Progress on Abstract Interpretation Based Formal Methods and Future Challenges

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Abstract. In order to contribute to the software reliability problem, tools have been designed in order to analyze statically the run-time behavior of programs. Because the correctness problem is undecidable, some form of approximation is needed. The whole purpose of abstract interpretation is to formalize this idea of approximation. We illustrate informally the application of abstraction to the semantics of programming languages as well as to program static analysis. The main point is that in order to reason or compute about a complex system, some information must be lost, that is the observation of executions must be either partial or at a high level of abstraction.

In the second part of the paper, we compare program static analysis with deductive methods, model-checking and type inference. Their foundational ideas are shortly reviewed, and the shortcomings of these four tools are discussed, including when they are combined. Alternatively, since program debugging is still the main program verification method used in the software industry, we suggest to combine formal with informal methods.

Finally, the grand challenge for all formal methods and tools is to solve the software reliability, trustworthiness or robustness problems. Few challenges more specific to program analysis by abstract interpretation are shortly discussed.

1 Introductive Motivations

The evolution of hardware by a factor of 10^6 over the past 25 years has lead to the explosion of the size of programs in similar proportions. The scope of application of very large programs (from 1 to 40 millions of lines) is likely to widen rapidly in the next decade. These big programs will have to be designed at a reasonable cost and then modified and maintained during their lifetime (which is often over 20 years). The size and efficiency of the programming and maintenance teams in charge of their design and follow-up cannot grow up in similar proportions. At a not so uncommon (and often optimistic) rate of one bug per thousand lines such huge programs might rapidly become hardly manageable in particular for safety critical systems [\(528\)](#page-62-0). Therefore in the next 10 years, the software reliability problem is likely to become a major concern and challenge to modern highly computer-dependent societies.

In the past decade a lot of progress has been done both on thinking/methodological tools (to enhance the human intellectual ability) to cope with complex software systems and *mecanical tools* (using the computer) to help the programmer to reason on programs.

The mecanical tools for computer aided program verification started empirically by executing or simulating the program in enough representative possible environments. However debugging of the compiled code or simulation of a model of the source program hardly scale up and often offer a low coverage of the program dynamic behavior.

Formal program verification methods attempt to mecanically prove that program execution is correct in all specified environments. This includes deductive methods, model checking, program typing and program analysis.

Since program verification is undecidable, computer aided program verification methods are all partial or incomplete. The undecidability or complexity is always solved by using some form of approximation. This means that the mechanical tool will sometimes suffer from practical time and space complexity limitations, rely on finiteness hypotheses or provide only semi-algorithms, require user interaction or be able to consider restricted forms of specifications or programs only. The mechanical program verification tools are all quite similar and essentially differ in their choices regarding the approximations which have to be done in order to cope with undecidability or complexity. The ambition of abstract interpretation is to formalize this notion of approximation in a unified framework [\(208;](#page-38-0) [214;](#page-39-0) [192;](#page-37-0) [195;](#page-37-1) [196;](#page-37-2) [199;](#page-37-3) [203;](#page-38-1) [204\)](#page-38-2).

2 Abstract Interpretation

Since program verification deals with properties, that is sets (of objects with these properties), abstract interpretation can be formulated in an application independent setting, as a theory for approximating sets and set operations as considered in set (or category) theory. A more restricted understanding of abstract interpretation is to view it as a theory of approximation of the behavior of dynamic discrete systems (such as the formal semantics of programs or a communication protocole specification). Since such behaviors can be characterized by fixpoints [\(213;](#page-38-3) [671\)](#page-72-0) (e.g. corresponding to iteration), an essential part of the theory provides constructive and effective methods for fixpoint approximation and checking by abstraction [\(218\)](#page-39-1).

2.1 Fixpoint Semantics

The semantics of a programming language defines the semantics of any program written in this language. The *semantics of a program* provides a formal mathematical model of all possible behaviors of a computer system executing this program in interaction with any possible environment. In the following we will try to explain informally why the semantic of a program can be defined as the solution of a fixpoint equation. Then, in order to compare semantics, we will show that all semantics of a program can be organized in a hierarchy by abstraction. By observing computations at different levels of abstraction, one can approximate fixpoints hence organize the semantics of a program in a lattice [\(206;](#page-38-4) [197\)](#page-37-4).

2.2 Trace Semantics

Our finer grain of observation of program execution, that is the most precise of the semantics that we will consider, is that of trace semantics , a model also frequently used in temporal logic [\(603;](#page-67-0) [275;](#page-43-0) [683\)](#page-73-0). An execution of a program for a given specific interaction with its environment is a sequence of states, observed at discrete intervals of time, starting from an initial state, then moving from one state to the next one by executing an atomic program step or transitions and either ending in a final regular or erroneous state or non terminating, in which case the trace is infinite (see Fig. [1\)](#page-2-0).

Fig. 1. Examples of Computation Traces

2.3 Least Fixpoint Trace Semantics

The trace semantics can be defined in fixpoint form [\(206;](#page-38-4) [198\)](#page-37-5), that is as a solution of an equation of the form $X = F(X)$ where X ranges over sets of finite and infinite traces.

More precisely, let **Behaviors** be the set of execution traces of a program, possibly starting in any state. We denote by **Behaviors**⁺ the subset of finite traces and by **Behaviors**[∞] the subset of infinite traces.

A finite trace $\stackrel{a}{\bullet}$...^Z in **Behaviors**⁺ is either reduced to a final state (in which case there is no possible transition from state $\frac{3}{2} = \frac{2}{9}$) or the initial state $\frac{3}{4}$ is not final and the trace consists of a first computation stan $\frac{3}{4}$. If or which $\stackrel{\circ}{\bullet}$ is not final and the trace consists of a first computation step $\stackrel{\circ}{\bullet}$ after which, from the intermediate state \overline{b} , the execution goes on with the shorter finite trace

 $\stackrel{b}{\bullet}$ $\stackrel{z}{\bullet}$ ending in the final state $\stackrel{z}{\bullet}$. The finite traces are therefore all well defined by induction on their length.

An infinite trace ^a—–...—–... in **Behaviors**[∞] starts with a first computation step $\overset{a}{\bullet}$ after which, from the intermediate state $\overset{b}{\bullet}$, the execution goes on with an infinite trace \overline{b} \overline{b} \overline{c} \overline{c} \overline{d} \overline{d} \overline{b} \overline{e} \overline{b} \overline{d} These remarks lead to the following fixpoint equation:

Behaviors =
$$
\{\stackrel{a}{\bullet} \mid \stackrel{a}{\bullet} \text{ is a final state}\}
$$

\n $\cup \{\stackrel{a}{\bullet} \stackrel{b}{\bullet} \dots \stackrel{z}{\bullet} \mid \stackrel{a}{\bullet} \stackrel{b}{\bullet} \text{ is an elementary step } \& \quad b \longrightarrow \dots \stackrel{z}{\bullet} \in \text{Behavior}^+\}$

\n $\cup \{\stackrel{a}{\bullet} \stackrel{b}{\bullet} \dots \stackrel{z}{\bullet} \dots \mid \stackrel{a}{\bullet} \stackrel{b}{\bullet} \text{ is an elementary step } \& \quad b \longrightarrow \dots \longrightarrow \dots \in \text{Behavior}^{\infty}\}$

In general, the equation has multiple solutions. For example if there is only state $\frac{a}{\bullet}$, it is not final and the only possible elementary step is $\frac{a}{\bullet}$ then the equation is **Behaviors** = $\{\stackrel{a}{\bullet} \stackrel{a}{\bullet} \cdots \stackrel{a}{\bullet} \cdots \stackrel{a}{\bullet} \cdots \stackrel{a}{\bullet} \cdots \stackrel{c}{\bullet}$ **Behaviors**. One solution is $\{\begin{matrix} a & a & a & a \\ \bullet & \bullet & \bullet & \bullet & \end{matrix}$} but another one is the empty set ∅. Therefore, we choose the least solution for the computational partial ordering:

« More finite traces \mathcal{C} less infinite traces ».

