ORD2           | [Qua92d] | : NUM100-1.p | p8_9b           | [Sch95] | : GRP193-2.p |
| ORD5.1         | [Qua92d] | : NUM101-1.p | p9.ver1.in      | [ANL]   | : CAT009-1.p |
| ORD5.2         | [Qua92d] | : NUM102-1.p | p9.ver3.in      | [ANL]   | : CAT009-3.p |
| ORD5 cor       | [Qua92d] | : NUM103-1.p | p09a            | [Sch95] | : GRP178-1.p |
| ORD6           | [Qua92d] | : NUM104-1.p | p09b            | [Sch95] | : GRP178-2.p |
| ORD7.1         | [Qua92d] | : NUM105-1.p | p10             | [Sch95] | : GRP179-1.p |
| ORD7.2         | [Qua92d] | : NUM106-1.p | p10.ver1.in     | [ANL]   | : CAT010-1.p |
| ORD8.1         | [Qua92d] | : NUM107-1.p | p11             | [Sch95] | : GRP180-2.p |
| ORD8.2         | [Qua92d] | : NUM108-1.p | p11.ver1.in     | [ANL]   | : CAT011-1.p |
| ORD9           | [Qua92d] | : NUM109-1.p | p11.ver2.in     | [ANL]   | : CAT011-2.p |
| ORD9 cor       | [Qua92d] | : NUM110-1.p | p11.ver3.in     | [ANL]   | : CAT011-3.p |
| ORD11          | [Qua92d] | : NUM111-1.p | p12             | [Sch95] | : GRP181-2.p |
| ORD12          | [Qua92d] | : NUM112-1.p | p12.ver1.in     | [ANL]   | : CAT012-1.p |
| ORD13          | [Qua92d] | : NUM113-1.p | p12.ver3.in     | [ANL]   | : CAT012-3.p |
| ORD13 cor.     | [Qua92d] | : NUM114-1.p | p12x            | [Sch95] | : GRP181-4.p |
| ORD14          | [Qua92d] | : NUM115-1.p | p13.ver1.in     | [ANL]   | : CAT013-1.p |
| ORD14 cor      | [Qua92d] | : NUM116-1.p | p13.ver3.in     | [ANL]   | : CAT013-3.p |
| ORD15          | [Qua92d] | : NUM117-1.p | p14.ver1.in     | [ANL]   | : CAT014-1.p |
| ORD16          | [Qua92d] | : NUM118-1.p | p14.ver2.in     | [ANL]   | : CAT014-2.p |
| ORD17          | [Qua92d] | : NUM119-1.p | p14.ver3.in     | [ANL]   | : CAT014-3.p |
| ORD18-5.1      | [Qua92d] | : NUM126-1.p | p15.related.in  | [ANL]   | : CAT015-3.p |
| ORD18-5.2      | [Qua92d] | : NUM127-1.p | p15.ver1.in     | [ANL]   | : CAT019-1.p |
| ORD18-5.3      | [Qua92d] | : NUM128-1.p | p15.ver2.in     | [ANL]   | : CAT019-2.p |
| ORD18-6.1      | [Qua92d] | : NUM129-1.p | p15.ver3.no1.in | [ANL]   | : CAT019-5.p |
| ORD18-6.2      | [Qua92d] | : NUM130-1.p | p15.ver3.no2.in | [ANL]   | : CAT019-3.p |
| ORD18-6.3      | [Qua92d] | : NUM131-1.p | p15.ver3.no4.in | [ANL]   | : CAT019-3.p |
| ORD18.1        | [Qua92d] | : NUM120-1.p | p16.ver3.in     | [ANL]   | : CAT016-3.p |
| ORD18.2        | [Qua92d] | : NUM121-1.p | p17.ver3.in     | [ANL]   | : CAT017-3.p |
| ORD18.3        | [Qua92d] | : NUM122-1.p | p17a            | [Sch95] | : GRP182-2.p |
| ORD18.4        | [Qua92d] | : NUM123-1.p | p17b            | [Sch95] | : GRP182-4.p |
| ORD18.5        | [Qua92d] | : NUM124-1.p | p18             | [Sch95] | : GRP179-3.p |
| ORD18.6        | [Qua92d] | : NUM125-1.p | p18.ver1.in     | [ANL]   | : CAT018-1.p |
| ORD20          | [Qua92d] | : NUM132-1.p | p18.ver3.in     | [ANL]   | : CAT018-3.p |
| ORD20 cor.     | [Qua92d] | : NUM133-1.p | p19             | [Sch95] | : GRP167-4.p |
| ORD21          | [Qua92d] | : NUM134-1.p | p20             | [Sch95] | : GRP183-2.p |
| ORD22          | [Qua92d] | : NUM135-1.p | p20x            | [Sch95] | : GRP183-4.p |
| ORD23          | [Qua92d] | : NUM136-1.p | p21             | [Sch95] | : GRP184-2.p |
| ORD24.1        | [Qua92d] | : NUM137-1.p | p21x            | [Sch95] | : GRP184-4.p |
| ORD24.2        | [Qua92d] | : NUM138-1.p | p22a            | [Sch95] | : GRP185-2.p |
| ORD24.3        | [Qua92d] | : NUM139-1.p | p22b            | [Sch95] | : GRP185-4.p |
| order2.ver3.in | [ANL]    | : GRP025-3.p | p23             | [Sch95] | : GRP186-2.p |
| order2.ver4.in | [ANL]    | : GRP025-4.p | p23x            | [Sch95] | : GRP186-4.p |
| order3.ver3.in | [ANL]    | : GRP026-3.p | p33             | [Sch95] | : GRP187-1.p |
| order3.ver4.in | [ANL]    | : GRP026-4.p | p35.in          | [ANL]   | : SYN064-1.p |
| ovb6           | [SET]    | : LCL111-1.p | p36.in          | [ANL]   | : SYN065-1.p |
| P1             | [Pfe88]  | : LCL083-1.p | p37.in          | [ANL]   | : SYN066-1.p |
| p1.lop         | [SET]    | : ANA003-4.p | p38a            | [Sch95] | : GRP188-2.p |
| p1.ver1.in     | [ANL]    | : CAT001-1.p | p38a.in         | [ANL]   | : SYN067-1.p |
| p1.ver2.in     | [ANL]    | : CAT001-2.p | p38b            | [Sch95] | : GRP189-2.p |
| p1.ver3.in     | [ANL]    | : CAT001-3.p | p38b.in         | [ANL]   | : SYN067-1.p |
| p01a           | [Sch95]  | : GRP168-1.p | p39.in          | [ANL]   | : SET043-5.p |

|                       |          |              |                         |           |              |
|-----------------------|----------|--------------|-------------------------|-----------|--------------|
| p39a                  | [Sch95]  | : GRP190-1.p | Pelletier 63            | [Pel86]   | : GRP011-4.p |
| p39b                  | [Sch95]  | : GRP191-1.p | Pelletier 64            | [Pel86]   | : GRP010-4.p |
| p39c                  | [Sch95]  | : GRP190-2.p | Pelletier 65            | [Pel86]   | : GRP001-4.p |
| p39d                  | [Sch95]  | : GRP191-2.p | Pelletier 66            | [Pel86]   | : LCL076-1.p |
| p40.in                | [ANL]    | : SET044-5.p | Pelletier 67            | [Pel86]   | : LCL077-1.p |
| p40a                  | [Sch95]  | : GRP192-1.p | Pelletier 68            | [Pel86]   | : LCL078-1.p |
| p41.in                | [ANL]    | : SET045-5.p | Pelletier 69            | [Pel86]   | : LCL039-1.p |
| p42.in                | [ANL]    | : SET046-5.p | Pelletier 72 (Size 4)   | [Pel86]   | : MSC007-1.g |
| p43.in                | [ANL]    | : SET047-5.p | Pelletier 73 (Size 4)   | [Pel86]   | : MSC007-2.g |
| p44.in                | [ANL]    | : SYN068-1.p | Pelletier 74            | [Pel86]   | : GRA001-1.p |
| p45.in                | [ANL]    | : SYN069-1.p | pigeon.in (Size 4)      | [OTT]     | : MSC007-1.g |
| p46.in                | [ANL]    | : SYN070-1.p | pigs.ver1.in            | [ANL]     | : PUZ029-1.p |
| PC1                   | [Qua92a] | : SET363-6.p | PO1                     | [Qua92a]  | : SET054-7.p |
| PC2                   | [Qua92a] | : SET364-6.p | PO3                     | [Qua92a]  | : SET027-7.p |
| PC3                   | [Qua92a] | : SET365-6.p | PRIM                    | [RRY+ 72] | : NUM015-1.p |
| PC4.1                 | [Qua92a] | : SET366-6.p | prob1.ver1.in           | [ANL]     | : ANA003-2.p |
| PC4.2                 | [Qua92a] | : SET367-6.p | prob1.ver1.in           | [ANL]     | : B00008-1.p |
| PC4.3                 | [Qua92a] | : SET368-6.p | prob1.ver2.in           | [ANL]     | : ANA003-1.p |
| PC5                   | [Qua92a] | : SET369-6.p | prob1.ver2.in           | [ANL]     | : B00008-2.p |
| PC6                   | [Qua92a] | : SET370-6.p | prob2.ver1.in           | [ANL]     | : ANA005-2.p |
| PC7                   | [Qua92a] | : SET371-6.p | prob2_part1.ver1.in     | [ANL]     | : B00003-1.p |
| PC8                   | [Qua92a] | : SET372-6.p | prob2_part1.ver2.in     | [ANL]     | : B00003-2.p |
| PC9                   | [Qua92d] | : SET373-6.p | prob2_part2.ver1        | [ANL]     | : B00004-1.p |
| PC10                  | [Qua92d] | : SET374-6.p | prob2_part2.ver2.in     | [ANL]     | : B00004-2.p |
| PC11                  | [Qua92d] | : SET375-6.p | prob3_part1.ver1.in     | [ANL]     | : B00005-1.p |
| PC12                  | [Qua92d] | : SET376-6.p | prob3_part1.ver2.in     | [ANL]     | : B00005-2.p |
| PC12 cor.1            | [Qua92d] | : SET377-6.p | prob3_part2.ver1        | [ANL]     | : B00006-1.p |
| PC12 cor.2            | [Qua92d] | : SET378-6.p | prob3_part2.ver2.in     | [ANL]     | : B00006-2.p |
| PC12 cor.3            | [Qua92d] | : SET379-6.p | prob4_part1.ver1        | [ANL]     | : B00009-1.p |
| Pelletier 1           | [Pel86]  | : SYN040-1.p | prob4_part1.ver2.in     | [ANL]     | : B00009-2.p |
| Pelletier 2 (Size 1)  | [Pel86]  | : SYN001-1.g | prob4_part2.ver1        | [ANL]     | : B00010-1.p |
