

Specifying Communication in Distributed Information Systems^{*}

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Abstract. In this paper, we present two logics that allow for specifying distributed information systems, emphasizing communication among sites. The low-level logic D_0 offers features that are easy to implement but awkward to use for specification, while the high-level logic D_1 offers convenient specification features that are not easy to implement. We show that D_1 specifications may be automatically translated to D_0 in a sound and complete way. In order to prove soundness and completeness, we define our translation as a simple map of institutions. Our result may be useful for making implementation platforms like CORBA easier accessible by providing high-level planning and specification methods for communication.

1 Introduction

Two logics are presented that allow for specifying distributed information systems, emphasizing communication among sites. The low-level logic D_0 offers features that are easy to implement but awkward to use for specification, while the high-level logic D_1 offers convenient specification features that are not easy to implement.

In this paper, we show that D_1 specifications may be automatically translated to D_0 in a sound and complete way. This suggests a method to use D_1 for high-level planning and specification, and to transform the result to D_0 from which the specification may be more easily implemented.

The result may help to make implementation platforms like CORBA easier accessible. These platforms facilitate implementation of distributed information systems, but high-level planning and specification methods are largely missing. This holds especially for communication issues.

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In [ECS98], we presented the basic idea of the two distributed logics and their translation in an informal way, using an extended example for illustration. The logics used in this paper are simplified versions that keep, however, the essential features.

Among the logic-based formal methods used for specifying information systems, the work reported here is based on experiences with developing the OBLOG family of languages and their semantic foundations. OBLOG is being developed into a commercial product [Esp93]. In the academic realm, there are several related developments: TROLL [HSJ⁺94, JSHS96, SJH93, SHJE94, HJ95, EH96, Har97], GNOME [SR94], LCM [FW93] and ALBERT [DDPW94].

There are other approaches to formal object specification with a sound theoretical basis. The ones most closely related to ours are FOOPS [GM87, RS92, GS95] and MAUDE [Mes93]. FOOPS is based on OBJ3 [GW88] which is in turn based on equational logic. MAUDE is based on rewriting logic that is a uniform model of concurrency [Mes92].

Other language projects working on related ideas are OOZE [AG91] and ETOILE [AB95].

In the OBLOG family, TROLL3 [DH97] is the first to address problems of concurrency and communication, and to integrate benefits from informal methods like OMT [JWH⁺94]. So there is a graphical notation for TROLL3 called OMTROLL. Theoretical foundations of concurrency as applied to this approach have been explored in [ES95, Ehr97, Kus97], among others. [EH96] gives a brief overview of TROLL3 and OMTROLL and their logic foundations. TROLL does not only have a formal syntax and semantics, but also a method and a workbench [HDK⁺97, GK97]. The approach is being developed along with a practical project [KKH⁺96, HDK⁺97, KG98].

For specifying and reasoning about concurrent and distributed systems, two major approaches have been advocated. On one hand, there was a systematic study of the relations and equivalences between behaviours of systems that started in [Mil80] and was subsequently pursued by many people working in process algebra [BK84, Hoa85, HM85, BW90, vG90]. On the other hand, the use of modal logics [Gol92] for characterizing properties of systems has evolved from the early works of Floyd [Flo67] and Hoare [Hoa69] on reasoning about programs. Among them we mention in particular dynamic logics [FL79, Har79, Pel87], temporal logics [Pnu77] and, more recently, logics of knowledge [HM90, HZ92, FHMV95].

The distributed logics defined in this paper are based on temporal logic and an extension towards concurrency called n -agent logic. Temporal logic has been successfully applied to a number of reactive systems specification problems [MP92], it is the simplest logic that can not only deal with safety properties but also with liveness properties [Lam77]. n -agent logic was introduced and developed in [LT87, LMRT91, LRT92, Thi94, Ram96]. An agent corresponds to an object that may be thought of as a site in a distributed system.

There are several distinct approaches to reasoning about concurrency within the framework of temporal logic. The first and simplest accepts the naive view

of a concurrent system modelled by nondeterministic interleaving together with adequate assumptions of fairness [GPSS80, Fra86] on the execution of its components. The use of branching temporal logics like *UB* [BAMP81], *CTL* [CE81] or *CTL** [EH83] and even of linear temporal logic for such purposes has been deeply studied [Pnu77, MP92, Wol95, Pen95]. In particular, most of the work on temporal logics for information systems and object orientation we rely on has been developed in this setting (e.g. [Ser80, SFSE89, FSMS91, FM92, SCS94, SSC95, SSR96, DRCS97, SSC98a]).

However, certain “subtleties” of concurrent systems are lost under such simplifications (see, for instance, [Pra86] for a discussion on the subject). The need for a precise notion of causality as reflected by the time structures adopted for the logics led to the study of partial order temporal logics [PW84, KP87, Pen95].

The basic difference is that the assumption of an omnipresent observer of the entire system being considered is dropped and replaced by a local causal perspective. It is the case of the logics for partially ordered computations introduced by Pinter and Wolper [PW84], of interleaving set temporal logics [KP87] and of temporal logics for reasoning about distributed transition systems [LPRT95], systems with product state spaces [Thi95a], occurrence nets [Rei92] and event structures [Pen88].

n -agent temporal logics can be found within the latter. They adopt event structures [Win87] enriched with information about its sequential agents [LT87] as models of concurrent systems.

This approach already complies with the fact that the view each individual agent may have of the whole distributed system at a particular instant in time is partial, due to the relative autonomy and spatial separation between agents, and has to be supported by communication [LRT92]. n -agent logics can explicitly distinguish sequential agents (localities) in the system, refer to the local viewpoint of each agent, and express communication between agents (the major feature of distribution) [LT87, LRT92, Ram96].