2.4 Abstractions

A programming language semantics is more or less precise according to the considered observation level of the program executions [\(403;](#page-53-0) [16;](#page-23-0) [350\)](#page-49-0). This intuitive idea can be formalized by Abstract interpretation [\(206\)](#page-38-4) and applied to different languages $(60; 311; 61)$ $(60; 311; 61)$ $(60; 311; 61)$ $(60; 311; 61)$ $(60; 311; 61)$, including for proof methods $(194; 493)$ $(194; 493)$ $(194; 493)$.

The abstract interpretation theory formalizes this notion of approximation/ abstraction in a mathematical setting which is independent of particular applications. In particular, abstractions must be provided for all mathematical constructions used in programming and specification languages semantic definitions [\(214;](#page-39-0) [218;](#page-39-1) [504;](#page-60-0) [545;](#page-63-0) [554;](#page-64-0) [555;](#page-64-1) [561;](#page-64-2) [564;](#page-64-3) [610;](#page-68-0) [611;](#page-68-1) [629;](#page-69-0) [630\)](#page-69-1).

If the approximation is rough enough, the abstraction of a concrete semantics can lead to an abstract semantics which is less precise but is effectively computable by a computer. By effective computation of the abstract semantics, the computer is able to analyze the behavior of programs and of software before and without executing them [\(207\)](#page-38-5). Abstract interpretation algorithmics provide approximate methods for computing this abstract semantics. The main abstract interpretation algorithmics provide effective methods for the exact or approxi-mate iterative resolution of fixpoint equations [\(208\)](#page-38-0).

We will first illustrate formal and effective abstractions for sets. Then we will show that such abstractions can be lifted to functions and finally to fixpoints.

The abstraction idea and its formalization are equally applicable in other areas of computer science such as artificial intelligence [\(334\)](#page-48-0) e.g. for intelligent

planning [\(94;](#page-29-0) [22\)](#page-23-1), proof checking [\(331\)](#page-48-1), automated deduction and theorem proving [\(332;](#page-48-2) [93;](#page-29-1) [95;](#page-30-0) [280;](#page-44-0) [330;](#page-48-3) [336;](#page-48-4) [333;](#page-48-5) [335;](#page-48-6) [94;](#page-29-0) [329\)](#page-47-0), etc.

2.5 Hierarchy of Abstractions

As shown in Fig. [2](#page-4-0) (from [\(206\)](#page-38-4), where **Behaviors**, denoted τ^{∞} for short, is the lattice infimum), all abstractions of a semantics can be organized in a lattice (which is part of the lattice of abstract interpretations introduced in [\(214;](#page-39-0) [212\)](#page-38-6)). The approximation partial ordering of this lattice formally corresponds to logic implication, intuitively to the idea that a semantics is more precise than another.

Fig. 2. The Hierarchy of Semantics

Fig. [3](#page-5-0) illustrates the derivation of a relational semantics [\(403;](#page-53-0) [527\)](#page-62-1) (denoted τ^{∞} in Fig. [2\)](#page-4-0) from a trace semantics (denoted τ^{∞} in Fig. 2). The abstraction α from trace to relational semantics consists in replacing the finite traces $\stackrel{a}{\bullet}$ $-\frac{z}{a}$ by the pair $\langle a, z \rangle$ of the initial and final states. The infinite traces a b ^a **b** \longrightarrow \longrightarrow \longrightarrow \longrightarrow are replaced by the pair $\langle a, \perp \rangle$ where the symbol \perp denotes non-termination. Therefore the abstraction is:

$$
\alpha(X) = \{ \langle a, z \rangle \mid \stackrel{a}{\bullet} \quad \dots \quad \stackrel{z}{\bullet} \in X \}
$$

$$
\cup \{ \langle a, \perp \rangle \mid \stackrel{a}{\bullet} \quad \stackrel{b}{\bullet} \quad \dots \quad \dots \in X \}.
$$

The denotational semantics [\(541;](#page-63-1) [639;](#page-70-0) [672\)](#page-72-1) (denoted τ^{\natural} in Fig. [2\)](#page-4-0) is the isomorphic representation of a relation by its right-image:

Fig. 3. Abstraction from Trace to Relational and Natural Semantics

$$
\alpha(R) = \lambda a \cdot \{x \mid \langle a, x \rangle \in R\}.
$$

The abstraction from relational to big-step operational or natural semantics (denoted τ^+ in Fig. [2\)](#page-4-0) [\(457;](#page-57-0) [601\)](#page-67-1) simply consists in forgetting everything about non-termination, so $\alpha(R) = \{ \langle a, x \rangle \in R \mid x \neq \bot \},\$ as illustrated in Fig. [3.](#page-5-0)

A non comparable abstraction consists in collecting the set of initial and final states as well as all transitions $\langle x, y \rangle$ appearing along some finite or infinite trace a •−−−... ^x •−−−^y • ... of the trace semantics. One gets the small-step operational or transition semantics [\(601;](#page-67-1) [463\)](#page-57-1) (denoted τ in Fig. [2](#page-4-0) and also called Kripke structure in modal logic [\(476\)](#page-58-0)) as illustrated in Fig. [4.](#page-5-1)

Fig. 4. Transition Semantics

A further abstraction consists in collecting all states appearing along some finite or infinite trace as illustrated in Fig. [5.](#page-6-0) This is the partial correctness semantics [\(194;](#page-37-6) [304;](#page-45-0) [402;](#page-53-1) [558\)](#page-64-4) or the collecting semantics [\(208\)](#page-38-0) for proving invariance properties of programs.

All abstractions considered in this paper are "from above" so that the abstract semantics describes a superset or logical consequence of the concrete

Fig. 5. Collecting / Partial Correctness Semantics

semantics. Abstractions "from below" are dual and consider a subset of the concrete semantics. An exemple of approximation "from below" is provided by debugging techniques which consider a subset of the possible program executions or by existential checking where one wants to prove the existence of an execution trace fullfilling some given specification. In order to avoid repeating two times dual concepts, we only consider approximations "from above", knowing that approximations "from below" can be easily derived by applying the duality principle (as found e.g. in lattice theory [\(53\)](#page-26-0)).

2.6Effective Abstractions

Numerical Abstractions Assume that a program has two integer variables X and Y. The trace semantics of the program (Fig. [1\)](#page-2-0) can be abstracted in the collecting semantics (Fig. [5\)](#page-6-0). A further abstraction consists in forgetting in a state all but the values x and y of variables X and Y. In this way the trace semantics is abstracted to a set of points, as illustrated in Fig. $6(a)$.

We now illustrate informally a number of effective abstractions of an [in]finite set of points.

Non-relational Abstractions The nonn-relational, attibute independent or cartesian abstractions [\(214,](#page-39-0) example 6.2.0.2) [\(448\)](#page-56-0) consists in ignoring the possible relationships between the values of the X and Y variables. So a set of pairs is approximated through projection by a pair of sets. Each such set may still be infinite and in general not exactly computer representable. Further abstractions are therefore needed.

The *sign abstraction* [\(214\)](#page-39-0) illustrated in Fig. $6(b)$ consists in replacing integers by their sign thus ignoring their absolute value.