| Pelletier 3           | [Pel86]  | : SYN041-1.p | prob4_part2.ver2.in     | [ANL]     | : B00010-2.p |
| Pelletier 4           | [Pel86]  | : LCL181-2.p | prob7.ver1              | [ANL]     | : B00011-1.p |
| Pelletier 5           | [Pel86]  | : LCL230-2.p | prob7.ver2.in           | [ANL]     | : B00011-2.p |
| Pelletier 6 (Size 1)  | [Pel86]  | : SYN001-1.g | prob8.ver1              | [ANL]     | : B00012-3.p |
| Pelletier 7 (Size 1)  | [Pel86]  | : SYN001-1.g | prob8.ver2.in           | [ANL]     | : B00012-2.p |
| Pelletier 8 (Size 1)  | [Pel86]  | : SYN001-1.g | prob9.ver1              | [ANL]     | : B00013-3.p |
| Pelletier 9 (Size 2)  | [Pel86]  | : SYN001-1.g | prob9.ver2.in           | [ANL]     | : B00013-2.p |
| Pelletier 10          | [Pel86]  | : SYN044-1.p | prob10.ver2.in          | [ANL]     | : B00014-2.p |
| Pelletier 11 (Size 1) | [Pel86]  | : SYN001-1.g | prob10.ver2.in          | [ANL]     | : B00015-2.p |
| Pelletier 12 (Size 3) | [Pel86]  | : SYN001-1.g | prob.10.ver1            | [ANL]     | : B00014-3.p |
| Pelletier 13          | [Pel86]  | : SYN045-1.p | Problem for C Reduction | [Sho76]   | : SYN011-1.p |
| Pelletier 14 (Size 2) | [Pel86]  | : SYN001-1.g | Problem 1               | [AZ89]    | : SYN037-1.p |
| Pelletier 15          | [Pel86]  | : SYN046-1.p | Problem 1               | [Ble90]   | : ANA003-4.p |
| Pelletier 16          | [Pel86]  | : SYN041-1.p | Problem 1               | [Jec93a]  | : LDA001-1.p |
| Pelletier 17          | [Pel86]  | : SYN047-1.p | Problem 1               | [LO85a]   | : GRP001-2.p |
| Pelletier 18          | [Pel86]  | : SYN048-1.p | Problem 1               | [WM89]    | : TOP006-1.p |
| Pelletier 19          | [Pel86]  | : SYN049-1.p | Problem 1               | [Wosb]    | : GRP029-1.p |
| Pelletier 20          | [Pel86]  | : SYN050-1.p | PROBLEM 1               | [Zha93]   | : GRP002-3.p |
| Pelletier 21          | [Pel86]  | : SYN051-1.p | Problem 2               | [Ble90]   | : ANA004-4.p |
| Pelletier 22          | [Pel86]  | : SYN052-1.p | Problem 2               | [Jec93a]  | : LDA002-1.p |
| Pelletier 23          | [Pel86]  | : SYN053-1.p | Problem 2               | [LO85a]   | : GRP022-2.p |
| Pelletier 24          | [Pel86]  | : SYN054-1.p | Problem 2               | [WM89]    | : TOP007-1.p |
| Pelletier 25          | [Pel86]  | : SYN055-1.p | Problem 2               | [WM88a]   | : COL049-1.p |
| Pelletier 26          | [Pel86]  | : SYN056-1.p | Problem 2               | [Wosb]    | : GRP030-1.p |
| Pelletier 27          | [Pel86]  | : SYN057-1.p | PROBLEM 2               | [Zha93]   | : ROB005-1.p |
| Pelletier 28          | [Pel86]  | : SYN058-1.p | Problem 2.01            | [WR27]    | : LCL169-1.p |
| Pelletier 29          | [Pel86]  | : SYN059-1.p | Problem 2.02            | [WR27]    | : LCL170-1.p |
| Pelletier 30          | [Pel86]  | : SYN060-1.p | Problem 2.03            | [WR27]    | : LCL171-1.p |
| Pelletier 31          | [Pel86]  | : SYN061-1.p | Problem 2.04            | [WR27]    | : LCL172-1.p |
| Pelletier 32          | [Pel86]  | : SYN062-1.p | Problem 2.05            | [WR27]    | : LCL173-1.p |
| Pelletier 33          | [Pel86]  | : SYN063-1.p | Problem 2.06            | [WR27]    | : LCL174-1.p |
| Pelletier 34          | [Pel86]  | : SYN036-1.p | Problem 2.07            | [WR27]    | : LCL175-1.p |
| Pelletier 35          | [Pel86]  | : SYN064-1.p | Problem 2.08            | [WR27]    | : LCL176-1.p |
| Pelletier 36          | [Pel86]  | : SYN065-1.p | Problem 2.1             | [WR27]    | : LCL176-1.p |
| Pelletier 37          | [Pel86]  | : SYN066-1.p | Problem 2.11            | [WR27]    | : LCL177-1.p |
| Pelletier 38          | [Pel86]  | : SYN067-1.p | Problem 2.12            | [WR27]    | : LCL178-1.p |
| Pelletier 39          | [Pel86]  | : SET043-5.p | Problem 2.13            | [WR27]    | : LCL179-1.p |
| Pelletier 40          | [Pel86]  | : SET044-5.p | Problem 2.14            | [WR27]    | : LCL180-1.p |
| Pelletier 41          | [Pel86]  | : SET045-5.p | Problem 2.15            | [WR27]    | : LCL181-1.p |
| Pelletier 42          | [Pel86]  | : SET046-5.p | Problem 2.16            | [WR27]    | : LCL182-1.p |
| Pelletier 43          | [Pel86]  | : SET047-5.p | Problem 2.17            | [WR27]    | : LCL183-1.p |
| Pelletier 44          | [Pel86]  | : SYN068-1.p | Problem 2.18            | [WR27]    | : LCL184-1.p |
| Pelletier 45          | [Pel86]  | : SYN069-1.p | Problem 2.2             | [WR27]    | : LCL185-1.p |
| Pelletier 46          | [Pel86]  | : SYN070-1.p | Problem 2.21            | [WR27]    | : LCL186-1.p |
| Pelletier 47          | [Pel86]  | : PUZ031-1.p | Problem 2.24            | [WR27]    | : LCL187-1.p |
| Pelletier 48          | [Pel86]  | : SYN071-1.p | Problem 2.25            | [WR27]    | : LCL188-1.p |
| Pelletier 49          | [Pel86]  | : SYN072-1.p | Problem 2.26            | [WR27]    | : LCL189-1.p |
| Pelletier 50          | [Pel86]  | : SYN073-1.p | Problem 2.27            | [WR27]    | : LCL189-1.p |
| Pelletier 51          | [Pel86]  | : SYN074-1.p | Problem 2.3             | [WR27]    | : LCL190-1.p |
| Pelletier 52          | [Pel86]  | : SYN075-1.p | Problem 2.31            | [WR27]    | : LCL191-1.p |
| Pelletier 53          | [Pel86]  | : SYN076-1.p | Problem 2.32            | [WR27]    | : LCL192-1.p |
| Pelletier 54          | [Pel86]  | : SYN077-1.p | Problem 2.33            | [WR27]    | : LCL192-1.p |
| Pelletier 55          | [Pel86]  | : PUZ001-2.p | Problem 2.36            | [WR27]    | : LCL193-1.p |
| Pelletier 56          | [Pel86]  | : SYN078-1.p | Problem 2.37            | [WR27]    | : LCL194-1.p |
| Pelletier 57          | [Pel86]  | : SYN079-1.p | Problem 2.38            | [WR27]    | : LCL195-1.p |
| Pelletier 58          | [Pel86]  | : SYN080-1.p | Problem 2.4             | [WR27]    | : LCL196-1.p |
| Pelletier 59          | [Pel86]  | : SYN081-1.p | Problem 2.41            | [WR27]    | : LCL197-1.p |
| Pelletier 60          | [Pel86]  | : SYN082-1.p | Problem 2.42            | [WR27]    | : LCL198-1.p |
| Pelletier 61          | [Pel86]  | : SYN083-1.p | Problem 2.43            | [WR27]    | : LCL198-1.p |
| Pelletier 62          | [Pel86]  | : SYN084-1.p | Problem 2.45            | [WR27]    | : LCL199-1.p |
| Pelletier 62          | [Pel86]  | : SYN084-2.p | Problem 2.46            | [WR27]    | : LCL200-1.p |

|               |          |              |                     |          |              |
|---------------|----------|--------------|---------------------|----------|--------------|
| Problem 2.47  | [WR27]   | : LCL201-1.p | Problem 8           | [Jec93a] | : LDA007-3.p |
| Problem 2.48  | [WR27]   | : LCL202-1.p | Problem 8           | [WM89]   | : TOP013-1.p |
| Problem 2.49  | [WR27]   | : LCL203-1.p | PROBLEM 8           | [Zha93]  | : COL003-1.p |
| Problem 2.5   | [WR27]   | : LCL204-1.p | Problem 9           | [AZ89]   | : SYN036-3.p |
| Problem 2.51  | [WR27]   | : LCL205-1.p | Problem 9           | [Jec93a] | : LDA008-1.p |
| Problem 2.52  | [WR27]   | : LCL206-1.p | Problem 9           | [WM89]   | : TOP014-1.p |
| Problem 2.521 | [WR27]   | : LCL207-1.p | Problem 9           | [Wosb]   | : GRP012-1.p |
| Problem 2.53  | [WR27]   | : LCL208-1.p | PROBLEM 9           | [Zha93]  | : RIG010-5.p |
| Problem 2.54  | [WR27]   | : LCL209-1.p | Problem 10          | [Jec93a] | : LDA009-1.p |
| Problem 2.55  | [WR27]   | : LCL210-1.p | Problem 10          | [WM89]   | : TOP015-1.p |
| Problem 2.56  | [WR27]   | : LCL211-1.p | PROBLEM 10          | [Zha93]  | : RIG011-5.p |
| Problem 2.6   | [WR27]   | : LCL212-1.p | Problem 11          | [Jec93a] | : LDA010-1.p |
| Problem 2.61  | [WR27]   | : LCL213-1.p | Problem 11          | [WM89]   | : TOP016-1.p |
| Problem 2.61  | [WR27]   | : LCL214-1.p | Problem 11          | [Wosb]   | : GRP013-1.p |
| Problem 2.62  | [WR27]   | : LCL215-1.p | Problem 12          | [Jec93a] | : LDA011-1.p |
