

SHIP SCHEDULING AND SERVICE NETWORK INTEGRATION FOR LINER SHIPPING COMPANIES AND STRATEGIC ALLIANCES

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Abstract: Liner shipping companies and strategic alliances can benefit greatly from using systematic methods to streamline their operations, thus it is highly desirable to improve ship scheduling on service route planning and integrate their service networks by analytical models. The purpose of this study is to propose a dynamic programming (DP) model for ship scheduling for planning a service route. This can help planners make better scheduling decisions under berth time-window constraints. The proposed model derives an optimal scheduling strategy including cruising speed and quay crane dispatching decisions, rather than a tentative and rough schedule arrangement. The proposed model is extended to cases of integrating one company's or strategic alliance partners' service networks to gain more efficient hub-and-spoke operations, tighter transshipment and better level-of-service.

Key Words: liner shipping, ship scheduling, network integration, dynamic programming

1. INTRODUCTION

Liner shipping provides regular services between specified ports according to timetables advertised in advance. The services are, in principle, open to all shippers and seem like public transport services. The provision of such services, often offering global or regional coverage, requires extensive infrastructure in terms of ships, equipment (e.g. containers, chassis, trailers) and needed to appoint agents at each calling port for the services. Since a service route of one containership fleet, once determined, is hard to alter for a certain period of time, the initial route planning and scheduling decisions should be made carefully after thorough study and planning. It is highly desirable to plan new routes and rearrange service networks by analytical methods, since improvement of ship scheduling can yield additional profits or cost savings.

There have been some studies on optimization models for fleet deployment problems, including fleet size and mix, cruising speed, routing or scheduling problems in sea transportation. However, most studies have been on industrial carriers, bulk carriers, or tankers. On liner fleet deployment, heuristic approaches rather than analytic optimization models have been dominant. A more detailed discussion and a survey of many relevant studies can be found in the papers of Ronen (1983, 1993). The available literature offers a comprehensive coverage of the various optimization problems that can be found in the shipping industry.

Scheduling is a fairly common problem in transport but, nevertheless, liner shipping has

certain intrinsic features that make the design of scheduling models particularly difficult. Ship scheduling is the most detailed level of planning liner fleet operations. In service route planning, ship scheduling concerns the assignment of arrival and departure times to ships operating on a route. It includes determining estimated time to berth (ETB), and estimated time to departure (ETD) when the ships will call at ports, as well as cruising speeds between two sequential ports and quay crane dispatching, buffer time arrangement decisions. Usually a given set of candidate calling ports' available time windows has to be determined in advance, and some congested ports' available berth time-windows are extremely limited. We deem these hard time windows. On the other hand, there may be flexibility in the available time windows, called soft time windows.

Additionally, regularity and frequency of service, the two imperatives of liner shipping, combined with deploying very large container ships, can easily lead to low capacity utilization for independent carriers. Therefore, strategic alliances have formed in order to extend economies of scale, scope and network, through strategies such as the integrating of individual service networks, vessel sharing, slot-chartering, joint ownership and/or utilization of equipment and terminals and similar endeavors on better harmonization of operations. Liner carrier alliances are developing at least two different types: (1) core alliances with a set of global partners, (2) multi-consortia networks of slot exchanges covering individual traders (Damas, 1996). Through this kind of global alliance arrangement, a lot of scale benefits can be achieved: more frequent service, shorter transit times, wider port coverage, lower slot costs and a stronger bargaining position in negotiating with terminal operators, container depots and inland/feeder transportation carriers.

Since liner shipping companies and strategic alliances can benefit greatly from using systematic methods to streamline their operations, it is highly desirable to improve ship scheduling on service route planning and integrate their service networks by analytical models. The purpose of this study is to propose a dynamic programming (DP) model for ship scheduling for planning a service route. This can help planners make better scheduling decisions under berth time-window constraints. The proposed model derives an optimal scheduling strategy including cruising speed and quay crane dispatching decisions, rather than a tentative and rough schedule arrangement. Additionally, the model is extended to cases of integrating one company's or strategic alliance partners' service networks to gain more efficient hub-and-spoke operations, tighter transshipment and better level-of-service.

This paper proceeds as follows: Section 2 introduces the procedures for liner service route planning and network integration, and Section 3 formulates a ship scheduling model through dynamic programming, and illustrates the model with a case study. In Section 4 there are concluding remarks and future research issues.

2. SERVICE ROUTE PLANNING AND NETWORK INTEGRATION

In liner shipping long-term operations, there are five key functions: customer relationship management, market monitoring, cost management, service route planning and ship scheduling. The latter two functions are for providing decision support to plan new service routes and modify or integrate the current service network so that companies can maximize their shipment potential.

