UNIVERSITÀ DEGLI STUDI DI FIRENZE
Dipartimento di Sistemi e Informatica

Dottorato di Ricerca in
Ingegneria Informatica, Multimedialità e Telecomunicazioni
ING-INF/05

FORMAL METHODS
IN THE DEVELOPMENT LIFE CYCLE
OF REAL-TIME SOFTWARE

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Dissertation submitted in partial fulfillment
of the requirements for the degree of
Doctor of Philosophy
in Informatics, Multimedia and Telecommunication Engineering

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XXII Ciclo – 2008-2010
To my parents and Marco
“The best thing for being sad,” replied Merlyn, beginning to puff and blow, “is to learn something. That is the only thing that never fails. You may grow old and trembling in your anatomies, you may lie awake at night listening to the disorder of your veins, you may miss your only love, you may see the world about you devastated by evil lunatics, or know your honour trampled in the sewers of baser minds. There is only one thing for it then – to learn. Learn why the world wags and what wags it. That is the only thing which the mind can never exhaust, never alienate, never be tortured by, never fear or distrust, and never dream of regretting. Learning is the thing for you. Look at what a lot of things there are to learn.”

Terence Hanbury White

The Once and Future King - The Sword in the Stone
This thesis was reviewed by Prof. Susanna Donatelli (University of Turin), Prof. Giuseppe Lipari (Scuola Superiore Sant’Anna - Pisa), and Prof. Tullio Vardanega (University of Padua), whom I sincerely thank for their valuable comments and suggestions.
Acknowledgements

I would like to sincerely thank my advisor Prof. Enrico Vicario, for his guidance and support during these three years, for his expertise and enthusiasm. I would also like to thank Prof. Giacomo Bucci, for his experience and advice.

A special thank goes to Luigi Sassoli, for his valuable and helpful suggestions during the first year of my PhD course, for his patience in answering my frequent questions, for the time spent in interesting and fruitful discussions.

I am very grateful to Leonardo Grassi, Lorenzo Ridi, and Irene Bicchierai, working with them has been a pleasure to me. I would also like to thank present and past people in the Software Technologies Laboratory at the University of Florence: Jacopo Torrini, Valeriano Sandrucci, Andrea Tarocchi, Francesco Poli, Fabrizio Baldini, Graziella Magnolfi, Jacopo Baldanzi, Luca Romano. Thanks for your support and for our funny talks about informatics, life, politics, food, and football.

Words cannot express my love and gratitude to my parents, for making my life so special. Last but certainly not least, thanks to Marco, for what was, what is, and what will be.
Abstract

Preemptive Time Petri Nets (pTPNs) support modeling and analysis of concurrent timed software components running under fixed priority preemptive scheduling. The model is supported by a well-established theory based on symbolic state-space analysis through Difference Bounds Matrix (DBM), with specific contributions on compositional modularization, trace analysis, and efficient over-approximation and clean-up in the management of suspension deriving from preemptive behavior.

The aim of this dissertation is to devise and implement a framework that brings the theory to application. To this end, the theory is cast into an organic tailoring of design, coding, and testing activities within a V-Model software life cycle in respect of the principles of regulatory standards applied to the construction of safety-critical software components. To implement the tool-chain subtended by the overall approach into a Model Driven Development (MDD) framework, the theory of state-space analysis is complemented with methods and techniques supporting semi-formal specification and automated compilation into pTPN models and real-time code, measurement-based Execution Time estimation, test-case selection and sensitization, coverage evaluation.
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SD2 System Design ..................................................... 33

SD3 Software/Hardware Requirements Analysis ..................... 34

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TPN Time Petri Net .................................................... xi

UML Unified Modeling Language ...................................... 35

UP Unified Process ..................................................... 32
WCET  Worst Case Execution Time ........................................ 11

WCCT  Worst Case Completion Time .................................... 65

XP   eXtreme Programming ............................................. 32
Intertwined effects of concurrency and timing comprise one of the most challenging factors of complexity in the development of safety-critical software components. Formal methods may provide a crucial help in supporting both design and verification activities, reducing the effort of development, and providing a higher degree of confidence in the correctness of products.

Integration of formal methods in the industrial practice is explicitly encouraged in certification standards such as RTCA/DO-178B [60], with specific reference to software with complex behavior deriving from concurrency, synchronization, and distributed processing. The RTCA/DO-178B standard recommends that the proposed methods are smoothly integrated with design and testing activities prescribed by a defined and documented software life cycle. In particular, this recommendation can be effectively referred to the framework of the V-Model [42], which is often adopted by process oriented standards ruling the development of safety-critical software subject to explicit certification requirements, such as airborne systems [60], railway and transport applications [50], medical control devices [77]. The integration of formal methods along multiple activities of the software life cycle is also a typical approach to Model Driven Development (MDD), where Domain Specific Modeling Languages (DSMLs) enable the formalization of system requirements and design, and transformation engines support the development of generators of concrete artifacts that may include code, documentation, complementary models, tests...
In this context, the adoption of formal methods may serve to attain various degrees of rigor, ranging from non-ambiguous specification to support for manual verification and even to automated verification [60].

Various tools [90], [14], [69] have been described and experimented in the application of the MDD concept, with different goals in the aspects of model formalization, implementation, and verification. Simulink [90] is a tool for mathematical modeling and simulation of complex control systems, based on a block diagram paradigm. Integrated within MATLAB environment [88] and coupled with other facilities such as Real-Time Workshop [89], Simulink supports automated generation of real-time C-code for a large variety of platforms and Real-Time Operating Systems (RTOSs). The direct translation of block diagrams into executable code emphasizes performance and signal-flow optimizations over correctness-related issues while hiding the effect of concurrency on resources allocation and usage. Charon [14] is a language for the specification of interacting hybrid systems and provides a modular description of both architectural and behavioral aspects. The conformance of the model with hybrid state machines allows the adoption of formal analysis techniques for validation purposes [12]. Code generation experiences from Charon models [13] are mainly focused on the preservation of concurrency correctness and mathematical constraints (i.e., differential or algebraic equations representing system dynamics), as this may be jeopardized by the discrepancy between continuous/concurrent behavior of the model and the discrete/preemptive behavior of the target platform. The Giotto Language [69] realizes a separation of concerns along the orthogonal issues of timing and functionality, through the introduction of an intermediate layer of abstraction between the mathematical model and the corresponding generated code. This layer defines an embedded software model, i.e., a solution to a given control problem that takes into account timing and concurrency constraints while neglecting functionality concerns and platform-dependent choices such as scheduling or preemption policies [70]. The actual execution of the generated software components on a target platform relies on the use of a Virtual Machine (called Embedded Machine) that accounts for scheduling, preemption, and resource allocation.
policies.

A different approach able to reduce the step of code generation to the synthesis of an on-line controller was proposed in [11], where the state-space of a discrete time model is enumerated and used to identify and synthesize an on-line controller that keeps the execution of the system within a range of correct behavior. A similar approach is reported in a continuous time setting in [122]. In both the cases, the exhaustive enumeration of the state-space becomes a precondition for the implementation stage, and on-line control puts an overhead on timing resources. Furthermore, the resulting code structure does not meet consolidated design and implementation practices, thus preventing smooth integration within an existing development software life cycle. In the Uppaal tool [22] various activities along the life cycle are supported by relying on the formal nucleus of Timed Automata. This supports state-space analysis based on Difference Bounds Matrix (DBM) theory, test case selection and execution [72], [84], and synthesis of a controller that drives the system along selected behaviors in the state-space [49]. However, the model does not encompass representation of suspension, thus ruling out the case of real-time systems running under preemptive scheduling. In the Times tool of Uppaal [15], the limitation is partially circumvented by resorting to the model of Timed Automata with Tasks (TAT) [59] through the composition of a model of asynchronous task releases and the usage of the analysis technique of [91], but this requires Execution Times of tasks to be deterministic integer values, which comprises an assumption that is not met in a large class of practical applications [124].

The model of Time Petri Nets (TPNs) is extended by preemptive Time Petri Nets (pTPNs) [34], [33] with a concept of resource that supports representation of suspension in the advancement of clocks. This realizes the so-called Preemptive ReSume execution policy (PRS) [87], providing an expressivity which compares to stopwatch automata [58] and Petri Nets with hyper-arcs [106], and which enables convenient modeling of the usual patterns of concurrency encountered in the practice of real-time systems [34], [33]. The analysis technique reported in [36] enumerates an over-approximation of
the state state-space that maintains the efficiency of DBM encoding of state
classes, and that supports exact identification of feasible timings of selected
behaviors through a clean-up algorithm. This enables efficient verification of
properties pertaining to reachability under timing constraints and to the sa-
tisfaction of real-time deadlines. Preliminary experimentations on the use of
pTPNs in individual steps of the construction of real-time software were re-
ported in [43], [44], [47], [46], about disciplined manual translation of pTPN
models into code running under RTAI [95], about the execution of timed test-
cases, and about a software framework supporting agile model transformations.

This dissertation develops and integrates the theory of pTPNs in order to
cast it into a comprehensive methodology that comprises an instance (tailo-
ring) of the V-Model framework [42]. To this aim, this work develops the way
how the theory of pTPNs is applied to support in organic manner: semi-formal
specification of real-time software components and automated translation into
the corresponding pTPN model; generation of code running under RTAI [95]
and preserving sequencing and timeliness properties; Execution Time profiling;
test case selection and sensitization, oracle verdict, and coverage evaluation.
Experimentation on a case example is reported to demonstrate the feasibility
and effectiveness of the approach.

The dissertation is organized in five chapters.

• Chapter 1 resumes characteristics and peculiarities of RTOSs, describes
  the architecture and the main features of RTAI [95], and devises a for-
  mal approach that applies the theory of pTPNs to the construction of
  real-time software components, reporting the principles of the V-Model
  software life cycle and introducing a running case example.

• Chapter 2 recalls the formal nucleus of pTPNs, devising their expressivity
  and state-space analysis techniques, illustrates the application of trace
  analysis to a concrete case, and discusses how common patterns of task
  concurrency and interaction can be effectively modeled through pTPNs.
• Chapters 3 describes two approaches to semi-formal specification of real-time software components and illustrates how pTPN models can be derived from semi-formal specifications.

• Chapter 4 illustrates how a semi-formal specification can be translated into code that preserves semantic properties of the corresponding pTPN model, enabling the definition of a measurement-based approach to Execution Time profiling based on pTPNs. An experimental assessment is provided to evaluate the accuracy of measures.

• Chapter 5 discusses how the pTPN model of real-time software supports test case selection and execution through state-space enumeration and trace analysis, how it allows the definition of different oracles for the evaluation of executed tests, and provides a measure of attained coverage.

• Chapter 6 resumes the methodology proposed in this dissertation with reference to a case example.
Chapter 1

A formal methodology for the development of real-time software

This Chapter resumes the main features of RTOSs and focuses on peculiarities of RTAI [95], the RTOS employed in the experimentation described in this work. Then, it provides a brief overview of software development processes and devises a formal approach that casts the theory of pTPNs within the V-Model software life cycle [42] in order to support the construction of real-time software components.

1.1 Real-time operating systems

Real-time systems are computing systems that must reach with precise time constraints to events in the environment [39]. The correct behavior of these systems depends not only on the logical result of the computation but also on the time at which the results are produced. Nowadays, a wide and increasing spectrum of complex systems relies, in part or completely, on real-time computing capabilities, from industrial automation to robotics, from automotive
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applications to railway and flight control systems, from military systems to space missions, from embedded systems to multimedia applications and virtual reality. As a consequence, the domain of real-time systems has become one of the most active and challenging research areas within computer science.

Despite the large application domain, many researchers, developers, and technical managers have serious misconceptions about real-time computing [112]. In fact, real-time systems are often erroneously said to be fast systems that quickly react to external events, and most real-time control applications are still designed using ad-hoc methods and heuristic approaches. These techniques often rely on the implementation of large portions of code in assembly language, on timers programming, on the development of low-level drivers for device handling, and on the manipulation of task and interrupt priorities. Although this approach produces code that can be optimized to run very fast, it implies various drawbacks:

- **Tedious programming.** Implementing complex control applications in assembly language is much more difficult and time consuming than using a high-level programming language. Moreover, the efficiency and the reliability of the code strongly relies on the ability of the programmer.

- **Difficult code understanding.** Programs written in assembly code are much more difficult to understand than those developed in high-level programming languages. In addition, clever hand-coding introduces additional complexities and makes assembly programs even more cryptic: the more the program gains in efficiency, the less intelligible it gets.

- **Difficult code maintainability.** Maintenance of assembly code becomes much more difficult as the complexity of the program increases, even for the original programmer.

- **Difficult verification of time constraints.** Verification of timing constraints becomes actually impractical without the support of specific tools and methodologies for code and schedulability analysis.
As a major consequence, software developed following empirical techniques can be highly unpredictable. Advances in computer hardware technology will improve system throughput and will increase the computational speed, but they will not be able to take care of any real-time requirement. In fact, whereas the objective of fast computing is to minimize the average response time of a given set of tasks, the objective of real-time computing is to meet the individual timing requirement of each task [112]. Hence, however short the average response time can be, if no formal methodology is adopted to support a priori verification of all timing constraints of the application and if the underlying operating system does not provide specific features to handle real-time tasks, then it is impractical to foresee certain rare but possible situations that lead to a system collapse. This is especially serious in the context of control applications for critical systems, where a failure can be catastrophic and may injure people or cause heavy damage to the environment.

A more robust guarantee of the performance of a real-time system under all workload conditions can be achieved only through more sophisticated design methodologies, static analysis of the source code, and specific operating systems mechanisms. The latter are purposely designed to support computation under timing constraints and they include scheduling algorithms, mutual exclusion and synchronization mechanisms, Inter Process Communication (IPC) mechanisms, interrupt and memory handling. Moreover, control systems of critical applications must be capable of handling all anticipated scenarios, and their design must be driven by pessimistic assumptions on the events generated by the environment so as to identify the most serious situations.

1.1.1 Definitions

Real-time software comprises a set of concurrent real-time tasks [39], [116].

- A real-time task is an executable entity of work which is subject to stringent timing constraints and consists of an infinite sequence of identical activities called instances or jobs.

A real-time task is typically constrained by a deadline.
Real-time operating systems

• The deadline is a point in time by which a real-time task must complete its execution without causing any damage to the system.

Real-time tasks are usually distinguished in two classes depending on the consequences that may occur because of a missed deadline:

• A real-time task is said to be hard if missing its deadline may cause catastrophic consequences on the environment under control (e.g., sensory data acquisition, detection of critical conditions, actuator serving, low-level control of critical system components, planning sensory-motor actions that tightly interact with the environment).

• A real-time task is said to be soft if meeting its deadline is desirable for performance reasons, but missing it does not cause serious damage to the environment and does not jeopardize correct system behavior (e.g., execution of the command interpreter of the user interface, handling input data from the keyboard, display of messages on the screen, graphical activities, saving report data).

A Hard Real-Time Operating System (HRTOS) is an RTOS that is capable of handling hard real-time tasks. Real-time applications typically include both hard and soft activities, therefore HRTOSs should be designed to handle both hard and soft tasks using different strategies. Hybrid task-sets are usually managed by guaranteeing individual timing constraints of hard real-time tasks while minimizing the average response time of soft real-time tasks.

A real-time task can also be characterized by the following parameters:

• Release time: it is the time at which a task becomes ready to execute; it is also referred to as arrival time.

• Computation time: it is the time which is necessary to execute a task on the processor without interruption.

• Start time: it is the time at which a task starts its execution.

• Finishing time: it is the time at which a task finishes its execution.
Real-time operating systems

• **Lateness**: it is the delay of a task completion with respect to its deadline (it is negative if a task completes the execution before its deadline).

• **Laxity**: it is the maximum time a task can be delayed on its activation to complete within its deadline.

Real-time tasks are distinguished in *periodic* and *aperiodic* depending on the regularity of their activations.

• A periodic task consists of an infinite sequence of jobs that are regularly activated at a constant rate. It is characterized by a *period* (which is the constant difference between the activation time of consecutive jobs), a computation time, and a deadline (which is often considered coincident with the end of the period).

• An aperiodic task consists of an infinite sequence of jobs that are not regularly activated at a constant rate. Each job is characterized by an arrival time, a computation time, and a deadline. An aperiodic task characterized by a minimum interarrival time between consecutive jobs is said to be a *sporadic* task.

### 1.1.2 Limits and desirable features of RTOSs

Most RTOSs are based on kernels that are modified versions of time-sharing operating systems and, thus, they exhibit some basic features of these systems that are not suited to handle real-time tasks. The main characteristics of time-sharing operating systems include:

• **Multitasking.** A set of primitives for task management (e.g., system calls to create, suspend, resume, and terminate real-time tasks) provides a support for concurrent programming. However, many of these primitives do not take time into account and, even worse, they introduce unbounded delays on the Execution Time of tasks. This may cause unpredictable deadline misses.
Real-time operating systems

• **Priority-based scheduling.** Various strategies for task management can be developed on priority-based scheduling by changing the rule according to which priorities are assigned to tasks. However, timing constraints of real-time tasks cannot be easily mapped into a set of priorities. This is even harder in dynamic environments, where the arrival of a task may require the remapping of the entire set of priorities. Moreover, the verification of timing constraints is quite impractical without the support of primitives that explicitly handle time.

• **Quick response to external interrupts.** This feature is usually obtained by assigning to external interrupts higher priorities than real-time tasks and by reducing the portions of code that are executed while interrupts are disabled. Quick interrupt handling reduces response time to external events but introduces unbounded delays on the Execution Time of tasks. Moreover, the number of interrupts that a process can experience during its execution cannot be bounded in advance.

• **Task communication and synchronization primitives.** Inter-task communication and synchronization mechanisms should be combined with specific access protocols to avoid undesirable phenomena, such as priority inversion, chained blocking, and deadlock.

• **Small kernel and fast context switch.** This feature reduces system overhead, thus improving the average response time of the task-set. However, this does not provide any guarantee that each task will meet its deadline. In addition, a small kernel does not support the implementation of functionalities required to manage real-time tasks.

• **Real-time clock as internal time reference.** Any real-time kernel that handles time-critical activities that interact with the environment requires an internal real-time clock. Nevertheless, in most commercial real-time kernels this is the only mechanism for time management, and there is not support for deadline specification and periodic task activation. Moreover, exception handling is usually performed through ad-hoc
alarm and timeout signals, which experience the same drawbacks as interrupt handling.

Basic design paradigms found in classical time-sharing systems must be radically changed in order to develop real-time kernels for critical control applications, which require stringent timing constraints that must be met to ensure safe behavior of the system. Such real-time systems must exhibit some basic properties, which include [39], [30]:

- **Predictability.** Both functional and timing behavior of a real-time system must be deterministic in order to guarantee that real-time requirements are met. To this end, system calls must have a bounded Execution Time, thus avoiding the introduction of unbounded delays on the Execution Time of tasks.

- **Timeliness.** Results produced by a real-time system must be correct both in their functional value and in the time domain. As a consequence, the operating system must provide specific kernel mechanisms to manage time and to handle periodic and aperiodic real-time tasks with explicit timing constraints and different criticality.

- **Reliability.** Real-time systems must conform to the specification of their behavior with an acceptable measure of success.

- **Availability.** The system should be operable and ready for correct usage when it needs to be used.

- **Maintainability.** The system should be designed according to a modular architecture to ensure that the real-time kernel can be easily modified and adapted to the needs of real-time applications.

- **Safety.** Real-time systems must achieve acceptable levels of risk of harm to people, the environment, or business.

- **Fault tolerance.** Critical components must be designed to be fault tolerant so as to prevent failures that cause the system to crash.
• **Design for peak load.** Real-time systems must be designed on the basis of pessimistic assumptions on the environment in order to manage all anticipated scenarios and, in particular, peak-load conditions.

### 1.1.3 Predictability as a central feature of RTOSs

Predictability is one of the most important features that an RTOS should have [114]. Both functional and timing behavior must be deterministic, so that the system is able to predict the evolution of tasks and guarantee in advance that all critical real-time requirements will be met. The reliability of the guarantee depends on a range of factors, which involve the architectural features of the hardware, the mechanisms and policies adopted by the kernel, up to the programming language used to implement the application.

• **Direct Memory Access.** The Direct Memory Access (DMA) is a technique that enables peripherals devices to read and write the main memory independently of the Central Processing Unit (CPU).

Since both the CPU and the I/O devices share the same bus, the CPU has to be blocked when the DMA device is performing a data transfer. One of the most common transfer methods is called *cycle stealing* and it allows the DMA device to steal a CPU memory cycle in order to execute a data transfer. During the DMA operation, the I/O transfer runs in parallel with the CPU program execution. However, in case of a contemporary bus request, the bus is assigned to the DMA device and the CPU waits until the DMA cycle is completed. As a consequence, it is not possible to predict how many times the CPU will have to wait for the DMA device to finish, and, thus, the response time of a task cannot be precisely determined.

The *time-slice method* [113] overcomes the problem by splitting each memory cycle into two adjacent time slots, one reserved for the CPU and the other one for the DMA device. This solution is less efficient than cycle stealing but it is more predictable. In fact, memory accesses
performed by the CPU and by the DMA device are disjoint in time and cannot come into conflict with each other; hence, computations of real-time tasks are not indefinitely delayed by DMA operations and their Execution Time can be predicted with higher accuracy.

- **Cache.** A cache is a temporary storage area between the CPU and the Random Access Memory (RAM) where frequently used data can be stored for fast access. This buffering technique speeds up the execution of programs and it is motivated by the fact that statistically the most frequent accesses to the main memory are limited to a small address space (program locality) and the same data are multiply accessed closely in time (temporal locality). Nevertheless, the use of the cache introduces some degree of nondeterminism which downgrades predictability. In fact, in case of a cache miss, the data access time is longer due to the additional data transfer from RAM to cache; in case of write operations in memory, any modification made on the cache must be copied to the memory in order to maintain consistency. According to this, worst-case analysis should assume a cache fault for each memory access and a higher degree of predictability can be achieved through processors without cache or with disabled cache.

In other approaches, the influence of the cache on the Execution Time of tasks is taken into account through a multiplicative factor, which depends on an estimated percentage of cache faults. A more precise estimation of the cache behavior can be achieved by analyzing the code of the tasks and estimating executions times by using a mathematical model of the cache.