| Problem 2.63  | [WR27]   | : LCL215-1.p | Problem 12          | [WM89]   | : TOP017-1.p |
| Problem 2.64  | [WR27]   | : LCL216-1.p | Problem 12          | [Wosb]   | : GRP032-3.p |
| Problem 2.65  | [WR27]   | : LCL217-1.p | Problem 13          | [Jec93a] | : LDA012-1.p |
| Problem 2.67  | [WR27]   | : LCL218-1.p | Problem 13          | [WM89]   | : TOP018-1.p |
| Problem 2.68  | [WR27]   | : LCL219-1.p | Problem 13          | [Wosb]   | : GRP033-3.p |
| Problem 2.69  | [WR27]   | : LCL220-1.p | Problem 13          | [Wosb]   | : GRP033-4.p |
| Problem 2.73  | [WR27]   | : LCL221-1.p | Problem 14          | [WM89]   | : TOP019-1.p |
| Problem 2.74  | [WR27]   | : LCL222-1.p | Problem 14          | [Wosb]   | : GRP034-3.p |
| Problem 2.75  | [WR27]   | : LCL223-1.p | Problem 15          | [Wosb]   | : GRP035-3.p |
| Problem 2.76  | [WR27]   | : LCL224-1.p | Problem 16          | [Wosb]   | : GRP036-3.p |
| Problem 2.77  | [WR27]   | : LCL225-1.p | Problem 17          | [LS74]   | : NUM016-1.p |
| Problem 2.8   | [WR27]   | : LCL226-1.p | Problem 17          | [Wosb]   | : GRP037-3.p |
| Problem 2.81  | [WR27]   | : LCL227-1.p | Problem 18          | [Wosb]   | : GRP038-3.p |
| Problem 2.82  | [WR27]   | : LCL228-1.p | Problem 20          | [Wosb]   | : GRP040-4.p |
| Problem 2.83  | [WR27]   | : LCL229-1.p | Problem 21          | [Wosb]   | : RIG001-5.p |
| Problem 2.85  | [WR27]   | : LCL230-1.p | Problem 22          | [Wosb]   | : RIG004-3.p |
| Problem 2.86  | [WR27]   | : LCL231-1.p | Problem 23          | [Wosb]   | : RIG005-1.p |
| Problem 3     | [Ble90]  | : ANA004-5.p | Problem 23          | [Wosb]   | : RIG005-2.p |
| Problem 3     | [Jec93a] | : LDA003-1.p | Problem 24          | [Wosb]   | : RIG037-1.p |
| Problem 3     | [LO85a]  | : RIG008-7.p | Problem 24          | [Wosb]   | : RIG037-2.p |
| Problem 3     | [WM89]   | : TOP008-1.p | Problem 25          | [Wosb]   | : RIG006-1.p |
| Problem 3     | [Wosb]   | : GRP007-1.p | Problem 25          | [Wosb]   | : RIG006-2.p |
| PROBLEM 3     | [Zha93]  | : B00002-1.p | Problem 25          | [Wosb]   | : RIG006-3.p |
| Problem 3.1   | [WR27]   | : LCL232-1.p | Problem 26          | [LS74]   | : NUM017-1.p |
| Problem 3.11  | [WR27]   | : LCL233-1.p | Problem 26          | [Smu78b] | : PUZ032-1.p |
| Problem 3.12  | [WR27]   | : LCL234-1.p | Problem 27          | [Smu78b] | : PUZ023-1.p |
| Problem 3.13  | [WR27]   | : LCL235-1.p | Problem 27          | [Wosb]   | : RIG038-1.p |
| Problem 3.14  | [WR27]   | : LCL236-1.p | Problem 27          | [Wosb]   | : RIG038-2.p |
| Problem 3.2   | [WR27]   | : LCL234-1.p | Problem 28          | [Wosb]   | : RIG039-1.p |
| Problem 3.21  | [WR27]   | : LCL237-1.p | Problem 28          | [Wosb]   | : RIG039-2.p |
| Problem 3.22  | [WR27]   | : LCL238-1.p | Problem 29          | [LS74]   | : NUM002-1.p |
| Problem 3.24  | [WR27]   | : LCL239-1.p | Problem 29          | [LS74]   | : NUM004-1.p |
| Problem 3.26  | [WR27]   | : LCL240-1.p | Problem 29          | [Wosb]   | : RIG040-1.p |
| Problem 3.27  | [WR27]   | : LCL241-1.p | Problem 29          | [Wosb]   | : RIG040-2.p |
| Problem 3.3   | [WR27]   | : LCL242-1.p | Problem 30          | [Wosb]   | : RIG041-1.p |
| Problem 3.31  | [WR27]   | : LCL243-1.p | Problem 31          | [Smu78b] | : PUZ024-1.p |
| Problem 3.33  | [WR27]   | : LCL244-1.p | Problem 32          | [Wosb]   | : SYN014-2.p |
| Problem 3.34  | [WR27]   | : LCL245-1.p | Problem 33          | [Wosb]   | : SYN015-2.p |
| Problem 3.35  | [WR27]   | : LCL246-1.p | Problem 35          | [Smu78b] | : PUZ025-1.p |
| Problem 3.37  | [WR27]   | : LCL247-1.p | Problem 39          | [Smu78b] | : PUZ026-1.p |
| Problem 3.4   | [WR27]   | : LCL248-1.p | Problem 41          | [LS74]   | : NUM019-1.p |
| Problem 3.41  | [WR27]   | : LCL249-1.p | Problem 42          | [Smu78b] | : PUZ027-1.p |
| Problem 3.42  | [WR27]   | : LCL250-1.p | Problem 76t1        | [LS74]   | : NUM025-2.p |
| Problem 3.43  | [WR27]   | : LCL251-1.p | Problem 95          | [Smu78b] | : PUZ021-1.p |
| Problem 3.44  | [WR27]   | : LCL252-1.p | Problem 221-223     | [BLM+86] | : ALG001-1.p |
| Problem 3.45  | [WR27]   | : LCL253-1.p | Problem 221-223     | [BLM+86] | : ALG001-2.p |
| Problem 3.47  | [WR27]   | : LCL254-1.p | Problem 224-225     | [BLM+86] | : GRP015-1.p |
| Problem 3.48  | [WR27]   | : LCL255-1.p | Problem 226-227     | [BLM+86] | : GRP016-1.p |
| Problem 4     | [Ble90]  | : ANA005-4.p | Problem 228-231     | [BLM+86] | : GRP001-3.p |
| Problem 4     | [Jec93a] | : LDA004-1.p | Problem 232         | [BLM+86] | : NUM008-1.p |
| Problem 4     | [LO85a]  | : GRP002-4.p | Problem 233         | [BLM+86] | : NUM009-1.p |
| Problem 4     | [WM89]   | : TOP009-1.p | Problem 234-235     | [BLM+86] | : NUM010-1.p |
| Problem 4     | [Wosb]   | : GRP008-1.p | Problem 236-237     | [BLM+86] | : NUM011-1.p |
| PROBLEM 4     | [Zha93]  | : GRP014-1.p | Problem 238-241     | [BLM+86] | : NUM012-1.p |
| Problem 5     | [Ble90]  | : ANA005-5.p | Problem 242-244     | [BLM+86] | : NUM013-1.p |
| Problem 5     | [Jec93a] | : LDA005-1.p | Problem 245         | [BLM+86] | : NUM018-1.p |
| Problem 5     | [LO85a]  | : B00002-1.p | Problem 246-248     | [BLM+86] | : NUM006-1.p |
| Problem 5     | [WM89]   | : TOP010-1.p | PROOF I             | [AH90]   | : RIG025-1.p |
| Problem 5     | [Wosb]   | : GRP031-1.p | PROOF II            | [AH90]   | : RIG034-1.p |
| PROBLEM 5     | [Zha93]  | : LCL109-2.p | PROOF III           | [AH90]   | : RIG028-2.p |
| Problem 5.1   | [Pla82]  | : MSC005-1.p | PROOF IV            | [AH90]   | : RIG027-2.p |
| Problem 5.2   | [Pla82]  | : SYN003-1.g | PROOF V             | [AH90]   | : RIG029-2.p |
| Problem 5.3   | [Pla82]  | : SYN004-1.g | PROOF VI            | [AH90]   | : RIG010-2.p |
| Problem 5.4   | [Pla82]  | : SYN005-1.g | Proposition 1a      | [Jec93b] | : COL077-1.p |
| Problem 5.5   | [Pla82]  | : PRV009-1.p | Proposition 1b      | [Jec93b] | : COL078-1.p |
| Problem 5.6   | [Pla82]  | : PUZ011-1.p | Proposition 2a      | [Jec93b] | : COL079-1.p |
| Problem 5.7   | [Pla82]  | : PLA002-1.p | Proposition 2b      | [Jec93b] | : COL080-1.p |
| Problem 5.8   | [Pla82]  | : SYN006-1.p | Proposition 2c      | [Jec93b] | : COL081-1.p |
| Problem 6     | [Jec93a] | : LDA006-1.p | PV1                 | [MOW76]  | : PRV001-1.p |
| Problem 6     | [LO85a]  | : RIG009-7.p | q1-10.lop (Size 10) | [SET]    | : PUZ034-1.g |
| Problem 6     | [WM89]   | : TOP011-1.p | q1-2.lop (Size 8)   | [SET]    | : PUZ034-1.g |
| Problem 6     | [Wosb]   | : GRP009-1.p | q1-9.lop (Size 9)   | [SET]    | : PUZ034-1.g |
| PROBLEM 6     | [Zha93]  | : COL049-1.p | Q2                  | [Qua89b] | : GEO074-2.p |
| Problem 7     | [Jec93a] | : LDA007-1.p | Q3.1                | [Qua89b] | : GEO075-2.p |
| Problem 7     | [WM89]   | : TOP012-1.p | QG1                 | [FSB93]  | : GRP123-1.g |
| Problem 7     | [Wosb]   | : GRP010-1.p | QG1                 | [Sla93]  | : GRP123-1.g |
| PROBLEM 7     | [Zha93]  | : RIG009-5.p |                     |          |              |

|             |          |              |                |           |              |
|-------------|----------|--------------|----------------|-----------|--------------|
| QG1         | [SFS95]  | : GRP123-1.g | RA-1           | [WWM+ 90] | : ROB024-1.p |
| QG1-ni      | [Sla93]  | : GRP131-1.g | RA-2           | [WWM+ 90] | : ROB025-1.p |
| QG1a        | [Sla93]  | : GRP123-6.g | ramsey1.lop    | [SET]     | : PUZ028-2.p |
| QG2         | [FSB93]  | : GRP124-1.g | ramsey3.lop    | [SET]     | : PUZ028-3.p |
| QG2         | [Sla93]  | : GRP124-1.g | ramsey3a.lop   | [SET]     | : PUZ028-4.p |
| QG2-ni      | [SFS95]  | : GRP124-1.g | RC-1           | [WWM+ 90] | : LCL119-1.p |
| QG2a        | [Sla93]  | : GRP132-1.g | RC-2           | [WWM+ 90] | : LCL168-1.p |
| QG3         | [Sla93]  | : GRP124-6.g | RE1            | [Qua92a]  | : SET515-6.p |