Regarding studies on ship scheduling or routing problems of the liner shipping, a few analytic optimization models have been proposed to solve routing and scheduling problems for liner fleets. Lane et al. (1987) tried to determine the most cost-effective size and mix for a fleet on one fixed route, and applied the model to the Australia-North America west coast route. Perakis and Jaramillo (1991), Jaramillo and Perakis (1991) developed a linear programming model for a routing strategy to minimize total fleet operating and lay-up cost and to assign each ship to some mix of the predetermined routes during a planning horizon. Rana and Vickson (1988, 1991) addressed some problems in liner shipping and developed nonlinear programming models to maximize total profit by finding an optimal sequence of calling ports for each ship. Cho and Perakis (1996) suggested two models, one of which is a linear programming model to maximize profit. This model provides an optimal routing mix for each ship and optimal service frequencies for each candidate route. The other model is a mixed integer programming model to minimize cost, providing optimal routing mixes and frequencies, as well as best capital investment alternatives to expand fleet capacity. Powell and Perakis (1997) developed an integer programming model to minimize the operating and lay-up costs for a fleet of liner ships operating on various routes. Xie et al. (2000) presented an algorithm, which combines linear programming with dynamic programming to improve the solution for a linear model of fleet planning. The volume of publications is fairly limited, especially in service route planning, because of the confidentiality that often shrouds highly commercial information such as service patterns, alliance operations and marketing strategies.

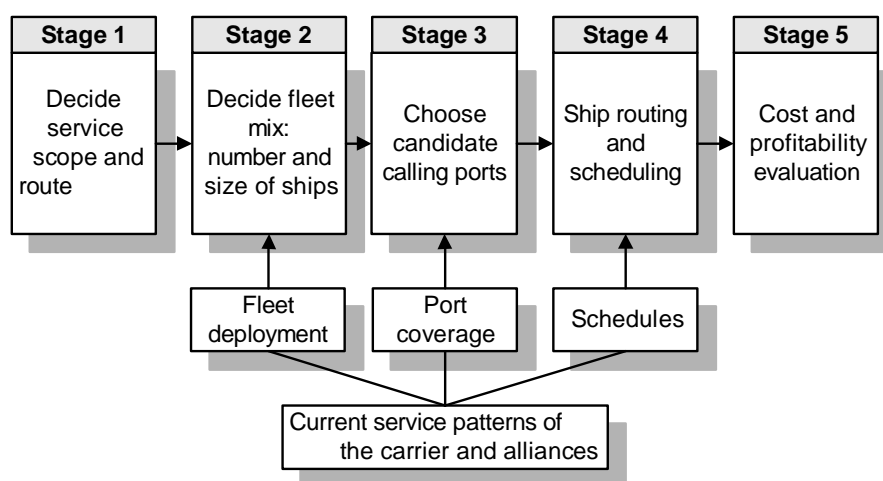


Figure 1. Procedure of Liner Service Route Planning and Network Integration

Generally, a liner company may follow the procedure shown in Figure 1 to plan a new service route and/or to integrate current service routes. The first stage in this process is to decide service scope and route types according to either cargo flow distribution and growth or service coverage requirements. Currently, shipping lines operate three general types of deep-sea itineraries shown in Figure 2: end to end, pendulum and round the world service routes (Lim, 1996). End to end services schedule vessels back and forth between two continents. Pendulum services schedule vessels back and forth between three continents with one of these continents as a fulcrum, with the points at either end of the pendulum swing linked only through the fulcrum. This type of service offers a way to fill container slots four times on the same voyage and to eliminate certain overlapping port calls in the fulcrum area. The merging of separate end-to-end services into a pendulum or round the world service serves the two main purposes of broadening the range of through services and reducing the number of ships required to provide the same coverage. This gives a major cost saving by merging the previously duplicated port calls in the central region of the pendulum. Also round the world

services can overcome the problems of end-to-end operations, by accommodating the needs of global corporations. The world's three principal trade corridors are tied together into one and this type of service can move in either direction, moving westward or eastward or in both directions.