The *interval abstraction* [\(207;](#page-38-5) [208;](#page-38-0) [192\)](#page-37-0) illustrated in Fig. $6(c)$ is more precise since it approximates a set of integers by it minimal and maximal values (including $-\infty$ and $+\infty$ as well as the empty set if necessary).

The *congruence abstraction* [\(345;](#page-49-1) [346;](#page-49-2) [348\)](#page-49-3) illustrated in Fig. $6(d)$ is not comparable.

Fig. 6. Non-relational Abstractions

Relational Abstractions Relational abstractions are more precise than non relational ones [\(448\)](#page-56-0) in that some of the relationships between values of the program states are preserved by the abstraction.

For example the *polyhedral abstraction* $(227; 353)$ $(227; 353)$ $(227; 353)$ illustrated in Fig. [7\(b\)](#page-8-0) approximates a set of integers by its convex hull. Only non-linear relationships between the values of the program variables are forgotten.

The use of an *octogonal abstraction* [\(30\)](#page-24-0) illustrated in Fig. $7(a)$ is less precise since only some shapes of polyhedra are retained or equivalently only linear relations between any two variables are considered with $+1$ or -1 coefficients (of the form $\pm x \pm y \leq c$ where c is an integer constant).

A non comparable relational abstraction is the linear congruence abstraction (347) illustrated in Fig. $7(c)$.

A combination of non-relational dense approximations (like intervals) and relational sparse approximations (like congruences) is the trapezoidal linear con*gruence abstraction* of $(509; 508)$ $(509; 508)$ $(509; 508)$ as illustrated in Fig. [7\(d\).](#page-8-3)

Symbolic Abstractions Most structures manipulated by programs are symbolic structures such as control structures (call graphs), data structures (search trees), communication structures (distributed & mobile programs), etc. It is very difficult to find compact and expressive abstractions of such sets of objects (sets of languages, sets of automata, sets of trees or graphs, etc.). For example Büchi automata or automata on trees are very expressive but algorithmically expensive [\(673\)](#page-72-2).

Fig. 7. Relational Abstractions

Fig. 8. Binary Decision Graphs

A compromise between semantic expressivity and algorithmic efficiency was recently introduced by [\(515;](#page-61-0) [514;](#page-61-1) [512;](#page-61-2) [513\)](#page-61-3) using Binary Decision Graphs and Tree Schemata to abstract infinite sets of infinite trees is illustrated in Fig. [8](#page-8-4) $\&$ [9.](#page-9-0)

2.7 Information Loss

Any abstraction introduces some loss of information. For example the abstraction of the trace semantics into relational or denotational semantics loses all information on the computation cost since all intermediate steps in the execution are removed.

All answers given by the abstract semantics are always correct with respect to the concrete semantics. For example if termination is proved using the relational semantics then there no execution abstracted to $\langle a, \perp \rangle$ so no infinite trace $a \rightarrow b$

Fig. 9. Tree Schemata

Fig. 10. Is 1/(X+1-Y) well-defined?

 $-$... in the trace semantics whence non termination is impossible when starting execution in initial state a.

However, because of the information loss, not all questions can be definitely answered with the abstract semantics. For example the natural semantics cannot answer questions about termination as can be done with the relational or denotational semantics. These semantics cannot answer questions about concrete computation costs

The more concrete semantics can answer more questions. The more abstract semantics are simpler. Non comparable abstract semantics (such as intervals and congruences) can neither answer more nor less questions.

To illustrate the loss of information, let us consider the problem of deciding whether the operation $1/(X+1-Y)$ appearing in a program is always well defined at run-time. The answer can certainly be given by the concrete semantics since it has no point on the line $x + 1 - y = 0$, as shown in Fig. [10\(a\).](#page-9-1)

In practice the concrete abstraction is not computable so it is hardly usable in a useful effective tool. The dense abstractions that we have considered are too approximate as illustrated in Fig. [10\(b\).](#page-9-2)

However the answer is positive when using the relational congruence abstraction, as shown in Fig. $10(c)$.

Abstract interpretation theory has mainly been concerned with the soundness of the abstract semantics/interpreter, relative to which questions can be answered corectly despite the loss of information, which is essential in practice and leads to a formal design method.

However completeness , relative to the formalization of the loss of information in a controlled way so as to answer a given set of questions, has also been studied [\(214;](#page-39-0) [322;](#page-47-1) [315;](#page-46-1) [321;](#page-47-2) [553;](#page-64-5) [320\)](#page-47-3), including in the context of model checking [\(205\)](#page-38-7). In practice complete abstractions, including a most abstract one do exist, but most often are not computable and even hard to design manually since the design of a complete abstraction is logically equivalent to a formal correctness proof [\(205\)](#page-38-7).

A more limited but certainly feasible objective towards expressive analyses is by combination of abstract domains (such as the reduced product [\(214\)](#page-39-0), disjunctive completion [\(214;](#page-39-0) [297;](#page-45-1) [298;](#page-45-2) [563;](#page-64-6) [316;](#page-46-2) [318;](#page-47-4) [319\)](#page-47-5), complementation [\(185;](#page-36-0) [184;](#page-36-1) [299\)](#page-45-3)) and their refinement [\(317\)](#page-46-3), which can be implemented in static analyser generators (e.g. [\(485;](#page-59-1) [189\)](#page-37-7)).

2.8 Function Abstraction

We now show how the abstraction of complex mathematical objects used in the semantics of programming or specification languages can be defined by composing abstractions of simpler mathematical structures.

For example knowing abstractions of the parameter and result of a monotonic function on sets, a function F can be abstracted into an abstract function F^{\sharp} as illustrated in Fig. [11](#page-10-0) [\(214\)](#page-39-0). Mathematically, F^{\sharp} takes its parameter x in the

Fig. 11. Function Abstraction

abstract domain. Let $\gamma(x)$ be the corresponding concrete set (γ is the adjoined, intuitively the inverse of the abstraction function α). The function F can be applied to get the concrete result \circ F $\circ \gamma(x)$. The abstraction function α can then be applied to approximate the result $F^{\sharp}(x) = \alpha \circ F \circ \gamma(x)$.

In general neither F nor α and γ is computable even though the abstraction α may be effective. So we have got a formal specification of the abstract function F^{\sharp} and an algorithm has to be found for an effective implementation.

2.9 Fixpoint Abstraction

A fixpoint of a function F can often be obtained as the limit of the iterations of F from a given initial value \perp . In this case the abstraction of the fixpoint can often be obtained as the abstract limit of the iteration of the abstraction F^{\sharp} of F starting from the abstraction $\alpha(\perp)$ of the initial value \perp . The basic result is that the concretization of the abstract fixpoint is related to the concrete fixpoint by the approximation relation expressing the soundness of the abstraction [\(214\)](#page-39-0). This is illusrated in Fig. [12.](#page-11-0)

Fig. 12. Fixpoint Abstraction

Often states have some finite component (e.g. a program counter) which can be used to get a fixpoint system of equations by projection along that component. Then chaotic and asynchronous iteration stategies can be used to solve the equations iteratively [\(209\)](#page-38-8). Various efficient iteration strategies have been studied [\(440;](#page-55-0) [123;](#page-32-0) [364;](#page-50-0) [449;](#page-56-1) [450;](#page-56-2) [441;](#page-55-1) [452;](#page-56-3) [556;](#page-64-7) [617;](#page-68-2) [636;](#page-70-1) [483;](#page-58-1) [692\)](#page-74-0), including ones taking particular properties of abstractions into account [\(129;](#page-32-1) [287;](#page-44-1) [293;](#page-45-4) [421;](#page-54-0) [473;](#page-58-2) [567;](#page-65-0) [572;](#page-65-1) [571;](#page-65-2) [641\)](#page-70-2) and others to speed up the convergence of the iterates [\(208;](#page-38-0) [219;](#page-39-2) [73;](#page-28-0) [207;](#page-38-5) [365;](#page-50-1) [366\)](#page-50-2).