- **Interrupts.** Interrupts generated by I/O peripheral devices may cause unbounded delays on the Execution Time of tasks. Each device is associated with a service routine (driver), which is executed at the arrival of an interrupt signal from the device. In many operating systems, interrupts are served using a fixed priority scheme, according to which each driver is scheduled based on a static priority, higher than priorities of
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tasks. This is due to the fact that I/O devices usually have more stringent real-time constraints than application programs. However, in RTOSs, a control task could be more urgent than an interrupt handling routine. Moreover, the interrupt mechanism may introduce unpredictable delays on the Execution Time of tasks, since the number of interrupts that a task may experience during its execution cannot be easily bounded a priori.

In the context of RTOSs, various strategies can be adopted to manage interrupts reducing the interference of the drivers on real-time tasks:

- A radical solution is to disable all external interrupts, except the one from the timer. All peripheral devices are handled by application tasks through polling. On the one hand, this solution provides great programming flexibility, eliminates delays due to the execution of drivers, enables precise evaluation of the time required for data transfer (which is charged to the task that performs the operation), and does not requires the kernel to be modified in case I/O devices are replaced or modified. On the other hand, the processor has low efficiency on I/O operations (due to the busy wait of the tasks while accessing device registers) and application tasks must have knowledge of low-level hardware details of peripheral devices. The latter problem can be solved by encapsulating all device-dependent routines in a set of library functions that can be invoked by the application tasks. This approach is adopted in RK, a research hard real-time kernel designed to support multi-sensory robotics applications [85].

- A modified version of the previous approach handles devices through dedicated kernel routines periodically activated by the timer. This approach does not introduce unbounded delays on the Execution Time of interrupt drivers, confines all I/O operations to one or more kernel tasks. Moreover, application tasks do not need to know hardware details of peripheral devices, which are encapsulated into
kernel procedures. However, the processor has a low efficiency on I/O operations, with a little higher system overhead with respect to the previous approach, due to the communication required among the application tasks and the I/O kernel routines for I/O data exchange. Moreover, the kernel needs to be updated when some device is replaced or added. This approach is adopted in the MARS system [54], [80].

- A third approach leaves all external interrupts enabled and reduces the drivers to the least possible size. In fact, each driver activates a proper task that will actually be the device manager: the dedicated task executes under the direct control of the operating system, it is scheduled and guaranteed like any other application task, and it can be assigned lower priority than those of control tasks. With respect to the first two solutions, this approach eliminates the busy wait during I/O operations. Moreover, compared to the traditional technique, it drastically reduces unbounded delays on the Execution Time of tasks. The approach is adopted in the ARTS system [119], [120], in HARTIK [41], [40], and in SPRING [115].

- **System calls.** Every kernel call should have a bounded Execution Time and should be preemptable. This permits to achieve a higher precision in the estimation of the *Worst Case Execution Time* (WCET) of tasks and avoids delays on task computations.

- **Semaphores.** In traditional operating systems, semaphore operations suffer from *priority inversion*, which occurs whenever a high priority task waits for a low priority task to finish its execution for an unbounded duration. Priority inversion can be avoided through the adoption of various protocols, which bound the maximum blocking time of tasks that share a critical section by controlling resource assignment and by modifying the priority of tasks on the basis of the current resource usage.

- **Memory management.** Techniques for memory management must
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not introduce nondeterministic delays on the Execution Time of tasks. Memory segmentation with fixed-memory management scheme and static partitioning are typical solutions adopted in most RTOSs. In general, static allocation schemes increase the predictability of the system but reduce its flexibility, which is a valuable feature in dynamic environments. Therefore, the system designer attempts to strike a balance between predictability and flexibility depending on the requirements of the applications.

- **Programming language.** In the context of real-time systems, programming languages should permit the specification of certain timing behavior and realize predictable real-time applications. Unfortunately, not all programming languages are expressive enough to support these features.

  - The Ada language [75] was developed by the Department of Defence of the United States. It does not support the definition of explicit time constraints on the execution of tasks and it embeds nondeterministic statements, thus preventing a reliable worst-case analysis. Moreover, since it does not provide any protocol for accessing shared resources, a high-priority task may wait for a low priority task to complete its execution for an unbounded duration.

  - The Ravenscar profile [38] is an ISO-level subset of the concurrency model of Ada which was specifically conceived to meet design and implementation requirements of high-integrity real-time systems, providing the basis for the implementation of deterministic and time-analyzable real-time applications. It supports the development of single-processor real-time applications, comprised of a fixed number of tasks which interact only by means of shared data or protected objects with mutually exclusive access.

  - Ada 2005 Real-Time Annex [19] is an update to the Ada language that includes the Ravenscar profile [38] for high-integrity systems, further dispatching policies such as *Round Robin (RR)* and *Earliest
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Deadline First (EDF), support for timing events and for control of CPU time utilization.

– Real-Time Euclid [79] is a programming language specifically designed to address reliability and guaranteed schedulability issues in real-time systems. It supports the specification of timing parameters (e.g., the timer resolution) and timing constraints of both periodic and aperiodic tasks (e.g., activation time, period). It provides a strict semantics that forces the programmer to specify time bounds and timeout exceptions in all loops, waits, and device accessing statements. Moreover, it addresses static real-time systems. As a consequence, it does not support dynamic data structures (which would prevent a correct evaluation of the time required by memory allocation and deallocation) and recursion (which prevents the determination of the Execution Time of subprograms).

– Real-Time Concurrent C [100] is a high-level programming language for hard real-time applications that extends Concurrent C [64] by providing facilities to specify periodicity and deadline constraints. As characterizing traits, it addresses dynamic systems, where tasks can be activated at run-time, and it allows the programmer to associate a deadline with any statement.

1.1.4 Standards for RTOSs

Standards play an important role in the context of operating systems, since they define syntax and semantics of system calls, thus providing the interface that the operating system exposes to the application layer. This facilitates portability of applications from one platform to another and enables the development of a single application on top of kernels supplied by different providers, thus promoting competition among vendors and increasing the quality of products. Current operating system standards mostly specify portability at the level of source code, thus requiring the application to be recompiled for every different platform. There are four main operating system standards available.
today:

- **RT-POSIX.** Portable Operating System Interface for UniX (POSIX) is a family of standards specifically designed to enable source code portability of software applications across different operating systems platforms. POSIX is standardized by IEEE as the IEEE Standard 1003, and also by ISO/IEC as the international standard ISO/IEC 9945. It defines the operating system interface by specifying syntax and semantics of core functions (e.g., file operations, process management, signals, devices), without indicating how these services should be implemented, so that system developers can choose their implementation as long as they follow the specification of the interface. Although POSIX is based on UNIX, it can be applied to any operating system. An operating system is said to be POSIX *conformant* if it implements the standard in its entirety and this is certified by the Posix Conformance Test Suite; an operating system is said to be POSIX *compliant* is it implements only portions of the standard.

RT-POSIX is the real-time extension of POSIX and it is one of the most successful and widely adopted standards in the area of RTOSs. It provides a set of system calls that facilitate concurrent programming and it supports task synchronization through mutual exclusion resources accessed according to the priority inheritance protocol, task synchronization by means of condition variables, data sharing among tasks, and prioritized message queues for inter-task communication. RT-POSIX also defines services that permit to achieve predictable timing behavior, such as fixed priority preemptive scheduling, sporadic server scheduling, time management with high resolution, sleep operations, multipurpose timers, Execution Time budgeting for measuring and limiting task Execution Times, and virtual memory management.

- **OSEK.** OSEK/VDX [7] is a standard that specifies the interface of an operating system for distributed control units in vehicles, supporting efficient utilization of resources and portability of software applications.
OSEK (Offene Systeme und deren Schnittstellen für die Elektronik in Kraftfahrzeugen; in English, Open Systems and their Interfaces for the Electronics in Motor Vehicles) has been founded as a joint project in the German automotive industry in May 1993. Initial project partners were BMW, Bosch, DaimlerChrysler, Opel, Siemens, Volkswagen Group, and the University of Karlsruhe. The French car manufacturers PSA Peugeot Citroën and Renault joined OSEK in 1994 introducing their VDX (Vehicle Distributed eXecutive) approach, which is a similar project within the French automotive industry. In October 1995, the OSEK/VDX group presented the results of the harmonized specification between OSEK and VDX.

The OSEK/VDX standard addresses safety-critical real-time applications, allocated to a huge number of units and characterized by tight timing constraints. For this reason, the standard attempts to reduce the memory footprint as much as possible in order to enhance the operating system performance. In order to support a wide range of systems with a high degree of scalability, modularity, and configurability, the standard defines four conformance classes that tightly specify the main features of an operating system and it provides a toolchain where some configuration tools help the designer in tuning the system services and the system footprint. Moreover, a language called OIL (OSEK Implementation Language) is proposed to help the definition of a standardized configuration information. The operating system defined by the OSEK/VDX standard does not specify any interface for the Input/Output subsystem: this reduces or even prevents the portability of the source code of applications, since the I/O system quite impacts on the architecture of the application software; however, the effort is not on achieving full compatibility between different application modules, but much more on supporting their direct portability between compliant operating systems.

The OSEK/VDX standard specifies a uniform communication environment for automotive control unit application software, called *OSEK Communication* (OSEK COM), which provides a standardized API for
software communication (between nodes and within a node) that is independent of the communication media.

OSEK/VDX also includes a standardization of inter-networking interfaces, called *OSEK Network Management* (OSEK NM), which ensures safety and reliability of communication networks. This is obtained by implementing access restrictions to each node, by keeping the whole network tolerant to faults, and by implementing diagnostic features capable of monitoring the status of the network.

- **ARINC 653.** Avionic Application Standard Software Interface 653 (ARINC 653) [9] is a specification for an application executive used to integrate avionics systems on modern aircrafts. It supports the implementation, certification, and execution of analyzable safety-critical real-time applications for Integrated Modular Avionics architectures.

The ARINC 653 standard defines an APplication EXecutive (APEX) for space and time partitioning which supports the development of multitasking applications. A partition represents a separate application, which is assigned a dedicated memory space and a time slot; each application is comprised of a set of tasks, which run under static priority scheduling within the assigned time slot and communicate with each other through message buffers, semaphores, and events. Tasks allocated to different partitions communicate by exchanging messages through ports provided by the API of the operating system. It is the responsibility of the system integrator to ensure that all ports and channels are defined prior to normal system operation. The mechanism used to write a message on an API output port depends on whether the message is to be sent to another partition running on the same processor, a partition running on another processor, or an interface device. However, the same interface is used in all the cases, making it relatively easy to move applications between processors and to substitute software simulations of hardware devices for testing. Each port may be configured to work in either sampling mode or queueing mode: in the first case, not yet read messages are overwritten.
by incoming messages; in the second case, incoming messages are queued up.

Since each application is isolated from the others, ARINC 653 conformance can be a step towards RTCA/DO-178B certification [60].

• **Micro-ITRON.** The Real-time Operating system Nucleus (TRON) is the name of a project started by Dr. Ken Sakamura of the University of Tokyo in 1984. The goal of the TRON Project has been to create a concept of a computer architecture and network, in which common everyday objects are embedded with computer intelligence and are able to communicate with each other, thus increasing the collaboration of electronic devices in the environment.

The TRON framework defines a complete architecture for different computing units. Industrial TRON (ITRON) is the specification of an RTOS for embedded systems which has become a de facto standard in the embedded systems field, especially in Japan, where it is widely used in mobile phones and other consumer products. Micro-ITRON 3.0 [108] is a standard for a real-time kernel developed by the ITRON project and includes the specification of communication features supporting the implementation of an embedded system within a network. The Micro-ITRON 4.0 specification [53] is based on the Micro-ITRON 3.0 specification and it has been developed to improve compatibility and conformance level, to increase productivity in software development, to allow reuse of application software, and to achieve more portability. To this end, Micro-ITRON 4.0 combines the loose standardization that is typical of ITRON standards with a strict standardization of kernel functions, called *Standard Profile*, that is needed for portability. The Standard profile supports the association of tasks with priorities, semaphores, message queues, and mutual exclusion primitives with priority ceiling and priority inheritance protocols.
1.1.5 Commercial and open source real-time kernels

At the present time, there are many commercial and open source RTOSs. This Section gives a brief overview on some of them and Section 1.2 will provide a more detailed description of the RTOS employed in the experimentation.

1.1.5.1 Commercial RTOSs

There are more than one hundred commercial RTOSs, from very small kernels with a memory footprint of a few kilobytes to large multiprocessor systems for complex real-time applications. Most of them support concurrent programming and static priority preemptive scheduling. Only a small subset of commercial RTOSs supports dynamic priority scheduling (e.g., deadline-driven priority scheduling) and implements some form of priority inheritance to prevent priority inversion while accessing mutually exclusive resources. In addition to traditional programming tools (e.g., editor, compiler, debugger), commercial RTOSs usually provide specific tools for the development of real-time applications (e.g., tools supporting performance profiling, tracing of kernel activities, memory analysis, schedulability analysis, WCET analysis). The most adopted commercial RTOSs are VxWorks [103], QNX, and OSE.

- VxWorks [103], [104], [105] is produced by Wind River Systems [8] and it is the most adopted RTOS in embedded industry. It supports fixed priority preemptive scheduling and RR scheduling; it enables inter-task communication through shared variables, semaphores (with support for priority inheritance protocol), message queues, pipes, sockets, and remote procedure calls; it provides a cross-compiler and associated programs, a performance profiler to estimate the Execution Time of routines, some utilities to monitor the way how the processor is used by tasks, and a simulator to emulate the target system along the development process or during the testing phase.

VxWorks 5.x and 6.x conform to the real-time POSIX 1003.1b standard. Support for graphics, multiprocessing, memory management, connecti-
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vity, Java, and file system is provided by separate services. Tornado and Workbench are the integrated development environments for VxWorks 5.x and 6.x releases, respectively.

- QNX Neutrino [73] is a microkernel RTOS that provides a comprehensive, integrated set of technologies supporting the development of robust and reliable mission-critical applications. Fundamental operating system services (i.e., signals, timers, and scheduling) are implemented in the microkernel, while the other components (i.e., file systems, drivers, protocol stacks, applications) run outside the kernel. As a result, a defected component can be automatically restarted without affecting other components or the kernel. QNX supports the priority inheritance protocol in order to avoid priority inversion, and nested interrupts in order to enable priority-driven interrupt handling. Communication among system components is performed through message passing.

The QNX RTOS complies with the POSIX 1003.1-2001 standard and with its real-time extension, and it includes a module for power management that allows the developer to control power consumption of system components and adopt specific power management strategies.

Since September 2007, QNX offers a licence for non-commercial use.

- OSE [97] is a modular, high-performance, full-featured RTOS, optimized for complex distributed systems that require the utmost in availability and reliability. It is produced by ENEA and it is widely used in automotive and communications industry. It provides three families of operating systems that implement the OSE API at different levels: OSE is the portable kernel, OSEck is the compact kernel for Digital Signal Processors (DSPs), and Epsilon is a set of highly optimized assembly kernels. It supports both static and dynamic processes, and different categories of processes which run under different scheduling principles: interrupt processes and priority-based processes are scheduled according to their priority; timer interrupt processes are are triggered cyclically; background processes are scheduled in RR manner; phantom processes
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are not scheduled at all and they are used to redirect signals. Communication among processes is performed through message queues.

1.1.5.2 Linux-based real-time kernels

Linux [5] is a free Unix-type operating system kernel, originally conceived and created by Linus Torvalds in 1991 and then developed with the assistance and contributions of thousands of programmers around the world.

Linux provides two distinct modes of operation of the CPU: kernel mode is a privileged mode in which the CPU is assumed to be executing trusted software and it can reference any memory address; user mode is other than kernel mode, and it is a non-privileged mode in which each running instance of a program is not allowed to access those portions of memory that have been allocated to the kernel or to other programs. The kernel is the core of the operating system and it is considered trusted software; any other program is considered untrusted software and must request the use of the kernel by means of a system call in order to perform privileged instructions (e.g., task creation and destruction, I/O operations).

The Linux kernel is non-preemptive through version 2.4: while a process runs in kernel mode, it cannot be suspended and replaced by another process (i.e., preempted), but it can be suspended only if it voluntarily relinquishes the control of the CPU or if an interrupt or an exception occurs. According to this, when a user process runs a portion of the kernel code via a system call, it temporarily becomes a kernel process and it runs in kernel mode until the kernel has satisfied the process request, no matter how long that might take. The Linux kernel version 2.6 (which was introduced in late 2003) is preemptive: a process running in kernel mode can be suspended in order to run a different process. This is obtained through the introduction of preemption points, which are instructions that allow the scheduler to run and possibly block the current process so as to schedule a higher priority process. Unreasonable delays in system calls are thus avoided by periodically testing a preemption point. This can be an important benefit for real-time applications but it is not enough
to guarantee strict timing constraints. To this end, the Linux kernel can be extended in different manners in order to support hard real-time applications.

- **RTLinux** [126] is a real-time extension for the Linux kernel initially developed by Victor Yodaiken, Michael Barabanov, and Cort Dougan at the New Mexico Institute of Mining and Technology. It is distributed by Finite State Machine Labs [4].

  RTLinux works as a small executive with a real-time scheduler that runs Linux as a completely preemptable thread with lowest priority. RTLinux real-time threads and Linux processes can communicate by means of a shared memory space or through a file-like interface. The standard Linux interrupt handler routine and the macros for interrupt enabling and disabling are modified so that the RTLinux interrupt routine is executed whenever an interrupt is raised: if the interrupt is related to a real-time activity, then a real-time thread is notified and RTLinux executes its own scheduler; otherwise, Linux interrupt service routine is delayed until no real-time thread is active.

  This approach provides a separation of concerns between the Linux kernel and the real-time micro-kernel and permits to execute Linux as a background activity in the real-time executive, thus reducing the latency on real-time activities. However, real-time tasks execute in the same address space of the Linux kernel and, thus, a fault in a user task may crash the kernel. Moreover, there is no direct support for resource management policies and it is often necessary to re-write drivers for real-time applications, since real-time threads cannot use the standard Linux device driver mechanism.

- **Real-Time Application Interface** (RTAI) [95] is a real-time extension for the Linux kernel that builds on the original idea of RTLinux [126]. Its main features will be discussed in Section 1.2.

- **Linux Resource/Kernel** (Linux/RK) [6], [96] is developed by the Real-time and Multimedia Systems Laboratory led by Dr. Raj Rajkumar
at Carnegie Mellon University. It provides a real-time extension of the Linux kernel according to a different approach with respect to RTLinux [126] and RTAI [95], by directly modifying the Linux kernel in order to supply it with those features that support the development and the execution of applications with strict timing constraints.

Linux/RK is a resource kernel based on Linux, i.e., a real-time kernel that provides timely, guaranteed, and enforced access to system resources for applications. An application can request the reservation of a certain amount of a resource (e.g., CPU time, physical memory page, network bandwidth, disk bandwidth) and the kernel can guarantee that the requested amount is available to the application. Such a guarantee of resource allocation gives an application the knowledge of the amount of its currently available resources. A Quality of Service (QoS) manager or an application itself can then optimize system behavior by computing the best QoS obtained from the available resources.

1.1.5.3 Research kernels

Research kernels are characterized by the ability to associate tasks with explicit time constraints (e.g., period, deadline) and with additional parameters used to analyze the dynamic performance of the system, by the possibility to verify in advance whether timing constraints of an application will be met during the execution, and by the use of specific resource access protocols not only to avoid priority inversion but also to limit the blocking time on mutually exclusive resources. Most of the kernels that exhibit these features are developed by universities and research centers, such as SHARK, MaRTE and ERIKA.

- Soft and HArd Real-time Kernel (SHARK) [63] is a dynamic configurable kernel architecture developed at the Scuola Superiore S. Anna in Pisa. It is expressively designed to support the implementation and testing of new scheduling algorithms and resource management protocols, and it manages hard real-time, soft real-time, and non real-time
applications. SHARK comprises a *Generic Kernel*, which does not implement any particular scheduling algorithm or resource management protocol, but postpones scheduling decisions and the adoption of access policies to shared resources to external *scheduling modules* and *resource modules*, respectively. Modules can be registered at initialization, thus achieving full modularity in scheduling and resource management policies. According to this, an application can be developed independently of a particular system configuration, so that new modules can be added or replaced in the same application, in order to evaluate the effects of specific scheduling policies in terms of predictability, overhead, and performance.

The system is compliant with almost all the POSIX 1003.13 PSE52 specifications in order to simplify the porting of application code developed for other POSIX compliant kernels.

- **Minimal Real-Time operating system for Embedded applications (MaRTE)** [102] is an HRTOS developed at the University of Cantabria, which provides an easy to use and controlled environment to develop multi-thread real-time applications. It follows the Minimal Real-Time POSIX 1003.13 subset and implements the Ada 2005 Real-Time Annex, which includes the Ravenscar profile [38]. It is available under the GNU General Public License 2 at http://marte.unican.es/.

  MaRTE supports the implementation and cross-development of mixed language applications in Ada, C, and C++ through the GNU compilers Gnat and Gcc. The kernel has an hardware abstraction layer which provides an interface to operations for interrupt management, clock and timer management, and thread context switches, thus facilitating migration of application code from one platform to another.

- **Embedded Real-tIme Kernel Architecture (ERIKA)** [2] is a free of charge, open-source implementation of the OSEK/VDX API [7] distributed by Evidence s.r.l. [3] under the GNU GPL licence. It provides two versions: ERIKA Enterprise, which supports new hardware platforms in
automotive applications, and ERIKA Educational, which is developed for teaching and didactical purposes.

ERIKA provides a set of modules which implement task management and real-time scheduling policies. The hardware abstraction layer contains the hardware dependent code that manages context switches and interrupt handling.

1.2 Real-Time Application Interface

Real-Time Application Interface (RTAI) [95] is a real-time extension for the Linux kernel that supports the development of real-time applications with strict timing constraints for several architectures (x86, x86_64, PowerPC, ARM). The project was initially started from the original RTLinux code [126] by Prof. Paolo Mantegazza from the Dipartimento di Ingegneria Aerospaziale of Politecnico di Milano and it is now a living open-source project developed by a wide community. Although the architectures of RTAI and RTLinux are quite similar, RTAI has considerably built on and enhanced the original idea of RTLinux and the API of the projects were developed according to opposite principles. The main features and system calls of RTAI are not POSIX compliant, although RTAI implements a compliant subset of POSIX 1003.1.c.