Several versions of n -agent logics can be found, still reflecting different perspectives on how non-local information can be accessed by each agent [Ram96]. The logics D_0 and D_1 we propose assume that an assertion about another agent is only possible at a communication point. But for instance, the logics in [LMRT91] assume that, at each instant, the actual information about another agent is the one corresponding to the last communication with it.

Other n -agent logics [Ram96] do even consider the existence of a “present knowledge” modality allowing reference to non-local properties of agents, cf. [KR94].

In the following section, we outline by means of an example the ideas of D_0 and D_1 and the translation from the latter to the former. In section 3, we present syntax and interpretation of the two logics. The interpretation part refers to event structures but is kept as elementary as possible. In section 4, we give a detailed and precise account of how to reduce D_1 specifications to D_0 specifications. In section 5, we prove soundness and completeness of this reduction. To this end, we get into the institutional framework as defined by [GB92] and

define our translation as a simple map of institutions as defined by [Mes89]. Our soundness and completeness results follow from well known results about institutions and their maps. Finally, concluding remarks in section 6 sum up the message of the paper and outline possibilities for further work.

2 Example

Suppose we want to specify that “*I will next call Jean and tell her to call you afterwards*”. The statement talks about a distributed system with three objects: I (i), Jean (j), and you (u). It says that u hears from i that i will next call j and tell her to call u sometime later. The following picture illustrates the communication structure.

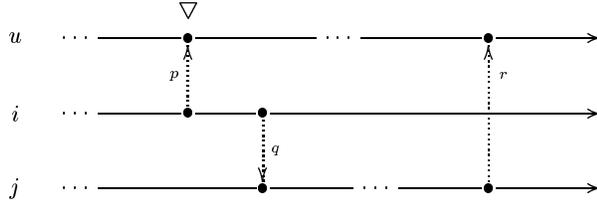


Fig. 1. communication structure of example

$p \equiv$ “ u hears from i that he will next call j and tell her to call u sometime later”;
 $q \equiv$ “ i calls j and tells her to call u afterwards”;
 $r \equiv$ “ j calls u ”.

Formally, the assertions may be expressed as follows. Let $x.\varphi$ mean that the formula φ holds true for object x , and let $x.@y$ mean that x is currently communicating with y .

$u.p$: in u , p holds true;
 $i.(p \Leftrightarrow (@u \wedge (\mathbf{X} q)))$: in i , p means that there is communication with u , and q will hold next;
 $j.(q \Leftrightarrow (@i \wedge (\mathbf{F} r)))$: in j , q means that there is communication with i , and r will hold sometime in the future;
 $u.(r \Leftrightarrow @j)$: in u , r means that there is communication with j .

The fact that p, q and r denote communications may be expressed by

$$\begin{aligned}
&u.(p \Rightarrow i.p) \text{ and } i.(p \Rightarrow u.p), \\
&j.(q \Rightarrow i.q) \text{ and } i.(q \Rightarrow j.q), \\
&u.(r \Rightarrow j.r) \text{ and } j.(r \Rightarrow u.r),
\end{aligned}$$

where p is shared by u and i , q is shared by i and j , and r is shared by u and j . In technical terms, “ p is shared by u and i ” means that there are two distinct propositional symbols, $u.p$ and $i.p$, and the same for q and r .

The formulae are all localized, they state facts from the viewpoints of objects. The communication expressions used so far are basic and simple synchronisation tags and state predicate callings:

- $@y$ is a synchronization tag, expressing that there is communication with y , and
- $(p \Rightarrow y.p)$ is state predicate calling, expressing that if p holds, then there is communication with y , whereupon p holds for y as well.

These are the communication primitives of our communication logic D_0 , see below. These primitives are used in the kernel version 3 of the TROLL specification language. It is straightforward to translate them to C^{++} [HDK+97, KG98].

This way of communication specification, however, is rather low-level. It is awkward because it requires to introduce auxiliary communication predicates, p, q and r in our example, that have no direct real-world meaning, and it requires to introduce many detailed assertions of a purely technical nature.

A higher-level way of expressing communication is conceivable if we allow for *arbitrary statements about other objects within objects*. Following this idea, the above example may be expressed as

$$u.i.(X j.(F @u)).$$

Locally for u , an assertion about i is being made, namely that $(X j.(F @u))$ holds for i . The intended meaning is that u *learns* the truth of this formula from i , namely that next $j.(F @u)$ will hold. The latter means that i learns from j : in her local view, $(F @u)$ holds. This means that, sometime in her future, $@u$ will hold: she will communicate with u .

This is the idea of communication logic D_1 : any assertion about any other object may be made, meaning that there is communication with that other object, and the assertion holds in this other object while communication takes place.

Note that the D_1 formula captures all the information that the above set of D_0 formulae expresses. So there should be a way to recover the D_0 specification from the D_1 specification. And indeed there is, as we show in the subsequent sections.

3 Distributed Logics

We take the view that a distributed system is a collection of communicating sequential objects, each with its own local logic. For object identification, we

Definition 2. Let $i \in I$ be an object. A *life cycle* for i over P is a triple $L_i = (Lv_i, \rightarrow_i^*, \lambda_i)$, where Lv_i and \rightarrow_i^* are as introduced above, and $\lambda_i : Lv_i \rightarrow 2^{P_i}$ is a labelling function.

Definition 3. A *distributed life cycle* over P is an I -indexed family $L = \{L_i\}_{i \in I}$ of object life cycles over P .

The events in a distributed life cycle are given by $Lv = \bigcup_{i \in I} Lv_i$. Sequencing is given by $(\bigcup_{i \in I} \rightarrow_i^*)^*$. Note that the latter is not a total ordering in general. Unrelated events represent concurrency, and events shared by the life cycles of several objects represent synchronous communication.