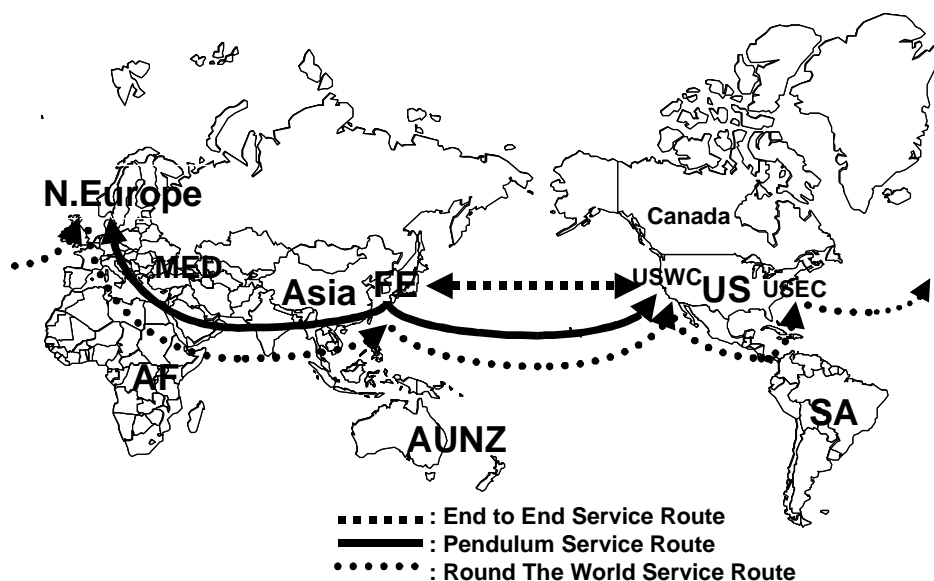


Figure 2. Three Types of Liner Service Routes

At the second stage, planners may consider trade scale (i.e. cargo transport demand) of the planned route and the available owned/chartered-in fleet of the carrier and alliances to determine fleet mix. At the same time, regularity and frequency of service are considered to determine number and size of ships, which are important factors for ship routing and scheduling decisions. At this stage, planners might determine approximate service frequencies on the planned route. Additionally, they might also decide which ships to add to the fleet, i.e. among a finite set of capital investment options which ships to reallocate, which ships to charter in for the planning horizon, which ships to build or purchase. Deploying improper size containerships, can easily lead to low capacity utilization for carriers who decide to operate independently, so carriers often develop cooperative partnerships or strategic alliances with other carriers. Alliances have emerged in order to exploit economies of scope among otherwise competing operators, using strategies such as the individual service network integration, vessel sharing, slot chartering, slot exchange, joint ownership and/or utilization of equipment and terminals.

Choosing candidate calling ports at the third stage is to maximize the shipment potential and port coverage on the planned route; and for this market information is required, including global/regional economic, trade development. Uncertainty of cargo demand plays a major role in liner operations. Therefore, planners need, as important preliminary data for the second stage, the cargo demand forecasts and port-pair cargo flows for the markets the shipping company plans to serve. According to the demand forecasts of each port pair for the planning horizon and current service routes on the same trade, they can suggest a finite set of candidate calling ports, which are derived from their negotiations, common sense, past experience, or view of future main cargo flows.

The first three stages as mentioned above are less structural problems and are difficult to formulate using analytical models. In this paper, we focus on issues regarding the fourth stage

of the planning procedure and develop analytical models, which determine the sequences and timetables of calling ports of the planned routes with integrating one company's or strategic alliance partners' service networks to gain more efficient hub-and-spoke operations, tighter transshipment and better level-of-service.

3. DYNAMIC PROGRAMMING (DP) SHIP-SCHEDULING MODEL

Scheduling is a fairly common problem in transport but, nevertheless, liner shipping has certain intrinsic features that make the design of scheduling models particularly difficult. Ship scheduling is the most detailed level of planning liner fleet operations. In service route planning or network integration, ship scheduling concerns the assignment of arrival and departure times to ships operating on a route. It includes determining estimated time to berth (ETB), and estimated time to departure (ETD) when the ships will call at ports, as well as cruising speeds between two sequential ports and quay crane dispatching, buffer time arrangement decisions (see Figure 3). Usually a given set of candidate calling ports' available time windows has to be determined in advance, and some congested ports' available berth time-windows are extremely limited. At main hub ports, the schedule time windows shall cope with the time windows of pre-arranged joint service routes, feeder services and rail services so that we can streamline container transportation operations. We deem these hard time windows. On the other hand, there may be flexibility in the available time windows, called soft time windows. Dynamic programming is a very useful technique for making a sequence of interrelated decisions, providing a systematic procedure for determining the combination of decisions that maximizes overall effectiveness. The proposed ship scheduling model is formulated through dynamic programming.