1.2.1 RTAI architecture

Both RTLinux and RTAI provide a small RTOS that runs the standard Linux kernel as the lowest priority task, which is allowed to execute whenever no real-time task is schedulable. While RTLinux applies most changes directly to the kernel source files, resulting in modifications and additions to numerous Linux files, RTAI limits the changes to the standard Linux kernel by adding a layer of virtual hardware between the standard Linux kernel and the hardware itself. Until RTAI 3.0, this layer relied on the so called Real-Time Hardware Abstraction Layer (RTHAL), which is comprised of an interrupt dispatcher.
that intercepts, processes, and redirects hardware interrupts (see Fig. 1.1). A real-time interrupt is immediately served by the real-time kernel through the invocation of the corresponding real-time handler; a non real-time interrupt is queued up as a pending interrupt, and it is served by the Linux kernel when no real-time task is running. In so doing, the RTHAL provides a framework onto which RTAI is mounted with the ability to fully preempt the Linux kernel. The RTHAL was implemented by modifying less than 20 lines of existing code, and by adding about 50 lines of new code, thus minimizing the changes on the standard Linux kernel and thereby improving the maintainability of RTAI and the Linux kernel code. The fact that every interrupt is intercepted by the RTHAL imposes an additional overhead and causes a little increase in the average value of latency; nevertheless, RTAI ensures much smaller maximum values of latency than a standard kernel, thus improving determinism and responsiveness [16], [86].

Figure 1.1. The RTHAL-based RTAI architecture.

RTLinux is covered by the US Patent 5995745, issued on November 30, 1999 and entitled “Adding Real-Time Support To General Purpose Operating
Real-Time Application Interface

Systems” . In order to avoid legacy constraints of this patent and to provide a more structured and flexible technology to add real-time features to Linux, the RTAI community has developed the Adaptive Domain Environment for Operating Systems (ADEOS). The general design of the Adeos nanokernel [1] has been proposed by Karim Yaghmour and it provides an extensible and adaptive environment that enables the sharing of hardware resources among multiple entities called domains, each represented by an operating system or by an instance of an operating system [125]. In the RTAI architecture, ADEOS provides a resource virtualization layer between the computer hardware on the one hand, and Linux and RTAI on the other one, as reported in Fig. 1.2.

![Figure 1.2. The ADEOS-based RTAI architecture.](image)

Resource sharing among different domains is achieved through an interrupt pipeline. Each domain is assigned a static priority level, which is used for a proper dispatch order of events. In fact, domains are queued up according to their respective priority and hardware interrupts are propagated through the pipeline, from its head (i.e., the highest priority domain) down to its tail (i.e., the lowest priority domain). A domain may:

- accept and handle the interrupt, and then decide whether to propagate it to the next stage or not;
- ignore and stall the interrupt, handling it in a subsequent moment, and
then decide whether to propagate it to the next domain or not;

- discard the interrupt and propagate it to the next stage;
- terminate the interrupt without propagating it through the pipeline.

In the ADEOS architecture, RTAI is installed as the highest priority domain, thus guaranteeing that it always intercepts and handles hardware interrupts before the standard Linux kernel, as is illustrated in Fig. 1.3.

![Diagram of event pipeline of ADEOS with RTAI and Linux]

Figure 1.3. The event pipeline of ADEOS with RTAI and Linux.

1.2.2 RTAI schedulers

RTAI is a full-featured real-time micro-kernel. Both basic services (e.g., the schedulers) and advanced services (e.g., POSIX compliant functions) are implemented as kernel modules, which can be loaded or unloaded using the standard Linux `insmod` and `rmmod` commands as their respective capabilities are required or released.

RTAI supports various types of schedulers, each suited to a specific combination of hardware and task requirements. In particular, RTAI provides three priority-based preemptive real-time schedulers:

- **UniProcessor (UP) scheduler**: it is used on uni-processor platforms.
- **Symmetric MultiProcessor (SMP) scheduler**: it is used on multi-processor platforms and supports symmetric workload distribution among the various CPUs. Tasks can run symmetrically on any CPU or on a cluster of CPUs, or they can be bound to run on a single CPU.
• **Multi-UniProcessor** (MUP) scheduler: it is used on multi-processor platforms. Each task is forced to execute on a single CPU, which is assigned when the task is created. This restricts the flexibility of MUP scheduler with respect to SMP scheduler, but increases its efficiency.

RTAI provides two scheduler’s operation modes, depending on the way how the timer is programmed:

• **Periodic mode**: the timer is programmed to emit interrupts at fixed time intervals and the scheduler is executed at the end of each period. The period of a periodic task should be a multiple of the scheduler’s period, otherwise it is approximated to the nearest multiple of the scheduler’s period.

• **One-shot mode**: the timer is re-programmed at each interrupt, according to the task that is going to execute. It allows a higher flexibility with respect to periodic mode, but it imposes an additional overhead due to the necessity to re-program the timer at each interrupt.

RTAI natively supports various scheduling policies:

• **First In First Out** (FIFO): tasks are statically associated with a priority level and the CPU is assigned to the task with highest priority until the task completes its execution or it voluntarily releases the CPU or a task with higher priority becomes active. Tasks with equal priority are queued up according to their activation time (i.e., priorities being equal, the first task queued up is the first to be resumed).

• **Round Robin** (RR): tasks are statically assigned a priority level and the CPU is assigned to the highest priority task for a time no longer than a predefined unit of time, called *time slice* or *quantum*. A task can be preempted if a higher priority task becomes active before the time slice has elapsed. Tasks with equal priority are queued up according to their activation time.
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- **Rate Monotonic Priority Order (RM):** tasks are statically assigned priorities according to their request rates (i.e., the higher the request rate, the higher the priority level). The request rate of a periodic task is represented by its period (i.e., the shorter the period, the higher the priority level). The currently executing task is preempted whenever a task with shorter period is released.

- **Earliest Deadline First (EDF):** tasks are dynamically assigned priorities according to their absolute deadlines (i.e., the earlier the deadline, the higher the priority level). The currently executing task is preempted whenever a task with earlier deadline becomes active.

RTAI enables the execution of hard real-time tasks both in the kernel space and in the user space. Real-time tasks that run in the kernel space are implemented as loadable kernel modules and, thus, they are integral part of the kernel. As a consequence, they are not bounded by the memory protection services of Linux and they have the ability to overwrite system-critical areas of memory.

*Linux Real-Time (LXRT)* is an extension of RTAI that enables the development of real-time tasks in the user space, where memory protection is enabled, and allows applications to dynamically switch between real-time and non real-time operation. This behavior is obtained by associating each task in the user space that has real-time requirements with a real-time agent in the kernel space. When the user task enters hard real-time mode, the real-time agent disables interrupts, takes the task out of the queue of running tasks of the Linux scheduler and adds it to the queue of the RTAI scheduler. Although performance under LXRT is quite good, it imposes higher values of latency with respect to the execution of real-time tasks in the kernel space.

### 1.2.3 RTAI IPC mechanisms

Real-time tasks are not allowed to use services provided by the standard Linux kernel. For this reason, RTAI developers implemented various IPC mecha-
nisms, which are employed to transfer and share data between tasks in both the real-time domain and Linux user space domain. IPC mechanisms are implemented as kernel modules, which can be loaded in addition to basic RTAI and schedulers modules only when they are requested by real-time tasks.

- **Real-Time FIFO queues**: they provide an asynchronous and unblocking one-way communication channel, whose size limit is assigned by the programmer when the queue is created.

- **Semaphores**: they are data structures associated with a counter and they enable mutual exclusion and synchronization among tasks.

- **Shared Memory**: it is a block of memory that can be read and written by any task in the system. This provides an alternative communication paradigm with respect to RTAI FIFOs and it is much more suitable when a big amount of data needs to be transferred.

- **Messages and Remote Procedure Calls**: they provide a point-to-point communication mechanism where the sender task and the receiver task are supposed to know each other.

- **Mailboxes**: they provide a flexible communication mechanism to exchange data among tasks. The size of a mailbox is defined by the programmer when it is created and multiple senders and receivers are allowed.

### 1.3 Software development processes

A software life cycle process comprises all the activities and work products necessary to develop a software system. In software engineering, various development models have been proposed and applied throughout the years. Section 1.3.1 provides a brief overview of various software life cycle processes and Section 1.3.2 focuses on the V-Model framework [42] which is considered as a reference in this dissertation.
1.3.1 From the waterfall model to eXtreme Programming

The *waterfall model* is a sequential approach to software development, which was first described by Winston Royce in 1970 [107]. Although the original model makes provision for feedback loops at the end of each activity, the majority of organizations that apply this life cycle process treat it as if it were strictly linear. The model begins with customer specification of requirements, which are reviewed and assessed with respect to completeness, consistency, and clarity; then, it progresses through planning, modeling, construction, and deployment; finally, it culminates in on-going maintenance of the completed software, which sustains the useful operation of the system in its target environment by providing requested functional enhancements, repairs, performance improvements, and conversions. The main criticism of this model is that each stage of the process must be completed before moving to the next one, which comprises an idealized framework that has difficulties in accommodating iterations and requirements changes. However, real projects rarely follow the sequential flow that the model proposes, primarily because it is often difficult for the customer to state all requirements explicitly at the beginning of the project. For this reason, various modified versions of the waterfall model have been proposed which may include slight or major variations upon this process.

The *spiral model* is an iterative software life cycle process proposed by Barry Boehm in 1986 to address the source of weaknesses in the waterfall model and accommodate frequent changes during software development [31]. The approach integrates the phases of the waterfall model with several activities addressing risk management, reuse, and prototyping. In particular, each development phase corresponds to one *cycle or round* of the spiral and involves the same sequence of steps: *Determine objectives, alternatives, and constraints*, which define the problem addressed by the current cycle; *Evaluate alternatives: identify and resolve risks*, which defines the solution space and serves to identify future problems that may turn out to be highly expensive; *Develop and verify next level product*, which is the realization of the cycle; *Plan next phases*, which prepares the next cycle.
The Unified Process (UP) is an iterative and incremental development process proposed by Grady Booch, Ivar Jacobson, and James Rumbaugh in 1999 [76]. Similar to the spiral model, in the UP, a project consists of several cycles each ending with the delivery of a product to the customer. Each cycle consists of four phases: Inception, Elaboration, Construction, and Transition. Each phase includes a number of iterations and each iteration, in turn, results in an increment, which is a release of the system that contains added or improved functionality compared with the previous release. The Inception phase provides an initial evaluation of feasibility costs; the Elaboration phase corresponds to the initiation process, during which the project is planned, the system is defined, and resources are allocated; the Construction phase addresses the implementation of system components; the Transition phase is responsible for system installation and post-development processes.

Agile software development refers to a group of software development methodologies based on iterative development, where requirements and solutions evolve through collaboration between self-organizing cross-functional teams. The eXtreme Programming (XP) [21] is a form of agile development that focuses on short development cycles and close interaction with customers. In traditional system development methods, system requirements are determined at the beginning of the development project and often fixed in subsequent phases, which can be extremely costly at later stages of development. Like other agile software development methods, XP attempts to reduce the cost of change through multiple short development cycles, rather than a single long one. In this doctrine, changes are a natural, inescapable, and desirable aspect of software development projects and they should be planned for, instead of attempting to define a stable set of requirements.

1.3.2 The V-Model software life cycle

The V-Model [42] is a framework for the organization of development, maintenance and modification processes in the life cycle of software systems, issued as a standard by the German Federal Administration and widely practiced in the...
industry of safety-critical software systems. It is a variation of the waterfall model that builds a V shape sequence of development activities, highlighting the relationship between each phase of design and its associated phase of testing and introducing feedback loops between them. Fig. 1.4 reports a scheme of the System Development (SD) Submodel, emphasizing the relation between Design and Verification activities (left/right) and the hierarchical decomposition from System Level to SW Module Level (top/down).

**Figure 1.4. V-Model: activities of the System Development Submodel.**

*System Requirements Analysis* (SD1) determines the overall system-level functional and non-functional User Requirements. *System Design* (SD2) generates a possible solution for the technical system structure called System...
Software development processes

Architecture, identifies its Units and the User Requirements managed by each of them, and defines the interfaces of the system to the environment and the interfaces between system Units. *Software/Hardware Requirements Analysis* (SD3) decomposes each Unit into SW and HW Components and allocates Technical Requirements to them. While SD1 and SD2 have system scope, SD3 is repeated for each single Unit.

*Preliminary Software Design* (SD4-SW) specifies the *Software Architecture* of each SW Unit as a set of concurrent and interacting tasks with assigned functional low-level modules, prescribed release times, and deadlines. The *Software Design* is completed in the subsequent activity SD5-SW with the allocation of resources and time requirements to SW Modules. The sub-activity *Analysis of Resources and Time Requirements* (SD5.2-SW), not shown in Fig. 1.4, investigates calculated requirements in order to verify their feasibility. If Software Design satisfies resources and time requirements with a sufficient margin of laxity, maintenance and modification measures can be taken without a huge effort in re-design.

*Software Implementation* (SD6-SW) translates the Software Design of each Unit into executable code, which is subject to self-assessment through the unit-testing of SW Modules in the sub-activity *Self Assessment of the Software Module* (SD6.3-SW), not shown in Fig. 1.4.

*Software Integration* (SD7-SW) verifies the integration of SW Modules within each SW Component (SW Component Level in Fig. 1.4) and then the integration of SW Components within each SW Unit (Unit Level in Fig. 1.4). Finally, *System Integration* (SD8) composes units and performs self-assessment of the system, while *Transition to Utilization* (SD9) operates the transition that leads to install the completed system at the intended application site and to put it into operation.
1.4 Mapping the theory of pTPNs onto a V-Model software life cycle

The development of real-time software can largely benefit from the application of formal methods, which add rigor to design and verification activities and reduce the possible gap between the verified abstraction and its actual implementation. This dissertation devises a formal methodology that casts the theory of pTPNs in a tailoring of the V-Model life cycle [42], facing the aspects of concurrency and timing in the construction of real-time software components and meeting the prescriptions of main regulatory standards [60], [50], [77] in the integration of formal methods along the development of safety-critical software. In the literature, various works provide specific contributions in the application of formal methods to individual phases of software life cycle. However, none of them devises a comprehensive approach that supports the development process in systematic and organic manner from software design through software implementation and testing. For this reason, the comparison with related works is addressed throughout the dissertation in the Chapters that illustrate the application of the proposed approach to specific steps of software life cycle.

The methodology proposed in this dissertation supports software development from the activity SD4-SW through the activity SD7-SW, as shown in Fig. 1.5. The process is illustrated with reference to an example in the field of Intelligent Visual Surveillance Systems (IVSSs), which will serve as running case along the treatment. The case study concerns a vision system which performs real-time 3D tracking of multiple people moving over an extended area by employing a pan-tilt-zoom (PTZ) camera [29]. In the activity SD1, User Requirements define parameters of the vision system, such as the frame rate (i.e., 25 frames per second), the image size (i.e., 160 x 120 pixels), the compression format (i.e., JPEG), the operating temperature (i.e., from 0°C to 40°C), the camera mass (i.e., up to 1.5 Kg). In the activity SD2, System Architecture is specified through the Unified Modeling Language (UML) profile for Modeling A FORMAL METHODOLOGY FOR THE DEVELOPMENT OF REAL-TIME SOFTWARE 35
and Analysis of Real-Time and Embedded systems (MARTE) [66], which is an extension of the UML [67], [68] expressively designed to support the specification of real-time and embedded systems. The UML-MARTE class diagram of System Architecture of the case example is reported in Fig. 1.6: the system consists of a Control Unit, a PTZ Camera, and a Video Processing Unit. The Control Unit receives images acquired by the PTZ Camera, sends them to the Video Processing Unit, and receives the elaborated images back. On the basis of these results, the Control Unit sets parameters of image processing algorithms (e.g., window size of non-linear filters) and parameters at which images are acquired (e.g., the levels of pan, tilt, and zoom), and sends them to the
Video Processing Unit and to the PTZ Camera, respectively. In the activity

![UML-MARTE class diagram of the System Architecture of an IVSS.](image)

Figure 1.6. UML-MARTE class diagram of the System Architecture of an IVSS. The \textit{ProcessingResource} stereotype models an active, protected, executing-type resource that is allocated to the execution of schedulable resources. The \textit{Device-Resource} stereotype specializes the concept of processing resource and typically represents an external device that may be manipulated or invoked by the platform and that may require specific services in the platform for its usage and/or management, but whose internal behavior is not a relevant part of the model under consideration. A \textit{CommunicationMedia} represents the mean to transport information from one location to another.

SD3, system units are detailed through the UML-MARTE class diagrams reported in Figs. 1.7 and 1.8 and their SW and HW Components are referred to as \textit{Computer Software Configuration Items} (CSCIs) and \textit{Hardware Configuration Items} (HCIs), respectively. The Control Unit communicates with the PTZ Camera and with the Video Processing Unit through a serial bus; boards of both the Control Unit and the Video Processing Unit run RTAI operating system [95]. The Control Unit comprises a CSCI (i.e., System Management CSCI) and two HCIs (i.e., a board and a battery): the CSCI is mapped on an RTAI task-set and allocated to the board. The PTZ Camera consists of two HCIs (i.e., the Image Sensor Unit and the Mechanical PTZ Unit). The Video Processing Unit comprises three CSCIs (i.e., Images Acquisition CSCI, Basic Features Extraction CSCI, and Multiple Target Tracking CSCI) and four HCIs (i.e., three boards and a battery): each CSCI is mapped on a different RTAI task-set and allocated to a different board.

The methodology that is proposed in this dissertation comes into play with the activities SD4-SW and SD5-SW, where each CSCI is mapped on a task-set according to the following model derived from the practice of real-time systems [39], [116] and described by the UML diagram [67], [68] of Fig. 1.9:

- A \textit{task} releases \textit{jobs} in recurrent manner with \textit{periodic}, \textit{sporadic} or \textit{jit-
Mapping the theory of pTPNs onto a V-Model software life cycle

Figure 1.7. UML-MARTE class diagram of the Control Unit and the PTZ Camera of the IVSS of Fig. 1.6. The rtUnit stereotype models a real-time application that owns one or more schedulable resources. A SchedulableResource is an active resource able to perform actions using the processing capacity brought from a processing resource by the scheduler that manages it. A Hw_Card symbolizes a printed circuit board, which typically comprises other sub-components like chips and electrical devices. The allocate stereotype identifies an allocation relation between elements of the application model, represented through the stereotype ApplicationAllocationEnd, and elements of the execution platform, modeled by the stereotype ExecutionPlatformAllocationEnd. A Hw_PowerSupply is a hardware component that supplies the hardware platform with power. The Hw_Bus stereotype represents a particular wired channel with specific functional properties.

A job is internally structured as a sequence of chunks, each characterized
by a non-deterministic Execution Time constrained within a minimum and a maximum value. Chunks representing a computation are also associated with an entry-point function for the attachment of functional behavior to the corresponding low-level module.
• Chunks belonging to jobs of different tasks may have dependencies (e.g., semaphore synchronization, message passing through a mailbox) and they may require resources (e.g., one or more processors), in which case they are associated with a priority level and run under static priority preemptive scheduling. Wait and signal semaphore operations are constrained to occur at the beginning and at the end of chunks, respectively, but a semaphore may be held across multiple subsequent chunks of the same task. Receipt and dispatch mailbox operations are constrained to occur at the beginning and at the end of chunks, respectively, and each mailbox is shared between two tasks.

Figure 1.9. UML diagram of the conceptual model of task-set.

The activity SD4-SW defines the structure of the task-set allocated to each CSCI, identifies minimum release inter-times and deadlines which are directly issued from Technical Requirements, and assigns task periods which are design choices. The activity SD5-SW refines the design of each task-set through the specification of target processors, task priorities, and allowed time-frames of computation chunks: in the usual practice, the latter design choice is initially based on analogy with previous realizations and may require iterations along the development process. In the activities SD4-SW and SD5-SW, task-sets are represented through a semi-formal specification and automatically translated.
Mapping the theory of pTPNs onto a V-Model software life cycle

into pTPN models through the Oris Tool [43]. The sub-activity SD5.2-SW is supported by pTPN theory and the Oris Tool through simulation and state-space analysis, which drive two nested cycles of feedback on design choice of temporal parameters until the structure of the *dynamic architecture* of each task-set proves to be adequate to meet sequencing and timeliness requirements.

Referring again to the RTCA/DO-178B standard [60], state-space analysis verifies the design with the level of rigor of full coverage, which is recommended there with explicit reference to the case of concurrent and timed behavior. When state-explosion prevents complete enumeration and analysis, the rigor degree of the approach downgrades to the level of a method that supports manual verification, but it is in any case able to verify a significant part of the state-space, by far beyond the limits that could be attained through code inspection and testing.

The activity SD6-SW automatically derives the implementation of the dynamic architecture of each CSCI from its semi-formal specification through the Oris Tool [43]. The structure of the code closely follows readable patterns of preemptive real-time programming and relies on conventional RTOS primitives. Again, this meets the RTCA/DO-178B [60] recommendation that the introduction of formal methods do not change the essential nature of development processes and, moreover, avoids legacy constraints on tools for automated generation, which also has relevance for industrial acceptance. SD6-SW also includes the implementation of functional code of low-level modules attached to the entry-points. The sub-activity SD6.3-SW is supported by pTPN theory in the verification of timing requirements of low-level modules through a measurement-based approach to Execution Time profiling.

In the activity SD7-SW, the theory of pTPNs impacts on the verification of the integration at the SW Component Level supporting test-case selection, test-case sensitization, oracle verdict and coverage evaluation. The activities SD8 and SD9 are out of the scope of impact of the methodology proposed in this dissertation.
Chapter 2

Design of real-time task-sets through preemptive Time Petri Nets

In the activities SD4-SW and SD5-SW, the representation of the dynamic architecture of a CSCI through pTPNs enables schedulability analysis and sequencing verification through simulation and state-space analysis.

2.1 Preemptive Time Petri Nets

pTPNs [33], [34] extend Petri Nets with the timing semantics of TPNs [92], [25], [122] and with an additional mechanism of resource assignment, that makes the progress of timed transitions be dependent on the availability of a set of preemptable resources.