Note that labelling is individual for objects. That means that an event shared by several objects has several labels, one for each sharing object.

In the sequel, we assume a fixed distributed life cycle L over P .

We first introduce D_0 , the lower-level distributed logic. Remember that the only communication formulae expressible in D_0 are state predicate callings and synchronisation tags.

Definition 4. The set of D_0 formulae over P is

$$D_0(P) ::= \dots \mid D_0^i(P) \mid \dots \quad (i \in I)$$

where, for each $i \in I$,

$$\begin{aligned} D_0^i(P) &::= i.H_0^i(P) \mid i.CC_0^i(P) \\ H_0^i(P) &::= @I^i \mid P_i \mid false \mid (H_0^i(P) \Rightarrow H_0^i(P)) \mid (H_0^i(P) \mathcal{U} H_0^i(P)) \\ CC_0^i(P) &::= \dots \mid (P_i \Rightarrow j.P_j) \mid \dots \quad (j \in I^i). \end{aligned}$$

I^i is defined to be $I \setminus \{i\}$. D_0^i is the logic at locality i with callings to other localities. H_0^i is the “home” logic of object i . CC_0^i are the communication formulae expressible in object i . Note that communication formulae are stand-alone, they may not be embedded as subformulae of other formulae.

For examples of D_0 , we refer to section 2.

The predicates in P are *flexible*, i.e., we intend to give them time-dependent meanings. The other symbols are *rigid*, i.e., we intend to give them time-independent meanings.

false is the usual logical constant, \Rightarrow denotes logical implication, and \mathcal{U} is the *until* temporal operator. $\varphi \mathcal{U} \psi$ means that φ will always be true from the next moment on until ψ becomes true for the next time; φ need not be true any more as soon as ψ holds; ψ must eventually become true.

As usual, we introduce derived connectives, e.g., $\neg \varphi$ for $\varphi \Rightarrow false$, *true* for $\neg false$, $\varphi \vee \psi$ for $\neg \varphi \Rightarrow \psi$, etc. We also make use of derived temporal operators like $X \varphi$ for *false* $\mathcal{U} \varphi$ expressing *next*, $F \varphi$ for $\varphi \vee true \mathcal{U} \varphi$ expressing *sometime*, $G \varphi$ for $\neg(F(\neg \varphi))$ expressing *always*, and $\varphi \mathcal{U}^o \psi$ for $\varphi \wedge \varphi \mathcal{U} \psi$ expressing *from now on ... until ...*

Furthermore, we apply the usual rules for omitting brackets.

Our second distributed logic is D_1 . It generalises D_0 in the sense that there are no special communication formulae: each D_1 formula *of another object* may serve as a communication formula—that may appear anywhere in context.

Definition 5. The set of D_1 formulas over P is

$$D_1(P) ::= \dots | D_1^i(P) | \dots \quad (i \in I)$$

where, for each $i \in I$,

$$\begin{aligned} D_1^i(P) &::= i.H_1^i(P) \\ H_1^i(P) &::= @I^i | P_i | false | (H_1^i(P) \Rightarrow H_1^i(P)) | (H_1^i(P) \mathcal{U} H_1^i(P)) | CC_1^i(P) \\ CC_1^i(P) &::= \dots | D_1^j(P) | \dots \quad (j \in I^i). \end{aligned}$$

It is obvious that $D_0(P) \subseteq D_1(P)$. Therefore, we define the satisfaction relation for a life cycle L on $D_1(P)$ and then just restrict it to $D_0(P)$.

Definition 6. The satisfaction relation $\models_{P,1}$ for L on $D_1(P)$ is defined by

$$L \models_{P,1} i.\varphi \quad \text{iff } L, e \models_{P,1}^i \varphi \text{ holds for every } e \in Lv_i.$$

For each $i \in I$ and $e \in Lv_i$, the relation $\models_{P,1}^i$ for L and e on $H_1^i(P)$ is inductively defined as follows

$$\begin{aligned} L, e \models_{P,1}^i @j & \quad \text{iff } e \in Lv_j; \\ L, e \models_{P,1}^i p & \quad \text{iff } p \in \lambda_i(e); \\ L, e \models_{P,1}^i false & \quad \text{does not hold} \\ L, e \models_{P,1}^i (\varphi \Rightarrow \psi) & \quad \text{iff } L, e \models_{P,1}^i \varphi \text{ implies } L, e \models_{P,1}^i \psi; \\ L, e \models_{P,1}^i (\varphi \mathcal{U} \psi) & \quad \text{iff there is an event } e' \in Lv_i \text{ with } e \rightarrow_i^+ e' \\ & \quad \text{where } L, e' \models_{P,1}^i \psi, \text{ and } L, e'' \models_{P,1}^i \varphi \text{ for every} \\ & \quad \text{event } e'' \in Lv_i \text{ such that } e \rightarrow_i^+ e'' \rightarrow_i^+ e'; \\ L, e \models_{P,1}^i j.\varphi & \quad \text{iff } e \in Lv_j \text{ and } L, e \models_{P,1}^j \varphi. \end{aligned}$$

Definition 7. The satisfaction relation $\models_{P,0}$ for L on D_0^P is defined by

$$L \models_{P,0} i.\varphi \quad \text{iff } L, e \models_{P,0}^i \varphi \text{ holds for every } e \in Lv_i.$$

For each $i \in I$ and $e \in Lv_i$, the relation $\models_{P,0}^i$ for L and e on $H_0^i(P)$ is defined by

$$L, e \models_{P,0}^i \varphi \quad \text{iff } L, e \models_{P,1}^i \varphi.$$

Note that in D_1 , a formula like $i.@j$ is equivalent to $i.j.true$. Still, this last formula is not in D_0 and therefore we chose to keep the $@$ synchronisation tag as primitive also in D_0 . Moreover, it makes the inclusion of $D_0(P)$ into $D_1(P)$ more explicit.