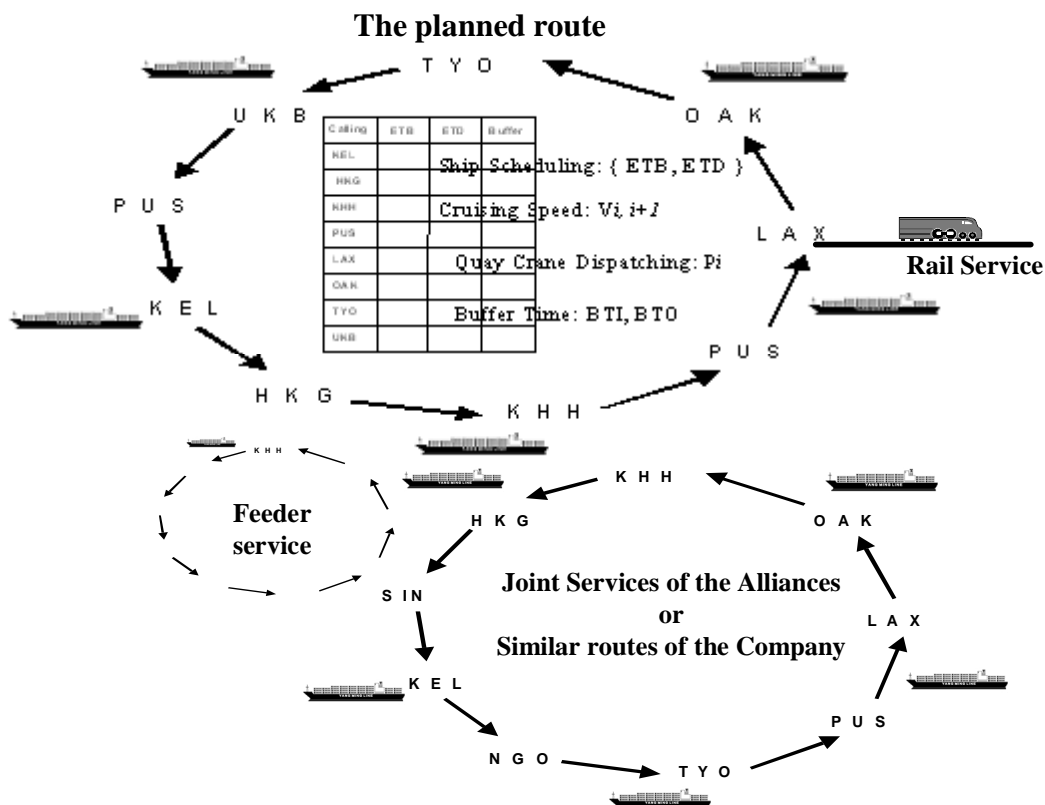


Figure 3. Ship Scheduling and Network Integration Problems of the Liner Shipping

3.1 Model formulation

Using dynamic programming, discrete stages are defined for the original problem, and states are defined for individual stages. In this case, the stages of the dynamic programming solution procedure are the sequential candidate ports where the route is planned to call. There are n candidate calling ports, so the dynamic programming solution procedure has n stages. We use index i to denote the candidate calling ports $i = 1, 2, \dots, n$. The dynamic programming problem of optimal ship scheduling is formulated as follows.

The following assumptions are imposed for the model:

1. The available berth time windows at each candidate calling port have been given by alliance negotiations and provided by the terminal operators;
2. The cruising speed can be adjusted to a certain extent depending on the ships' design;
3. The volume of each port cargo movement including way-port cargo can be estimated approximately;
4. The container handling productivity of terminals at each calling port can be adjusted to a certain extent to accommodate the carrier's requirements.

Based on the assumptions as mentioned above, the states of each stage are defined as a set associated with the major factors that affect estimated schedules at the next calling port. The problem is divided into n stages with an action of cruising speed, quay crane dispatching and buffer time decisions at each stage i . Each stage has some factors associated with the next stage. The state at each stage i is defined as follows:

$$S_i = \{P_i, BTO_i, V_{i,i+1}, BTI_{i+1}\} \quad (1)$$

where,

P_i = Gantry crane productivity at calling port i (unit: moves per hour), which is in the set \mathbf{Pi} of available crane productivity offered by the terminal operators at port i , i.e. $P_i \in \mathbf{Pi}$,

BTO_i = Buffer time for departing from calling port i (unit: hour),

$V_{i,i+1}$ = Cruising speed from calling port i to the next calling port $i + 1$ (unit: knot, nautical miles per hour), which is in the interval between minimum critical speed, V_{\min} and maximum critical speed, V_{\max} , i.e. $V_{i,i+1} \in \mathbf{V}[V_{\min}, V_{\max}]$,

BTI_{i+1} = Buffer time for arriving at the very next calling port $i + 1$ (unit: hour).

ETW_i , the estimated time windows at port i (i.e. stage i) is represented as follows:

$$ETW_i = \{ETB_i, ETD_i\} \quad (2)$$

where,

ETB_i = Estimated time to arrival at the assigned berth (ETB) of calling port i ,

ETD_i = Estimated time to departure (ETD) from calling port i .

The voyage time of each leg (i.e. one-trip voyage from port i to the next port $i + 1$) for scheduling is illustrated by Figure 4 and explained below.