2.10 Composing Abstractions

Abstractions hence abstract interpreters for program analysis can be designed compositionally by stepwise abstraction, combination or refinement [\(214;](#page-39-0) [312;](#page-46-4) [296\)](#page-45-5).

An example of stepwise abstraction is the functional abstraction of Sec. [2.8.](#page-10-1) The abstraction of a function is parameterized by abstractions for the function parameters and the function result which can be chosen later in the modular design of the abstract interpreter. An example of abstraction combination is the reduced product of two abstractions [\(214;](#page-39-0) [163;](#page-35-0) [321\)](#page-47-2) which is the most abstract abstraction more precises than these two abstractions. An example of refinement is the power operation [\(214;](#page-39-0) [298;](#page-45-2) [316;](#page-46-2) [317;](#page-46-3) [318;](#page-47-4) [319\)](#page-47-5) which complete an abstract domain by adding missing disjunctions and the complement [\(185;](#page-36-0) [184\)](#page-36-1) adding missing negations.

It is always possible to refine an abstraction so as to check a given specification for a given program [\(205;](#page-38-7) [322;](#page-47-1) [315;](#page-46-1) [320\)](#page-47-3). Nevertheless this approach has severe practical limitations since, in general, the design of this abstraction is logically equivalent to the design of an inductive argument for the formal proof that the given program satisfies the given specification while the soundness proof of this abstraction logically amounts to checking the inductive verification conditions of this formal proof [\(205\)](#page-38-7). Such proofs can hardly be fully automated hence human interaction is unavoidable. Moreover the whole process has to be repeated each time the program or specification is modified.

Instead of considering such strong specifications for a given specific program, the objective of program analysis is to consider (often predefined) specifications and all possible programs. The practical problem in program analysis is therefore to design useful abstractions which are computable for all programs and expressive enough to yield interesting information for most programs.

3 Program Analysis

Program analysis is the automatic static determination of dynamic run-time properties of programs.

3.1 Foundational Ideas of Program Analysis

Given a program and a specification, a program analyzer will check if the program semantics satisfies the specification (Fig. $13(a)$). In case of failure, the analyser will provide hints to understand the origin of errors (e.g. by providing necessary conditions to be satisfied by counter-examples).

The principle of the analysis is to compute an approximate semantics of the program in order to check a given specification. Abstract interpretation is used to derive, from a standard semantics, the approximate and computable abstract semantics. The derivation can often be done by composing standard abstractions to fit a particular kind of information which has to be discovered about program execution. This derivation is itself not (fully) mechanizable but static analyser generators such as PAG [\(288;](#page-44-2) [10\)](#page-22-0), GENA [\(285\)](#page-44-3)and others [\(31;](#page-24-1) [201;](#page-38-9) [202;](#page-38-10) [274;](#page-43-1) [273;](#page-43-2) [277;](#page-43-3) [278;](#page-43-4) [682;](#page-73-1) [431;](#page-55-2) [484;](#page-59-2) [485;](#page-59-1) [586;](#page-66-0) [491;](#page-59-3) [576;](#page-65-3) [118\)](#page-31-0) can provide generic abstractions to be composed with problem specific ones.

Fig. 13. Program Analysis

In practice, the program analyser contains a generator reading the program text and producing equations or constraints which solution is a computer representation of the program abstract semantics. A *solver* is then used to solve these abstract equations/constraints. A popular resolution method is to use iteration. In this case the convergence may have to be accelerated using widening to over estimate the solution followed by a narrowing to improve it [\(208;](#page-38-0) [192;](#page-37-0) [219\)](#page-39-2). The approximation of the abstract semantics is then used by a diagnoser to check the specification. Because of the loss of information, the diagnosis is always of the form "yes", "no", "unknown" or "irrelevant" (e.g. a safety specification for unreachable code). The general structure of program analysers is illustrated in Fig. [13\(b\).](#page-13-1)

3.2 Shortcomings of Program Analysis

Static program analysis can be used for large programs (220 000 lines of C) without user interaction. The abstractions are chosen to be of wide scope without specialization to a particular program. Abstract algebras can be designed and implemented into libraries which are resuable for different programming languages. The objective is to discover invariants that are likely to appear in many programs so that the abstraction must be widely reusable for the program analyzer to be of economic interest.

The drawback of this general scope is that the considered abstract specifications and properties are often simple, mainly concerning elementary safety properties. For example non-linear abstractions of sets of points are very difficult et very few mathematical results are of practical interest and directly applicable to program analysis [\(40\)](#page-25-0). Checking termination and similar liveness properties is trivial with finite state systems, at least from a theoretical if not algorithmical point of view (e.g. finding loops in finite graphs). The same problem for infinite state systems with potentially infinite data structures (as considered e.g. in partial evaluation (446)) requires the discovery of variant functions which is also very difficult in full generality [\(15;](#page-23-2) [27;](#page-24-2) [78;](#page-28-1) [77;](#page-28-2) [221;](#page-39-3) [328;](#page-47-6) [459;](#page-57-2) [501;](#page-60-3) [544;](#page-63-2) [616;](#page-68-3) [657;](#page-71-0) [592;](#page-66-1) [693\)](#page-74-1) and even more for fair concurrent systems [\(514\)](#page-61-1).

Even when considering restricted simple abstract properties, the semantics of real-life programming languages is very complex (recursion, concurrency, modularity, etc.) whence so is the corresponding abstract interpreter. The abstraction of this semantics hence the design of the analyzer is mostly manual (and beyond the hability of casual programmers or theorem provers) whence costly. The considered abstractions must have a large scope of application and must be easily reusable to be of economic interest.

From a user point of view, the results of the analysis have to be presented in a simple way (for example by pointing at errors only or by providing abstract counter-examples, or less frequently concrete ones). Experience shows that the cases of uncertainty represent 5 to 10 % of the possible cases. They must be handle with other empirical or formal methods (including more refined abstract interpretations).