4 Reduction

In this section, we give a precise account on how specifications in $D_1(P)$ can be reduced to specifications in $D_0(P \uplus C)$ where $P = (I, \{P_i\}_{i \in I})$ is a fixed system signature, and C is a new I -indexed family of sets of (communication)

predicates. Naturally, $P \uplus C$ denotes the family $\{P_i \uplus C_i\}_{i \in I}$. \uplus denotes disjoint union.

As illustrated above, the idea is that all communication subformulae in a given formula are replaced by explicit new communication predicates whose meaning is defined to be equivalent to that of the subformulae. Let us recall our example “*I will next call Jean and tell her to call you afterwards*”. In D_1 , this may be expressed by the formula

$$u.i.(X j.(F @u)).$$

The idea is to recurrently scan this formula and replace its innermost communication subformulae by new communication predicates. The process terminates and yields a D_0 formula. Thus, in a first step, we should go as deep as $j.(F @u)$ and introduce a new communication predicate $c(i, j.(F @u))$ to be shared by i and j . By replacing the subformula by the new symbol, we obtain

$$u.i.(X c(i, j.(F @u))).$$

Iterating the process, we have to replace $i.(X c(i, j.(F @u)))$. It occurs in the scope of u , so the new communication predicate is denoted by $c(u, i.(X c(i, j.(F @u))))$ and shared by u and i . After replacing, we obtain

$$u.c(u, i.(X c(i, j.(F @u)))).$$

This formula is already in D_0 .

Note that if we match p with $c(u, i.(X c(i, j.(F @u))))$ and q with $c(i, j.(F @u))$, we obtain the intended result, cf. section 2. However, we do not have a communication predicate corresponding to r : there is no need to replace $@u$ because it is already in D_0 .

The sharing axioms for the new communication predicates are obvious:

$$\begin{aligned} j.(c(i, j.(F @u)) &\Leftrightarrow (@i \wedge (F @u))); \\ i.(c(u, i.(X c(i, j.(F @u)))) &\Leftrightarrow (@u \wedge (X c(i, j.(F @u)))). \end{aligned}$$

In general, for translating $D_1(P)$ formulae, the family C of new communication predicates can be given an inductive definition, according to the motivation above. Remember that $I^i = I \setminus \{i\}$.

Definition 8. For each $i \in I$, let

- $C_i^0 = \emptyset$;
- $C_i^{n+1} = \{c(i, j.\varphi) : j \in I^i, j.\varphi \in D_0(P \uplus C^n)\} \cup \{c(k, i.\psi) : k \in I^i, i.\psi \in D_0(P \uplus C^n)\}$.

The family $C = \{C_i\}_{i \in I}$ is defined by $C_i = \bigcup_{n \in \mathbb{N}} C_i^n$ for each $i \in I$.

As suggested in section 2, all these symbols must be properly axiomatized. The following axioms serve the purpose. Note that they are formulated in the logic $D_0(P \uplus C)$.

Definition 9. The set of axioms corresponding to the family C of new communication predicates is $\star = \bigcup_{i \in I} \star_i \subseteq D_0(P \uplus C)$ where, for each $i \in I$, we have

$$\begin{aligned} \star_i = & \{i.(c(i, j.\varphi) \Rightarrow j.c(i, j.\varphi)) : c(i, j.\varphi) \in C_i\} \cup \\ & \{i.(c(k, i.\psi) \Rightarrow k.c(k, i.\psi)) : c(k, i.\psi) \in C_i\} \cup \\ & \{i.(c(k, i.\psi) \Leftrightarrow (@k \wedge \psi)) : c(k, i.\psi) \in C_i\}. \end{aligned}$$

The first two sets give the sharing axioms for each new communication predicate, while the third set gives the definition axioms for each new symbol.

In order to translate each formula from $D_1(P)$ to $D_0(P \uplus C)$, it suffices to capture the intuition outlined in section 2: we recurrently scan the formula and replace its innermost communication subformulae by their corresponding communication predicates. Clearly, this iteration stops after a finite number of loops—which is the maximum nesting depth of communication subformulae in the given formula. If the maximum nesting depth is m , then only new communication predicates up to C^m are necessary. Thus, if the formula is already in D_0 , it is obvious that $m = 0$ and so no new symbols are needed.

Definition 10. For each $n \in \mathbb{N}$, let $\eta : D_1(P \uplus C^n) \rightarrow D_1(P \uplus C^{n+1})$ be defined by

- $\eta(i.\psi) = i.\psi$ if $i.\psi \in D_0(P \uplus C^n)$;
- $\eta(i.\psi) = i.\psi'$ otherwise,

where ψ' is obtained from ψ by replacing each innermost communication subformula $j.\varphi \in D_0(P \uplus C^n)$ occurring in the scope of k by $c(k, j.\varphi)$.

Definition 11. The translation function $\alpha : D_1(P) \rightarrow D_0(P \uplus C)$ is defined by

- $\alpha(i.\psi) = i.\psi$ if $i.\psi \in D_0(P \uplus C)$;
- $\alpha(i.\psi) = \alpha(\eta(i.\psi))$ otherwise.

Proposition 12. *The translation $\alpha : D_1(P) \rightarrow D_0(P \uplus C)$ as given above is well defined.*

Proof. Each application of η reduces the maximum depth of nesting communication subformulae. The result then follows from the fact that formulae without communication subformulae must be in D_0 . \square

With respect to interpretation structures, it is obvious that a life cycle over P may be obtained from a life cycle over $P \uplus C$ by simply omitting the C symbols from the labelling. That is, for each $i \in I$ and each $e \in Lv_i$, we just consider $\lambda_i(e) \cap P_i$. This is enough to guarantee that our translation is complete.