| QG3         | [FSB93]  | : GRP125-1.g | RE2            | [Qua92a]  | : SET516-6.p |
| QG3         | [Sla93]  | : GRP125-1.g | RE3            | [Qua92a]  | : SET517-6.p |
| QG3         | [SFS95]  | : GRP125-1.g | RE4            | [Qua92a]  | : SET518-6.p |
| QG3-ni      | [Sla93]  | : GRP133-1.g | RE5.1          | [Qua92a]  | : SET519-6.p |
| QG4         | [FSB93]  | : GRP126-1.g | RE5.2          | [Qua92a]  | : SET520-6.p |
| QG4         | [Sla93]  | : GRP126-1.g | RE6.1          | [Qua92a]  | : SET521-6.p |
| QG4         | [SFS95]  | : GRP126-1.g | RE6.2          | [Qua92a]  | : SET522-6.p |
| QG4-ni      | [Sla93]  | : GRP134-1.g | RE7            | [Qua92a]  | : SET523-6.p |
| QG5         | [FSB93]  | : GRP127-1.g | RE8.1          | [Qua92a]  | : SET524-6.p |
| QG5         | [Sla93]  | : GRP127-1.g | RE8.2          | [Qua92a]  | : SET525-6.p |
| QG5         | [SFS95]  | : GRP127-1.g | RE9.1          | [Qua92a]  | : SET526-6.p |
| QG5-ni      | [Sla93]  | : GRP135-1.g | RE9.2          | [Qua92a]  | : SET527-6.p |
| QG6         | [FSB93]  | : GRP128-1.g | RE9 cor.       | [Qua92a]  | : SET528-6.p |
| QG6         | [Sla93]  | : GRP128-1.g | RE10.1         | [Qua92a]  | : SET529-6.p |
| QG6         | [SFS95]  | : GRP128-1.g | RE10.2         | [Qua92a]  | : SET530-6.p |
| QG7         | [FSB93]  | : GRP129-1.g | RG-102         | [MW92]    | : LCL121-1.p |
| QG7         | [Sla93]  | : GRP129-1.g | RG-103         | [MW92]    | : LCL122-1.p |
| QG7         | [SFS95]  | : GRP129-1.g | RG-104         | [MW92]    | : LCL123-1.p |
| QG8         | [Sla93]  | : GRP130-1.g | RG-105         | [MW92]    | : LCL124-1.p |
| Question 1  | [Wos93]  | : COL029-1.p | RG-106         | [MW92]    | : LCL125-1.p |
| Question 2  | [Wos93]  | : COL049-1.p | RG-107         | [MW92]    | : LCL126-1.p |
| Question 3  | [Wos93]  | : COL003-1.p | RG-108         | [MW92]    | : LCL127-1.p |
| Question 4  | [Wos93]  | : COL067-1.p | RG-109         | [MW92]    | : LCL128-1.p |
| Question 5  | [Wos93]  | : COL003-1.p | RG-110         | [MW92]    | : LCL129-1.p |
| Question 5  | [Wos93]  | : COL040-1.p | RG-111         | [MW92]    | : LCL130-1.p |
| Question 5  | [Wos93]  | : COL042-1.p | RG-112         | [MW92]    | : LCL131-1.p |
| Question 5  | [Wos93]  | : COL043-1.p | RL1            | [Qua92a]  | : SET380-6.p |
| Question 5  | [Wos93]  | : COL044-1.p | RL2            | [Qua92a]  | : SET381-6.p |
| Question 5  | [Wos93]  | : COL067-1.p | RL2 cor.2      | [Qua92a]  | : SET382-6.p |
| Question 6  | [Wos93]  | : COL069-1.p | RL2 cor.2      | [Qua92d]  | : SET383-6.p |
| Question 7  | [Wos93]  | : COL047-1.p | RL3 cor.1      | [Qua92a]  | : SET384-6.p |
| Question 11 | [Wos93]  | : COL068-1.p | RL3 cor.2      | [Qua92a]  | : SET385-6.p |
| Question 12 | [Wos93]  | : COL070-1.p | RL4            | [Qua92d]  | : SET386-6.p |
| Question 13 | [Wos93]  | : COL008-1.p | ROB1           | [MRS72]   | : SYN035-1.p |
| Question 14 | [Wos93]  | : COL071-1.p | ROB1           | [WMT76]   | : SYN035-1.p |
| Question 15 | [Wos93]  | : COL005-1.p | ROB2           | [MRS72]   | : GRP001-5.p |
| Question 16 | [Wos93]  | : COL072-1.p | ROB2           | [WMT76]   | : GRP001-5.p |
| Question 17 | [Wos93]  | : COL047-1.p | Robbins        | [LM92]    | : ROB023-1.p |
| Question 18 | [Wos93]  | : COL073-1.p | robbins.in     | [OTT]     | : ROB003-1.p |
| QW          | [MRS72]  | : SYN034-1.p | robbins.occ.in | [OTT]     | : ROB005-1.p |
| QW          | [WMT76]  | : SYN034-1.p | RP1.1          | [Qua92a]  | : SET477-6.p |
| R1          | [MOW76]  | : RIG001-1.p | RP1.2          | [Qua92a]  | : SET478-6.p |
| R1          | [MOW76]  | : RIG001-4.p | RP2.1          | [Qua92a]  | : SET479-6.p |
| R2          | [MOW76]  | : RIG004-1.p | RP2.2          | [Qua92a]  | : SET480-6.p |
| R2          | [MOW76]  | : RIG004-2.p | RP3            | [Qua92a]  | : SET481-6.p |
| R2.1        | [Qua89b] | : GE0054-3.p | RP4            | [Qua92a]  | : SET482-6.p |
| R2.2        | [Qua89b] | : GE0055-3.p | RP5            | [Qua92a]  | : SET483-6.p |
| R3          | [MOW76]  | : RIG008-2.p | RP6            | [Qua92a]  | : SET484-6.p |
| R3.1        | [Qua89b] | : GE0056-3.p | RP7            | [Qua92a]  | : SET485-6.p |
| R3.2        | [Qua89b] | : GE0057-3.p | RP8            | [Qua92a]  | : SET486-6.p |
| R4          | [Qua89b] | : GE0058-3.p | RP9            | [Qua92a]  | : SET487-6.p |
| R5          | [Qua89b] | : GE0059-3.p | RP10           | [Qua92a]  | : SET488-6.p |
| R6          | [Qua89b] | : GE0060-2.p | RP11.1         | [Qua92a]  | : SET489-6.p |
| R-85        | [MW92]   | : LCL117-1.p | RP11.2         | [Qua92a]  | : SET490-6.p |
| R-86        | [MW92]   | : LCL118-1.p | RS0            | [Qua92d]  | : SET237-6.p |
| R-87        | [MW92]   | : LCL119-1.p | RS0 cor.       | [Qua92d]  | : SET238-6.p |
| R-88        | [MW92]   | : LCL120-1.p | RS1            | [Qua92a]  | : SET239-6.p |
| RA1         | [LW92]   | : ROB003-1.p | RS2            | [Qua92a]  | : SET240-6.p |
| RA1.1       | [Qua92a] | : SET302-6.p | RS3            | [Qua92a]  | : SET241-6.p |
| RA1.2       | [Qua92a] | : SET303-6.p | RS4            | [Qua92a]  | : SET242-6.p |
| RA1.3       | [Qua92a] | : SET304-6.p | RS5            | [Qua92a]  | : SET243-6.p |
| RA2         | [LW92]   | : ROB010-1.p | RS6.1          | [Qua92a]  | : SET244-6.p |
| RA2.1       | [Qua92a] | : SET305-6.p | RS6.2          | [Qua92a]  | : SET245-6.p |
| RA2.2       | [Qua92a] | : SET306-6.p | RS6.3          | [Qua92a]  | : SET246-6.p |
| RA3         | [LW92]   | : ROB005-1.p | RS6.4          | [Qua92a]  | : SET247-6.p |
| RA3         | [Qua92a] | : SET307-6.p | RS7            | [Qua92a]  | : SET248-6.p |
| RA3 cor.1   | [Qua92a] | : SET308-6.p | RS8            | [Qua92a]  | : SET249-6.p |
| RA3 cor.2   | [Qua92a] | : SET309-6.p | RS8 cor.       | [Qua92a]  | : SET250-6.p |
| RA3 cor.3   | [Qua92a] | : SET310-6.p | RS9.1          | [Qua92a]  | : SET251-6.p |
| RA4         | [LW92]   | : ROB006-1.p | RS10.1         | [Qua92a]  | : SET252-6.p |
| RA4         | [Qua92a] | : SET311-6.p | RS10.2         | [Qua92a]  | : SET253-6.p |
| RA5         | [LW92]   | : ROB007-1.p | RS11.1         | [Qua92a]  | : SET254-6.p |
| RA5         | [Qua92a] | : SET312-6.p | RS11.2         | [Qua92a]  | : SET255-6.p |
| RA6         | [Qua92a] | : SET313-6.p | RS11.3         | [Qua92a]  | : SET256-6.p |
| RA7         | [Qua92a] | : SET314-6.p | RS12           | [Qua92a]  | : SET257-6.p |
| RA7 cor.    | [Qua92a] | : SET315-6.p | RT1            | [LW91]    | : RIG008-7.p |
| RA8         | [Qua92a] | : SET316-6.p | RT2            | [LW91]    | : RIG009-7.p |
| RA8 cor.1   | [Qua92a] | : SET317-6.p | RT3            | [LW91]    | : RIG035-7.p |
| RA8 cor.2   | [Qua92a] | : SET318-6.p | RT4            | [LW91]    | : RIG036-7.p |
| RA8 cor.3   | [Qua92a] | : SET319-6.p | S1             | [MOW76]   | : SET012-1.p |
| RA8 cor.4   | [Qua92a] | : SET320-6.p | S1n            | [Pfe88]   | : LCL082-1.p |
| RA9.1       | [Qua92a] | : SET321-6.p | S2             | [Pla94]   | : SYN085-1.g |
| RA9.2       | [Qua92a] | : SET322-6.p | S2n            | [MOW76]   | : SET013-1.p |
| RA10        | [Qua92d] | : SET323-6.p |                | [Pla94]   | : SYN086-1.g |

|                               |                       |              |                       |          |              |
|-------------------------------|-----------------------|--------------|-----------------------|----------|--------------|
| S3                            | [MOW76]               | : SET015-1.p | SP10.1                | [Qua92a] | : SET511-6.p |
| S3n                           | [Pla94]               | : SYN087-1.g | SP10.2                | [Qua92a] | : SET512-6.p |
| S4                            | [MOW76]               | : SET014-2.p | SP10.3                | [Qua92a] | : SET513-6.p |
| S4n                           | [Pla94]               | : SYN088-1.g | SP11                  | [Qua92a] | : SET514-6.p |