3.3 Applications of Program Analysis

Among the numerous applications of program analysis, let us cite Data flow analysis [\(226;](#page-40-1) [214;](#page-39-0) [503;](#page-60-4) [620;](#page-68-4) [631;](#page-69-2) [632;](#page-69-3) [624\)](#page-69-4); program optimization [\(121;](#page-32-2) [120\)](#page-32-3) and transformation [\(69;](#page-27-2) [67;](#page-27-3) [518;](#page-61-4) [562\)](#page-64-8) (including partial evaluation and program specialization [\(445;](#page-56-5) [295;](#page-45-6) [307;](#page-46-5) [384;](#page-52-0) [443;](#page-56-6) [444;](#page-56-7) [570;](#page-65-4) [605;](#page-67-2) [489\)](#page-59-4) and data dependence analysis for the parallelisation of sequential languages [\(229;](#page-40-2) [361;](#page-50-3) [454;](#page-56-8) [458;](#page-57-3) [525;](#page-62-2) [615;](#page-68-5) [666;](#page-72-3) [678;](#page-73-2) [679\)](#page-73-3)); set-based analysis [\(222;](#page-39-4) [6;](#page-22-1) [281;](#page-44-4) [388;](#page-52-1) [387;](#page-52-2) [389;](#page-52-3) [390\)](#page-52-4); Type *inference* [\(200;](#page-38-11) [210\)](#page-38-12) (including undecidable systems $(536; 538)$ $(536; 538)$ $(536; 538)$ and soft typing [\(109;](#page-31-1) [302;](#page-45-7) [701\)](#page-74-2)); Verification of reactive [\(433;](#page-55-3) [294;](#page-45-8) [354;](#page-50-4) [357\)](#page-50-5), real-time [\(360\)](#page-50-6) and (linear) hybrid systems $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ $(359; 245; 395; 396; 580)$ including state space reduction $(223; 76)$ $(223; 76)$ $(223; 76)$; cryptographic protocol analysis (533) ; Abstract model-checking of infinite systems [\(224;](#page-39-6) [226;](#page-40-1) [257\)](#page-42-0); Abstract debugging, testing and verification [\(193;](#page-37-8) [72;](#page-28-4) [74;](#page-28-5) [176;](#page-36-2) [174;](#page-36-3) [175;](#page-36-4) [173;](#page-36-5) [172;](#page-36-6) [225;](#page-39-7) [303;](#page-45-9) [577\)](#page-65-6); Cache and pipeline behavior pre-diction [\(289;](#page-44-5) [9;](#page-22-2) [633\)](#page-69-5); Probabilistic analysis [\(534;](#page-62-5) [108\)](#page-31-2); Communication topology analysis for mobile/distributed code [\(292;](#page-45-10) [167;](#page-35-1) [291;](#page-44-6) [370;](#page-51-0) [152;](#page-34-0) [614;](#page-68-6) [687;](#page-73-4) [688\)](#page-73-5); Automatic differentiation of numerical programs [\(665\)](#page-72-4); Abstract simulation of temporal specifications [\(107\)](#page-31-3); Semantic tattooing/watermarking of software; etc.

Program static analysis has been intensively studied for grammars and polynomial systems [\(197;](#page-37-4) [532\)](#page-62-6), term graph rewriting [\(339;](#page-48-7) [340;](#page-48-8) [130;](#page-32-4) [131\)](#page-32-5), typesetting languages [\(406;](#page-53-2) [405\)](#page-53-3), procedural languages [\(70;](#page-27-4) [211;](#page-38-13) [71\)](#page-28-6) (for alias analysis [\(689;](#page-74-3) [91;](#page-29-2) [250;](#page-41-1) [259;](#page-42-1) [260;](#page-42-2) [261;](#page-42-3) [362;](#page-50-8) [399;](#page-53-4) [407;](#page-53-5) [428;](#page-55-4) [516;](#page-61-5) [608;](#page-68-7) [686\)](#page-73-6), pointer analysis [\(262;](#page-42-4) [267;](#page-43-5) [112;](#page-31-4) [310;](#page-46-6) [635;](#page-70-3) [622;](#page-69-6) [623\)](#page-69-7), parameter boxing/unboxing [\(341\)](#page-49-6), copy elimination [\(634\)](#page-69-8), dependence analysis [\(507;](#page-60-5) [606;](#page-67-3) [679\)](#page-73-3), exception analysis [\(628\)](#page-69-9), constant propagation [\(468\)](#page-57-4), (linear) equality or inequality relationskips analysis [\(227;](#page-40-0)