We prove this in the next chapter, and also that the translation is sound. This is the case because, given any life cycle over P , there is a unique way of extending it to a life cycle over $P \uplus C$ that satisfies \star .

5 Soundness and Completeness

In order to prove soundness and completeness of the reduction translation from D_1 to D_0 , we get into the institutional framework as defined by [GB92] and define our translation as a simple map of institutions as defined by [Mes89]. Our soundness and completeness results follow from well known results about institutions and their maps.

We use the notion of an (elementary) institution. For the purpose of this paper, morphisms between models are not relevant. Just recall that *Set* denotes the category of sets and functions, and *Cls* denotes the category of classes and functions. For an introduction into these and other category theoretic issues, we refer to [Mac71].

Definition 13. An (elementary) institution is a triple (Sig, Sen, Mod, \models) where

- *Sig* is a category (of signatures),
- $Sen : Sig \rightarrow Set$ is a (syntax) functor,
- $Mod : Sig^{op} \rightarrow Cls$ is a (semantics) functor,
- \models is a family of (satisfaction) relations $\{\models_{\Sigma} \subseteq Mod(\Sigma) \times Sen(\Sigma)\}_{\Sigma \in |Sig|}$,

such that the following (satisfaction) condition holds for each signature morphism $\sigma : \Sigma \rightarrow \Sigma'$, $\varphi \in Sen(\Sigma)$ and each model $m' \in Mod(\Sigma')$,

$$m' \models_{\Sigma'} Sen(\sigma)(\varphi) \text{ iff } Mod(\sigma)(m') \models_{\Sigma} \varphi.$$

Both our logics D_0 and D_1 can be seen as institutions. Both share the same category *Sig* whose objects are system signatures with morphisms $\sigma : (I, \{P_i\}_{i \in I}) \rightarrow (J, \{Q_j\}_{j \in J})$ such that $I \subseteq J$ and $\sigma = \{\sigma_i : P_i \rightarrow Q_i\}_{i \in I}$ is a family of functions.

As for the syntax functor Sen_1 of D_1 , it assigns to each signature P the set $Sen_1(P) = D_1(P)$ of its formulae. For each signature morphism $\sigma : P \rightarrow Q$, $Sen_1(\sigma) : D_1(P) \rightarrow D_1(Q)$ is the obvious translation replacing each symbol $p \in P_i$ in a formula by its image $\sigma_i(p) \in Q_i$. The syntax functor Sen_0 of D_0 is a restriction of Sen_1 .

The two logics also share the same model functor *Mod*. To each signature P , *Mod* assigns the class of all distributed life cycles over P . As for signature morphisms $\sigma : P \rightarrow Q$, $Mod(\sigma)$ reduces each distributed life cycle L' over Q to a distributed life cycle L over P by defining $L_i = (Lv'_i, \rightarrow'_i, \sigma_i^{-1} \circ \lambda'_i)$. This means that the event structure is unchanged, and the labels are restricted to those in P .

The satisfaction relations for D_0 and D_1 are given by $\models_{P,0}$ and $\models_{P,1}$, respectively, cf. definitions 6 and 7.

Proposition 14. Both $D_0 = (Sig, Sen_0, Mod, \models_0)$ and $D_1 = (Sig, Sen_1, Mod, \models_1)$ constitute (elementary) institutions.

Proof. In both cases, the satisfaction condition is straightforward and may be proved by induction on the structure of formulae. Since translation of formulae along a signature morphism σ just amounts to replacing each $p \in P_i$ by $\sigma_i(p)$, it is enough to point out the fact that $p \in \sigma_i^{-1}(\lambda'_i(e))$ iff $\sigma_i(p) \in \lambda'_i(e)$. \square

Given any institution (Sig, Sen, Mod, \models) , it is straightforward to define a category $Pres$ of theory presentations whose objects are pairs of the form (Σ, Δ) where $\Delta \subseteq Sen(\Sigma)$, and a morphism $\sigma : (\Sigma, \Delta) \rightarrow (\Sigma', \Delta')$ consists of a signature morphism $\sigma : \Sigma \rightarrow \Sigma'$ such that $Sen(\sigma)(\Delta) \subseteq \Delta'$. It is obvious to define a forgetful functor $S : Pres \rightarrow Sig$ which only keeps the signature from a theory presentation. And it is also obvious to promote the functor $Mod : Sig^{op} \rightarrow Cls$ to a functor $Mod : Pres^{op} \rightarrow Cls$ by defining $Mod((\Sigma, \Delta)) = \{m \in Mod(\Sigma) : m \models_{\Sigma} \delta, \text{ for every } \delta \in \Delta\}$. The satisfaction condition of the institution guarantees that this functor is well defined.

With these auxiliary definitions, we can make precise the notion of a simple map of institutions.

Definition 15. A *simple map* from institution (Sig, Sen, Mod, \models) to institution $(Sig', Sen', Mod', \models')$ is a triple (Φ, α, β) where

- $\Phi : Sig \rightarrow Pres'$ is a functor;
- $\alpha : Sen \Rightarrow Sen' \circ S' \circ \Phi$ is a natural transformation;
- $\beta : Mod' \circ \Phi^{op} \Rightarrow Mod$ is a natural transformation,

such that, for each $\Sigma \in |Sig|$, $\varphi \in Sen(\Sigma)$ and $m' \in Mod'(\Phi(\Sigma))$, the following (structurality) condition holds

$$m' \models'_{S'(\Phi(\Sigma))} \alpha_{\Sigma}(\varphi) \text{ iff } \beta_{\Sigma}(m') \models_{\Sigma} \varphi.$$

We now proceed to state the reduction presented above in terms of a simple map from the institution D_1 to the institution D_0 .