2.1.1 Syntax

A pTPN is a tuple

\[ (P; T; A^-; A^+; A^*; M_0; EFT^s; LFT^s; \tau_0; Res; Req; Prio) \]  

\[(2.1)\]
Preemptive Time Petri Nets

where:

- $P$ and $T$ are disjoint sets of places and transitions, respectively.
- $A^-$, $A^+$, and $A^\cdot$ are sets of precondition, postcondition, and inhibitor arcs, respectively, connecting places and transitions:
  \begin{align*}
  A^- & \subseteq P \times T, \\
  A^+ & \subseteq T \times P, \\
  A^\cdot & \subseteq P \times T. 
  \end{align*} \tag{2.2}

A place $p$ is said to be an input or output place for a transition $t$ if there exists a precondition or a postcondition arc from $p$ to $t$ or vice versa (i.e., if $\langle p, t \rangle \in A^-$ or $\langle t, p \rangle \in A^+$, respectively). A place $p$ is said to be an inhibitor place for a transition $t$ if there exists an inhibitor arc from $p$ to $t$ (i.e., if $\langle p, t \rangle \in A^\cdot$).

- $M_0$ is the (initial) marking associating each place with a non-negative number of tokens:
  \[ M_0 : P \rightarrow \mathbb{N}. \] \tag{2.3}

- $EFT^s$ and $LFT^s$ associate each transition $t \in T$ with a static firing interval made by a static Earliest Firing Time and a (possibly infinite) static Latest Firing Time:
  \begin{align*}
  EFT^s : T & \rightarrow \mathbb{R}_0^+, \\
  LFT^s : T & \rightarrow \mathbb{R}_0^+ \cup \{+\infty\}, \\
  EFT^s(t) & \leq LFT^s(t) \quad \forall t \in T, \tag{2.4}
  \end{align*}

where $\mathbb{R}_0^+$ denotes the set of non-negative real numbers.

- $\tau_0$ associates each transition $t \in T$ with an (initial) time to fire:
  \[ \tau_0 : T \rightarrow \mathbb{R}_0^+. \] \tag{2.5}

- $\text{Res}$ is a set of resources disjoint from $P$ and $T$. 

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Preemptive Time Petri Nets

- *Req* associates each transition with a set of requested resources (i.e., a subset of *Res*) called *resource request*:

\[ \text{Req} : T \rightarrow 2^{\text{Res}} \]  

(2.6)

- *Prio* associates each transition with a natural number representing the priority level associated with its resource request:

\[ \text{Prio} : T \rightarrow \mathbb{N} \]  

(2.7)

\(P, T, A^-, A^+, A^\cdot\) comprise a bipartite graph: \(P\) and \(T\) are disjoint classes of nodes, accounting for conditions and events, respectively; \(A^-, A^+, A^\cdot\) are relations between nodes. In the graphic representation (see Fig. 2.1), places are represented as circles, transitions as bars, precondition and post-condition arcs as directed arcs, inhibitor arcs as dot-terminated arcs; tokens of the initial marking are represented as dots inside places; static firing intervals, resource requests, and priority levels are annotated close to their corresponding transitions.

2.1.2 Semantics

The state of a pTPN is a pair

\[ s = \langle M, \tau \rangle \]  

(2.8)

where \(M : P \rightarrow \mathbb{N}\) is a marking and \(\tau : T \rightarrow \mathbb{R}_0^+\) associates each transition with a (dynamic) time to fire. The state dynamically evolves according to a transition rule made by two clauses of firability and firing.

**Firability.** A transition \(t_0\) is *enabled* if each of its input places contains at least one token and none of its inhibitor places contains any token (i.e., \(M(p) \geq 1 \quad \forall p. \langle p, t_0 \rangle \in A^-\) and \(M(p) = 0 \quad \forall p. \langle p, t_0 \rangle \in A^\cdot\)). An enabled transition \(t_0\) is *progressing* if and only if every resource it requires is not required by any other enabled transition with a higher level of priority (i.e., \(\text{Prio}(t_0) \geq \)).
Preemptive Time Petri Nets

\[ Prio(t_i) \quad \forall t_i \in T^e(M) \ , \ \text{Req}(t_0) \cap \text{Req}(t_i) \neq \{\emptyset\}, \] where \( T^e(M) \) denotes the set of transitions enabled by marking \( M \). Transitions that are enabled but not progressing are said to be suspended. A progressing transition \( t_0 \) is firable if its time to fire is not higher than the time to fire of any other progressing transition (i.e., \( \tau(t_0) \leq \tau(t_i) \quad \forall t_i \in T^e(M) \)).

Firing. When a transition \( t_0 \) fires, the state \( s = \langle M, \tau \rangle \) is replace by a new state \( s' = \langle M', \tau' \rangle \). The marking \( M' \) is derived from \( M \) by removing a token from each input place of \( t_0 \) and by adding a token to each output place of \( t_0 \):

\[
\begin{align*}
M_{\text{tmp}}(p) &= M(p) - 1 \quad \forall p \cdot \langle p, t_0 \rangle \in A^- , \\
M'(p) &= M_{\text{tmp}}(p) + 1 \quad \forall p \cdot \langle t_0, p \rangle \in A^+.
\end{align*}
\]

(2.9)

Transitions that are enabled both by the temporary marking \( M_{\text{tmp}} \) and by the final marking \( M' \) are said to be persistent, while those that are enabled by \( M' \) but not by \( M_{\text{tmp}} \) are said to be newly enabled. If \( t_0 \) is still enabled after its own firing, it is always regarded as newly enabled. The time to fire \( \tau' \) of transitions enabled by \( M' \) is computed in different manner depending on whether they are newly enabled, persistent-progressing, or persistent-suspended.

- The time to fire of any newly enabled transition \( t_x \) takes a nondeterministic value within the static firing interval:

\[
EFT^s(t_x) \leq \tau(t_x) \leq LFT^s(t_x).
\]

(2.10)

- The time to fire of any persistent transition \( t_y \) that was progressing in the previous state \( s \) is reduced by the time elapsed in \( s \). This is equal to the time to fire of \( t_0 \) as it was measured at the entrance in the previous state \( s \):

\[
\tau'(t_y) = \tau(t_y) - \tau(t_0).
\]

(2.11)

- The time to fire of any persistent transition \( t_z \) that was suspended in the previous state \( s \) remains unchanged:

\[
\tau'(t_z) = \tau(t_z).
\]

(2.12)
Note that the time to fire of any non-enabled transition does not condition the firability of any transition and thus the future evolution of the net, and it will be reset to a new value as soon as the transition will be enabled again. According to this, the state of a pTPN is sufficiently described by the marking and by the time to fire of enabled transitions.

### 2.2 Modeling real-time task-sets through pTPNs

The expressivity of pTPN models compares with stopwatch automata [58] and with TPNs with inhibitor hyperarcs [106], providing a convenient setting for the representation of the patterns of concurrency and IPC encompassed by the task-set model presented in Sect. 1.4. The process is illustrated with reference to the construction of the CSCI of the Video Processing Unit of the IVSS example of Fig. 1.6. In particular, Fig. 2.1 reports the pTPN model for the Software Design of the Basic Features Extraction CSCI of Fig. 1.8. The task-set is made by five recurrent tasks synchronized by two binary semaphores and a mailbox: $Tsk_1$ performs noise reduction through a median filter; $Tsk_2$ manipulates parameters employed by the noise reduction algorithm; $Tsk_3$ and $Tsk_4$ accomplish edge and corner detection through Sobel and Moravec operators, respectively; $Tsk_5$ manipulates parameters employed by edge and corner detection algorithms. In particular, $Tsk_2$ sends values for parameters of the noise reduction algorithm to $Tsk_1$ by means of a mailbox; $Tsk_3$, $Tsk_4$, and $Tsk_5$ are synchronized on a binary semaphore in order to access a shared memory space, where $Tsk_3$ and $Tsk_4$ read values for parameters of edge and corner detection algorithms written by $Tsk_5$; $Tsk_3$ and $Tsk_4$ are also synchronized on a second binary semaphore in order to write into a second shared memory space the results of edge and corner detection algorithms, respectively.

#### 2.2.1 Tasks, jobs, and chunks

$Tsk_1$, $Tsk_2$, $Tsk_3$ and $Tsk_4$ are periodic tasks, with period equal to 40, 40, 80, and 100 time units, respectively; $Tsk_5$ is a sporadic task with minimum
Figure 2.1. The pTPN model for the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8, representing a task-set composed of five recurrent tasks synchronized by two binary semaphores and a mailbox.

interarrival time equal to 120 time units. Transitions $t_{10}$, $t_{20}$, $t_{30}$, $t_{40}$, and $t_{50}$ model recurrent job releases of $Tsk_1$, $Tsk_2$, $Tsk_3$, $Tsk_4$, and $Tsk_5$, respectively: they have no input places and do not require any resource, so as to fire repeatedly with intertines falling within their respective firing intervals. Job chunks are modeled by transitions with static firing intervals corresponding to the min-max range of Execution Time, associated with resource requests and static priorities (low priority numbers run first). For instance, transition $t_{12}$ represents the completion of the unique chunk of each job of $Tsk_1$, which requires resource cpu with priority 1 for an Execution Time ranging between 5 and 10 time units. In a similar manner, transitions $t_{21}$ and $t_{22}$, transitions
transitions $t_{32}$, $t_{33}$, and $t_{35}$, transitions $t_{43}$, $t_{44}$, and $t_{47}$, and transitions $t_{51}$ and $t_{54}$ model the completion of subsequent chunks for jobs of tasks $Tsk_2$, $Tsk_3$, $Tsk_4$, and $Tsk_5$, respectively. Computations in different jobs may compete for resource $cpu$: for instance, both transitions $t_{21}$ and $t_{51}$ require resource $cpu$, with priority 2 and 5, respectively; if $t_{21}$ becomes enabled while $t_{51}$ is progressing, then $t_{21}$ preempts $t_{51}$ and $t_{51}$ becomes suspended.

### 2.2.2 Semaphore synchronization and priority ceiling

We assume that the access to shared resources is regulated by the priority ceiling emulation protocol [111], which raises the priority of any locking chunk to the highest priority of any chunk that ever uses that lock (i.e., its priority ceiling). Although the protocol does not require the use of semaphores on single-core systems, we assume semaphore synchronization in compliance with the general case of multi-core systems, which are in fact naturally encompassed in modeling and analysis of the approach proposed in this dissertation.

Semaphores are modeled in a straightforward manner as places initially marked with a number of tokens equal to the capacity of the semaphore (i.e., 1 token in case of binary semaphores) and their acquisition operations are modeled as immediate transitions. In the task-set of Fig. 2.1, place $mux_1$ models a binary semaphore synchronizing the first chunk of $Tsk_3$, the first chunk of $Tsk_4$, and the second chunk of $Tsk_5$: wait operations are modeled by transitions $t_{31}$, $t_{42}$, and $t_{53}$; signal operations are represented by transitions $t_{32}$, $t_{43}$, and $t_{54}$, which also account for the completion of the three synchronized chunks. In a similar manner, place $mux_2$ represents a binary semaphore synchronizing the third chunk of $Tsk_3$ with the third chunk of $Tsk_4$: wait operations are modeled by transitions $t_{34}$ and $t_{46}$; signal operations are represented by transitions $t_{35}$ and $t_{47}$, which also account for chunk completions.

According to the priority ceiling emulation protocol, in Fig. 2.1, priorities of tasks $Tsk_4$ and $Tsk_5$ are raised in the sections where they hold a resource. Priority boost operations are modeled in explicit manner by the immediate transitions $t_{41}$, $t_{45}$, and $t_{52}$, which precede semaphore wait operations.
Conversely, the corresponding *deboost* operations are allocated to transitions $t_{43}$, $t_{47}$, and $t_{54}$, which also account for the completion of computation chunks. In fact, preemption by a different task within the priority ceiling can occur at the boost operation but not at deboost, and thus the model does not need to distinguish chunk completion and priority deboost.

2.2.3 Message passing and mailbox synchronization

In real-time programming, semaphores have a well-established and unambiguous semantics which lets them be modeled in a straightforward manner; conversely, message passing primitives are strictly tied to the underlying RTOS. For this reason, this Section refers to a subset of the IPC primitives employed in kernel-mode programming under RTAI [95] and describes how they can be represented through pTPN models. The main intent is to illustrate how pTPNs provide a formal basis for unambiguous specification of the primitives of an RTOS. To this end, various send/receive primitives for message queues and mailboxes are considered, taking into account both blocking and non-blocking communication. Nevertheless, the implementation of message exchanging through mailboxes encompassed by the task-set model of Sect. 1.4 avoids the use of blocking primitives for the sender task, as this would be not suitable for a safety-critical real-time environment.

Moreover, this Section takes into account the problem of *determinization* of the implementation with respect to the specification due to some mechanisms of the RTAI operating system [47]. This enables the identification of the subset of behaviors of the specification that are actually feasible in the implementation, which turns out to have a great importance in the definition of coverage objectives during the testing phase.

2.2.3.1 RTAI Messages

RTAI Messages provide a point-to-point inter-task facility that enables two real-time tasks to pass messages to each other. Messages have a dimension of 4 byte and they are queued up according to the priority of the sender task.
The RTAI primitives \texttt{rt\_send} and \texttt{rt\_receive}

The RTAI primitive \texttt{rt\_send(RT\_TASK* task, unsigned int msg)} sends the message \texttt{msg} to the task \texttt{task}: if the receiver task is ready to get the message, \texttt{rt\_send} does not block the caller task, but its execution can be preempted if the receiver task has a higher priority; otherwise, the caller task is blocked and queued up in priority order on the receive list of the receiver task. The RTAI primitive \texttt{rt\_receive(RT\_TASK* task, unsigned int* msg)} receives a message from the task \texttt{task} and stores it in the 4 byte sized buffer pointed by \texttt{msg}: if there is a pending message, \texttt{rt\_receive} does not block the caller task, but its execution can be preempted if the task that sent the just received message has a higher priority; otherwise, the caller task is blocked waiting for a message to be sent by the sender task. If \texttt{task} is equal to 0, the receiver task accepts messages from any task: if there is a pending message, the task receives the first pending message sent by the sender task with highest priority; otherwise, it is blocked.

Message passing through \texttt{rt\_send} and \texttt{rt\_receive}

Given two real-time tasks that pass messages to each other, the number of messages that the sender task attempts to dispatch during a certain time interval should be equal to the number of messages that the receiver task tries to get; in particular, two periodic tasks whose jobs send/receive the same number of messages should have the same period.

Fig. 2.2 reports the pTPN model for two periodic tasks with equal period and priority that exchange RTAI messages: at each period, \texttt{Tsk\_1} invokes the RTAI primitive \texttt{rt\_send} to pass a message to \texttt{Tsk\_2}, which receives it by means of the RTAI primitive \texttt{rt\_receive}. Transitions \texttt{t\_11} and \texttt{t\_21} model the invocation of primitives \texttt{rt\_send} and \texttt{rt\_receive} by \texttt{Tsk\_1} and \texttt{Tsk\_2}, respectively, and they are post-conditioned by places \texttt{msg} and \texttt{msg\_wait}, respectively: place \texttt{msg} models the message queue and it contains a token if \texttt{Tsk\_1} has sent a message and \texttt{Tsk\_2} has not yet received it; place \texttt{msg\_wait} represents the
Modeling real-time task-sets through pTPNs

waiting queue for jobs of $Tsk_2$ and it contains a token if the current job of $Tsk_2$ is waiting to receive a message. Transitions $t_{12}$ and $t_{22}$ model the return of control to $Tsk_1$ and $Tsk_2$, respectively; after the completion of message dispatch and receipt, respectively: since $rt\_send$ and $rt\_receive$ are both blocking primitives, $t_{12}$ and $t_{22}$ are preconditioned by places $msg$ and $msg\_wait$, respectively.

According to the semantics of pTPNs, transitions $t_{10}$, $t_{11}$, $t_{20}$, and $t_{21}$ fire at the same time under the constraint that the firings of $t_{10}$ and $t_{20}$ precede the firings of $t_{11}$ and $t_{21}$, respectively; after the firing of $t_{11}$ and $t_{21}$, equal-priority transitions $t_{12}$ and $t_{22}$ can fire in any order. However, the implementation of the task-set of Fig. 2.2 under RTAI restricts the set of possible behaviors: tasks with equal period and priority are released in reverse order as they are initially started; tasks with equal period and priority are resumed in reverse order as they are suspended; a task cannot be obviously preempted by another task with equal priority. According to this:

- If $Tsk_1$ is the first task to be released, then it blocks on $rt\_send$ (since $Tsk_2$ is not ready to receive a message); then task $Tsk_2$ is released, it does not block on $rt\_receive$ (since $Tsk_1$ has already sent a message), it cannot be preempted by the equal-priority task $Tsk_1$, and thus it completes the current job by suspending itself until the next period; $Tsk_1$ is then unblocked and it completes the current job by suspending itself until the next period; at the next period, $Tsk_1$ is the first task to be resumed, since it is the last suspended task, and the execution pattern of subsequent periods turns out to be the same.

- If $Tsk_2$ is the first task to be released, then it blocks on $rt\_receive$ (since $Tsk_1$ has not sent a message); then task $Tsk_1$ is released, it does not block on $rt\_send$ (since $Tsk_2$ is ready to receive a message), it cannot be preempted by the equal-priority task $Tsk_2$, and thus it completes the current job by suspending itself until the next period; $Tsk_2$ is then unblocked and it completes the current job by suspending itself until the next period; at the next period, $Tsk_2$ is the first task to be resumed, since
it is the last suspended task, and the execution pattern of subsequent
periods turns out to be the same.

Therefore, in the implementation of the pTPN model of Fig. 2.2 under RTAI,
the only feasible firing sequence is either \{t_{10} \rightarrow t_{11} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{22} \rightarrow t_{12}\}
or \{t_{20} \rightarrow t_{21} \rightarrow t_{10} \rightarrow t_{11} \rightarrow t_{12} \rightarrow t_{22}\},
depending on whether \(Tsk_1\) or \(Tsk_2\) is released first \(^1\).

Figure 2.2. The pTPN model for two periodic real-time tasks with equal period
and priority that exchange messages through a message queue by means of the
RTAI primitives \texttt{rt\_send} and \texttt{rt\_receive}.

If the sender task \(Tsk_1\) has higher priority than the receiver task \(Tsk_2\), the
pTPN model of Fig. 2.2 is modified by assigning transitions \(t_{11}\) and \(t_{12}\) higher
priority than that of transitions \(t_{21}\) and \(t_{22}\). According to the semantics of
pTPNs, transitions fire following the same execution pattern of the model of
Fig. 2.2 under the additional constraints that transitions \(t_{11}\) and \(t_{12}\) overtake
transitions \(t_{21}\) and \(t_{22}\), respectively, when they are concurrently enabled. In
the implementation under RTAI, the higher-priority task \(Tsk_1\) is the first to
be released and it blocks on \texttt{rt\_send}; then task \(Tsk_2\) is released, it does not
block on \texttt{rt\_receive} but it is preempted by \(Tsk_1\), which is thus unblocked and

\(^1\)The braces denote none or more repetitions of the enclosed sequence according to the
Backus-Naur Form (BNF) notation [20].
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completes the current job by suspending itself until the next period; Task2 is in turn unblocked and it completes the current job by suspending itself until the next period; at the next period, the higher-priority task Task1 is the first task to be resumed and the execution pattern of subsequent periods turns out to be the same. Therefore, in the implementation under RTAI, the only feasible firing sequence is $t_{10} \rightarrow t_{11} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{12} \rightarrow t_{22}$.

The case in which the receiver task has higher priority than the sender task is modeled in analogous manner and the only feasible firing sequence of the implementation under RTAI is $t_{20} \rightarrow t_{21} \rightarrow t_{10} \rightarrow t_{11} \rightarrow t_{22} \rightarrow t_{12}$.

The RTAI primitives `rt_send_if` and `rt_receive_if`

The RTAI primitive `rt_send_if(RT_TASK* task, unsigned int msg)` sends the message `msg` to the task `task` if the latter is ready to receive, otherwise it returns with error: the caller task is never blocked, but its execution can be preempted if the receiver task is ready to receive a message and has a higher priority. The RTAI primitive `rt_receive_if(RT_TASK* task, unsigned int* msg)` tries to get a message from the task `task`: if there is a pending message, `rt_receive_if` stores it in the 4 byte sized buffer pointed by `msg`, otherwise it returns with error. The caller task is never blocked but it can be preempted if the task that sent the just received message has a higher priority. If `task` is equal to 0, the caller task accepts messages from any task.

If a task sends messages through `rt_send_if` to a task that attempts to receive them by means of `rt_receive_if`, then neither dispatch nor receipt will be successfully completed. In fact, on the one hand, if the sender task arrives first, then `rt_send_if` returns with error without sending the message, since the receiver task is not ready to receive a message: when the receiver task arrives, `rt_receive_if` returns with error too, because no message is pending. On the other hand, if the receiver task arrives first, then `rt_receive_if` returns with error too, because no message is pending. Since the sender task has not yet sent a message: when the sender task arrives, `rt_send_if` returns with error too, because the receiver task is not waiting for a message. On the basis
of this, if the sender task invokes `rt_send_if` then the receiver task should not invoke `rt_receive_if` and vice versa.

**Message passing through `rt_send` and `rt_receive_if`**

Fig. 2.3 reports the pTPN model for two periodic tasks with equal period and priority that exchange RTAI messages: at each period, `Tsk_1` employs the RTAI primitive `rt_send` to pass a message to `Tsk_2`, which attempts to receive it by means of the RTAI primitive `rt_receive_if` (the case in which the sender task invokes `rt_send_if` and the receiver task invokes `rt_receive` is modeled in analogous manner). Transitions $t_{11}$ and $t_{21}$ model the invocation of primitives `rt_send` and `rt_receive_if` by `Tsk_1` and `Tsk_2`, respectively. Transition $t_{11}$ is post-conditioned by place `msg`, which models the message queue and contains as many tokens as the number of messages sent by `Tsk_1` and not yet received by `Tsk_2`; transition $t_{21}$ is post-conditioned by place `msg_wait`, which represents the waiting queue for jobs of `Tsk_2` and it contains a token if a job of `Tsk_2` is waiting to receive a message. Transition $t_{12}$ models the return of control to `Tsk_1` after the completion of message dispatch and it is pre-conditioned by place `msg_wait`, since `rt_send` is a blocking primitive; transitions $t_{22}$ and $t_{23}$ model the return of control to `Tsk_2` after the successful and unsuccessful completion of message receipt, respectively. According to the semantics of `rt_receive_if`, if the sender task has already sent a message (i.e., if place `msg` contains at least one token), then the message will be correctly received by the caller task; otherwise, if the sender task has not yet sent a message (i.e., if place `msg` contains no tokens), the caller task is not blocked and the primitive returns with error (i.e., a token is removed from place `msg_wait`): based on this, $t_{22}$ has `msg` as input place, and $t_{23}$ has `msg_wait` as input place and `msg` as inhibiting place.