[461;](#page-57-5) [272;](#page-43-6) [353\)](#page-49-4) etc.), parallel procedural languages [\(230;](#page-40-3) [338;](#page-48-9) [127;](#page-32-6) [128;](#page-32-7) [132;](#page-33-0) [133;](#page-33-1) [168;](#page-35-2) [233;](#page-40-4) [660;](#page-71-1) [472\)](#page-58-3), functional languages (for binding time analysis [\(685;](#page-73-7) [19;](#page-23-3) [90;](#page-29-3) [92;](#page-29-4) [243;](#page-41-2) [308;](#page-46-7) [391;](#page-52-7) [393;](#page-52-8) [422;](#page-54-1) [481;](#page-58-4) [456;](#page-57-6) [569;](#page-65-7) [587;](#page-66-2) [621;](#page-69-10) [654\)](#page-71-2), strictness analysis [\(101;](#page-30-1) [220;](#page-39-8) [550;](#page-64-9) [29;](#page-24-3) [37;](#page-25-1) [100;](#page-30-2) [97;](#page-30-3) [102;](#page-30-4) [98;](#page-30-5) [178;](#page-36-7) [244;](#page-41-3) [259;](#page-42-1) [279;](#page-44-7) [392;](#page-52-9) [409;](#page-53-6) [414;](#page-54-2) [419;](#page-54-3) [420;](#page-54-4) [434;](#page-55-5) [436;](#page-55-6) [439;](#page-55-7) [442;](#page-56-9) [451;](#page-56-10) [477;](#page-58-5) [478;](#page-58-6) [510;](#page-61-6) [511;](#page-61-7) [539;](#page-63-4) [549;](#page-63-5) [560;](#page-64-10) [566;](#page-65-8) [565;](#page-65-9) [574;](#page-65-10) [247;](#page-41-4) [642;](#page-70-4) [643;](#page-70-5) [642;](#page-70-4) [644;](#page-70-6) [653;](#page-71-3) [655;](#page-71-4) [697;](#page-74-4) [702\)](#page-75-0), inverse image analysis [\(271;](#page-43-7) [270;](#page-43-8) [415;](#page-54-5) [412;](#page-53-7) [411;](#page-53-8) [413\)](#page-54-6), projection analysis [\(99;](#page-30-6) [416;](#page-54-7) [417;](#page-54-8) [480;](#page-58-7) [482;](#page-58-8) [595;](#page-67-4) [645;](#page-70-7) [698\)](#page-74-5), comportment analysis [\(221;](#page-39-3) [557;](#page-64-11) [596;](#page-67-5) [597\)](#page-67-6), dependency analysis [\(59\)](#page-27-5), path/trace analysis [\(169;](#page-35-3) [58;](#page-26-1) [57\)](#page-26-2), closure analysis [\(588;](#page-66-3) [20;](#page-23-4) [21;](#page-23-5) [228;](#page-40-5) [531\)](#page-62-7), control flow analysis [\(649;](#page-71-5) [251;](#page-41-5) [284;](#page-44-8) [429;](#page-55-8) [542;](#page-63-6) [578;](#page-65-11) [579;](#page-65-12) [590;](#page-66-4) [590;](#page-66-4) [618;](#page-68-8) [658;](#page-71-6) [669;](#page-72-5) [681\)](#page-73-8), value flow analysis [\(62;](#page-27-6) [410;](#page-53-9) [543;](#page-63-7) [650;](#page-71-7) [703\)](#page-75-1), compile-time garbage collection [\(418\)](#page-54-9), stackability and escape analysis [\(55;](#page-26-3) [32;](#page-24-4) [368\)](#page-51-1), data structures and abstract data type analysis [\(494;](#page-59-5) [42;](#page-25-2) [435;](#page-55-9) [437;](#page-55-10) [438;](#page-55-11) [573;](#page-65-13) [646\)](#page-70-8), heap shape analysis [\(447;](#page-56-11) [663;](#page-71-8) [327;](#page-47-7) [309\)](#page-46-8), exception analysis [\(705;](#page-75-2) [704;](#page-75-3) [706\)](#page-75-4), polymorphic function analysis [\(34;](#page-25-3) [5;](#page-22-3) [33;](#page-24-5) [177\)](#page-36-8), kind/sort analysis [\(351;](#page-49-7) [122\)](#page-32-8), typing [\(200;](#page-38-11) [179;](#page-36-9) [367;](#page-50-9) [378;](#page-51-2) [379;](#page-51-3) [474;](#page-58-9) [475;](#page-58-10) [526;](#page-62-8) [529;](#page-62-9) [535;](#page-62-10) [400;](#page-53-10) [537;](#page-63-8) [538;](#page-63-3) [536;](#page-62-3) [551;](#page-64-12) [552\)](#page-64-13), effect systems [\(455;](#page-57-7) [668;](#page-72-6) [568;](#page-65-14) [423;](#page-54-10) [424;](#page-54-11) [674\)](#page-72-7), termination analysis [\(592\)](#page-66-1), time complexity analysis [\(612;](#page-68-9) [268;](#page-43-9) [627;](#page-69-11) [696\)](#page-74-6), parallelization [\(677\)](#page-73-9), etc.), functional parallel languages [\(234;](#page-40-6) [231;](#page-40-7) [232;](#page-40-8) [408;](#page-53-11) [499\)](#page-60-6), data parallel languages [\(119\)](#page-31-5), logic languages including Prolog [\(217;](#page-39-9) [248;](#page-41-6) [84\)](#page-29-5) (for mode [\(521;](#page-61-8) [252;](#page-42-5) [253;](#page-42-6) [498;](#page-60-7) [519;](#page-61-9) [520;](#page-61-10) [522;](#page-61-11) [667;](#page-72-8) [425\)](#page-54-12) and type analysis [\(404;](#page-53-12) [36;](#page-25-4) [38;](#page-25-5) [430;](#page-55-12) [301\)](#page-45-11) and their combination [\(83\)](#page-29-6), finiteness analysis [\(52\)](#page-26-4), relational argument size analysis [\(637;](#page-70-9) [652\)](#page-71-9), dependency analysis [\(548;](#page-63-9) [18;](#page-23-6) [17;](#page-23-7) [113;](#page-31-6) [114;](#page-31-7) [306\)](#page-46-9), detecting determinate/functional computations [\(323\)](#page-47-8), mutually exclusive rules detection [\(604\)](#page-67-7), occur check reduction [\(656\)](#page-71-10), WAM code optimization [\(236\)](#page-40-9), copy avoidance [\(305\)](#page-46-10), groundness analysis [\(188;](#page-37-9) [157;](#page-34-1) [158;](#page-35-4) [186;](#page-37-10) [186;](#page-37-10) [116;](#page-31-8) [505;](#page-60-8) [613;](#page-68-10) [640\)](#page-70-10), sharing analysis [\(183;](#page-36-10) [24;](#page-24-6) [25;](#page-24-7) [162;](#page-35-5) [164;](#page-35-6) [162;](#page-35-5) [164;](#page-35-6) [183;](#page-36-10) [397;](#page-53-13) [427;](#page-54-13) [709;](#page-75-5) [707\)](#page-75-6), freeness analysis [\(156;](#page-34-2) [181;](#page-36-11) [398\)](#page-53-14) and their combinations [\(165;](#page-35-7) [80;](#page-28-7) [81;](#page-28-8) [82;](#page-28-9) [349;](#page-49-8) [182;](#page-36-12) [187;](#page-37-11) [286;](#page-44-9) [246;](#page-41-7) [492;](#page-59-6) [547;](#page-63-10) [664\)](#page-72-9), termination analysis [\(459;](#page-57-2) [27;](#page-24-2) [28;](#page-24-8) [78;](#page-28-1) [79;](#page-28-10) [77;](#page-28-2) [254;](#page-42-7) [255;](#page-42-8) [258;](#page-42-9) [638;](#page-70-11) [328;](#page-47-6) [490;](#page-59-7) [501;](#page-60-3) [544;](#page-63-2) [602;](#page-67-8) [616;](#page-68-3) [657;](#page-71-0) [693;](#page-74-1) [694;](#page-74-7) [691;](#page-74-8) [690\)](#page-74-9), time complexity and cost analysis [\(249;](#page-41-8) [2\)](#page-22-4), parallelisation [\(86;](#page-29-7) [87\)](#page-29-8), etc.) including its search rule and the cut [\(300;](#page-45-12) [117;](#page-31-9) [530\)](#page-62-11) and database programming languages [\(12;](#page-23-8) [13;](#page-23-9) [14;](#page-23-10) [43;](#page-25-6) [581;](#page-66-5) [675\)](#page-72-10), concurrent logic languages [\(103;](#page-30-7) [126;](#page-32-9) [159;](#page-35-8) [161;](#page-35-9) [160;](#page-35-10) [651;](#page-71-11) [469;](#page-57-8) [470;](#page-58-11) [471;](#page-58-12) [680\)](#page-73-10), functional logic languages [\(372;](#page-51-4) [45;](#page-25-7) [369;](#page-51-5) [374;](#page-51-6) [710;](#page-75-7) [375\)](#page-51-7), constraint logic languages [\(54;](#page-26-5) [23;](#page-24-9) [68;](#page-27-7) [110;](#page-31-10) [166;](#page-35-11) [269;](#page-43-10) [313;](#page-46-11) [314;](#page-46-12) [371;](#page-51-8) [363;](#page-50-10) [373;](#page-51-9) [432;](#page-55-13) [453;](#page-56-12) [464;](#page-57-9) [115;](#page-31-11) [486;](#page-59-8) [506;](#page-60-9) [524\)](#page-62-12), concurrent constraint logic languages [\(708;](#page-75-8) [282\)](#page-44-10), specification languages [\(326;](#page-47-9) [324;](#page-47-10) [325\)](#page-47-11), synchronous languages [\(357;](#page-50-5) [46;](#page-26-6) [356;](#page-50-11) [437\)](#page-55-10) (such as LUSTRE $(111; 358; 355)$ $(111; 358; 355)$ $(111; 358; 355)$ $(111; 358; 355)$ $(111; 358; 355)$), concurrent/parallel languages [\(216;](#page-39-10) [35;](#page-25-8) [233;](#page-40-4) [1\)](#page-22-5), communicating and distributed languages [\(215;](#page-39-11) [523;](#page-61-12) [125;](#page-32-10) [283;](#page-44-11) [460\)](#page-57-10) and more recently object-oriented languages [\(56;](#page-26-7) [8;](#page-22-6) [256;](#page-42-10) [352;](#page-49-9) [682;](#page-73-1) [488;](#page-59-9) [575;](#page-65-15) [589;](#page-66-6) [591;](#page-66-7) [154;](#page-34-3) [695\)](#page-74-10).

Abstract interpretation has been used (including interval analysis) for the static analysis of the embedded ADA software of the Ariane 5 launcher^{[1](#page-15-0)} [\(479;](#page-58-13) [263\)](#page-42-11). The static program analysis aims at the automatic detection of the defi-

¹ Flight software $(60,000)$ lines of Ada code) and Inertial Measurement Unit $(30,000)$ lines of Ada code).

niteness, potentiality, impossibility or inaccessibility of run-time errors such as scalar and floating-point overflows, array index errors, divisions by zero and related arithmetic exceptions, uninitialized variables, data races on shared data structures, etc. The analyser was able to automatically discover the Ariane 501 flight error. This was a success for the later 50[2](#page-16-0) and 503 flights and the $ARD²$ [\(479;](#page-58-13) [263\)](#page-42-11) and in the verification of avionic software [\(609\)](#page-68-11).

3.4 Industrialization of Static Analysis by Abstract Interpretation

The impressive results obtained by the static analysis of real-life embedded critical software [\(479;](#page-58-13) [609\)](#page-68-11) is quite promising for the industrialization of abstract interpretation.