Clearly, Φ shall associate to each system signature P the presentation $(P \uplus C, \star)$ as defined in the previous section. It is obvious to extend this definition to a functor.

α corresponds to the iterative reduction function as defined in the previous section, also called α .

As also presented in the previous section, β simply turns each distributed life cycle L over $P \uplus C$ into a life cycle L over P by forgetting about the new C symbols.

For both α and β , it is straightforward to check that they are natural transformations.

Lemma 16. Let $c(i, j, \varphi) \in C_i$ and L a life cycle over $P \uplus C$ such that $L \models_{P \uplus C, 0} \gamma$, for every $\gamma \in \star$. Then we have that, for each $e \in Lv_i$,

$$L, e \models_{P \uplus C, 0}^i c(i, j, \varphi) \text{ iff } L, e \models_{P \uplus C, 0}^i j, \varphi.$$

Proof. Let $L, e \models_{P \uplus C, 0}^i c(i, j, \varphi)$. Since $i.(c(i, j, \varphi) \Rightarrow j.c(i, j, \varphi)) \in \star$, necessarily also $L, e \models_{P \uplus C, 0}^i j.c(i, j, \varphi)$. Therefore, $e \in Lv_j$ and $L, e \models_{P \uplus C, 0}^j c(i, j, \varphi)$. But $j.c(i, j, \varphi) \Leftrightarrow (@i \wedge \varphi) \in \star$ thus $L, e \models_{P \uplus C, 0}^j \varphi$ and therefore $L, e \models_{P \uplus C, 0}^i j, \varphi$.

On the other hand, let $L, e \models_{P \uplus C, 0}^i j, \varphi$. Necessarily, $e \in Lv_j$ and $L, e \models_{P \uplus C, 0}^j \varphi$. Reusing $j.c(i, j, \varphi) \Leftrightarrow (@i \wedge \varphi) \in \star$, from the fact that $e \in Lv_i$ it follows that

$L, e \models_{P \uplus C, 0}^j c(i, j, \varphi)$. But $j.(c(i, j, \varphi) \Rightarrow i.c(i, j, \varphi)) \in \star$, so $L, e \models_{P \uplus C, 0}^j i.c(i, j, \varphi)$ and thus $L, e \models_{P \uplus C, 0}^i c(i, j, \varphi)$. \square

Proposition 17. *The triple $(\Phi, \alpha, \beta) : D_1 \rightarrow D_0$ constitutes a simple map of (elementary) institutions.*

Proof. The structurality condition is an immediate consequence of the lemma above. In fact, let $i.\varphi \in D_1(P)$ and L a life cycle over $P \uplus C$ such that $L \models_{P \uplus C, 0} \gamma$, for every $\gamma \in \star$. To prove that $L \models_{P \uplus C, 0} \alpha(i.\varphi)$ iff $L \models_{P, 1} i.\varphi$, it is enough to proceed by induction on the maximum nesting depth of communication subformulae in $i.\varphi$. In each step of α , the innermost communication subformulae are replaced by symbols with equivalent meaning as proved in the lemma above. Thus the overall meaning of $i.\varphi$ is maintained. \square

As promised, we now prove that D_0 and D_1 are equally expressible by using well known results about institutions and simple maps.

Given any institution (Sig, Sen, Mod, \models) , we can introduce semantic entailment in the usual way. For each signature $\Sigma \in |Sig|$, we define $\models_{\Sigma} \subseteq \mathcal{P}(Sen(\Sigma)) \times Sen(\Sigma)$ by $\Delta \models_{\Sigma} \varphi$ iff for each $m \in Mod(\Sigma)$, $m \models_{\Sigma} \varphi$ whenever $m \models_{\Sigma} \delta$, for every $\delta \in \Delta$. Of course, although we use the same symbol \models_{Σ} both for satisfaction and entailment, it is easy to distinguish between the two concepts in any given context.

Proposition 18. *Let $(\Phi, \alpha, \beta) : (Sig, Sen, Mod, \models) \rightarrow (Sig', Sen', Mod', \models')$ be a simple map of institutions. Then, for each signature $\Sigma \in |Sig|$, $\Delta \subseteq Sen(\Sigma)$ and letting $\Phi(\Sigma) = (\Sigma', \star')$, the following condition holds*

$$Mod((\Sigma, \Delta)) \supseteq \beta_{\Sigma}(Mod'((\Sigma', \alpha_{\Sigma}(\Delta) \cup \star'))).$$

Consequently, for each $\varphi \in Sen(\Sigma)$, we have that

$$\Delta \models_{\Sigma} \varphi \text{ implies } \alpha_{\Sigma}(\Delta) \cup \star' \models'_{\Sigma'} \alpha_{\Sigma}(\varphi).$$

Proof. Let $m' \in Mod'((\Sigma', \alpha_{\Sigma}(\Delta) \cup \star'))$. This is equivalent to saying that $m' \models'_{\Sigma'} \delta'$ for every $\delta' \in \alpha_{\Sigma}(\Delta) \cup \star'$. Clearly, $m' \in Mod'((\Sigma', \star'))$ and $\beta_{\Sigma}(m')$ is well defined. Thus, by the structurality condition of the map, we have that $\beta_{\Sigma}(m') \models_{\Sigma} \delta$ for every $\delta \in \Delta$ or, equivalently, $\beta_{\Sigma}(m') \in Mod((\Sigma, \Delta))$.