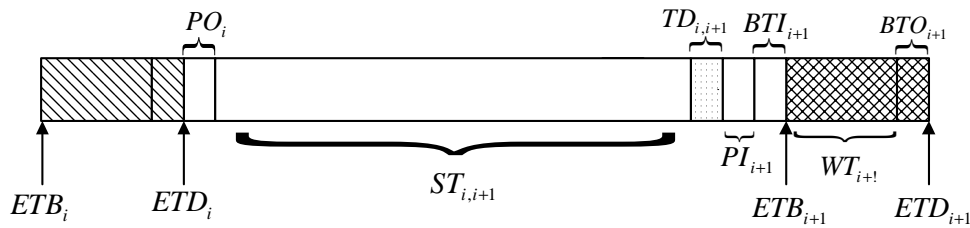


Figure 4. Voyage Time from Port i to the Next Port $i + 1$

ETB_{i+1} , estimated time to berth at the very next calling port can be derived from Equation (3).

$$ETB_{i+1} = ETD_i + PO_i + ST_{i,i+1} + TD_{i,i+1} + PI_{i+1} + BTI_{i+1} \quad (3)$$

where,

PO_i = Pilot-out time at calling port i (unit: hour),

$ST_{i,i+1}$ = Steaming time from calling port i to the next calling port $i + 1$ (unit: hour),

$TD_{i,i+1}$ = Time zone difference between calling port i and the next calling port $i + 1$ (unit: hour),

PI_{i+1} = Pilot-in time at calling port $i + 1$ (unit: hour).

Experienced captains can estimate the pilot in/out time at a calling port. Time zone differences are tabulated in world port time zone tables. The steaming time from calling port i to the next calling port $i + 1$ can be calculated by Equation (4),

$$ST_{i,i+1} = D_{i,i+1} / V_{i,i+1} \quad (4)$$

where,

$D_{i,i+1}$ = Distance from calling port i to the next calling port $i + 1$ (unit: nautical mile).

ETD_i , estimated time to departure from the very next calling port can be derived from Equation (5),

$$ETD_i = ETB_i + WT_i + BTO_i \quad (5)$$

where,

WT_i = Working time for unloading and loading containers at calling port i (unit: hour).

Working time to unload and load containers can be calculated by Equation (6),

$$WT_i = (TM \times M_i) / P_i \quad (6)$$

where,

TM = Total expected container moves on the round-trip voyage (unit: move),

M_i = Expected cargo proportion at calling port i (unit: %).

Total expected container moves can be calculated by Equation (7),

$$TM = N \times CP \times U \times (TF / 2 + 0.5) \quad (7)$$

where,

$N = 4$, when the planned route type is end-to-end service,

$N = 6$, when the planned route type is pendulumn service,
 $N = 8$, when the planned route type is round-the-world service,
 CP = Average vessel operational capacity of the fleet (unit: TEU, Twenty-foot equivalent unit),
 U = Expected capacity utilization (unit: %),
 $TF = 20'$ container proportion on this trade (unit: %).

Once ETB_i is determined, ETD_i , ETB_{i+1} and ETD_{i+1} can be derived from Equations (3)~(7) above; and P_i , BTO_i , $V_{i,i+1}$ and BTI_{i+1} are factors to determine estimated time windows, of which P_i and $V_{i,i+1}$ are two key factors. The action of the dynamic programming is defined as the decisions for cruising speed, quay crane dispatching, and buffer time chosen at any stage i to minimize the total expected variations in time from available berth time windows to estimated berth time windows for the planned voyage. We illustrate the optimal ship scheduling policy with Figure 5, in which each voyage leg is arranged to meet terminal time-window constraints as closely as possible.