This is the explicit objective of [AbsInt Angewandte Informatik GmbH](http://www.absint.com) cl created in Germany by R. Wilhelm and C. Ferdinand in 1998 commercializing the program analyser generator PAG and an application to determine the worst-case execution time for modern computer architectures with memory caches pipelines, etc [\(290\)](#page-44-12).

[Polyspace Technologies](http://www.polyspace.com) Polyspace was created in France by A. Deutsch and D. Pilaud in 1999 to develop and commercialize ADA and C program analyzers.

Other companies like [Connected Components Corporation](http://www.concmp.com/index.html) \blacksquare created in the U.S.A. by W.L. Harrison in 1993 use abstract interpretation internally e.g. for compiler design [\(381\)](#page-51-10).

4Abstract Formal Methods

No automatic formal method can ultimately find all errors in a software system and so for their combinations. We will shortly review the automatic formal methods for computer-aided program verification, briefly discussing their principles, advantages and shortcomings. Since program analysis has already been discussed, we now consider typing, model-checking, deductive methods and their combination.

4.1 Typing

Polymorphic typing and type inference [\(526;](#page-62-8) [238\)](#page-40-10) was a definite step in the design of programming languages and compilers [\(379;](#page-51-3) [380\)](#page-51-11). The question for the next decade seems to be to scale to more expressive properties.

Foundational Ideas of Typing Typing is based on decidable program analyses. This approach is always possible by restricting both on specifications (allowed types) and on programs, as shown when considering types as abstract interpretations [\(200\)](#page-38-11). In theory, type systems have a clean presentation of the type analysis (inference algorithm [\(526\)](#page-62-8)) through an equivalent logical formal

² Atmospheric Reentry Demonstrator: module coming back to earth.

system (type verification [\(238\)](#page-40-10). Monomorphic typing [\(400\)](#page-53-10) was extended to polymorphism [\(526\)](#page-62-8), complex data structures, references [\(376;](#page-51-12) [377\)](#page-51-13), exceptions and separate modules [\(378\)](#page-51-2) in a way that scales up for very large programs. It is nicely integrated in the compiler and the certification can go down to the generated code (proof-carrying code [\(559\)](#page-64-14), certified compiler [\(670;](#page-72-11) [540\)](#page-63-11)).

Shortcomings of Typing Type systems (e.g. with subtle subtyping) can be very complex to understand for the casual user. One difficulty is that typing is compositional but not fully abstract (e.g. the same polymorphic code can type differently in different utilization contexts). The interaction with the user is often crude (no hint is given to understand why wrong programs do not type well). It is hardly possible for the user to provide hints to help the typing process. The logical specification of the type system is often inexistent in the reference manual, not equivalent to the type inference algorithm or so inextricable that it is useless both to the programmer and compiler designer. The programs considered in type theory are both complex (higher-order modules) and too restricted (mainly functional languages). The most severe restrictions are on the considered properties (arithmetic, out of range, null pointer dereferencing, … errors are checked at run-time, all liveness properties are ignored). These restrictions and the difficulty to generalize to more expressive properties mainly follow from the encoding of types as terms/formulæ and from the one iterate fixpoint approximation.

4.2 Deductive Methods

Foundational Ideas of Deductive Methods Deductive methods use a (manually designed abstraction of) the program semantics to obtain minimal verification conditions to prove program correctness. These verification conditions can be derived from the program trace semantics by abstract interpretation [\(206\)](#page-38-4). Then a theorem prover [\(585;](#page-66-8) [584\)](#page-66-9) or a proof assistant [\(598;](#page-67-9) [180\)](#page-36-13) is used to check the verification conditions.

Shortcomings of Deductive Methods Deductive methods use the schema of Fig. $13(b)$ but for the fact that the solver is replaced by a verifier or checker thus avoiding fixpoint computations. So the constraints or equations corresponding to the verification conditions are not solved. This means that an inductive argument (e.g. invariant, variant function) has to be provided, generally by the user. Since the implication involved in the verification condition is itself undecidable, the proof verification can only be partially automatized, even though the solution to the equations/constraints is provided. Therefore interaction of the programmer with the prover is ultimately needed. This (wo)man/prover interaction is hard if not despairing, in particular because the size of the proof is often exponential in the program size. Therefore debugging an unsuccessful proof (because of a program error or a prover weakness) can be as complex as (if not much more complex than) debugging the program itself.

An alternative [\(487\)](#page-59-10) consists in restricting the form of predicates considered by the prover, (which is an abstract interpretation $(214, \text{Sec. } 5)$ $(214, \text{Sec. } 5)$). This can go up to unsound verification condition simplifications, essentially to make verifier simpler (e.g. modular arithmetic).

Because theorem provers are driven by unformalized heuristics, and these heuristics and their interactions are changed over time for improving proof strategies, theorem provers are often unstable over time (e.g. proof strategies get changed so that old proofs no longer work). Another weakness which makes interaction with other formal methods somewhat difficult is the uniform encoding of properties as syntactical terms/formulæ (so that e.g. BBDs are hardly efficiently encodable). It follows that the theorem prover has ultimately to be extented with program analysers, model checkers, typing, among others [\(648;](#page-70-12) [582;](#page-66-10) [583;](#page-66-11) [647\)](#page-70-13), often without supporting theory, in particular for mechanizing and combining abstractions.

4.3 Model Checking

Model checking [\(134;](#page-33-2) [607;](#page-68-12) [47;](#page-26-8) [136;](#page-33-3) [140;](#page-33-4) [546\)](#page-63-12) has been very successful for the verification of hardware [\(51;](#page-26-9) [124;](#page-32-11) [235;](#page-40-11) [600\)](#page-67-10), communication protocoles [\(142;](#page-33-5) [64;](#page-27-8) [63;](#page-27-9) [144;](#page-33-6) [143;](#page-33-7) [148\)](#page-34-4), cryptographic protocoles [\(48\)](#page-26-10), and real-time [\(106;](#page-30-8) [75;](#page-28-11) [105;](#page-30-9) [386;](#page-52-10) [385;](#page-52-11) [394;](#page-52-12) [155;](#page-34-5) [699\)](#page-74-11) or probabilistic [\(684;](#page-73-11) [383;](#page-52-13) [26\)](#page-24-10) processes. As far as software systems are concerned, the question for the next decade is whether model checking can be extended to the verification of very large real-life programs.

Foundational Ideas of Model Checking First a model of the program (i.e. manually designed abstraction of the program semantics) must be designed (in the form of a transition system similar to a small step operational semantics). Then a specification of the program must be provided by the user in a very expressive temporal logic [\(603;](#page-67-0) [39\)](#page-25-9). A model checker can then check the specification by exhaustive search/symbolic exploration of the state space.

The spectacular success of model checking followed from the clever design of data structures (e.g. BDDs [\(7;](#page-22-7) [85;](#page-29-9) [96;](#page-30-10) [191;](#page-37-12) [190;](#page-37-13) [517;](#page-61-13) [676\)](#page-72-12) or QDDs [\(65\)](#page-27-10)) and algorithms (e.g. minimal state graph generation (66) , fixpoint computation $(497;$ [44;](#page-25-10) [48;](#page-26-10) [151;](#page-34-6) [145;](#page-34-7) [146;](#page-34-8) [237;](#page-40-12) [276;](#page-43-11) [659;](#page-71-12) [496\)](#page-59-11) or SAT [\(49;](#page-26-11) [4;](#page-22-8) [50\)](#page-26-12)) for representing very large sets of booleans and their transformations.