Let us further consider $\varphi \in Sen(\Sigma)$ and assume that $\Delta \models_{\Sigma} \varphi$. As proved before, any $m' \models'_{\Sigma'} \delta'$ for every $\delta' \in \alpha_{\Sigma}(\Delta) \cup \star'$ is such that $\beta_{\Sigma}(m') \models_{\Sigma} \delta$ for every $\delta \in \Delta$. Therefore, by definition of semantic entailment, $\beta_{\Sigma}(m') \models_{\Sigma} \varphi$ and thus $m' \models'_{\Sigma'} \alpha_{\Sigma}(\varphi)$ follows from the structurality condition. \square

This result immediately applies to our reduction map from D_1 to D_0 .

Corollary 19. *Let $\Delta \subseteq D_1(P)$. Then,*

$$Mod((P, \Delta)) \supseteq \beta(Mod((P \uplus C, \alpha(\Delta) \cup \star))).$$

Consequently, for each $i.\varphi \in D_1(P)$,

$$\Delta \models_{P, 1} i.\varphi \text{ implies } \alpha(\Delta) \cup \star \models_{P \uplus C, 0} \alpha(i.\varphi).$$

We may see this property as stating the completeness of our reduction map: everything that can be obtained from the original D_1 specification can also be obtained from its translation into D_0 . Of course, this is a desirable property but it is only meaningful if we can also guarantee soundness. For that purpose we need another general result about simple maps of institutions, cf. [CM93].

Proposition 20. *Let $(\Phi, \alpha, \beta) : (Sig, Sen, Mod, \models) \rightarrow (Sig', Sen', Mod', \models')$ be a simple map of institutions such that each $\beta_\Sigma : Mod'(\Phi(\Sigma)) \rightarrow Mod(\Sigma)$ is surjective. Then, for each signature $\Sigma \in |Sig|$, $\Delta \subseteq Sen(\Sigma)$ and letting $\Phi(\Sigma) = (\Sigma', \star')$, the following condition holds*

$$Mod((\Sigma, \Delta)) = \beta_\Sigma(Mod'((\Sigma', \alpha_\Sigma(\Delta) \cup \star'))).$$

Consequently, for each $\varphi \in Sen(\Sigma)$, we have that

$$\Delta \models_\Sigma \varphi \text{ iff } \alpha_\Sigma(\Delta) \cup \star' \models'_{\Sigma'} \alpha_\Sigma(\varphi).$$

Proof. We need to prove that $Mod((\Sigma, \Delta)) \subseteq \beta_\Sigma(Mod'((\Sigma', \alpha_\Sigma(\Delta) \cup \star')))$. Let $m \models_\Sigma \delta$, for every $\delta \in \Delta$. By the surjectivity of β_Σ , there exists $m' \in Mod'(\Sigma')$ such that $m' \models_{\Sigma'} \star'$ and $\beta_\Sigma(m') = m$. Then, it easily follows from the structurality condition that $m' \models'_{\Sigma'} \alpha_\Sigma(\delta)$ for every $\delta \in \Delta$.

With respect to semantic consequence, given $\varphi \in Sen(\Sigma)$, we have to prove the *if* part. Assume that $\alpha_\Sigma(\Delta) \cup \star' \models'_{\Sigma'} \alpha_\Sigma(\varphi)$ and let $m \models_\Sigma \delta$ for every $\delta \in \Delta$. As shown above, $m = \beta_\Sigma(m')$ for some $m' \in Mod'((\Sigma', \alpha_\Sigma(\Delta) \cup \star'))$. Then, by definition of semantic entailment, $m' \models'_{\Sigma'} \alpha_\Sigma(\varphi)$. Easily now, again by using the structurality condition, we obtain $m \models_\Sigma \varphi$. \square

In order to obtain our soundness result we therefore have to show that our model translation fulfils the surjectivity property stated above.

Proposition 21. *If L is a distributed life cycle over P then it is possible to extend L to $P \uplus C$ in such a way that $L \models_{P \uplus C, 0} \star$.*

Proof. Suppose that $L = \{L_i\}_{i \in I}$ and that each $L_i = (Lv_i, \rightarrow_i^*, \lambda_i)$. The proof proceeds by inductively extending L to L^n by extending its labelling function to $\lambda_i^n : Lv_i \rightarrow 2^{P \uplus C^n}$. Since each $C_i^0 = \emptyset$, we take $\lambda_i^0 = \lambda_i$. In each step, for each new symbol $c(i, j, \varphi) \in C^{n+1} \setminus C^n$, proceed as follows

- first, taking into account the definitional axiom
 - $j.(c(i, j, \varphi) \Leftrightarrow (@i \wedge \varphi))$
 - build $\lambda_j^{n+1}(e)$ by extending $\lambda_j^n(e)$ with $c(i, j, \varphi)$ iff
 - $L^n, e \models_{P \uplus C^n, 0}^j (@i \wedge \varphi)$;
- then, taking into account the sharing axioms
 - $j.(c(i, j, \varphi) \Rightarrow i.c(i, j, \varphi))$ and $i.(c(i, j, \varphi) \Rightarrow j.c(i, j, \varphi))$
 - build $\lambda_i^{n+1}(e)$ by extending $\lambda_i^n(e)$ with $c(i, j, \varphi)$ iff
 - $e \in Lv_j$ and $c(i, j, \varphi) \in \lambda_j^{n+1}(e)$.

Clearly, if we take the limit of this definition, we obtain a life cycle L over $P \uplus C$ that satisfies \star . \square

In fact, it turns out that our model translation is an isomorphism. The uniqueness of the extension presented above can be easily inferred from the proof.

We can now conclude that our reduction map is sound. So we have proved the main result of this paper: any D_1 specification Δ is equivalent to the D_0 specification $\alpha(\Delta) \cup \star$, in the sense that they have exactly the same models once you forget about the new symbols in the labelling.

Theorem 22. *Let $\Delta \subseteq D_1(P)$. Then we have*

$$\text{Mod}((P, \Delta)) = \beta(\text{Mod}((P \uplus C, \alpha(\Delta) \cup \star))).$$

As for entailment, an immediate consequence is the following.