| Sages and Combinatory Logic   | [Wos88]               | : COL003-1.p | SR1                   | [Qua92a] | : SET451-6.p |
| Salt and Mustard Problem      | [LO85a]               | : PUZ030-1.p | SR2                   | [Qua92a] | : SET452-6.p |
| Salt-and-Mustard Problem      | [MB88]                | : PUZ030-1.p | SR3                   | [Qua92a] | : SET453-6.p |
| salt.in                       | [OTT]                 | : PUZ030-2.p | SS1                   | [Qua92a] | : SET077-7.p |
| SAM's lemma                   | [LM92]                | : LAT005-2.p | SS1 cor.              | [Qua92d] | : SET078-7.p |
| SAM's lemma                   | [MOW76]               | : LAT005-1.p | SS2                   | [Qua92a] | : SET024-7.p |
| SAM's lemma                   | [McC88]               | : LAT005-3.p | SS2 cor.              | [Qua92a] | : SET079-6.p |
| SAM's lemma                   | [Wos88]               | : LAT005-4.p | SS2 cor.1             | [Qua92a] | : SET079-7.p |
| SAM's lemma                   | [Wos88]               | : LAT005-6.p | SS2 cor.2             | [Qua92d] | : SET080-7.p |
| sam.in                        | [OTT]                 | : LAT005-2.p | SS3                   | [Qua92a] | : SET081-7.p |
| SAMslemma.ver1.in             | [ANL]                 | : LAT005-1.p | SS4                   | [Qua92a] | : SET082-7.p |
| SAMslemma.ver1.in             | [ANL]                 | : LAT005-5.p | SS5.1                 | [Qua92a] | : SET083-7.p |
| sam_hyp.in                    | [OTT]                 | : LAT005-2.p | SS5.2                 | [Qua92a] | : SET084-7.p |
| sax1.in                       | [OTT]                 | : GRP058-1.p | SS5.5                 | [Qua92d] | : SET085-7.p |
| sax2.in                       | [OTT]                 | : GRP064-1.p | SS6.1                 | [Qua92a] | : SET086-7.p |
| SB2.1                         | [Qua92a]              | : SET123-6.p | SS6.2                 | [Qua92a] | : SET087-7.p |
| SB2.2                         | [Qua92d]              | : SET124-6.p | SS6.3                 | [Qua92a] | : SET088-7.p |
| SB2.3                         | [Qua92d]              | : SET125-6.p | SS6.4                 | [Qua92a] | : SET089-7.p |
| SB3                           | [Qua92d]              | : SET126-6.p | SS7                   | [Qua92a] | : SET090-7.p |
| SB4                           | [Qua92d]              | : SET127-6.p | SS8.1                 | [Qua92a] | : SET091-7.p |
| SB5.1                         | [Qua92d]              | : SET128-6.p | SS8.2                 | [Qua92a] | : SET092-7.p |
| SB5.10                        | [Qua92d]              | : SET137-6.p | SS9                   | [Qua92a] | : SET093-7.p |
| SB5.11                        | [Qua92d]              | : SET138-6.p | SS10                  | [Qua92a] | : SET094-6.p |
| SB5.2                         | [Qua92d]              | : SET129-6.p | SS10                  | [Qua92a] | : SET094-7.p |
| SB5.3                         | [Qua92d]              | : SET130-6.p | SS11                  | [Qua92a] | : SET095-6.p |
| SB5.4                         | [Qua92d]              | : SET131-6.p | SS11                  | [Qua92a] | : SET095-7.p |
| SB5.5                         | [Qua92d]              | : SET132-6.p | SS12                  | [Qua92a] | : SET096-6.p |
| SB5.6                         | [Qua92d]              | : SET133-6.p | SS12                  | [Qua92a] | : SET096-7.p |
| SB5.7                         | [Qua92d]              | : SET134-6.p | SS13                  | [Qua92a] | : SET097-6.p |
| SB5.8                         | [Qua92d]              | : SET135-6.p | SS13                  | [Qua92a] | : SET097-7.p |
| SB5.9                         | [Qua92d]              | : SET136-6.p | SS13                  | [Qua92a] | : SET099-6.p |
| SB6.1                         | [Qua92d]              | : SET139-6.p | SS13 cor.             | [Qua92a] | : SET098-6.p |
| SB6.2                         | [Qua92d]              | : SET140-6.p | SS13 cor.1            | [Qua92a] | : SET098-7.p |
| SB6.3                         | [Qua92d]              | : SET141-6.p | SS13 cor.2            | [Qua92a] | : SET099-7.p |
| SB7                           | [Qua92d]              | : SET142-6.p | SS14                  | [Qua92d] | : SET100-7.p |
| SC1.1                         | [Qua92a]              | : SET344-6.p | SST                   | [WB87]   | : PUZ031-1.p |
| SC1.2                         | [Qua92a]              | : SET345-6.p | stage1.in & stage2.in | [OTT]    | : COL025-1.p |
| SC2                           | [Qua92a]              | : SET346-6.p | steam.in              | [OTT]    | : PUZ031-1.p |
| SC3.1                         | [Qua92a]              | : SET347-6.p | steamroller.ver1.in   | [ANL]    | : PUZ031-1.p |
| SC3.2                         | [Qua92a]              | : SET348-6.p | SU1                   | [Qua92a] | : SET183-6.p |
| SC3.3                         | [Qua92a]              | : SET349-6.p | SU2                   | [Qua92a] | : SET184-6.p |
| SC3.4                         | [Qua92d]              | : SET350-6.p | SU3                   | [Qua92a] | : SET185-6.p |
| SC4                           | [Qua92a]              | : SET351-6.p | SU4                   | [Qua92a] | : SET186-6.p |
| SC5                           | [Qua92a]              | : SET352-6.p | SU5                   | [Qua92a] | : SET187-6.p |
| SC5 cor.                      | [Qua92a]              | : SET353-6.p | SU6                   | [Qua92a] | : SET188-6.p |
| SC6                           | [Qua92a]              | : SET354-6.p | SU6 cor.              | [Qua92d] | : SET189-6.p |
| SC7                           | [Qua92a]              | : SET355-6.p | SU7                   | [Qua92a] | : SET190-6.p |
| SC7 cor.                      | [Qua92a]              | : SET356-6.p | SU8                   | [Qua92a] | : SET191-6.p |
| SC8                           | [Qua92a]              | : SET357-6.p | SU9                   | [Qua92a] | : SET192-6.p |
| SC9                           | [Qua92a]              | : SET358-6.p | SU10                  | [Qua92a] | : SET193-6.p |
| SC10                          | [Qua92a]              | : SET359-6.p | subgroup.in           | [OTT]    | : GRP039-6.p |
| SC11.1                        | [Qua92a]              | : SET360-6.p | Subgroups of Index 2  | [Wos88]  | : GRP039-4.p |
| SC11.2                        | [Qua92a]              | : SET361-6.p | subset.ver1.in        | [ANL]    | : SET014-2.p |
| SC12                          | [Qua92d]              | : SET362-6.p | subset.ver2.in        | [ANL]    | : SET014-4.p |
| School Boys                   | [LO85a]               | : PUZ014-1.p | SUC1.1                | [Qua92d] | : NUM140-1.p |
| SE1                           | [Qua92d]              | : NUM089-1.p | SUC1.2                | [Qua92d] | : NUM141-1.p |
| SE1 cor                       | [Qua92d]              | : NUM090-1.p | SUC1.3                | [Qua92d] | : NUM142-1.p |
| SE2                           | [Qua92d]              | : NUM091-1.p | SUC1 cor.             | [Qua92d] | : NUM143-1.p |
| SE2 cor. 1                    | [Qua92d]              | : NUM092-1.p | SUC2                  | [Qua92d] | : NUM144-1.p |
| SE2 cor. 2                    | [Qua92d]              | : NUM093-1.p | SUC2 cor.             | [Qua92d] | : NUM145-1.p |
| SE3.1                         | [Qua92d]              | : NUM094-1.p | SUC3                  | [Qua92d] | : NUM146-1.p |
| SE3.2                         | [Qua92d]              | : NUM095-1.p | SUC4                  | [Qua92d] | : NUM147-1.p |
| SE4                           | [Qua92d]              | : NUM096-1.p | SUC5                  | [Qua92d] | : NUM148-1.p |
| SE4 cor.                      | [Qua92d]              | : NUM097-1.p | SUC6                  | [Qua92d] | : NUM149-1.p |
| SG1                           | [Qua92d]              | : NUM057-1.p | SUC6 cor. 1           | [Qua92d] | : NUM150-1.p |