The approximation is that the model must be finite-state or some form of abstract interpretation must be used [\(137;](#page-33-8) [343;](#page-49-10) [3;](#page-22-9) [41;](#page-25-11) [661;](#page-71-13) [138;](#page-33-9) [141;](#page-33-10) [150;](#page-34-9) [170;](#page-35-12) [171;](#page-35-13) [240;](#page-41-9) [241;](#page-41-10) [239;](#page-41-11) [594;](#page-67-11) [242;](#page-41-12) [342;](#page-49-11) [266;](#page-43-12) [426;](#page-54-14) [465;](#page-57-11) **?**; [462;](#page-57-12) [466;](#page-57-13) [467;](#page-57-14) [495;](#page-59-12) [500;](#page-60-11) [593\)](#page-66-12) to reduce the verification problem to finite state, including symmetries [\(135\)](#page-33-11), etc. Also clever semantics of concurrent systems have been considered, e.g. to avoid the combinatorial explosion of interleaving [\(142;](#page-33-5) [139;](#page-33-12) [599;](#page-67-12) [662\)](#page-71-14).

Another trend in infinite-state model checking consider safety properties only and polyhedral abstractions, with variants (e.g. Presburger arithmetic [\(88;](#page-29-10) [89;](#page-29-11) [700\)](#page-74-12)). This is a direct application of polyhedral program analysis [\(227;](#page-40-0) [353\)](#page-49-4), including the use of widenings. This allows e.g. for the analysis of reactive [\(294;](#page-45-8) [337\)](#page-48-10), real-time [\(354;](#page-50-4) [104;](#page-30-11) [147;](#page-34-10) [149;](#page-34-11) [264;](#page-42-12) [265;](#page-42-13) [382;](#page-51-14) [394;](#page-52-12) [401\)](#page-53-15) and hybrid systems [\(357;](#page-50-5) [11;](#page-22-10) [89;](#page-29-11) [359;](#page-50-7) [360;](#page-50-6) [580\)](#page-65-5).

Shortcomings of Model Checking Although model checking gained a factor of 100 in 10 years, it is very difficult to scale up because of the state explosion problem. So, the necessary restriction to available computer resources often reduces the model checker from formal verification to debugging on part of the state space. Since the model must ultimately be finite (to allow for exhaustive search/symbolic exploration), abstraction is mandatory, which is a very difficult task to do manually and/or is left informal. Moreover, some forms of abstractions (such as interval [\(208;](#page-38-0) [192\)](#page-37-0) or polyhedral [\(227;](#page-40-0) [353\)](#page-49-4) abstractions) do not abstract concrete transition systems into abstract transition systems so that the model checker may not be reusable in the abstract [\(224;](#page-39-6) [205\)](#page-38-7). One can use abstraction for model checking which are complete in that there always exists a program specific abstraction into a finite model to prove a given specification correct (see [\(205\)](#page-38-7) for safety properties) but none will be complete for all programs, even for simple properties as considered in program analysis [\(219\)](#page-39-2). It follows that complete abstractions are difficult and not reusable hence not cost effective.

5 Combining Program Verification Methods

Since no single formal method can ultimately solve the verification problem, a current trend is to combine formal methods.

For example, one can rely on a user designed abstraction and derive a a program finite abtract model by abstract interpretation, prove the correctness of the abstraction by deductive methods and later verify the abstract model by model-checking [\(626;](#page-69-12) [344;](#page-49-12) [619;](#page-68-13) [153;](#page-34-12) [502;](#page-60-12) [625\)](#page-69-13).

A fundamental limitation [\(205\)](#page-38-7) is that the abstraction discovery and the abstract semantics derivation are respectively logically equivalent hence practically as difficult as invariant discovery and invariant verification in a formal proof. So we have the feeling that combination of tools might simplify formal proofs but still will ultimately not solve the program verification problem.

6 Combining Empirical and Formal Methods

Formal methods have made a lot of progress in the last decade. Nevertheless there are few automatic light weight tools to apply them in practice. Integration of such tools is difficult and cannot ultimately solve all verification problems.

It follows that the only mechanical tool for verifying programs, which defaults and incompleteness are well known, is still debugging. There again progress was slow, in particular because theory never took debugging seriously. The main advantage of debugging is that a debugger is a light weight tool which is very easily understood by all programmers. Because of its well-known incredible cost for weak results, debugging may not scale up in the next decade for very large software.

An alternative which still remains to be investigated is the combination of informal methodslike debugging with verification tools. Let us consider for example abstract testing [\(225;](#page-39-7) [72;](#page-28-4) [74;](#page-28-5) [176;](#page-36-2) [174;](#page-36-3) [175;](#page-36-4) [173;](#page-36-5) [172;](#page-36-6) [193;](#page-37-8) [303;](#page-45-9) [577\)](#page-65-6).

The classical debugging methodology consists in running the program on test data, checking if the execution satisfies informal specifications. This process is repeated by providing more tests until reaching a satisfactory coverage.

By an easily understandable analogy, the abstract testing methodology [\(225\)](#page-39-7) consists in computing the abstract semantics for a finitary or infinitary abstraction chosen by the programmer among a predefined palette (not user defined, which would be too difficult). The abstract semantics is then checked against user-provided abstract assertions or the abstraction of a formal specification. This process is repeated with more refined abstractions until enough assertions are proved or no predefined abstraction can do.

Observe that one can prove the absence of (some categories of) bugs, not only their presence. Moreoever abstract evaluation can range from an analogy with program execution to the application of proof methods (using e.g. forward as well as backward reasonings providing abstract counter-examples) without attempting to make a one-shot complete formal proof of the specification.

7 Conclusions on the Past Decade

Full program verification by formal methods (e.g. model checking/deductive methods), which requires user interaction (for discovering an abstraction or inductive argument) is very costly in human resources hence is not likely to scale up for very large software. Abstraction is mandatory for program verification but difficult, hardly automatizable and beyond the common capabilities of most programmers.

Partial program verification by static analysis (with typing being considered as a particular and successfull case) is $\cos t \cdot \text{effective}^3$ $\cos t \cdot \text{effective}^3$ because no user intervention is mandatory for performing the analysis and universal abstractions are reusable hence commercializable.

For large and complex programs, complete verification by formal methods is not likely to be viable at low cost. Program debugging is still and will probably remain for some time the prominent industrial program "verification" method.

In this context, abstract interpretation based program static analysis can be extended to abstract program testing. Abstract interpretation based methods offer powerful techniques which, in the presence of approximation, can be viable alternatives or complements both to the exhaustive search of model-checking and to the partial exploration methods of classical debugging.

³ e.g. less than 0.25\$ per program line costing 50 to 80\$.

8 Grand Challenge for the Next Decade

We believe that in the next decade the software industry will certainly have to face its responsability imposed by a computer-dependent society. Consequently, SOFTWARE RELIABILITY^{[4](#page-21-0)} will be a grand challenge for computer science and practice.

The grand challenge for formal methods, in particular abstract interpretation based formal tools, is both the large scale industrialization and the intensification of the fundamental research effort.

General-purpose, expressive and cost-effective abstractions have to be developped e.g. to handle floating point numbers, data dependences (e.g. for parallelization), liveness properties with fairness (to extend finite-state model-checking to software), probabilistic properties, etc. Present-day tools will have to be enhanced to handle higher-order compositional modular analyses and to new programming paradigms (such as threads, mobile/network programming, etc.), to automatically combine and refine abstracts, to interact nicely with users and other formal or informal methods.

The most challenging objective might be to integrate formal analysis by abstract interpretation in the full software development process.

⁴ other suggestions were "trustworthiness" (C. Jones) and "robustness" (R. Leino).

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