Corollary 23. *For each $i.\varphi \in D_1(P)$, we have*

$$\Delta \models_{P,1} i.\varphi \text{ iff } \alpha(\Delta) \cup \star \models_{P \uplus C,0} \alpha(i.\varphi).$$

We can say even more: the same holds if we do not translate $i.\varphi$ on the right-hand side, and consider entailment in $D_1(P \uplus C)$.

Corollary 24. *Let $\Delta \subseteq D_1(P)$ and $i.\varphi \in D_1(P)$. Then we have*

$$\Delta \models_{P,1} i.\varphi \text{ iff } \alpha(\Delta) \cup \star \models_{P \uplus C,1} i.\varphi.$$

Proof. We are, of course, using the inclusions $D_1(P) \subseteq D_1(P \uplus C)$ and $D_0(P \uplus C) \subseteq D_1(P \uplus C)$. The result immediately follows from the fact that $\text{Mod}((P, \Delta)) = \beta(\text{Mod}((P \uplus C, \alpha(\Delta) \cup \star)))$ and by noting that β just forgets about C symbols, and so does not lose any information which may be relevant for evaluating $i.\varphi$ that is written using only symbols in P . \square

Of course, despite the fact that C is in general a rather large set, in practice, given a finite specification Δ in D_1 only a finite part of C is necessary. In that case, the reduction procedure can be made effective and our equal-expressibility result still applies.

6 Concluding Remarks

The main result presented in this paper is to show how—and prove that— D_1 specifications may be automatically translated to D_0 specifications in a sound and complete way. D_1 is more suitable for specification, and D_0 may be more easily implemented, e.g., translated to C^{++} . This suggests a practical method to use D_1 for high-level planning and specification, especially of communication aspects in distributed information systems. The results may help to make implementation platforms like CORBA easier accessible.

We experimented with D_1 specifications in the framework of a TROLL application project (cf. [ECSD98] for an extended example). The experiences are

encouraging, but further work is needed before D_1 specification can be part of a well-understood methodology.

A thorough study of D_0 and D_1 is still needed. So far, many important theoretical issues with great practical impact remain to be studied. Among these, we should emphasize the analysis of their expressive power, the search for complete axiomatizations and, most of all, decidability results. Another important topic concerns the possibility of encoding D_0 and D_1 into plain old linear temporal logic. A result of “trace consistency”, i.e., invariance under choice of sequentialization [Pel93, Thi95b], then paves the way to an efficient adaptation to our logics of well-known partial-order verification techniques such as model-checking [Val90, GW94, BGS98]. This approach also hints to the possibility of basing a decision procedure for our logics on distributed tableaux methods, in a spirit similar to the one found in [Mas98].

Another interesting problem, related to the expressive power of our logics, is their relationship with other versions of n -agent logics. It is obvious that there is no way in our logics to talk about the last communication with another object, as in [LMRT91], or of asserting that for sure some property must hold for another object even if we are not currently communicating with it, as in [Ram96]. However, it would be quite easy to extend our logics with a since \mathcal{S} operator, with a meaning dual to that of until \mathcal{U} , but referring to the past instead of the future. In that case, the last communication with another agent could be expressed as an abbreviation by

$$i.(\text{LAST}_j \varphi) \equiv i.(j.\varphi \vee ((\neg @j) \wedge ((\neg @j) \mathcal{S} j.\varphi))).$$

That is, “ i knows that φ held for j the last time they talked” is given by “either they are communicating now and φ holds for j , or that is not the case now but it happened sometime in the past and i and j have not talked since then”.

Even more interestingly, present knowledge about another agent can be expressed by

$$i.(\text{NOW}_j \varphi) \equiv i.(j.\varphi \vee ((\neg @j) \wedge ((\neg @j) \mathcal{S} j.(\varphi \mathcal{U} @i)))).$$

That is, “ i is sure that φ must presently hold for j ” is given by “either they are communicating now and φ holds for j , or that is not the case now but sometime ago j ensured that she would have φ until she talked to i again, and they have not talked ever since”.

What is more, all the work on reduction presented in this paper seems to carry on smoothly to this extension with past operators. Moreover, results like decidability or completeness also seem easy to extend, once established for future-only versions.

In fact, a deeper analysis of these distributed logics in terms of general mechanisms for combining the local logics of each object is also in progress [CSS98, SSC98b, SSCM98, SSC97a, SSC97b]. And we expect that this effort may help on several of the open tasks previously mentioned, since general transfer theorems for these combination mechanisms often exist [BdR97a, BdR97b,

FG92, FG96, Gab96b, Gab96a]. In particular, we expect that an axiomatization, decision procedure, etc. for these logics can be obtained by suitably combining the axiomatizations, decision procedures, etc. for the local logics, whenever they exist. This idea is consistent with a remark by R. Ramanujam in [Ram96] about existing axiomatizations for certain versions of n -agent logic: “What is particularly interesting about the axiom systems is that we can present them in two layers: at the local level, we have a system for each agent, and at the global level, a system to put them together”.

At this point, a word of justification is due for getting into the institutional framework. Clearly, we could have stated and proved everything about D_0 and D_1 directly. Even if we were completely unaware of institutions. Or knowing of their existence and importance, we could as well have omitted them from the presentation. However, we are convinced that the importance of general results such as those made available by nearly two decades of research in the field of institutions is not generally recognized. And this paper is a mere example of their usefulness. In fact, not only our logics are much more concisely presented as institutions (although harder to grasp, technically speaking) but also our reduction mechanism, already outlined in [ECSD98], is stated in a much more elegant way. And what is more, we manage to prove the equal-expressibility of D_0 and D_1 in a detailed way, by just applying suitable well-known results about simple maps of institutions.

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