| SG2                           | [Qua92d]              | : NUM058-1.p | SUC6 cor. 2           | [Qua92d] | : NUM151-1.p |
| SG3                           | [Qua92d]              | : NUM059-1.p | SUC6 cor. 3           | [Qua92d] | : NUM152-1.p |
| SG4.1                         | [Qua92d]              | : NUM060-1.p | SUC6 cor. 4           | [Qua92d] | : NUM153-1.p |
| SG4.2                         | [Qua92d]              | : NUM061-1.p | SUC6 cor. 5           | [Qua92d] | : NUM154-1.p |
| SG5                           | [Qua92d]              | : NUM062-1.p | SUC7                  | [Qua92d] | : NUM155-1.p |
| SG6                           | [Qua92d]              | : NUM063-1.p | SUC9.1                | [Qua92d] | : NUM156-1.p |
| SHORTBURST                    | [RRY <sup>+</sup> 72] | : COM001-1.p | SUC9.2                | [Qua92d] | : NUM157-1.p |
| SHORTBURST                    | [WM76]                | : COM001-1.p | SUC9.3                | [Qua92d] | : NUM158-1.p |
| Simple Theorem on Betweenness | [Wos88]               | : GE0002-4.p | SUC9.4                | [Qua92d] | : NUM159-1.p |
| SP1                           | [Qua92a]              | : SET060-7.p | SUC10                 | [Qua92d] | : NUM160-1.p |
| SP2                           | [Qua92a]              | : SET061-7.p | SUC10 cor.            | [Qua92d] | : NUM161-1.p |
| SP3                           | [Qua92a]              | : SET062-7.p | SUC11                 | [Qua92d] | : NUM162-1.p |
| SP3 cor.                      | [Qua92a]              | : SET063-7.p | SUC12.1               | [Qua92d] | : NUM163-1.p |
| SP4                           | [Qua92a]              | : SET064-7.p | SUC12.2               | [Qua92d] | : NUM164-1.p |
| SP5                           | [Qua92a]              | : SET065-7.p | SUC13.1               | [Qua92d] | : NUM165-1.p |
| SP6                           | [Qua92a]              | : SET503-6.p | SUC13.2               | [Qua92d] | : NUM166-1.p |
| SP6 cor.1                     | [Qua92a]              | : SET504-6.p | SUC14                 | [Qua92d] | : NUM167-1.p |
| SP6 cor.2                     | [Qua92a]              | : SET505-6.p | SUC14 cor.            | [Qua92d] | : NUM168-1.p |
| SP7.1                         | [Qua92a]              | : SET506-6.p | SUC15.1               | [Qua92d] | : NUM169-1.p |
| SP7.2                         | [Qua92a]              | : SET507-6.p | SUC15.2               | [Qua92d] | : NUM170-1.p |
| SP8.1                         | [Qua92a]              | : SET508-6.p | SUC15.3               | [Qua92d] | : NUM171-1.p |
| SP8.2                         | [Qua92a]              | : SET509-6.p | SUC16                 | [Qua92d] | : NUM172-1.p |
| SP9                           | [Qua92a]              | : SET510-6.p | SUC17                 | [Qua92d] | : NUM173-1.p |

|                         |          |              |                 |          |              |
|-------------------------|----------|--------------|-----------------|----------|--------------|
| SUC18                   | [Qua92d] | : NUM174-1.p | Test Problem 11 | [Wos88]  | : GEO073-1.p |
| SUC19                   | [Qua92d] | : NUM175-1.p | Test Problem 12 | [Wos88]  | : LAT005-4.p |
| SUC20                   | [Qua92d] | : NUM176-1.p | Test Problem 13 | [Wos88]  | : LAT005-6.p |
| SUC21.1                 | [Qua92d] | : NUM177-1.p | Test Problem 15 | [Wos88]  | : B00002-2.p |
| SUC21.2                 | [Qua92d] | : NUM178-1.p | Test Problem 16 | [Wos88]  | : ALG001-2.p |
| SUC21.3                 | [Qua92d] | : NUM179-1.p | Test Problem 17 | [Wos88]  | : LCL024-1.p |
| SV1                     | [Qua92a] | : SET425-6.p | Test Problem 2  | [Wos88]  | : COL003-1.p |
| SV3.1                   | [Qua92a] | : SET426-6.p | Test Problem 2  | [Wos88]  | : GRP002-1.p |
| SV3.2                   | [Qua92a] | : SET427-6.p | Test Problem 7  | [Wos88]  | : GRP002-4.p |
| SV3.3                   | [Qua92a] | : SET428-6.p | Test Problem 8  | [Wos88]  | : GRP113-1.p |
| SV4                     | [Qua92a] | : SET429-6.p | Test Problem 8  | [Wos88]  | : RIG008-1.p |
| SV5                     | [Qua92a] | : SET430-6.p | Test Problem 8  | [Wos88]  | : RIG008-7.p |
| SV6                     | [Qua92a] | : SET431-6.p | TF              | [Ver94]  | : B00012-4.p |
| SY1                     | [Qua92d] | : NUM028-1.p | TG              | [Ver94]  | : B00011-4.p |
| SY2                     | [Qua92d] | : NUM029-1.p | TG              | [Ver94]  | : B00018-4.p |
| SY3                     | [Qua92d] | : NUM030-1.p | TH              | [Ver94]  | : B00014-4.p |
| SY4                     | [Qua92d] | : NUM031-1.p | TH              | [Ver94]  | : B00015-4.p |
| SY5                     | [Qua92d] | : NUM032-1.p | THEOREM (Levi)  | [ML92]   | : GRP024-4.p |
| SY6                     | [Qua92d] | : NUM033-1.p | Theorem A       | [Qua90]  | : SYN036-4.p |
| SY7                     | [Qua92d] | : NUM034-1.p | THEOREM EQ-1    | [LM93]   | : GRP002-3.p |
| SY8                     | [Qua92d] | : NUM035-1.p | THEOREM EQ-10   | [LM93]   | : RIG011-5.p |
| SY9                     | [Qua92d] | : NUM036-1.p | THEOREM EQ-2    | [LM93]   | : ROB005-1.p |
| SY10.1                  | [Qua92d] | : NUM037-1.p | THEOREM EQ-3    | [LM93]   | : B00002-1.p |
| SY10.2                  | [Qua92d] | : NUM038-1.p | THEOREM EQ-4    | [LM93]   | : GRP014-1.p |
| Sym(M(T2n))             | [Pla94]  | : SYN099-1.g | THEOREM EQ-5    | [LM93]   | : LCL109-2.p |
| Sym(M(T3n))             | [Pla94]  | : SYN100-1.g | THEOREM EQ-6    | [LM93]   | : COL049-1.p |
| Sym(S2n)                | [Pla94]  | : SYN091-1.g | THEOREM EQ-7    | [LM93]   | : RIG009-5.p |
| Sym(S3n)                | [Pla94]  | : SYN092-1.g | THEOREM EQ-8    | [LM93]   | : COL003-1.p |
| Sym(U(T2n))             | [Pla94]  | : SYN097-1.g | THEOREM EQ-9    | [LM93]   | : RIG010-5.p |
| Sym(U(T3n))             | [Pla94]  | : SYN098-1.g | Theorem P       | [Qua90]  | : SYN037-2.p |
| Symmetry of Betweenness | [Wos88]  | : GEO001-4.p | THEOREM 1       | [LM93]   | : GRP001-1.p |
| T1                      | [MOW76]  | : GEO001-1.p | Theorem 1       | [OMW76]  | : GRP002-1.p |
| T1                      | [Qua89b] | : GEO001-3.p | Theorem 1.1     | [Win90]  | : ROB006-1.p |
| t1.ver1.in              | [ANL]    | : GEO001-1.p | Theorem 1.1     | [Win90]  | : ROB006-2.p |
| T2                      | [MOW76]  | : GEO002-1.p | Theorem 1.1     | [Win90]  | : ROB006-3.p |
| T2                      | [Qua89b] | : GEO002-3.p | Theorem 1.2     | [Win90]  | : ROB007-1.p |
| t2.ver1.in              | [ANL]    | : GEO002-1.p | Theorem 1.2     | [Win90]  | : ROB007-2.p |
| T2n                     | [Pla94]  | : SYN089-1.g | Theorem 1.2     | [Win90]  | : ROB007-3.p |
| T3                      | [MOW76]  | : GEO003-1.p | Theorem 1.2     | [Win90]  | : ROB007-4.p |
| T3                      | [Qua89b] | : GEO003-3.p | THEOREM 2       | [LM93]   | : GRP002-1.p |
| t3.ver1.in              | [ANL]    | : GEO003-1.p | Theorem 2       | [OMW76]  | : RIG008-2.p |
| T3n                     | [Pla94]  | : SYN090-1.g | THEOREM 3       | [LM93]   | : RIG008-6.p |
| T4                      | [MOW76]  | : GEO004-1.p | Theorem 3       | [OMW76]  | : GRP039-4.p |
| T4                      | [Qua89b] | : GEO004-2.p | THEOREM 4       | [LM93]   | : LCL024-1.p |
| t4.ver1.in              | [ANL]    | : GEO004-1.p | Theorem 4       | [OMW76]  | : B00008-1.p |
| T5                      | [MOW76]  | : GEO005-1.p | THEOREM 5       | [LM93]   | : LCL038-1.p |
| T5                      | [Qua89b] | : GEO005-2.p | Theorem 5       | [OMW76]  | : GEO001-1.p |
| t5.ver1.in              | [ANL]    | : GEO005-1.p | THEOREM 6       | [LM93]   | : LCL111-1.p |
| T6                      | [MOW76]  | : GEO006-1.p | THEOREM 7       | [LM93]   | : LCL114-1.p |
| T6                      | [Qua89b] | : GEO006-3.p | Third problem   | [Bon91]  | : LCL165-1.p |
| t6.ver1.in              | [ANL]    | : GEO006-1.p | TO1             | [Qua92d] | : NUM052-1.p |