According to the semantics of pTPNs, at the first period, if $t_{11}$ fires before or immediately after $t_{21}$, then $t_{12}$ and $t_{22}$ can fire in any order, while $t_{23}$ is not enabled (i.e., `Tsk_2` successfully receives a message); otherwise, $t_{23}$ fires (i.e., `Tsk_2` fails to receive a message). In the first case, at the end of the period,
each place contains no tokens (i.e., there are no pending jobs) and the next period is thus characterized by the same execution pattern. In the latter case, instead, at the end of the period, places $p_{12}$ and $msg$ contain one token each (i.e., the job of $Tsk_1$ that sent a message during the first period is waiting for a job of $Tsk_2$ to receive it) and the next period is thus characterized by a different execution pattern: the firings of transitions $t_{11}$ and $t_{21}$ add a token to places $p_{12}$ and $msg$ and to places $p_{22}$ and $msg\_wait$, respectively (note that places $p_{12}$ and $msg$ turn out to contain two tokens); this enables the firings of transitions $t_{12}$ and $t_{22}$ (i.e., $Tsk_2$ successfully receives a message); at the end of the period, places $p_{12}$ and $msg$ contain one token each and, thus, all subsequent periods are characterized by this execution pattern (i.e., if a job of $Tsk_2$ fails to receive a message, then the job of $Tsk_1$ released in the same period blocks on $rt\_send$ after sending a message: in all subsequent periods, the new job of $Tsk_2$ successfully receives the pending message and the new job of $Tsk_1$ blocks on $rt\_send$).

The implementation of the task-set of Fig. 2.3 under RTAI restricts the set of feasible behaviors in the following manner:

- If $Tsk_1$ is the first task to be released, it blocks on $rt\_send$ (since $Tsk_2$ is not ready to receive a message); then $Tsk_2$ is released, it successfully receives the pending message (it cannot be preempted by the equal priority task $Tsk_1$) and suspends itself until the next period; $Tsk_1$ is then unblocked and it completes the current job by suspending itself until the next period; at the next period, $Tsk_1$ is the first task to be resumed, since it is the last suspended task, and the execution pattern of subsequent periods turns out to be the same.

- If $Tsk_2$ is the first task to be released, it fails to receive a message (since there are no pending messages) and completes the current job by suspending itself until the second period; then $Tsk_1$ is released and it blocks on $rt\_send$ (since $Tsk_2$ is not ready to receive a message); at the second period, $Tsk_2$ successfully receives the pending message (it cannot be preempted by the equal priority task $Tsk_1$) and it completes the current job and suspends itself until the next period.
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job by suspending itself until the third period; \( Tsk_1 \) is then unblocked and completes the current job by suspending itself until the second period, which has just elapsed; thus, \( Tsk_1 \) is immediately resumed and it blocks on \texttt{rt\_send}; at the third period, \( Tsk_2 \) successfully receives the pending message and the execution pattern of all subsequent periods is the same of the second period.

According to this, in the implementation of the pTPN model of Fig. 2.3 under RTAI, the only feasible firing sequence is either \( \{t_{10} \rightarrow t_{11} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{22} \rightarrow t_{12}\} \) or \( t_{20} \rightarrow t_{21} \rightarrow t_{23} \rightarrow \{t_{10} \rightarrow t_{11} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{22} \rightarrow t_{12}\} \), depending on whether \( Tsk_1 \) or \( Tsk_2 \) is released first.

If the sender task \( Tsk_1 \) has higher priority than the receiver task \( Tsk_2 \), the pTPN model of Fig. 2.3 is modified by assigning transitions \( t_{11} \) and \( t_{12} \) higher priority than that of transitions \( t_{21}, t_{22}, \) and \( t_{23} \). According to the semantics of pTPNs, transitions fire following the same execution pattern of

\begin{figure}[h]
\centering
\includegraphics[width=\textwidth]{image}
\caption{The pTPN model for two periodic real-time tasks with equal period and priority that exchange messages through a message queue by means of the RTAI primitives \texttt{rt\_send} and \texttt{rt\_receive\_if}.}
\end{figure}
the model of Fig. 2.3, under the additional constraint that transitions $t_{11}$ and $t_{12}$ overtake transitions $t_{21}$, $t_{22}$, and $t_{23}$ when they are concurrently enabled.

In the implementation under RTAI, at the first period, the higher-priority task $Tsk_1$ is the first to be released and it blocks on rt_send (since $Tsk_2$ is not ready to receive a message); then $Tsk_2$ is released, it attempts to receive the pending message and it is preempted by $Tsk_1$, which is unblocked and completes the current job by suspending itself until the next period; $Tsk_2$ is then given the control and it completes the current job by suspending itself until the next period; at the next period, the higher-priority task $Tsk_1$ is the first to be resumed and the execution pattern of subsequent periods turns out to be the same. Therefore, in the implementation under RTAI, the only feasible firing sequence is $\{t_{10} \rightarrow t_{11} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{12} \rightarrow t_{22}\}$.

The case in which the receiver task has higher priority than the sender task is modeled in analogous manner and the only feasible firing sequence of the implementation under RTAI turns out to be the same of the case in which the two tasks have equal priority and the receiver task is released first: $t_{20} \rightarrow t_{21} \rightarrow t_{23} \rightarrow \{t_{10} \rightarrow t_{11} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{22} \rightarrow t_{12}\}$.

### 2.2.3.2 RTAI Mailbox

RTAI Mailboxes provide a flexible method for inter-task communications: real-time tasks can send arbitrarily sized messages and multiple senders and receivers are allowed.

The RTAI primitives rt_mbx_send and rt_mbx_receive

The RTAI primitive rt_typed_mbx_init(MBX* mbx, int size, int type) initializes a mailbox mbx of size bytes and type type. The mailbox type defines the policy according to which tasks are queued up: FIFO_Q, PRIOR_Q, and RES_Q for FIFO queueing, task-priority queueing, and task-priority queueing with priority inheritance, respectively. The RTAI primitive rt_mbx_send(MBX* mbx, void* msg, int msg_size) sends a message msg of msg_size bytes to the mailbox mbx: the caller will be blocked until the whole message is copied
into the mailbox or an error occurs, and its execution can be preempted if there is a higher-priority task waiting to receive from the mailbox. The RTAI primitive `rt_mbx_receive(MBX* mbx, void* msg, int msg_size)` receives a message of `msg_size` bytes from the mailbox `mbx` and stores it in the buffer pointed by `msg`: the caller will be blocked until all bytes of the message arrive or an error occurs.

**Mailbox synchronization through `rt_mbx_send` and `rt_mbx_receive`**

Fig. 2.4 reports the pTPN model for two periodic tasks with equal period and priority that exchange messages through an RTAI mailbox: at each period, `Tsk1` invokes the RTAI primitive `rt_mbx_send` to pass a message to `Tsk2`, which receives it by means of the RTAI primitive `rt_mbx_receive`. Transition `t_{11}` models the invocation of `rt_mbx_send` by `Tsk1` and it is post-conditioned by place `mbx`, which represents the mailbox and is initially empty (i.e., place `mbx` contains a token if `Tsk1` has sent a message and `Tsk2` has not yet received it); transition `t_{12}` represents the return of control to `Tsk1` after the completion of message dispatch. Transition `t_{21}` models the invocation of `rt_mbx_receive` by `Tsk2`; transition `t_{22}` represent the return of control to `Tsk2` after the completion of message receipt and it is preconditioned by place `mbx` since `rt_mbx_receive` is a blocking primitive.

According to the semantics of pTPNs, transitions of the model can fire in any order under the constraints that: the firings of `t_{10}` and `t_{20}` precede the firings of `t_{11}` and `t_{21}`, respectively; the firings of `t_{11}` and `t_{21}` precede the firings of `t_{12}` and `t_{22}`, respectively; the firing of `t_{12}` precedes the firing of `t_{22}`. In the implementation of the task-set of Fig. 2.4 under RTAI, the set of feasible behaviors is restricted in the following manner:

- If `Tsk1` is the first task to be released, then it sends a message to the mailbox and completes the current job by suspending itself until the next period; then `Tsk2` is released, it receives the pending message from the mailbox and completes the current job by suspending itself until the next period; at the next period, `Tsk2` is the first task to be resumed (since
it is the last suspended task) and it blocks on \texttt{rt_mbx_receive}; \(Tsk_1\) is then given the control, it sends a message to the mailbox, it cannot be preempted by the equal-priority task \(Tsk_2\) and thus completes the current job by suspending itself until the next period; \(Tsk_2\) is given the control again, it receives the pending message from the mailbox and completes the current job by suspending itself until the next period; at the next period, \(Tsk_2\) is again the first task to be resumed and the execution pattern of all subsequent periods turns out to be the same of the second period.

- If \(Tsk_2\) is the first task to be released, then it blocks on \texttt{rt_mbx_receive}; then \(Tsk_1\) is released, it sends a message to the mailbox, it cannot be preempted by the equal-priority task \(Tsk_2\) and thus completes the current job by suspending itself until the next period; \(Tsk_2\) is given the control again, it receives the pending message from the mailbox and completes the current job by suspending itself until the next period; at the next period, \(Tsk_2\) is the first task to be resumed and the execution pattern of all subsequent periods turns out to be the same of the first period.

According to this, in the implementation of the pTPN model of Fig. 2.4 under RTAI, the only feasible firing sequence is either \(t_{10} \rightarrow t_{11} \rightarrow t_{12} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{22} \rightarrow \{t_{20} \rightarrow t_{21} \rightarrow t_{10} \rightarrow t_{11} \rightarrow t_{12} \rightarrow t_{22}\}\) or \(\{t_{20} \rightarrow t_{21} \rightarrow t_{10} \rightarrow t_{11} \rightarrow t_{12} \rightarrow t_{22}\}\) depending on whether \(Tsk_1\) or \(Tsk_2\) is the first task to be released.

If the sender task \(Tsk_1\) has higher priority than the receiver task \(Tsk_2\), the pTPN model of Fig. 2.4 is modified by assigning transitions \(t_{11}\) and \(t_{12}\) higher priority than transitions \(t_{21}\) and \(t_{22}\). According to the semantics of pTPNs, transitions fire following the same execution pattern of the model of Fig. 2.4, under the additional constraint that transitions \(t_{11}\) and \(t_{12}\) overtake transitions \(t_{21}\) and \(t_{22}\) when they are concurrently enabled. In the implementation under RTAI, at the first period, the higher-priority task \(Tsk_1\) is the first task to be released, it sends a message to the mailbox and completes the current job by suspending itself until the next period; then \(Tsk_2\) is released, it receives the
pending message from the mailbox and completes the current job by suspending itself until the next period; at the next period, the higher-priority task \( Tsk_1 \) is the first to be resumed and the execution pattern of subsequent periods turns out to be the same. Therefore, in the implementation under RTAI, the only feasible firing sequence is \( \{t_{10} \rightarrow t_{11} \rightarrow t_{12} \rightarrow t_{20} \rightarrow t_{21} \rightarrow t_{22}\} \).

The case in which the receiver task has higher priority than the sender task is modeled in analogous manner and the only feasible firing sequence of the implementation under RTAI turns out to be \( \{t_{20} \rightarrow t_{21} \rightarrow t_{10} \rightarrow t_{11} \rightarrow t_{22} \rightarrow t_{12}\} \).

Figure 2.4. The pTPN model for two periodic real-time tasks with equal period and priority that exchange messages through a mailbox by means of the RTAI primitives \( \text{rt_mbx_send} \) and \( \text{rt_mbx_receive} \).

Mailbox synchronization with multiple senders/receivers

The pTPN model of Fig. 2.4 can be easily extended to encompass the case of multiple senders to a single mailbox, by letting \( \text{mbx} \) be an output place for each transition that represents the dispatch of a message.

On the contrary, the case of multiple receivers from a single mailbox cannot be modeled in a straightforward manner through pTPNs and it is thus not taken into account in this dissertation. In fact, the data structure that represents an RTAI mailbox embeds a semaphore, which is acquired by the
first task that attempts to receive a message from the mailbox; subsequent receiver tasks are queued up in FIFO order, priority order, or priority order with priority inheritance, depending on the policy selected when the mailbox was initialized. According to this, when multiple tasks are waiting to receive a message, the first dispatched message is received by the first queued task and subsequent messages are received by the other queued tasks in the order defined by the selected policy. This comprises a behavior that cannot be represented by extending the pTPN model of Fig. 2.4 along the same line as the case of multiple senders, i.e., by letting \( \text{mbx} \) be an input place for each transition that represents the receipt of a message. In such a model, in fact, if place \( \text{mbx} \) is empty and then receives a token, the transition that becomes firable is the transition of the task with the highest priority that is waiting to receive a message, which means that the first dispatched message is received by the waiting task with the highest priority. For this reason, this dissertation does not encompass the case of task-sets with multiple receiver tasks synchronized on the same mailbox.

2.2.3.3 Mailbox synchronization in the example case

In the task-set represented in Fig. 2.1, tasks \( Tsk_1 \) and \( Tsk_2 \) are synchronized through a mailbox, modeled by place \( \text{mbx} \) according to the semantics of RTAI Mailboxes. In particular, the first chunk of each job of \( Tsk_2 \) sends a message to the mailbox according to the semantics of the RTAI primitive \( \text{rt_mbx_send} \), and the unique chunk of each job of \( Tsk_1 \) attempts to receive a message from the mailbox according to the semantics of the RTAI primitive \( \text{rt_mbx_receive} \). Message dispatch is modeled by transition \( t_{21} \), which also accounts for the completion of the first chunk of \( Tsk_1 \); message receipt is modeled by the immediate transition \( t_{11} \).
2.3 Architectural verification of real-time task-sets through pTPNs

Simulation and state-space analysis of pTPN models support early verification of the dynamic architecture of task-sets with respect to correctness requirements pertaining the ordering of events and their quantitative timing.

2.3.1 Simulation of pTPN models

Simulation consists in dynamic execution of the specification model, either in interactive on-line manner (token game animation) or in off-line batch mode. In the latter case, various heuristic strategies can be devised and easily implemented to enlarge coverage of feasible behaviors. Simulation is implemented in a straightforward manner by leveraging on the native operational semantics of pTPNs, without encountering particular limits in the complexity of manageable models. However, while helping in the rapid detection of defects during the early stages of modeling, simulation is not able to guarantee their absence neither to detect subtle defects occurring under critical timing and sequencing conditions. State-space analysis can overcome the limit by attaining complete symbolic coverage of the state-space of the specification model.

2.3.2 State-space analysis of pTPN models

The transition rule of pTPNs defines the way how the state of the model evolves owing to the firing of a transition and, thus, implies the notion of a reachability relation between states. In this relation, the firing of the same transition with different values of the firing time leads to states having the same marking but different valuations of timers associated with transitions. Since the firing time can take values within a dense interval, the set of states that can be reached through the firing of any transition is, in general, a dense one. To obtain a discretely enumerable reachability relation, the state-space is thus partitioned into equivalence classes called state classes, each collecting a
dense variety of states. More specifically, a state classe is comprised of a pair

$$S = \langle M, D \rangle,$$

(2.13)

where $M$ is a marking and $D$ is a firing domain encoded as the space of solutions for the set of constraints limiting the times to fire of enabled transitions. A reachability relation is established among classes:

**Definition 2.3.1** A state class $S'$ is reachable from class $S$ through transition $t_0$, and we write $S \xrightarrow{t_0} S'$, if and only if $S'$ contains all and only the states that are reachable from some state collected in $S$ through some feasible firing of $t_0$.

This reachability relation, sometimes called AE relation [98], defines a graph of reachability among classes that is called state class graph (SCG) and turns out to collect together the states that are reached through the same firing sequence but with different times [25], [27], [122], [34]. A path in the SCG thus assumes the meaning of symbolic run, representing the dense variety of runs that fire a given set of transitions in a given qualitative order with a dense variety of timings between subsequent firings. A symbolic run is then identified by a sequence of transitions starting from a state class in the SCG, and it is associated with a completion interval, calculated over the set of completion times of the dense variety of runs it represents. Note that the same sequence of firings may be firable from different starting classes. According to this, a symbolic execution sequence is the finite set of symbolic runs with the same sequence of firing but with different starting classes.

If the model does not include preemptive behavior, i.e., if it can be represented as a TPN, a firing domain can be expressed as a set of linear inequalities in the form of a DBM constraining the times to fire of enabled transitions [122], i.e., a set of inequalities constraining the difference between the times to fire of any two enabled transitions:

$$D = \{ \tau(t_i) - \tau(t_j) \leq b_{ij} \mid t_i, t_j \in T^e(S) \cup \{t_\ast\}, \text{ with } t_i \neq t_j \} ,$$

(2.14)

where $b_{ij} \in \mathbb{R} \cup \{-\infty, +\infty\}$, $T^e(S)$ is the set of transitions enabled by the marking of class $S$, and $t_\ast$ is the fictitious event of entrance into the class (i.e., $\tau(t_\ast)$
represents the ground time at which the class was entered). A set of inequalities in DBM form allows for multiple evaluations of coefficients \(b_{ij}\) which yield the same space of solutions, and it is associated with a normal form in which each coefficient \(b_{ij}\) coincides with the maximum value of the difference \(\tau(t_i) - \tau(t_j)\) that yields solutions for \(D\). The normal form uniquely exists and can be computed in cubic time in the number of timers as the solution of an all shortest path problem on a complete graph in which each timer \(\tau(t_i)\) is a vertex and each coefficient \(b_{ij}\) is the length of the directed edge from \(\tau(t_j)\) to \(\tau(t_i)\) \cite{55}, \cite{122}, \cite{10}. A firing domain is in normal form if and only if:

\[
b_{ij} \leq b_{ih} + b_{hj} \quad \forall t_i, t_j, t_h \in T^e(S) \cup \{t_s\}.
\] (2.15)

The representation in DBM form of firing domains supports efficient derivation and encoding of successor classes in time \(O(|T^e(S)|^2)\) \cite{122}. The set of timings for the transitions fired along a symbolic run can also be encoded as a DBM, thus providing an effective and compact profile for the range of timings that let the model run along a given firing sequence \cite{122}.

If the model includes preemptive behavior, constraints on timers of suspended transitions can take the form of any kind of linear inequality and thus break the DBM structure of firing domains, which take the form of linear convex polyhedra and require exponential complexity for derivation and encoding \cite{33}, \cite{34}, \cite{106}, \cite{26}. To avoid the complexity, \cite{34} enumerates an approximate relation of succession among state classes, which replaces underlying firing domains with their tightest enclosing DBM. This permits to maintain polynomial complexity in the representation and derivation of state classes, but it does not tightly encompass the constraints deriving from preemptive behavior, thus yielding an over-approximation of the SCG. For any selected path in the over-approximated SCG, the exact set of constraints limiting the set of feasible timings can be recovered, thus supporting clean-up of false behaviors and derivation of exact tightening durational bounds along selected critical runs. In particular, the algorithm provides a tight bound on the minimum and maximum time that can be spent along any symbolic run and provides an encoding of the linear convex polyhedron enclosing all and only the timings.
that let the model execute along a symbolic run.

### 2.3.3 Application to the example case

The Oris Tool [109] supports enumeration of the SCG, selection of symbolic runs attaining specific sequencing and timing conditions and tight evaluation of their range of timings. For the pTPN model of Fig. 2.1, the state-space includes 433 reachable markings, covered by 51079 state classes. For each task, the analysis of the SCG identifies the paths between release and completion of each job and the corresponding execution sequences. Specifically, tasks $Tsk_1$, $Tsk_2$, $Tsk_3$, $Tsk_4$, and $Tsk_5$ have 15295, 10967, 21170, 491703, and 156574 symbolic runs and 497, 113, 935, 25377, and 14044 symbolic execution sequences, respectively. The analysis provides the **Worst Case Completion Time (WCCT)** for each task (12, 14, 30, 58, and 60 time units for $Tsk_1$, $Tsk_2$, $Tsk_3$, $Tsk_4$, and $Tsk_5$, respectively), thus verifying that all deadlines are met with minimum laxity of 28, 26, 50, 22, and 60 time units for $Tsk_1$, $Tsk_2$, $Tsk_3$, $Tsk_4$, and $Tsk_5$, respectively.

As an example, Fig. 2.5 reports the results of trace analysis on a symbolic run of $Tsk_4$ that was selected through state-space analysis as a case in which $Tsk_4$ may attain its WCCT of 58 time units. After the initial job release (i.e., the firing of transition $t_{40}$, not shown in the schema of Fig. 2.5), task $Tsk_4$ is suspended until time +30: first, it undergoes preemption by the releases of tasks $Tsk_1$, $Tsk_2$, and $Tsk_3$; then, it is overtaken by the first chunk of $Tsk_2$, by the unique chunk of $Tsk_1$, and by the second chunk of $Tsk_2$; next, it undergoes preemption by the second chunk of $Tsk_5$ and by the three chunks of $Tsk_3$. Finally, after the completion of its first chunk and before the completion of its second and third chunks, $Tsk_4$ is overtaken again by the releases of tasks $Tsk_1$ and $Tsk_2$, by the first chunk of $Tsk_2$, by the unique chunk of $Tsk_1$, and by the second chunk of $Tsk_2$. Note that $Tsk_5$ is the lowest priority task, but its priority is raised to the level of $Tsk_3$ before the acquisition of the binary semaphore $mux_1$.