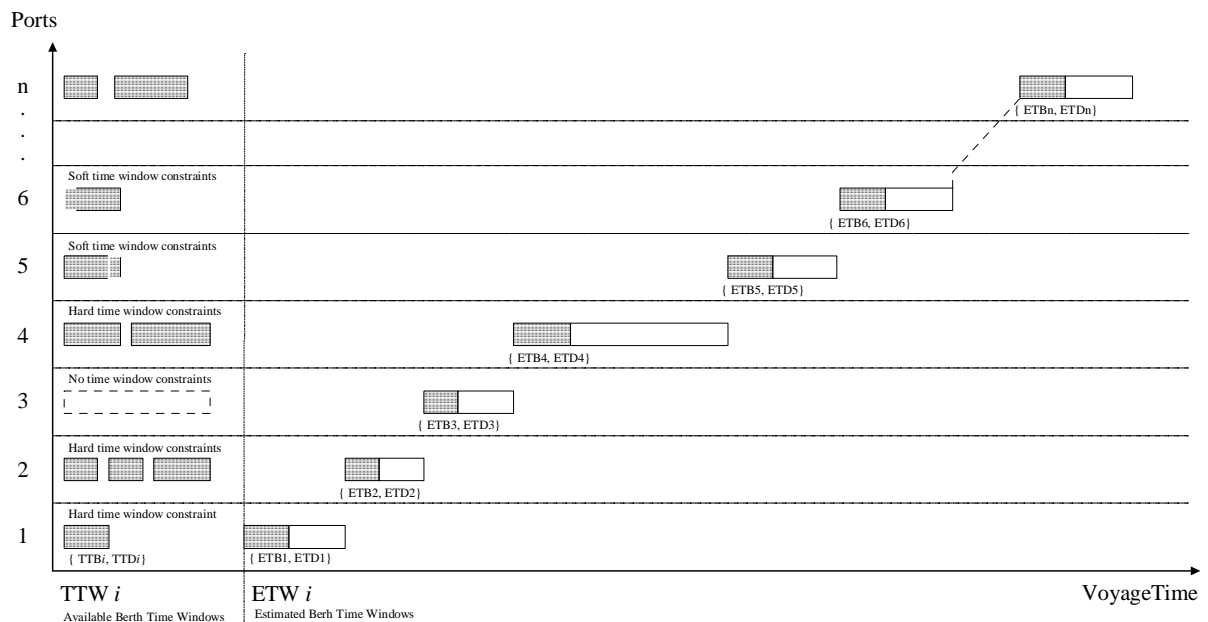


Figure 5. Ship Scheduling with Berth Time-Window Constraints

Let $TTW_i = \{ TTB_i, TTD_i \}$, available terminal time window at calling port i ,

where,

TTB_i = Available berthing time at calling port i terminal,

TTD_i = Available departing time at calling port i terminal.

At main hub ports, the schedule time windows shall cope with the time windows of pre-arranged joint service routes, feeder services and rail services so that we can streamline container transportation operations. These time window constraints are deemed as single-side hard time-window constraints. Additionally, the terminal operators at calling ports might offer single or multiple time windows with hard or soft constraints. There are some patterns with respect to time-window conditions offered by terminal operators or port authorities, which can be categorized into three types, as follows:

1. $\{\hat{TTB}_i, \hat{TTD}_i\}$: both-side hard time-window constraints,
2. $\{\hat{TTB}_i, \tilde{TTD}_i\}, \{\tilde{TTB}_i, \hat{TTD}_i\}$: single-side hard time-window constraints, i.e. one-side soft time window constraints,
3. $\{\tilde{TTB}_i, \tilde{TTD}_i\}$: no time-window constraints, i.e. both-side soft time window constraints.

An appropriate recursive relationship for ship scheduling problem must be formulated, one which is divided into n stages that correspond to the n voyage legs of the rotation. This recursive relationship minimizes the total expected variations in time from available berth time windows to estimated berth time windows, as represented in Equation (8),

$$Z_{i+1}^* = Z_i^* + \underset{P_i \in \Pi, BTO_i}{\text{Min}} (ETD_i - TTD_i)^2 + \underset{V_{i,i+1} \in V, BTI_{i+1}}{\text{Min}} (ETB_{i+1} - TTB_{i+1})^2 \quad (8)$$

When we use this recursive relationship, the solution procedure moves forward (or backward) stage by stage, each time finding the optimal policy for that stage until it finds the optimal policy stopping at the last (or first) stage. The algorithm for ship scheduling is shown as Figure 6 and explained as follows:

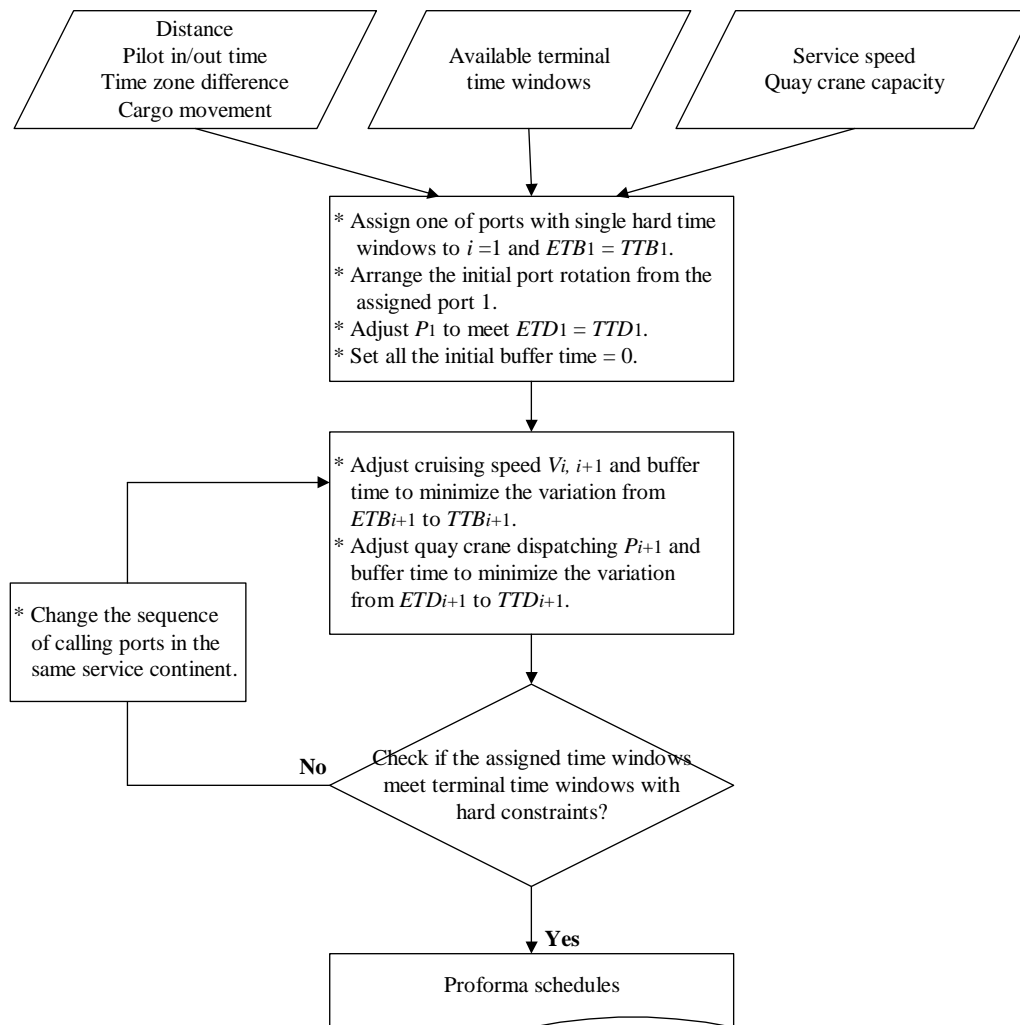


Figure 6. Solution Procedure for Ship Scheduling

- Step 1. Input the needed data including distance, pilot in/out time, time zone difference, cargo movement, available terminal time windows, service speed, and quay crane capacity.
- Step 2. Assign one of the ports with single hard time windows to $i = 1$ and $ETB_1 = TTB_1$. Adjust P_1 to meet $ETD_1 = TTD_1$. Set all the initial buffer time = 0.
- Step 3. Adjust cruising speed $V_{i,i+1}$ and buffer time to minimize the variation from ETB_{i+1} to TTB_{i+1} . Adjust quay crane dispatching P_{i+1} and buffer time to minimize the variation from ETD_{i+1} to TTD_{i+1} .
- Step 4. Check if the assigned time windows meet terminal time windows with hard constraints. If no, try to change the sequence of calling ports in the same service continent and go back to Step 3; if yes, output ship scheduling results (i.e. proforma schedules).

3.2 Model implementation

A new Asia – US West Coast service route planning for a Taiwan liner company is used as a case study. The company plans to deploy 5 full-container vessels with loadable capacity 5,200 TEU and 25-knot service speed on this service route to provide weekly services. The candidate calling ports and initial rotation are shown in Figure 3, planned to call at Los Angeles (LAX) and Oakland (OAK) on the U.S. West Coast, as well as Tokyo (TYO), Kobe (UKB), Busan (PUS), Keelung (KEL), Kaohsiung (KHH) and Hong Kong (HKG) in Asia.

Calling Ports	Steaming Time Dist. Spd. Time	Time Diff.	Pilot In/Out PI PO	Working Time Cgo M/h L/D Time	Buffer In Out	ETB D H M W. Day	ETD D H M	Arr. til time U (hours)	Dep. V (1)
KEL	475 24 20.2	0	0.0 1.0	486 50 9.7	0.0 0.0	0 8 0 THU	0 17 30	0.05	8.0
HKG	350 24 14.9	0	1.0 1.0	1459 60 24.3	0.0 0.0	1 16 0 FRI	2 16 30	0.15	39.9
KHH	922 24 39.2	1	2.0 2.0	1265 60 21.1	0.0 0.0	3 10 0 SUN	4 7 0	0.13	82.2
PUS	5,520 23 245.3	-17	1.0 1.0	438 45 9.7	0.0 0.0	6 2 30 WED	6 12 0	0.045	146.5
LAX	360 23 15.7	0	2.0 1.0	3950 60 65.8	0.0 0.0	16 3 30 SAT	18 21 30	0.406	387.5
OAK	4,862 23 216.1	17	3.0 2.0	710 48 14.8	0.0 1.0	19 17 0 TUE	20 9 0	0.073	473.0
TYO	316 24 13.4	0	3.0 2.0	486 60 8.1	2.0 1.0	30 9 0 SAT	30 18 0	0.05	728.9
UKB	611 24 26.0	0	3.0 2.0	438 60 7.3	2.0 1.0	31 14 30 SUN	31 23 0	0.045	758.5
PUS	715 23 31.8	-1	1.0 1.0	496 45 11.0	4.0 0.0	33 8 0 TUE	33 19 0	0.051	799.8
KEL			1.0 0.0	0 0 0.0	4.5 0.0	35 8 0 THU	35 8 0	Capacity	848.1
TOTAL DISTANCE (miles) 14,131 TOTAL STEAMING TIME (hours) 623 TOTAL MANEUVERING TIME (hours) 30 TOTAL WORKING TIME (hours) 172 TOTAL BUFFER TIME (hours) 16 GRAND TOTAL TIME (hours) 840 ROUND VOYAGE DAYS 35.0 FLEET 5.0 5,200 TEU vessels for weekly service.								9,729	
								Utilization	0.9
								20'	15%
								40'	85%