| T7                      | [MOW76]  | : GEO007-1.p | TO2             | [Qua92d] | : NUM053-1.p |
| T7                      | [Qua89b] | : GEO007-3.p | TR1             | [Qua92d] | : NUM083-1.p |
| t7.ver1.in              | [ANL]    | : GEO007-1.p | TR2             | [Qua92d] | : NUM084-1.p |
| T8                      | [MOW76]  | : GEO008-1.p | TR3             | [Qua92d] | : NUM085-1.p |
| T8                      | [Qua89b] | : GEO008-3.p | TR4             | [Qua92d] | : NUM086-1.p |
| t8.ver1.in              | [ANL]    | : GEO008-1.p | TR5             | [Qua92d] | : NUM087-1.p |
| T9                      | [MOW76]  | : GEO009-1.p | TR6             | [Qua92d] | : NUM088-1.p |
| T9                      | [Qua89b] | : GEO009-3.p | TREC2           | [Qua92d] | : NUM218-1.p |
| t9.ver1.in              | [ANL]    | : GEO009-1.p | TREC3           | [Qua92d] | : NUM219-1.p |
| T10                     | [MOW76]  | : GEO010-1.p | TREC3-5         | [Qua92d] | : NUM221-1.p |
| T10                     | [Qua89b] | : GEO010-3.p | TREC3-7         | [Qua92d] | : NUM222-1.p |
| t10.ver1.in             | [ANL]    | : GEO010-1.p | TREC3-9.1       | [Qua92d] | : NUM223-1.p |
| T11                     | [MOW76]  | : GEO011-1.p | TREC3-9.2       | [Qua92d] | : NUM224-1.p |
| T11                     | [Qua89b] | : GEO011-3.p | TREC3-9.3       | [Qua92d] | : NUM225-1.p |
| t11.ver1.in             | [ANL]    | : GEO011-1.p | TREC3-9.4       | [Qua92d] | : NUM226-1.p |
| t11.ver2.in             | [ANL]    | : GEO011-5.p | TREC3-9.5       | [Qua92d] | : NUM227-1.p |
| T12                     | [MOW76]  | : GEO012-1.p | TREC3 cor.      | [Qua92d] | : NUM220-1.p |
| T12                     | [Qua89b] | : GEO012-3.p | TREC5.1         | [Qua92d] | : NUM245-2.p |
| t12.ver1.in             | [ANL]    | : GEO012-1.p | TREC5.2         | [Qua92d] | : NUM246-2.p |
| T13                     | [MOW76]  | : GEO013-1.p | TREC6           | [Qua92d] | : NUM247-2.p |
| T13                     | [Qua89b] | : GEO013-3.p | TREC7           | [Qua92d] | : NUM248-2.p |
| t13.ver1.in             | [ANL]    | : GEO013-1.p | TREC7-5         | [Qua92d] | : NUM249-2.p |
| TA                      | [Ver94]  | : B00003-4.p | TREC8           | [Qua92d] | : NUM250-2.p |
| TA                      | [Ver94]  | : B00004-4.p | TREC9           | [Qua92d] | : NUM251-2.p |
| tand127.ver1.in         | [ANL]    | : PUZ023-1.p | TREC10          | [Qua92d] | : NUM252-2.p |
| tand131.ver1.in         | [ANL]    | : PUZ024-1.p | TREC11          | [Qua92d] | : NUM253-2.p |
| tand135.ver1.in         | [ANL]    | : PUZ025-1.p | TREC12          | [Qua92d] | : NUM254-2.p |
| tand139.ver1.in         | [ANL]    | : PUZ026-1.p | TREC13          | [Qua92d] | : NUM255-2.p |
| tand142.ver1.in         | [ANL]    | : PUZ027-1.p | TREC14          | [Qua92d] | : NUM256-2.p |
| tand1.ver1.in           | [ANL]    | : PUZ032-1.p | TREC15          | [Qua92d] | : NUM257-2.p |
| TB                      | [Ver94]  | : B00005-4.p | TREC16          | [Qua92d] | : NUM258-2.p |
| TB                      | [Ver94]  | : B00006-4.p | TREC17          | [Qua92d] | : NUM259-2.p |
| tba_gg.in               | [OTT]    | : B00001-1.p | TREC18.1        | [Qua92d] | : NUM260-2.p |
| TC                      | [Ver94]  | : B00009-4.p | TREC18.2        | [Qua92d] | : NUM261-2.p |
| TC                      | [Ver94]  | : B00010-4.p | TREC18.3        | [Qua92d] | : NUM262-2.p |
| TD                      | [Ver94]  | : B00007-4.p | TREC18.4        | [Qua92d] | : NUM263-2.p |
| TD                      | [Ver94]  | : B00008-4.p | TREC18.5        | [Qua92d] | : NUM264-2.p |
| TE                      | [Ver94]  | : B00013-4.p | TREC.LEMMA0     | [Qua92d] | : NUM229-1.p |
| Teichmuller Identity    | [Ste87]  | : RIG026-6.p | TREC.LEMMA1     | [Qua92d] | : NUM230-1.p |
| Test Problem 1          | [Wos88]  | : GRP039-4.p | TREC.LEMMA2     | [Qua92d] | : NUM231-1.p |
| Test Problem 10         | [Wos88]  | : GEO008-1.p | TREC.LEMMA3     | [Qua92d] | : NUM232-1.p |

|                             |          |              |                                |          |              |
|-----------------------------|----------|--------------|--------------------------------|----------|--------------|
| TREC.LEMMA4                 | [Qua92d] | : NUM233-1.p | wos2                           | [WM76]   | : GRP030-1.p |
| TREC.LEMMA5                 | [Qua92d] | : NUM234-1.p | wos3                           | [WM76]   | : GRP007-1.p |
| TREC.LEMMA6                 | [Qua92d] | : NUM235-1.p | wos4                           | [WM76]   | : GRP008-1.p |
| TREC.LEMMA6 cor.1           | [Qua92d] | : NUM236-1.p | wos5                           | [WM76]   | : GRP031-1.p |
| TREC.LEMMA6 cor.2           | [Qua92d] | : NUM237-1.p | wos6                           | [WM76]   | : GRP009-1.p |
| TREC.LEMMA7                 | [Qua92d] | : NUM238-1.p | wos7                           | [WM76]   | : GRP010-1.p |
| TREC.LEMMA8                 | [Qua92d] | : NUM239-1.p | wos8                           | [WM76]   | : GRP022-1.p |
| TREC.LEMMA9.1               | [Qua92d] | : NUM240-1.p | wos9                           | [WM76]   | : GRP012-1.p |
| TREC.LEMMA9.2               | [Qua92d] | : NUM241-1.p | wos10                          | [WM76]   | : GRP001-1.p |
| TREC.LEMMA9.3               | [Qua92d] | : NUM242-1.p | wos11                          | [WM76]   | : GRP013-1.p |
| TREC.LEMMA10                | [Qua92d] | : NUM243-1.p | wos12                          | [WM76]   | : GRP032-3.p |
| TREC.LEMMA11                | [Qua92d] | : NUM244-1.p | wos13                          | [WM76]   | : GRP033-3.p |
| TRECDEF1 cor.1              | [Qua92d] | : NUM216-1.p | wos14                          | [WM76]   | : GRP034-3.p |
| TRECDEF1 cor.2              | [Qua92d] | : NUM217-1.p | wos15                          | [WM76]   | : GRP035-3.p |
| TRECDEF4 cor.               | [Qua92d] | : NUM228-1.p | wos16                          | [WM76]   | : GRP036-3.p |
| Truth-tellers and the Liars | [LO85a]  | : PUZ032-1.p | wos17                          | [WM76]   | : GRP037-3.p |
| two.inverter.val.ver1.in    | [ANL]    | : CIV002-1.p | wos18                          | [WM76]   | : GRP038-3.p |
| two.inverter.ver1.in        | [ANL]    | : CID003-1.p | wos19                          | [WM76]   | : GRP039-3.p |
| two.inverter.ver2.in        | [ANL]    | : CID003-2.p | wos20                          | [WM76]   | : GRP040-4.p |
| U1                          | [Qua92a] | : SET159-6.p | wos21                          | [WM76]   | : RIG001-5.p |
| U2                          | [Qua92a] | : SET160-6.p | wos22                          | [WM76]   | : RIG004-3.p |
| U3                          | [Qua92a] | : SET161-6.p | wos23                          | [WM76]   | : RIG005-2.p |
| U4                          | [Qua92a] | : SET162-6.p | wos24                          | [WM76]   | : RIG037-2.p |
| U5                          | [Qua92a] | : SET163-6.p | wos25                          | [WM76]   | : RIG006-2.p |
| U6                          | [Qua92a] | : SET164-6.p | wos26                          | [WM76]   | : NUM017-1.p |
| U6 cor.                     | [Qua92a] | : SET165-6.p | wos27                          | [WM76]   | : RIG038-2.p |
| U7.1                        | [Qua92a] | : SET166-6.p | wos28                          | [WM76]   | : RIG039-2.p |
| U7.2                        | [Qua92a] | : SET167-6.p | wos29                          | [WM76]   | : RIG040-2.p |
| U7.3                        | [Qua92a] | : SET168-6.p | wos30                          | [WM76]   | : RIG041-1.p |
| U(T2n)                      | [Pla94]  | : SYN093-1.g | wos31                          | [WM76]   | : SYN013-1.p |
| U(T3n)                      | [Pla94]  | : SYN094-1.g | wos32                          | [WM76]   | : SYN014-2.p |