Trace analysis detects mutual dependencies among transition firing times
Architectural verification of real-time task-sets through pTPNs

Figure 2.5. A schema illustrating the range of feasible timings for the symbolic run $\rho = S_{5605} \stackrel{t_{10}}{\rightarrow} S_{5795} \stackrel{t_{20}}{\rightarrow} S_{6092} \stackrel{t_{30}}{\rightarrow} S_{6591} \stackrel{t_{40}}{\rightarrow} S_{7198} \stackrel{t_{50}}{\rightarrow} S_{7741} \stackrel{t_{60}}{\rightarrow} S_{8120}$ in the state-space of the pTPN model of Fig. 2.1. The run starts with the release of a job of $Tsk_4$ (i.e., the firing of transition $t_{40}$ that enters state-class $S_{5605}$, not shown in the schema) and terminates with its completion (i.e., the firing of transition $t_{47}$). Time advances along the horizontal axis. Transition firings are represented by arrows and they are positioned at their latest feasible time, while grey-filled rectangles indicate their allowed range of variation (e.g., transition $t_{12}$ fires twice along the sequence: the first time it can fire within time +10 and +12 and the second time it can fire within +46 and +52, and the two firings are displayed at time +12 and +52, respectively). Transitions enabling-periods are marked through rectangles that are either black or white whether the transition is progressing or suspended, respectively (e.g., transition $t_{22}$ fires twice along the sequence and both the times it is suspended until the firing of transition $t_{12}$ and it is then progressing until its own firing). Classes entered at transition firings are listed over the schema (e.g., the firing of transition $t_{10}$ enters state-class $S_{5795}$, which is left at the firing of transition $t_{20}$ to enter state-class $S_{6092}$).
along the sequence (e.g., transition $t_{44}$ can fire between $+47$ and $+56$ and transition $t_{47}$ can fire between $+48$ and $+58$, but the assumption that transition $t_{44}$ fires at time $+56$ restricts $t_{47}$ to fire between $+57$ and $+58$). This may serve to identify the timings that let the system run along that sequence and the specific values that yield the WCCT. In so doing, anomalies are detected as the cases where the WCCT along the run requires that some previous firing occurs before its latest feasible value.
In the activities SD4-SW and SD5-SW, the dynamic architecture of a CSCI is modeled through a semi-formal specification and subsequently translated into the corresponding pTPN model. This enables a direct formalization of the task-set at a higher-level of abstraction, supplying a sort of front-end notation [18] that smooths the complexities of pTPN domain, provides modeling convenience, and facilitates industrial acceptance [23], [17]. This Chapter introduces the semi-formal specification of timelines and illustrates in detail how timeline schemas are translated into pTPN models. An alternative description of task-sets based on UML-MARTE class diagrams [66] is also presented and it is illustrated with reference to a case example.
3.1 Specification of real-time task-sets through timeline schemas

The dynamic architecture of a CSCI can be specified through a graphical representation based on the concept of timeline schema. This comprises a behavioral model which restricts the expressivity of pTPNs in a manner that gives explicit representation to the structural concepts of task, job, chunk, deadline, period, and entry-point, defined in Chapter 1. The Oris Tool [109] supports the specification of a real-time task-set through timelines and enables its automated translation into the corresponding pTPN model through the JComposer MDD framework [43].

3.1.1 Tasks, jobs, and chunks

A task is specified by a name $Tsk$ and a release interval $[min, max]$ (see Fig. 3.1 (a)); in the equivalent pTPN model (see Fig. 3.1 (b)), it is accounted by a transition with no input places. A task can also be associated with a deadline, which has no counterpart in the pTPN model, being part of the descriptive requirements rather than of the operational specification of the task-set. When not specified, the deadline is implicitly assumed to be coincident with the minimum inter-arrival time of task releases.

A chunk is specified by a name $C$, an execution interval $[bcet, wcet]$, a set of resource requests specifying the processors to which the chunk is statically allocated, and the level of priority of its scheduling (see Fig. 3.2 (a)). The set of

\[ Tsk \]

\[ [min, max] \]

\[ \text{deadline} \]

\[ Tsk \]

\[ [min, max] \]

(a) (b)

Figure 3.1. The timeline schema for a task (a) and the transition modeling its job releases in the equivalent pTPN model (b).
resource requests is empty in case the chunk accounts for a waiting state rather than for a computation. In the pTPN model (see Fig. 3.2 (b)), each chunk $C$ is translated into a transition with an input place $C_{in}$. The sequence of chunks that form a task is represented by chaining input places of individual chunks with the initial task release transition. Entry-point functions associated with computation chunks have no counterpart in the pTPN model, but serve in the later stages of coding and testing to attach functional behavior to low-level modules.

![Timeline Schema for a Task with Two Chunks](a) ![Equivalent pTPN Model](b)

Figure 3.2. The timeline schema for a task with two chunks (a) and the equivalent pTPN model (b).

### 3.1.2 Semaphore synchronization and priority ceiling

Semaphore operations are specified by decorating chunks with circles, which are annotated with a (non-atomic) sequence of semaphore operations, each referred to a semaphore name $mutex$, and have different colors depending on the capacity of the semaphore (see Fig. 3.3 (a)). In the corresponding pTPN model (see Fig. 3.3 (b)), each semaphore is translated into a place initially marked with a number of tokens equal to the capacity of the semaphore (i.e., 1 token in case of binary semaphores); a wait operation is accounted by an immediate transition preconditioned by the semaphore place, while a signal operation is collapsed with the completion of the chunk that releases the semaphore. Note that the translation in the pTPN schema incorporates the priority ceiling emulation protocol [111], and thus a boost transition is added, while priority deboost is collapsed with the completion of the chunk.
that releases the semaphore.

![Figure 3.3. The timeline schema for a task with two chunks and a binary semaphore synchronization (a) and the corresponding pTPN model (b).](image)

### 3.1.3 Mailbox synchronization

Mailbox operations are specified by decorating chunks with rectangles annotated with a (non-atomic) sequence of mailbox operations, each referred to a mailbox name `mbx` (see Fig. 3.4 (a)). In the corresponding pTPN model (see Fig. 3.4 (b)), each mailbox is translated into a place with no tokens; a send operation is collapsed with the completion of the chunk that dispatches the message, while a receive operation is accounted by an immediate transition preconditioned by the mailbox place.

### 3.1.4 Example

As a final example, Fig. 3.5 reports the timeline schema for the pTPN of Fig. 2.1, which models the task-set of the Basic Features Extraction CSCI of Fig. 1.8. In the example, entry-point $f_{11}$ performs noise reduction; entry-points $f_{21}$ and $f_{22}$ are the routines that manipulate parameters employed by the noise reduction algorithm; entry-points $f_{31}$ and $f_{41}$ acquire values for parameters employed by the edge and corner detection algorithms, respectively (these values are written in a memory space shared with task $Tsk_5$); entry-points
3.2 Specification of real-time task-sets through UML-MARTE

The dynamic architecture of a CSCI can also be modeled through UML-MARTE class diagrams [66], which support the specification of structural ele-
Figure 3.5. The timeline schema that generates the pTPN model of Fig. 2.1.

ments of a task-set. The representation is illustrated with reference to the UML-MARTE class diagram of Fig. 3.6, which models the task-set of the Basic Features Extraction CSCI of Fig. 1.8. It is worth noting that the UML-MARTE class diagram comprises a structural representation of the task-set, which is not sufficient to recover the behavioral semantics of the timeline specification shown in Fig. 3.5. The translation of UML-MARTE class diagrams into pTPN models is omitted, since the process is analogous to the case of the derivation of pTPN models from timeline schemas.

- Each task is represented by an object of class Task, specified through the stereotype SwSchedulableResource which represents a resource that executes concurrently with other resources under the supervision of a scheduler. The class Task supports the definition of a deadline, a priority
Figure 3.6. The UML-MARTE class diagram that generates the pTPN model of Fig. 2.1.

level, a resource request, and release policy; in particular, it is specialized into the classes *Periodic Task* and *Sporadic Task* depending on whether the release policy is periodic or sporadic (note that, in this schema, the jittering release policy can be considered as a particular case of the
In Fig. 3.6, the object $Tsk1$ accounts for a periodic task with period of 40 time units and deadline coincident with its period, which releases jobs made by chunks which require resource $CPU$ with priority level 1.

- Each chunk is accounted by an object of class $Chunk$, associated with the stereotype $EntryPoint$ which supplies a routine to be executed. The class $Chunk$ also supports the specification of a minimum and a maximum Execution Time. The task $Tskx$ which a chunk $Cxy$ belongs to is specified by a dependency from the object $Tskx$ to the object $Cxy$. In Fig. 3.6, the object $C11$ represents the unique chunk of jobs of task $Tsk1$, having an Execution Time comprised between 1 and 2 time units.

- Binary semaphores are modeled as objects of class $Binary\_Semaphore$, specified through the stereotype $SwMutualExclusionResource$ which represents a resource used to synchronize access to shared variables. An operation on a semaphore $mux$ performed by a chunk $Cxy$ belonging to task $Tskx$ is specified through a dependency from the object $Tskx$ to the object $mux$, annotated with the chunk name and with the type of operation (i.e., $wait$ or $signal$). In Fig. 3.6, chunk $C31$ of task $Tsk3$ performs a wait and a signal operation on semaphore $mux1$.

- Mailboxes are represented by objects of class $Mailbox$, specified through the stereotype $MessageComResource$, which models a communication resource used to exchange messages. An operation on a mailbox $mbx$ performed by a chunk $Cxy$ belonging to task $Tskx$ is specified through a dependency from the object $Tskx$ to the object $mbx$, annotated with the chunk name and with the type of operation (i.e., $send$ or $receive$). In Fig. 3.6, chunk $C11$ of task $Tsk1$ performs a receive operation on mailbox $mbx$. 
In the activity SD6-SW, the implementation of the dynamic architecture of each CSCI is derived from the timeline model, either in automated manner or through disciplined manual programming. As a salient trait, in any case the resulting code has a readable structure, which follows natural and readable patterns of concurrent programming and which closely mirrors the structure of the corresponding pTPN model. The translation of a timeline schema into C-code has been developed and experimented for a single-processor application for both RTAI [95] versions 3.3 and 3.6 and VxWorks [103] releases 5.5 and 6.2. This Chapter reports the salient aspects of the code produced by the JComposer MDD framework [43] of the Oris Tool [109] which assumes an RTAI 3.6 patch on Linux kernel 2.6.25 as target platform.

The correspondence between the pTPN model and the code also enables a measurement-based approach to Execution Time profiling, supports the assessment of the accuracy of measures and permits to gain insight in the behavior of the underlying RTOS pertaining ordering and timeliness of events. In parti-
cicular, this Chapter reports results of the experimentation conducted on RTAI concerning the verification of time-frame requirements of low-level modules, the evaluation of the Execution Time of various primitives, and the estimation of the context switch time.

4.1 Implementation of the dynamic architecture of a CSCI under RTAI

The implementation of the dynamic architecture of a CSCI assumes the following responsibilities: release task jobs according to their policies; invoke semaphore operations and connected priority handling operations; invoke mailbox operations; enforce sequenced invocation of entry-point methods. The UML-MARTE class diagram [61], [66] reported in Fig. 4.1 describes the architecture of the implementation. Listings 4.1, 4.2, 4.3, and 4.4 report fragments of the code that implements the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8, specified by the timeline schema of Fig. 3.5 and by the corresponding pTPN model of Fig. 2.1; Fig. 4.2 illustrates the correspondence of components of the timeline schema, the code, and the underlying pTPN model with reference to task Task 4 of Fig. 3.5. Temporal parameters of the timeline schema and the pTPN model are assumed to be expressed in milliseconds.

The task-set is implemented as a kernel module, loaded into the kernel space through the entry-point init_module (class Load_Module in Fig. 4.1) and unloaded at the end of the execution through the exit-point cleanup_module (class Unload_Module in Fig. 4.1). The entry-point init_module allocates data structures that are used in the task-set and the exit-point cleanup_module deletes them: in Listings 4.1 and 4.2, these include two binary semaphores mux1 and mux2 and a mailbox mbx, which are explicitly represented in the timeline model of Fig. 3.5, a binary semaphore named asynch_mux5 and a shared memory space named ASYNCH_SHM, which are instrumental to the implementation of the sporadic task Task 5.
Figure 4.1. UML-MARTE class diagram for the implementation structure of the dynamic architecture of a CSCI under RTAI. The stereotype SwResource represents a software structural entity provided to the user by the execution support. SwMutualExclusionResource, MessageComResource, and SharedDataComResource are subtypes of SwResource and they describe a resource commonly used to synchronize access to shared variables, a communication resource used to exchange messages, and a specific resource used to share the same area of memory among concurrent resources, respectively. The stereotype SwConcurrentResource specializes SwResource and represents an entity that provides a routine with an executing context; the stereotype SwSchedulableResource, in turn, specializes SwConcurrentResource and describes a resource that executes concurrently with other resources under the supervision of a scheduler, modeled by the stereotype Scheduler. An EntryPoint supplies a routine executed in the context of a SwConcurrentResource and a BehavioralFeature actually represents the routine to be executed.
Binary semaphores are implemented as RTAI binary semaphores (class BinarySemaphore in Fig. 4.1). A semaphore is created through the RTAI primitive `rt_typed_sem_init(SEM* sem, int value, int type)`, which initializes a semaphore `sem` of initial value `value` and type `type` (the type of a semaphore is BIN_SEM, CNT_SEM, and RES_SEM for binary, counting, and resource semaphores, respectively), and it is deleted by means of the RTAI primitive `rt_sem_delete(SEM* sem)`. RTAI binary semaphores require explicit priority handling operations to implement the priority ceiling emulation protocol [111]. Actually, RTAI resource semaphores natively implement priority inheritance and they could be encompassed in the model by extending the semantics of pTPNs with marking-dependent priorities without significantly impacting on state-space analysis techniques [33]; however, the construct was not used to facilitate portability across different RTOSs.

Mailboxes are implemented as RTAI Mailboxes (class Mailbox in Fig. 4.1), created and deleted through the RTAI primitives `rt_typed_mbx_init` and `rt_mbx_delete` described in Section 2.2.3, respectively. A shared memory space (class SharedMemorySpace in Fig. 4.1) is created through the RTAI primitive `void* rtai_kmalloc(unsigned long name, int size)`, which allocates in the kernel space a chunk of memory of size `size` bytes and identifier `name` to be shared among kernel modules and Linux tasks, and returns a pointer to the allocated space on success \(^1\); a shared memory space is deleted by means of the RTAI primitive `rtai_kfree(void* adr)`, which frees the chunk of memory pointed by `adr`.

### 4.1.1 Implementation of periodic tasks

For each task \(Tsk_x\) of the specification, the entry-point `init_module` creates a real-time task `tskx` through the RTAI primitive `rt_task_init(RT_TASK* task, void (*)(int), int data, int stack_size, int priority, int uses_fpu, void (*)(void))`, which associates a

\(^1\)The RTAI primitive `nam2num(const char* name)` converts a 6-characters string name to its corresponding unsigned long identifier.
// Define constants
#define MILLISEC 1000000
#define ASYNCH_SHM_SIZE 10000

// Initialize semaphores and message box
SEM mux1, mux2, asynch_mux5;
MBX mbx;
long long* asynch_shared_memory;

// Initialize the kernel module
int init_module(void)
{
    RT_TASK tsk1, tsk2, tsk3, tsk4, tsk5, asynch_tsk5;
    long long start1, start2, start3, start4, start5, time;

    rt_typed_sem_init(&mux1, 1, BIN_SEM);
    rt_typed_sem_init(&mux2, 1, BIN_SEM);
    rt_typed_sem_init(&asynch_mux5, 0, BIN_SEM);
    rt_typed_mbx_init(&mbx, 1024, PRIO_Q);
    asynch_shared_memory = (long long*) rtai_kmalloc(nam2num(ASYNCH_SHM),
                                                      ASYNCH_SHM_SIZE*sizeof(long long));

    rt_task_init(&tsk1, (void*) tsk1_job, 0, 10000, 1, 0, 0);
    rt_task_init(&tsk2, (void*) tsk2_job, 0, 10000, 2, 0, 0);
    rt_task_init(&tsk3, (void*) tsk3_job, 0, 10000, 3, 0, 0);
    rt_task_init(&tsk4, (void*) tsk4_job, 0, 10000, 4, 0, 0);
    rt_task_init(&tsk5, (void*) tsk5_job, 0, 10000, 5, 0, 0);
    rt_task_init(&asynch_tsk5, (void*) asynch_tsk5_job, 0, 2000, 0, 0, 0);

    rt_set_periodic_mode();
    start_rt_timer(nano2count(500000));
    time = rt_get_cpu_time_ns();

    start1 = nano2count(time + 1000*MILLISEC + 40*MILLISEC);
    start2 = nano2count(time + 1000*MILLISEC + 40*MILLISEC);
    start3 = nano2count(time + 1000*MILLISEC + 80*MILLISEC);
    start4 = nano2count(time + 1000*MILLISEC + 100*MILLISEC);
    start5 = nano2count(time + 1000*MILLISEC + 120*MILLISEC);

    rt_task_make_periodic(&tsk1, start1, nano2count(40*MILLISEC);
    rt_task_make_periodic(&tsk2, start2, nano2count(40*MILLISEC);
    rt_task_make_periodic(&tsk3, start3, nano2count(80*MILLISEC);
    rt_task_make_periodic(&tsk4, start4, nano2count(100*MILLISEC);
    rt_task_make_periodic(&asynch_tsk5, start5, nano2count(120*MILLISEC);

    rt_task_resume(&tsk5);

    return 1;
}

Listing 4.1. The entry-point init_module of the kernel module implementing
the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8.
void cleanup_module(void)
{
    stop_rt_timer();

    rt_sem_delete(&mux1);
    rt_sem_delete(&mux2);
    rt_sem_delete(&asynch_mux5);
    rt_mbx_delete(&mbx);

    rt_task_delete(&tsk1);
    rt_task_delete(&tsk2);
    rt_task_delete(&tsk3);
    rt_task_delete(&tsk4);
    rt_task_delete(&tsk5);
    rt_task_delete(&async_tsk5);
}

Listing 4.2. The exit-point cleanup_module of the kernel module implementing the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8.

real-time task task with an entry-point function rt_thread, with a priority level priority, and with a stack of stack_size bytes (class Task in Fig. 4.1). The exit-point cleanup_module deletes the real-time tasks through the RTAI primitive rt_task_delete(RT_TASK* task). In Listing 4.1, the entry-point function associated with a real-time task tskx is named tskx_job and it is responsible for the execution of task jobs (class Job in Fig. 4.1).

For each periodic task of the specification (tasks Tsk1, Tsk2, Tsk3, and Tsk4 in the timeline model of Fig. 3.5), init_module also defines a start time and a period, through the RTAI primitive rt_task_make_periodic(RT_TASK* task, RTIME start_time, RTIME period)2 (class Periodic_Task in Fig. 4.1). The primitive does not make the real-time task actually recurrent and periodic, but only guarantees that an invocation of the RTAI primitive rt_task_wait_period(void) will suspend the task until the start-time of the next period.

To make the task recurrent, an explicit loop control structure is programmed in the function tskx_job that performs job executions, and each repetition of the loop is completed with an invocation of rt_task_wait_period, as re-