Figure 7. Microsoft Excel Working Sheets for Ship Scheduling

By applying Microsoft Excel working sheets (see Figure 7) with solution procedure, the available berth time window, distance, time zone difference, pilot in/out time and cargo distribution proportion data are manually input into the relevant cells, and the volume of

containers handled at each port is generated by automatic calculation. Estimated time windows to berth will be calculated and output in relevant cells. It should be emphasized that in this system port rotation exchange and the buffer time must be adjusted by human estimation.

For weekly service routes, the total voyage time must not exceed the maximum fleet round voyage time, which can be represented as Equation (9),

$$\sum_{i=1}^n (ST_i + WT_i + PI_i + PO_i + BTI_i + BTO_i) \leq 24 \times F \times 7 \quad (9)$$

where,

F = number of vessels deployed on the route.

$TT_{i,i+1}$, the transit time from calling port i to the next calling port $i+1$ can be derived from Equation (10), which will be needed by marketing and pricing personnel to provide shippers with transit time information and to compare their own strengths and weaknesses with other competitors for pricing strategies at each market. The transit time for trans-Atlantic service (see Table 1 and Table 2) is calculated by working sheets when the proforma schedule is adjusted and finalized.

$$TT_{i,i+1} = ETB_{i+1} - ETD_i \quad (10)$$

There are some marketing implications for the transit time. The shorter transit time can provide shippers with better service. In general, carriers arrange shorter transit time to ports where there is large container throughput or niche markets. The transit time also indicates the competitive advantage compared with other competitors.

Table 1. Asia – US West Coast Eastbound Service (days)

Ports	TYO	UKB	PUS	KEL	KHH	HKG
LAX	23	22	12	18	14	16
OAK	25	24	14	20	16	18

Table 2. Asia – US West Coast Westbound Service (days)

Ports	TYO	UKB	PUS	KEL	KHH	HKG
LAX	12	13	15	17	21	19
OAK	10	11	13	15	19	17

4. CONCLUSIONS

Planners of liner shipping companies typically respond to service route planning and network integration by using insights acquired through experience, without any help from analytical models for ship scheduling problems. However, as terminal berth time-window constraints increase, the scheduling problems must consider increasingly more complex factors that humans alone cannot process simultaneously. To provide planners with better methods, this paper proposes a DP ship scheduling model. This can help planners make better scheduling decisions under berth time-window constraints, as well integrate one company's or strategic alliance partners' service networks to gain more efficient hub-and-spoke operations, tighter transshipment and better level-of-service. It also can be useful for rescheduling berth time

windows to cope with feeder schedules, inland transport schedules and partners' route schedules, so as to gain more efficient operations. Further conclusions are listed below:

1. Compared with the traditional methods, the proposed DP ship scheduling model pursues an optimal scheduling strategy including cruising speed and quay crane dispatching decisions, rather than a tentative and rough schedule arrangement. This improvement not only gives this new mathematical model, but also could yield cost savings due to decreases of vessel fuel consumption and port time.
2. The computational results presented in this paper are based on a specific Asia – US West Coast Eastbound service route planning. However, the proposed model, with similar solution algorithm should be applicable to other route planning and network integration. Additionally, this model is flexible in its use, and the Microsoft Excel working sheets with VBA (Visual Basic Application) can be utilized for other cases with some slight adjustments.
3. The proposed model has several advantages over current practice. The solution procedure is relatively easy to implement and flexibly handles a large number of time-window constraints that may arise in many real life routing and scheduling applications. However, the major drawback of the proposed model and solution algorithm is that regional port rotation changes and buffer time decisions must be by means of human observations and manual modifications.

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