| union.ver1.in               | [ANL]    | : SET015-2.p | wos33                          | [WM76]   | : SYN015-2.p |
| union.ver2.in               | [ANL]    | : SET015-4.p | wos.nie                        | [SPR]    | : GRP034-3.p |
| UP1                         | [Qua92a] | : SET066-7.p | x2_quant.in                    | [OTT]    | : GRP001-4.p |
| UP2.1                       | [Qua92a] | : SET067-7.p | XGK and Equivalential Calculus | [Wos88]  | : LCL024-1.p |
| UP2.2                       | [Qua92a] | : SET068-7.p | xsquared.ver1.in               | [ANL]    | : GRP001-1.p |
| UP2.3                       | [Qua92a] | : SET069-7.p | xsquared.ver2.in               | [ANL]    | : GRP001-2.p |
| UP2.4                       | [Qua92a] | : SET070-7.p | zero.ver1.in                   | [ANL]    | : RIG001-1.p |
| UP3                         | [Qua92a] | : SET071-7.p | -                              | [ANL]    | : GRP012-3.p |
| UP4                         | [Qua92a] | : SET071-7.p | -                              | [ANL]    | : GRP012-4.p |
| UP5                         | [Qua92a] | : SET072-7.p | -                              | [Bon91]  | : LCL109-3.p |
| UP6.1                       | [Qua92a] | : SET073-6.p | -                              | [Bru91]  | : COM003-2.p |
| UP6.1                       | [Qua92a] | : SET073-7.p | -                              | [Bur87a] | : COM003-1.p |
| UP6.2                       | [Qua92a] | : SET074-6.p | -                              | [Fer94]  | : SYN313-1.g |
| UP6.2                       | [Qua92a] | : SET074-7.p | -                              | [Fer94]  | : SYN314-1.g |
| UP6 cor.                    | [Qua92d] | : SET075-7.p | -                              | [GO86]   | : COL058-1.p |
| UP7                         | [Qua92a] | : SET076-7.p | -                              | [GO86]   | : COL058-2.p |
| v1.lop                      | [SET]    | : PRV002-1.p | -                              | [GO86]   | : COL058-3.p |
| v2.lop                      | [SET]    | : PRV003-1.p | -                              | [GO86]   | : COL059-1.p |
| v3.lop                      | [SET]    | : PRV004-1.p | -                              | [Jec93b] | : COL074-1.p |
| v4.lop                      | [SET]    | : PRV005-1.p | -                              | [Jec93b] | : COL074-2.p |
| v5.lop                      | [SET]    | : PRV006-1.p | -                              | [Jec93b] | : COL074-3.p |
| v6.lop                      | [SET]    | : PRV007-1.p | -                              | [Jec93b] | : COL075-1.p |
| v7.lop                      | [SET]    | : PRV008-1.p | -                              | [Jec93b] | : COL075-2.p |
| W axiom 1                   | [Bon91]  | : LCL161-1.p | -                              | [Jec93b] | : COL076-1.p |
| W axiom 2                   | [Bon91]  | : LCL162-1.p | -                              | [Jec93b] | : COL076-2.p |
| W axiom 3                   | [Bon91]  | : LCL163-1.p | -                              | [MB88]   | : PUZ001-3.p |
| W axiom 4                   | [Bon91]  | : LCL164-1.p | -                              | [MW88]   | : COL007-1.p |
| W1                          | [Qua89b] | : GEO070-3.p | -                              | [MW88]   | : COL008-1.p |
| W2.1                        | [Qua89b] | : GEO071-3.p | -                              | [MW88]   | : COL009-1.p |
| W2.2                        | [Qua89b] | : GEO072-3.p | -                              | [MW88]   | : COL010-1.p |
| W3                          | [Qua89b] | : GEO073-3.p | -                              | [MW88]   | : COL011-1.p |
| W' axiom 1                  | [Bon91]  | : LCL153-1.p | -                              | [MW88]   | : COL012-1.p |
| W' axiom 2                  | [Bon91]  | : LCL154-1.p | -                              | [MW88]   | : COL013-1.p |
| W' axiom 3                  | [Bon91]  | : LCL155-1.p | -                              | [MW88]   | : COL014-1.p |
| W' axiom 4                  | [Bon91]  | : LCL156-1.p | -                              | [MW88]   | : COL015-1.p |
| W' axiom 5                  | [Bon91]  | : LCL157-1.p | -                              | [MW88]   | : COL016-1.p |
| W' axiom 6                  | [Bon91]  | : LCL158-1.p | -                              | [MW88]   | : COL017-1.p |
| W' axiom 7                  | [Bon91]  | : LCL159-1.p | -                              | [MW88]   | : COL018-1.p |
| W' axiom 8                  | [Bon91]  | : LCL160-1.p | -                              | [MW88]   | : COL019-1.p |
| wang1.in                    | [OTT]    | : SYN013-1.p | -                              | [MW88]   | : COL020-1.p |
| WE1                         | [Qua92d] | : NUM064-1.p | -                              | [MW88]   | : COL021-1.p |
| WE2.1                       | [Qua92d] | : NUM065-1.p | -                              | [MW88]   | : COL022-1.p |
| WE2.2 cor                   | [Qua92d] | : NUM066-1.p | -                              | [MW88]   | : COL023-1.p |
| WE3.1                       | [Qua92d] | : NUM067-1.p | -                              | [MW88]   | : COL024-1.p |
| WE3.2                       | [Qua92d] | : NUM068-1.p | -                              | [MW88]   | : COL025-1.p |
| WE3 cor.                    | [Qua92d] | : NUM069-1.p | -                              | [MW88]   | : COL026-1.p |
| WE4.1                       | [Qua92d] | : NUM070-1.p | -                              | [MW88]   | : COL027-1.p |
| WE4.2                       | [Qua92d] | : NUM071-1.p | -                              | [MW88]   | : COL028-1.p |
| WE5                         | [Qua92d] | : NUM072-1.p | -                              | [MW88]   | : COL029-1.p |
| WE5 cor.                    | [Qua92d] | : NUM073-1.p | -                              | [MW88]   | : COL030-1.p |
| WE6                         | [Qua92d] | : NUM074-1.p | -                              | [MW88]   | : COL031-1.p |
| WE7                         | [Qua92d] | : NUM075-1.p | -                              | [MW88]   | : COL032-1.p |
| WE8                         | [Qua92d] | : NUM076-1.p | -                              | [MW88]   | : COL033-1.p |
| WE8 cor. 1                  | [Qua92d] | : NUM077-1.p | -                              | [MW88]   | : COL034-1.p |
| WE8 cor. 2                  | [Qua92d] | : NUM078-1.p | -                              | [MW88]   | : COL035-1.p |
| WE9.1                       | [Qua92d] | : NUM079-1.p | -                              | [MW88]   | : COL036-1.p |
| WE9.2                       | [Qua92d] | : NUM080-1.p | -                              | [MW88]   | : COL037-1.p |
| WE9 cor.                    | [Qua92d] | : NUM081-1.p | -                              | [MW88]   | : COL038-1.p |
| WE10                        | [Qua92d] | : NUM082-1.p | -                              | [MW88]   | : COL039-1.p |
| winds.ver1.in               | [ANL]    | : PUZ033-1.p | -                              | [MW88]   | : COL040-1.p |
| wos1                        | [WM76]   | : GRP029-1.p | -                              | [MW88]   | : COL041-1.p |





- [SE94] : SYN293-1.p  
- [SE94] : SYN294-1.p  
- [SE94] : SYN295-1.p  
- [SE94] : SYN296-1.p  
- [SE94] : SYN297-1.p  
- [SE94] : SYN298-1.p  
- [SE94] : SYN299-1.p  
- [SE94] : SYN300-1.p  
- [SE94] : SYN301-1.p  
- [Ste87] : RING023-6.p  
- [Ste87] : RING024-6.p  
- [Ste87] : RING025-4.p  
- [Sti93] : PUZ015-2.g  
- [Sti93] : PUZ016-2.g  
- [Ver92] : GRP041-2.p  
- [Ver92] : GRP042-2.p  
- [Ver92] : GRP043-2.p  
- [Ver92] : GRP044-2.p  
- [Ver92] : GRP045-2.p  
- [Ver92] : GRP046-2.p  
- [Ver92] : GRP047-2.p  
- [Ver92] : GRP048-2.p  
- [Wos89] : COL045-1.p  
- [Wos89] : COL046-1.p  
- [Wos94a] : GRP114-1.p  
- [Wos94a] : ROB026-1.p  
- [Wos94a] : ROB027-1.p  
- [WOLB92] : CID001-1.p  
- [WOLB92] : CID003-1.p  
- [WOLB92] : CID003-2.p  
- [WOLB92] : CIV001-1.p  
- [WOLB92] : CIV003-1.p  
- [WOLB92] : CIV004-1.p

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