2The RTAI primitive nano2count(RTIME nanosecs) converts the time of nanosecs nanoseconds into internal count units.
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```c
int message1, message2;
static void tsk1_job(int t) {
    while(1) {
        rt_mbx_receive(&mbx, &message1, sizeof(int));
        f11();
        rt_task_wait_period();
    }
}
static void tsk2_job(int t) {
    while(1) {
        f21();
        rt_mbx_send(&mbx, &message2, sizeof(int));
        f22();
        rt_task_wait_period();
    }
}
static void tsk3_job(int t) {
    while(1) {
        rt_sem_wait(&mux1);
        f31();
        rt_sem_signal(&mux1);
        f32();
        rt_sem_wait(&mux2);
        f33();
        rt_sem_signal(&mux2);
        rt_task_wait_period();
    }
}
static void tsk4_job(int t) {
    while(1) {
        rt_change_prio(rt_whoami(), 3);
        rt_sem_wait(&mux1);
        f41();
        rt_sem_signal(&mux1);
        rt_change_prio(rt_whoami(), 4);
        f42();
        rt_change_prio(rt_whoami(), 3);
        rt_sem_wait(&mux2);
        f43();
        rt_sem_signal(&mux2);
        rt_change_prio(rt_whoami(), 4);
        f44();
        rt_task_wait_period();
    }
}
```

Listing 4.3. Implementation of job executions for periodic tasks Tsk₁, Tsk₂, Tsk₃, and Tsk₄ of the timeline schema of Fig. 3.5, which models the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8.
ported in Listing 4.3. The loop body of $\text{t}sk_x\_\text{job}$ implements a single job by performing: invocation of entry-point functions that execute chunk computations (in Listing 4.3, $\text{t}sk_1\_\text{job}$ invokes the entry-point $f_{11}$ of the unique chunk of $Tsk_1$; $\text{t}sk_2\_\text{job}$ invokes the entry-points $f_{21}$ and $f_{22}$ of the two chunks of $Tsk_2$; $\text{t}sk_3\_\text{job}$ invokes the entry-points $f_{31}$, $f_{32}$, and $f_{33}$ of the three chunks of $Tsk_3$; $\text{t}sk_4\_\text{job}$ invokes the entry-points $f_{41}$, $f_{42}$, and $f_{43}$ of the three chunks of $Tsk_4$); wait and signal semaphore operations (by means of the RTAI primitives $\text{rt\_sem\_wait}(\text{SEM* sem})$ and $\text{rt\_sem\_signal}(\text{SEM* sem})$, respectively); priority boost and deboost operations according to the priority ceiling emulation protocol (through the RTAI primitive $\text{rt\_change\_prio}(\text{RT\_TASK* task, int priority})$, which is passed the pointer to the current real-time task returned by the RTAI primitive $\text{RT\_TASK* rt\_whoami(\text{void})}$); mailbox send and receive operations (by means of the RTAI primitives $\text{rt\_mbx\_send}$ and $\text{rt\_mbx\_receive}$ described in Section 2.2.3).

Before activating any real-time task, the entry-point $\text{init\_module}$ starts the timer in periodic mode with a period of 500 $\mu$s through the RTAI primitives $\text{rt\_set\_periodic\_mode(\text{void})}$ and $\text{start\_rt\_timer(\text{int period})}$. The exit-point $\text{cleanup\_module}$ stops the timer through the RTAI primitive $\text{stop\_rt\_timer(\text{void})}$.

### 4.1.2 Implementation of jittering and sporadic tasks

Jittering and sporadic tasks of the specification (the sporadic task $Tsk_5$ in the timeline model of Fig. 3.5) account for asynchronous jobs that must be scheduled on reaction to external stimuli, whose timing is not under control of the task-set but only subject to an expected restriction on the minimum and maximum time that can elapse between subsequent occurrences (class $\text{Sporadic\_Task}$ in Fig. 4.1). In the dynamic architecture, they are thus implemented as jobs scheduled on reaction to the arrival of a signal. Synchronization is performed by the way of a semaphore (the binary semaphore $\text{t}sk_5\_\text{mux}$ in Listings 4.1, 4.2, and 4.4) which is supposed to receive a signal on each release. According to this, each real-time task $\text{t}sk_x$ implemen-
Implementation of the dynamic architecture of a CSCI under RTAI

Figure 4.2. A fragment of the code implementing the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8, reporting the implementation of job executions for the periodic task Task4 and illustrating the correspondence between the timeline schema, the code, and the pTPN model.

ting an asynchronous task of the specification (the real-time task tsk5 with entry-point tsk5_job in Listings 4.1, 4.2, and 4.4) is activated through the RTAI primitive rt_task_resume(RT_TASK* task), which makes the newly created task ready to run. The entry-point tskx_job associated with tskx embeds a while loop and blocks on the semaphore at each repetition. Asynchronous signals of the semaphore are performed by an additional periodic real-time task that varies its period at each activation through the RTAI primitive rt_set_period(RT_TASK* task, RTIME new_period) (the real-time
Listing 4.4. Implementation of sporadic job releases and job executions for task $T_{sk5}$ of the timeline schema of Fig. 3.5, which models the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8.

Task $\text{async}_t$ with entry-point $\text{async}_t$ in Listings 4.1, 4.2, and 4.4). The new period is sampled according to a given probability distribution within the interval constrained between the minimum and the maximum inter-arrival time of the asynchronous task of the specification.

Since function $\text{double rand()}$ cannot be invoked within a kernel module, values are pre-calculated by a task in the user space (not represented in Listings 4.1, 4.2, and 4.4) and written in a memory space shared with the kernel module (the memory space pointed by $\text{async}_t$ in Listings 4.1, 4.2, and 4.2). To ensure that the inter-time between subsequent signals of the
Implementation of the dynamic architecture of a CSCI under RTAI

Semaphore actually follows the given probability distribution, the additional periodic real-time task is given maximum priority (i.e., priority level 0).

4.1.3 Observation of reentrant jobs

Possibly reentrant job releases (which occur whenever the completion time of a job exceeds the time between subsequent releases) are included by the semantics of pTPNs, but they are not encompassed by the proposed implementation architecture. They could be included by employing a separate task for each job release. As illustrated in Listing 4.5, for each task $Tsk_x$ of the specification, \texttt{init\_module} would create a real-time task $tsk_x$ with entry-point $tsk_x\_release$ and would start it through the RTAI primitive \texttt{rt\_task\_make\_periodic} or \texttt{rt\_task\_resume} depending on whether $Tsk_x$ is periodic or asynchronous, respectively: at each repetition, the body loop of $tsk_x\_release$ would spawn a real-time task that performs a task job, using a mechanism of multiple buffering to associate each real-time task with a different task handler (the buffer $tsk_x\_job\_array$ in Listing 4.5). To ensure that job releases occur timely, $tsk_x$ is given maximum priority (i.e., priority level 0). This implementation pattern would keep the Execution Time of each loop in $tsk_x\_release$ short, thus avoiding the case in which the completion of a job comes after the task deadline has elapsed, i.e., the case in which the invocation of \texttt{rt\_task\_make\_periodic} by a periodic real-time task comes after the end of the task release period or the completion of a loop repetition by an asynchronous real-time task comes after the end of the task minimum release intertime. However, this would break the recommendation of main regulatory standards applied to the construction of safety-critical software that real-time tasks do not create any other task (e.g., the Ravenscar profile [38]), and it could be adopted in the early implementation stage in order to detect reentrant job releases until verification guarantees that all jobs are completed within the minimum release intertime of their respective tasks.
Implementation of the dynamic architecture of a CSCI under RTAI

Listing 4.5. A fragment of the code of the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8 following a pattern that supports the observation of reentrant jobs.
4.2 Executable Architecture of a CSCI

The code produced in the implementation of the dynamic architecture of a CSCI provides an opportunity to concretely realize the concept of *Executable Architecture* that comprises one of the core principles of UP development [82]. To this end, chunk computations attached to the entry-points and job releases of asynchronous tasks can be replaced through calls to busy-sleep and wait functions providing a scaffolding implementation conforming with expected timing requirements: this yields an executable code that implements the architecture of the task-set before the construction of any of its functional capabilities. As usual in UP development, this provides a baseline for incremental integration and testing of low-level modules. In particular, in the activity SD6.3-SW, this supports separate *Execution Time measurement* and *unit-testing* of low-level modules embedded within their expected operation environment. This has a number of relevant advantages: the scaffolding effort needed to support unit testing of each module is largely reduced; Execution Time measurement accounts for pipeline and cache damage induced by the execution in preemptive interrupted mode; unit testing is carried out under the general setting of the specification model rather than under a specific integration scenario where each module implements only a subset of behaviors accepted by the specification; this anticipates part of integration testing and confines the effects of changes in individual modules.

4.3 Execution Time profiling

The specification of the task-set allocated to a CSCI includes temporal parameters playing different roles that subtend different hurdles in the development process: task periods are a design choice that can be easily enforced in the implementation; minimum release inter-times and deadlines are derived from high-level requirements and do not have a direct counterpart in the implementation; whereas, chunk Execution Times account for the time spent by functions attached to the entry-points of the specification, and thus comprise
requirements for low-level software components, which are not easy at all to predict and control.

In the early stages of development, Execution Times are determined through a tentative approach which mainly relies on analogy with previous realizations of comparable functionalities on comparable platforms. As the development process advances and functions attached to the entry-points become available, actual Execution Times must be evaluated, to verify the satisfaction of allocated bounds or to relax/tighten the initial estimates. To this end, the development process requires that an agile approach to the estimation of Worst Case Execution Times (WCETs) and Best Case Execution Times (BCETs) be integrated in the life cycle. In general, this can be done either through a static or through a measurement-based method [124]. Static tools (e.g., Heptane [52], aiT [65], Bound-T [74]) provide lower and upper bounds for Execution Times by combining control-flow analysis of code structure to a model of the hardware architecture; measurement-based tools (e.g., RapiTime [24], MTime [123], Symta/P [32], [117]) derive estimates through the conjoint use of analysis of the code architecture and measurements of the Execution Time of sections of code by means of partial/full hardware tracing support or simulation.

### 4.3.1 A measurement-based approach through pTPNs

In the context of the methodology proposed in this dissertation, imprecise estimates on Execution Times may jeopardize sensitization and coverage analysis; moreover, verification is in any case supported by the evidence of testing. Precise estimates thus appear to be more relevant than safe bounds. According to this, a measurement-based approach is assumed, which can be implemented in a simple yet effective manner by developing on the formal basis of pTPNs. In fact, the pTPN model enables the reconstruction of the Execution Time of chunk computations from a proper sequence of time-stamped logs and provides estimates for BCETs and WCETs, the distribution of observed Execution Times, and a measure of coverage of the state-space. In particular, the approach is independent of the complexity of the code and of the correspon-
ding pTPN model. As a salient trait, unlike RapiTime and MTime tools, in the proposed method, measurements are carried out by letting chunks run in the Executable Architecture of the task-set, and thus enabling to account for possible dataflow dependencies as well as for cache and pipeline damages due to the execution in interrupted mode within a concurrent preemptive context.

The proposed approach can be efficiently implemented through automated instrumentation of the task-set architecture code in order to produce a time-stamped log for each event corresponding to each transition in the pTPN model of the dynamic architecture. By construction, these are: the release of a task job; the completion of a chunk; the completion of a wait operation on a semaphore; the boost of a priority before a semaphore access; the completion of the receipt of a message from a mailbox. The initial state of an execution is easily identified, either through the implementation of a reset function, or though a technique of state identification such as that employed in [62]. The sequence of time-stamped logs supports reconstruction of the sequence of states visited during the execution and enables the evaluation of the sojourn time in each state. In turn, each state also determines which transitions are newly enabled or persistent and which are progressing or suspended. The Execution Time of a chunk can thus be evaluated as the time during which the transition that represents the chunk completion has been enabled and progressing since it was newly enabled. This can be derived off-line as the sum of sojourn times in the visited states where the transition is progressing:

$$ET(t^n_i) = \sum_{k=n}^{K_{i,n}-1} c_{i,k} \cdot (\tau_{k+1} - \tau_k) \quad (4.1)$$

where: $t^n_i$ is the instance of transition $t_i$ newly enabled in the $n$-th state visited by the trace; $c_{i,k}$ is either 1 or 0 whether $t_i$ is progressing or suspended in the $k$-th state visited by the trace; $K_{i,n}$ is the index (in the trace) of the state reached through the firing of $t^n_i$; $\tau_k$ is the time of entrance into the $k$-th state visited by the trace, i.e., the $k$-th time-stamp in the log.
4.3.2 Code instrumentation

The responsibility of time-stamped logging is conveniently allocated to the implementation of the dynamic architecture, supporting reuse and avoiding the need to perturb the code of functions attached to chunk entry-points. Listing 4.6 reports a fragment of the instrumented code that implements the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8. Since file operations are not available in the kernel space (and would in any case take time beyond the acceptable limits), the time-stamped log is written on an RTAI FIFO queue by the real-time task-set and transferred on a file by a low-priority task running in the user space (not represented in Listing 4.6). The FIFO queue is created by the entry-point \texttt{init\_module} through the RTAI primitive \texttt{rtf\_create(unsigned int fifo, int size)}, which initializes a real-time fifo queue of size \texttt{size} and assigns it the identifier \texttt{fifo} (\texttt{LOG\_FIFO} in Listing 4.6), and it is destroyed by the exit-point \texttt{cleanup\_module} by means of the RTAI primitive \texttt{rtf\_destroy(unsigned int fifo)}.

Each event is described by the variable \texttt{struct Timed\_Action}, which comprises the action identifier (i.e., the identifier of the transition which the action corresponds to) and the time at which the action occurred. Time-stamped actions are logged on the FIFO queue through the RTAI primitive \texttt{rtf\_put(unsigned int fifo, void * buf, int count)}, which writes the block of data of \texttt{count} bytes pointed by \texttt{buf} on the FIFO queue with identifier \texttt{fifo}. In order to observe the timely release of jobs, recurrent real-time tasks are given highest priority and a separate task for each job is used, according to the implementation pattern described in Section 4.1.3.

4.3.3 Experimental results

The proposed approach to Execution Time profiling is supported by the Oris Tool and was applied in the development of the Basic Features Extraction CSCI of Fig. 1.8 in unit-testing of low-level modules. As an example, Fig. 4.3 reports experimental results obtained for an input-data dependent implementation of the edge detection module, represented by computation chunk $C_{21}$.
#define LOG_FIFO 0

struct Timed_Action { int action; long long time;};

int init_module(void) {
    rtf_create(LOG_FIFO, 100000)
    ...
    return 1;
}

tsk4_release(int t) {
    static RT_TASK tsk4_job_array[TASK_BUFFER_SIZE];
    struct Timed_Action ta;
    int i = 0;
    while (1) {
        rt_task_init(&tsk4_job_array[i], (void*) tsk4_job, 0, 100000, 4, 0, 0);
        rt_task_resume(&tsk4_job_array[i]);
        i = (i + 1)% TASK_BUFFER_SIZE;
        ta.time = (long long) rt_get_cpu_time_ns();
        ta.transition = 40;
        rtf_put(LOG_FIFO, &ta, sizeof(struct TimedAction));
        rt_task_wait_period();
    }
}

tsk4_job(int t) {
    struct Timed_Action ta;
    rt_change_prio(rt_whoami(), 3);
    ta.time = (long long) rt_get_cpu_time_ns();
    ta.transition = 41;
    rtf_put(LOG_FIFO, &ta, sizeof(struct TimedAction));
    rt_sem_wait(&mux1);
    ta.time = (long long) rt_get_cpu_time_ns();
    ta.transition = 42;
    rtf_put(LOG_FIFO, &ta, sizeof(struct TimedAction));
    ... 
f43();
    rt_sem_signal(&mux2);
    rt_change_prio(rt_whoami(), 4);
    ta.time = (long long) rt_get_cpu_time_ns();
    ta.transition = 47;
    rtf_put(LOG_FIFO, &ta, sizeof(struct TimedAction));
}

void cleanup_module(void) {
    rtf_destroy(LOG_FIFO);
    ...
}

Listing 4.6. A fragment of the instrumented code that implements the dynamic architecture of the Basic Features Extraction CSCI of Fig. 1.8.
associated with entry-point \( f_{21} \) in the timeline model of Fig. 3.5. Observed Execution Times fall in the interval \([7.771, 8.620]\) ms with a peak on 7.955 ms, accomplishing the time-frame requirement of \([5, 10]\) ms. Note that Execution Times exhibit a quite wide spectrum with various peaks, due to a set of input-data dependent alternatives in the implementation of the module, and the distribution of peaks depends on the distribution of input-data.

An input-data independent implementation of the edge detection module was developed and Execution Times observed on the same data-set are reported in the histogram of Fig. 4.4: they fall in the interval \([7.279, 7.371]\) ms with a peak on 7.334 ms, showing a thinner spectrum and thus evidencing a substantial independence from input-data.
4.4 Timing observability and control

An experimental assessment was carried out to evaluate the accuracy of measures and the perturbation induced by time-stamped logging. Reported results refer to the case of an Intel Core 2 Quad Q6600 desktop processor, without loss of generality of the methodology which is platform-independent.

4.4.1 Estimation of the Execution Time of primitives

The Execution Time of various RTAI primitives (listed in Table 4.1) was estimated through a periodic real-time task that repeatedly measures time before and after calling the primitive under test. Timings were measured through the RTAI primitive `rt_get_cpu_time_ns(void)`, whose overhead was made negligible through the repetition of multiple calls of the primitive between subsequent timings: this is based on the assumption that the Execution Time of a primitive is constant and not affected by the repetition of consecutive calls.
Timing observability and control

To support the hypothesis, a preliminary experiment was carried out through a periodic task that repeatedly observes the completion time of each execution of the primitive under test: the difference between subsequent observed values of time represents a coarse estimation of the Execution Time of the primitive, but it is suitable to reveal significant jitters. Fig. 4.5 reports the pTPN model that specifies the behavior of the task: periodic releases are modeled by the firings of transition $job\_release$; each job repeatedly performs a call of the primitive under test and a call of the primitive that measures time, which are accounted by the firings of transitions $primitive\_under\_test$ and $get\_time$, respectively, and it finally writes the observed values of time on a FIFO queue, which corresponds to the firing of transition $fifo\_put$; multiple calls of the primitive under test and related measures of time are modeled by means of transition $loop$ and place $iterations$, which prevent transition $fifo\_put$ from firing until transitions $primitive\_under\_test$ and $get\_time$ have fired a number of times equal to the number of tokens in place $iterations$ (one hundred thousand tokens in Fig. 4.5). Temporal parameters of the pTPN model of Fig. 4.5 are expressed in milliseconds and they are directly derived from preliminary experimental results, which point out that the Execution Time of each of the RTAI primitives under consideration plus $rt\_get\_cpu\_time\_ns$ is lower than $2 \mu s$: according to this, the completion of a primitive is modeled through an immediate transition and the task is given a period of $200 ms$ (since the repetition of one hundred thousand calls of one of the primitives under test

---

**Figure 4.5.** The pTPN model for a periodic task that repeatedly logs the completion time of each execution of a given primitive. Temporal parameters are expressed in milliseconds.
Timing observability and control

and one hundred thousand calls of \texttt{rt\_get\_cpu\_time\_ns} turns out to have an Execution Time lower than 200 ms).

Listing 4.7 reports the code for the real-time task that implements the pTPN model of Fig. 4.5 in order to observe the completion time of the primitive \texttt{rt\_get\_cpu\_time\_ns}. Values logged on the FIFO queue are processed by

```
#define ITERATIONS 100000
#define FIFO 0

int init_module (void) {
    RT_TASK task;
    long long start;
    rtf_create(FIFO, 2000000);
    rt_task_init(&task, (void *) tsk_job, 0, 10000, 0, 0, 0);
    rt_set_periodic_mode();
    start = nano2count (500000);
    rt_task_make_periodic(&tsk, start, nano2count (100* MILLISEC));
    return 1;
}

void cleanup_module () {
    stop_rt_timer();
    rtf_destroy (FIFO);
    rt_task_delete (&tsk);
}

static void tsk_job (int t) {
    long long time [ITERATIONS];
    int count;
    while (1) {
        for (count = 0; count < ITERATIONS; count++) {
            rt_get_cpu_time_ns();
            time [count] = rt_get_cpu_time_ns();
        }
        rtf_put (FIFO, time, sizeof (long long)*ITERATIONS);
        rt_task_wait_period();
    }
}
```

Listing 4.7. Implementation of the periodic real-time task that repeatedly logs the completion time of each execution of the RTAI primitives \texttt{rt\_get\_cpu\_time\_ns}.

a low priority task running in the user space (not represented in the model of Fig. 4.5 and in Listing 4.7) which computes the difference between subsequent
logged values of time. Experimental results show that the Execution Time of the RTAI primitives under consideration is not affected by significant jitters and it is thus assumed to be constant, although it suffers of spurious variations between a hundred of nanoseconds to a few microseconds. These fluctuations are quite regularly distributed over time and they can be ascribed to timing uncertainties due to processor and bus effects, which are reported to cause jitters on the order of a microsecond to a few tens of microseconds on general purpose CPUs running an HRTOS [56], [99].

The periodic task specified by the pTPN model of Fig. 4.6 estimates the Execution Time of a primitive by measuring time before and after multiple calls to the primitive under test: periodic releases are modeled by the firings of transition job_release; each job measures time, performs multiple calls to the primitive under test, and then measures time again, which correspond to the firings of transitions get_time_1, primitive_under_test, and get_time_2 respectively; finally, each job writes on a FIFO queue the two measured values of time, which is represented by the firing transition fifo_put; multiple calls to the primitive under test are modeled by means of transition loop and place iterations, which prevent transition get_time_2 from firing until transition primitive_under_test has fired a number of times equal to the number of tokens in place iterations (one hundred thousand tokens in Fig. 4.6).

![Figure 4.6](image_url)

*Figure 4.6. The pTPN model for a periodic task that estimates the Execution Time of a primitive by measuring time before and after multiple calls to the primitive under test. Temporal parameters are expressed in milliseconds.*

Listing 4.8 reports the code for the real-time task that implements the pTPN model of Fig. 4.6 in order to estimate the Execution Time of the
#define ITERATIONS 100000
#define FIFO 0
struct Interval { long long time1, time2;};

int init_module(void) {
    RT_TASK tsk;
    long long start;
    rtf_create(FIFO, 2000000);
    rt_task_init(&tsk, (void *)&tsk_job, 0, 10000, 0, 0, 0);
    rt_set_periodic_mode();
    start = nano2count(500000);
    start = nano2count(time + 100*MILLISEC + 100*MILLISEC);
    rt_task_make_periodic(&tsk, start, nano2count(100*MILLISEC));
    return 1;
}

void cleanup_module() {
    stop_rt_timer();
    rtf_destroy(FIFO);
    rt_task_delete(&tsk);
}

static void tsk_job(int t) {
    struct Interval ti;
    int count;
    while(1) {
        ti.time1 = rt_get_cpu_time_ns();
        for(count=0; count<ITERATIONS; count++) {
            rt_get_cpu_time_ns();
        }
        ti.time2 = rt_get_cpu_time_ns();
        rtf_put(FIFO, &ti, sizeof(ti));
        rt_task_wait_period();
    }
}

Listing 4.8. Implementation of the real-time task that performs the estimation of the Execution Time of the RTAI primitive \texttt{rt\_get\_cpu\_time\_ns}.

RTAI primitive \texttt{rt\_get\_cpu\_time\_ns}. Values logged on the FIFO queue are processed by a low priority task running in the user space (not represented in the model of Fig. 4.6 and in Listing 4.8) which computes the Execution Time of the primitive under test observed by each job, dividing the difference between the two logged values of time by the number of repetitive calls, and then derives the mean value and the standard deviation. Table 4.1 reports
results of the experimentation on various RTAI primitives, assuming that each job performs one hundred thousand calls to the primitive under test and that the number of executed jobs is one thousand. Experimental results evidence the fact that the Execution Time of the RTAI primitives under test can be considered negligible with respect to the time-scale of models discussed in this dissertation, whose temporal parameters are expressed in milliseconds.

<table>
<thead>
<tr>
<th>RTAI primitive</th>
<th>mean</th>
<th>std dev</th>
</tr>
</thead>
<tbody>
<tr>
<td>rt_get_cpu_time_ns</td>
<td>61.47 ns</td>
<td>0.08 ns</td>
</tr>
<tr>
<td>rt_task_init</td>
<td>1233.41 ns</td>
<td>18.12 ns</td>
</tr>
<tr>
<td>rt_task_make_periodic</td>
<td>74.75 ns</td>
<td>0.05 ns</td>
</tr>
<tr>
<td>rt_task_resume</td>
<td>16.36 ns</td>
<td>0.99 ns</td>
</tr>
<tr>
<td>rt_task_delete</td>
<td>26.97 ns</td>
<td>0.06 ns</td>
</tr>
<tr>
<td>rt_whoami</td>
<td>2.51 ns</td>
<td>0.01 ns</td>
</tr>
<tr>
<td>rt_change_prio</td>
<td>45.91 ns</td>
<td>1.73 ns</td>
</tr>
<tr>
<td>rt_set_period</td>
<td>49.70 ns</td>
<td>1.05 ns</td>
</tr>
<tr>
<td>rt_sem_wait + rt_sem_signal</td>
<td>51.96 ns</td>
<td>2.29 ns</td>
</tr>
<tr>
<td>rt_mbx_send</td>
<td>145.33 ns</td>
<td>0.32 ns</td>
</tr>
<tr>
<td>rt_mbx_receive</td>
<td>145.10 ns</td>
<td>0.48 ns</td>
</tr>
<tr>
<td>rtf_put</td>
<td>104.28 ns</td>
<td>0.94 ns</td>
</tr>
<tr>
<td>rtf_get</td>
<td>107.64 ns</td>
<td>0.79 ns</td>
</tr>
</tbody>
</table>

Table 4.1. Estimate of the mean Execution Time of various RTAI primitives and the corresponding standard deviation. Messages sent to and received from a mailbox by the RTAI primitives `rt_mbx_send` and `rt_mbx_receive`, respectively, and messages written on and read from a FIFO queue by the RTAI primitives `rtf_put` and `rtf_get`, respectively, consist of a struct variable comprised of an int variable and a long long variable.

4.4.2 Estimation of the accuracy of the function `busy_sleep`

A `busy_sleep` function that uses the cpu for a controlled Execution Time was implemented to support the construction of the Executable Architecture of the task-set before all entry-points are implemented. Actually, RTAI natively
provides a function `void rt_busy_sleep(int nanosecs)`, but this tends to jam the operating system clock when applied for timings over few hundreds of microseconds and, concretely, it only controls the completion time. In fact, `rt_busy_sleep` embeds a `while` loop that exits when the current time overtakes the completion time, which is set equal to the time at which the loop is entered plus the specified duration; however, if a task is suspended while executing the loop, the current time may surpass the completion time and, thus, the actual Execution Time will turn out to be lower than the specified duration.

A `busy_sleep` fitting the needs of the application context described in this dissertation was thus implemented as a simple deterministic loop with trivial expedients to avoid compiler optimizations, and it was experimentally tuned on the specific HW platform, assuming that its actual duration is a linear function with a constant start-up time plus a duration proportional to the number of iterations. Listing 4.9 reports the code of the `static void busy_sleep(long long volatile time_units)` function that operates on timings expressed as multiples of 1 ms. The Execution Time of function `busy_sleep` was estimated as described in Section 4.4.1, by measuring time through the RTAI primitive `rt_get_cpu_time_ns` and by performing multiple calls of the function between subsequent time measures. Fig. 4.7 plots the results of the experimentation, showing that a linear approximation effectively fits the relation between the number of iterations of the deterministic loop and its duration.

```c
double volatile m = 239236.173409;
double volatile q = -24.631101;

static void busy_sleep(long long volatile time_units)
{
    long long volatile i;
    long long volatile x = 0;
    long long volatile iterations = m*((double)time_units) + q;

    for(i=0; i<iterations; i++)
        x++;
}
```

Listing 4.9. Implementation of a function `busy_sleep` that uses the cpu for a controlled Execution Time.
4.4.3 Estimation of the context switch time

A context switch occurs when the currently executing real-time task is stopped so that another real-time task can run. The context switch time was estimated by means of two real-time tasks with equal period and different priority, synchronized on a binary semaphore. Fig. 4.8 reports the pTPN model that specifies the behavior of the two tasks. At each period:

- \( Tsk_1 \), which is the high priority task, blocks on a wait operation on the semaphore, represented by place \( mux \) (which is empty at the beginning of each period), and the low priority task \( Tsk_2 \) is thus given the control;

- \( Tsk_2 \) measures time and performs a signal on the semaphore, which correspond to the firings of transitions \( tsk2_{get\_time} \) and \( signal \), respectively, and it is then preempted by the high priority task \( Tsk_1 \);
• *Tsk*₁ is thus unblocked and completes semaphore acquisition, it measures time, and then it logs the observed value on a FIFO queue, which are accounted by the firings of transitions *wait*, *tsk₁_get_time*, and *tsk₁_fifo_put*, respectively;

• *Tsk*₂ is then given the control and logs on the real-time FIFO queue the previously measured value of time, which is represented by the firing of transition *tsk₂_fifo_put*.

At each period, the difference between the value of time observed by the *Tsk*₁ and that observed by *Tsk*₂ is an upper bound on the context switch time.

![Figure 4.8. The pTPN model for two periodic tasks employed to estimate the context switch time. Temporal parameters are expressed in milliseconds.](image)

Listing 4.10 reports the code that implements the pTPN model of Fig. 4.8. Values logged on the FIFO queue are processed by a low priority task in the user space (not represented in the model of Fig. 4.8 and in Listing 4.10), which derives minimum and maximum observed values of the context switch time, the mean value and the standard deviation. The experimentation was carried out on one hundred thousand observations, i.e., one hundred thousand jobs were executed for each of the two tasks. Results show that the context switch time is bounded within 180 ns and 735 ns, with spurious variations between 2850 ns and 2959 ns, due to timing uncertainties caused by a general purpose CPU running an HRTOS [56], [99]. Therefore, the context switch time is assumed to be negligible in the implementation of models discussed in this dissertation, whose timings are expressed in milliseconds.
Timing observability and control

```c
#define MILLISEC 1000000
#define ITERATIONS 100000
#define FIFO 0
SEMS
struct Timed_Action { int action; long long time;};
int init_module (void) {
    RT_TASK tsk1, tsk2; long long start, time;
    rt_typed_sem_init(&mux, 0, BIN_SEM);
    rtf_create(FIFO, 2000000);
    rt_task_init(&task1, (void*)tsk1_job, 0, 10000, 0, 0, 0);
    rt_task_init(&task2, (void*)tsk2_job, 0, 10000, 1, 0, 0);
    rt_set_periodic_mode();
    start = nano2count(time + 1000* MILLISEC + 100*LILLISEC);
    rt_task_make_periodic(&tsk1, start, nano2count(100*MILLISEC));
    rt_task_make_periodic(&tsk2, start, nano2count(100*MILLISEC));
    return 1;
}
void cleanup_module() {
    stop_rt_timer();
    rt_sem_delete(&mux);
    rtf_destroy(FIFO);
    rt_task_delete(&tsk1);
    rt_task_delete(&tsk2);
}
static void tsk1_job(int t) {
    struct Timed_Action ta;
    ta.action = 1;
    while(1) {
        rt_sem_wait(&mux);
        ta.time = rt_get_cpu_time_ns();
        rtf_put(FIFO, &ta, sizeof(struct Timed_Action));
        rt_task_wait_period();
    }
}
static void tsk2_job(int t) {
    struct Timed_Action ta;
    ta.action = 2;
    while(1) {
        ta.time = rt_get_cpu_time_ns();
        rt_sem_signal(&mux);
        rtf_put(FIFO, &ta, sizeof(struct Timed_Action));
        rt_task_wait_period();
    }
}
```

Listing 4.10. Implementation of the two real-time tasks that perform the estimation of the context switch time.

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4.4.4 Estimation of the perturbation of time-stamped logging

An experimentation was carried out in order to evaluate the accuracy and the confidence that can be attained in logged time-stamps. To this end, a constant Execution Time was repeatedly applied through the function `busy_sleep`, logging the completion time of each execution on an RTAI FIFO queue. Experiments were repeated for various values of the nominal Execution Time. Fig. 4.9 plots the histogram of the difference between the nominal value of the Execution Time and the difference between subsequent logged time-stamps, for an Execution Time of 25 ms. The figure also reports the minimum and maximum delay measured with respect to the nominal value, its mean value and standard deviation. Note that these values of error encompass various factors: the (variable) overhead due to the acquisition of a time measure through `rt_get_cpu_time_ns`; the overhead for the log onto the RTAI FIFO queue; the finite accuracy of `busy_sleep` in controlling the applied Execution Time. Results show that values of error are in the range [214, 1120] ns with spurious
variations between 3174 ns and 3710 ns, thus having negligible impact in the application context of this work where the precision of temporal parameters is 1 ms. Error peaks are regularly distributed over time and, again, they can be ascribed to timing uncertainties due to the effects of a general purpose CPU running an HRTOS [56], [99].
Chapter 5

Unit and Integration Testing Processes

In the activity SD7-SW, confidence in the conformance of the implementation to design specification and to high-level requirements is attained through testing. This follows the industrial practice, which is reluctant to abandon consolidated processes, and reflects critical and mature application contexts, where testing is in any case requested for certification purposes [60], [50].

5.1 Defect and failure model

According to [30], this dissertation distinguishes between defects (i.e., flaws in a component or system that can cause the component or system to fail to perform its required function) and failures (i.e., deviations of the component or system from its expected delivery, service or result). On the one hand, defects that are observable in the abstraction of pTPNs are:

- task programming defect: a defect in concurrency control and task interactions that may consist in wrong priority assignment, semaphore opera-
tion not appropriately combined with priority handling, flawed usage of any IPC mechanism, out-of-turn invocation of entry-point functions, invocation of IPC primitives within entry-point functions without explicit representation in the task-set architecture;

- cycle stealing: a defect consisting in the presence of additional tasks and activities that steal computational resources, which may arise from unexpected overheads of the operating system, tasks intentionally not represented in the specification as considered not critical for real-time behavior, exceeding additional overhead induced by the executable architecture.

Note that defects in the sequential code of entry-point functions are not encompassed as they are not observable in the pTPN abstraction and are more conveniently addressed at the level of unit-testing [60] through consolidated control-flow and data-flow strategies [101], [94].

On the other hand, failures that can be observed with respect to the semantics of a pTPN specification are:

- un-sequenced execution: an execution run that breaks sequencing requirements, e.g., a priority inversion;

- time-frame violation: a temporal parameter assuming a value out of its nominal interval, e.g., the untimely release of a job, a computation chunk breaking its expected Execution Time interval;

- deadline miss: a job breaking its end-to-end timing requirement.

## 5.2 Test-case selection and coverage analysis

Formal methods in test-case selection for reactive and real-time systems have been reported in various experiences, mostly following a functional approach. In the partial-WpMethod [62], a deterministic Finite State Machine (FSM) specification is used to derive a test suite, which achieves state identification
and guarantees full fault coverage under the assumption of a correctly implemented reset function and of an upper bound on the number of states in the implementation. The approach is extended to real-time systems in [57] where a test suite is derived by applying the Wp-method on the FSM obtained through a finite sampling of the Region Graph of a specification model expressed as a Timed Input Output Automaton (TIOA). The method still guarantees full fault detection, but the complexity of the test suite tends to explode and the assumptions on the number of states in the implementation become much less realistic than in the untimed context. In [93], an untimed system is specified in a gray-box style as a SW architecture which is supposed to be translatable into a Labeled Transition System (LTS). A test suite is derived by achieving some FSM coverage criterion over a bisimulation reduction of the LTS which hides unobservable events.

In [71], [83], a real-time system is specified as a deterministic and output-urgent Timed Automaton. Test cases are deterministically timed event sequences, which can be selected either as witnesses of real-time logic expressions capturing specific testing purposes or as elements of a test suite achieving some coverage over the locations of the specification automaton. In particular, all-nodes and all-edges criteria [94] are extended with a nice timed interpretation of dataflow testing principles [101] covering paths between the definition and the usage of clock variables.

[72] proposes an on-the-fly global algorithm for model-based generation of test-suites according to a given coverage criterion, in order to support automated verification of the conformance of an implementation to its specification. The test generation problem is formulated as a reachability problem, where a coverage criterion is regarded as a set of items to be covered, called coverage items. Reachability analysis generates and explores the state space of the model, and returns a set of paths for all reachable coverage items, without including redundant paths. In particular, knowledge about the total coverage found in the currently generated state space is used to guide and prune the remaining exploration.
Test-case selection and coverage analysis

The state-space of the pTPN model supports an automated approach to test-case-selection and coverage-analysis providing an abstraction that focuses on the aspects of concurrency and timing. This can be regarded as grey-box or black-box testing depending on the possible prior qualification of the automated code generator: if the specification is compiled into code through a generator that has been previously qualified as correct, then the state-space of the pTPN model reflects the actual implementation of the dynamic architecture of the task-set and can be used to evaluate a structural measure of coverage and to drive architectural testing of entry-point functions and asynchronous task releases; whereas, if the code generator is not qualified or if the code is manually written, then the state-space of the pTPN provides a functional abstraction for test-case selection in the verification of conformance of the overall implementation composed by the dynamic architecture along with entry-point functions and asynchronous task releases [118], [93].

Certification standards explicitly prescribe structural coverage criteria that refer to the control-flow graph of the code: these may be all-statements or all-decisions, with various variants and notably modified condition decision coverage (MCDC) [51], depending on the criticality of the software component and on the level of integration in the testing process [60], [94]. Data-flow testing, and notably all-uses, can be applied to improve the effectiveness of coverage beyond the external contractual needs imposed by the certification [101]. While effectively exerting control structures and data-flow dependencies within the code attached to entry-point functions, these criteria provide a limited coverage of the variety of behaviors that may result from the concurrent and interrupted execution of the dynamic architecture of a task-set. In fact, more than by lines of code and data-flow dependencies, this complexity is represented by the variety of behaviors that may occur in the state-space of the dynamic architecture. The SCG provides an effective abstraction to account for this variety, supporting the selection of symbolic runs as the witnesses of a specific test purpose determined through a model checking technique [71] or as part of a test suite defined through various criteria that can be used to automate test-case selection and/or coverage analysis [72].
Without loss of generality a few test-case selection criteria are described that capture relevant testing goals with reference to the state-space abstraction.

- **All-Markings**: is satisfied when each reachable marking has been visited by at least one test-case. This covers all the acceptable states of concurrency and thus observes all the possible configurations of the set of chunks that are concurrently ready/runningblocked (e.g., a state of priority inversion). The criterion is a kind of all-nodes and its complexity is thus proportional to the number of reachable markings, and can be efficiently resolved on the SCG of the pTPN model: for each reachable marking $m$, select any class $S_m$ with marking $m$, and include in the test-suite any path from a controllable starting point to $S$.

- **All-Marking-Edges**: is satisfied when each edge between any two reachable markings has been traversed by at least one test-case. This includes All-Markings and adds the guarantee to observe the transitions between subsequent states of concurrency. This notably includes the events of preemption following to asynchronous releases, chunk completions, semaphore operations and priority boost/deboost. The criterion is a kind of all-edges and its complexity is thus proportional to the number of reachable markings multiplied by the maximum number of events that may occur within each marking, which in turn is limited by the number of tasks in the set. As for the all-marking criterion, the selection is performed on the SCG: for each edge between two markings $m_1$ and $m_2$, select in the SCG any class $S_1$ with marking $m_1$ that accepts an event leading to a class $S_2$ with marking $m_2$, and include in the test-suite any path starting from a controllable starting point and covering the edge.

- All-Markings and All-Marking-Transitions can be refined into **All-Classes** and **All-Class-Edges**, by requiring coverage of all reachable state-classes and all edges between reachable state-classes, respectively. All-Classes and All-Class-Edges include their correspondent marking-based criteria and add the capability to partially account for the difference among
paths whenever this results in different timing restrictions (e.g., the two sequences $\rho_1 = t_{10}, t_{20}, t_{30}, t_{21}, t_{11}, t_{12}, t_{22}, t_{31}, t_{32}, t_{33}, t_{34}, t_{35}, t_{53}, t_{54}, t_{41}, t_{42}, t_{43}, t_{20}, t_{10}, t_{30}, t_{21}, t_{11}, t_{12}, t_{22}, t_{44}, t_{45}, t_{46}, t_{47}$ and $\rho_2 = t_{10}, t_{20}, t_{30}, t_{21}, t_{11}, t_{12}, t_{22}, t_{31}, t_{32}, t_{33}, t_{34}, t_{35}, t_{53}, t_{54}, t_{41}, t_{42}, t_{43}, t_{44}, t_{45}, t_{46}, t_{0}, t_{47}$ of the task-set of Fig. 2.1 reach the same state of concurrency, but they accept different future behaviors due to the different previous sequencing). However, they also largely increase the actual complexity of coverage (e.g., in the state-space of the task-set of Fig. 2.1, 433 markings are refined into 51079 classes).

- **All-symbolic-Runs**: covers every path in the SCG that starts with a job release and terminates with the job completion or its deadline miss.

  All-Symbolic-Runs properly-includes All-Class-Edges and thus also All-Marking-Edges, adding the capability to cover all the possible concurrency states and transitions within the context of the same job execution. This can be relevant for instance to account for possible implicit data-flow and timeliness dependencies among chunks in the same job.

  In the usual case in which the deadline of synchronous and asynchronous jobs is not higher than the task period and the minimum release-intertime, respectively, test-cases can be selected on the SCG in a straightforward manner. Under this assumption, releases and completions are directly represented by specific transitions, while deadline misses can be identified whenever a release occurs for any task with a job still pending. The test-suite thus includes every path that starts from any task release and terminates either with the task completion or with a new release (which indicates a deadline miss). In the special case in which deadlines are anticipated with respect to the period or minimum release-intertime, deadline misses are not directly represented on the SCG, but they can be made observable by extending the pTPN model with watch transitions as proposed in [27]).

  The resulting number of test-cases is guaranteed to be finite under the reasonable assumption that all tasks have a finite deadline and that all
tasks require a non-null minimum Execution Time. In fact, if the number of paths would be infinite, there should be a marking \( m \) that can be visited an infinite number of times between a release and the completion/deadline of some task \( T \). Since the time between a release and the completion/deadline is bounded, the Infimum of the time spent between two subsequent visits of \( m \) should be equal to 0. However, every sequence between two subsequent visits of \( m \) must include an event that advances the state of a task \( T' \neq T \) and thus changes the marking in a place \( p_{T'} \) belonging to \( T' \); to bring back the marking of \( p_{T'} \) to its value in \( m \), \( T' \) must complete its execution, restart a new release, and execute all the steps prior to \( m \), which requires a time not lower than the minimum Execution Time of the task which is supposed to be strictly higher than 0.

- **All-Symbolic-Executions**: covers any feasible sequence of events in the SCG that starts with the release of a job and terminates with its completion or deadline miss. This reduces the complexity of All-symbolic-Runs by avoiding to include multiple runs that follow the same event sequence and are distinguished only by the starting class. This basically answers the same rational that suggests to prefer All-Markings and All-Marking-Edges with respect to All-Classes and All-Class-Edges.

## 5.3 Test-case execution

In the process of testing, sensitization is the activity that identifies the inputs that let the system run along selected test-cases. In the context of reactive timed software components, this becomes a matter of determining timed inputs that force the Implementation Under Test (IUT) to execute selected symbolic runs.

The problem is considered in various works. In [71], [83], test-cases are deterministically timed event sequences executed under the assumption that all events can be observed and that all inputs can be controlled so as to assume
a deterministic value and time. However, not all timers of a real implementation can be actually managed: periodic and asynchronous release times can be effectively controlled through conventional primitives of an RTOS; whereas, computation times are often impractical to handle. Moreover, timers may take values within a subset of their nominal range of variation due to the determinization of the implementation with respect to the specification [47]. This causes legal behaviors of the specification model to be unfeasible in the IUT [28] and arises from various practical factors: i) many abstractions taken in the specification model cannot exactly correspond to the actual implementation, e.g., the release of a synchronous task suffers of some jitter, semaphore and priority handling operations require a non-null Execution Time, preemption does not occur in zero time and impacts on Execution Times due to cache and pipeline performances; ii) temporal parameters of the specification are usually associated with a nondeterministic range of variation, to make the model robust with respect to possible variations of the implementation; iii) when a model is developed as the description of an existing implementation (e.g., in a re-engineering process), its temporal parameters range within boundaries which over-approximate those of the actual implementation, to circumvent the difficulty in obtaining a precise estimate of Execution Times and release times; iv) specification usually neglects dependencies among Execution Times of computation chunks, which are difficult to quantify and definitely unreliable as an assumption for schedulability; v) the operating system may contribute to the partial determinization of the implementation, e.g., RTAI turns out to assign a fixed order to the releases of periodic tasks with the same priority at times multiple of their hyper-period, insensitively to the order in which tasks are initially started.

Assumptions on deterministic behavior and observability of the IUT are relaxed in [81], [83]. In particular, [81] proposes a framework for black-box conformance testing of real-time systems specified as nondeterministic and partially-observable timed automata, introducing a timed version of the input output conformance relation of [121]. The execution of test-cases is performed by means of an adaptive strategy in a game against the IUT and two types
of tests are proposed, analog-clock tests and digital-clock tests, which differ in the capability to observe and react to nondeterministic choices and delays of the IUT. The construction of the tester is described as a general algorithm, but it is not instantiated with respect to specific coverage strategies or testing purposes. [83] proposes a relativized timed input output conformance (rtioco) that explicitly takes environment assumptions into account and describes an on-the-fly testing algorithm which performs online test-case generation, test-case execution, and conformance verdict assignment. The approach is based on randomized testing and does not provide any coverage evaluation on the variety of timed behaviors. As a relevant trait, the specification automaton adopted in [81], [83] does not encompass preemptive behavior.

5.3.1 Supporting test-case execution through pTPNs

The theory of pTPNs supports the definition of an approach to the execution of test-cases on real-time preemptive systems [47]. The approach distinguishes between controllable and non-controllable timers, represented by tasks release times and chunks computation times, respectively. According to this, controllable classes are identified as the classes where no computation chunk is pending and all jobs are waiting for their next release, and the IUT can be started from any state collected in one such class.

Given a test-case $\rho$ that originates from state class $S_{p_0}$ and reaches state class $S_{p_n}$ through the firing of the sequence of transitions $t_{p_1} \rightarrow t_{p_2} \rightarrow \cdots \rightarrow t_{p_n}$ (i.e., $\rho = S_{p_0} \xrightarrow{t_{p_1}} S_{p_1} \xrightarrow{t_{p_2}} \cdots \xrightarrow{t_{p_n}} S_{p_n}$), the SCG can be inspected to identify a path $\sigma$ that starts from the initial state class $S_0$, reaches state class $S_{p_0}$ and terminates with $\rho$ (i.e., $\sigma = S_0 \xrightarrow{t_{\sigma_1}} S_{\sigma_1} \xrightarrow{t_{\sigma_2}} \cdots \xrightarrow{t_{\sigma_n}} S_{p_0} \xrightarrow{t_{p_1}} S_{p_1} \xrightarrow{t_{p_2}} \cdots \xrightarrow{t_{p_n}} S_{p_n}$). The execution of test-case $\rho$ could be enforced by letting the IUT start from any state in the subset of the initial state class that admits $\sigma$ as a feasible run and by letting controllable timers of the model take values within the exact set of timing constraints of $\sigma$. However, when $S_{p_n}$ is distant from $S_0$, this results in a major computational complexity, and incurs in a high probability that uncontrollable actions let the IUT diverge from $\sigma$. To
reduce the problem, the IUT is not started from the initial state class but from a controllable class which is suitably selected in the SCG, according to the following testing procedure:

- The SCG is inspected to identify a path $\omega$ that i) starts from a controllable class $S_c$ and ii) covers the selected test-case $\rho$ without visiting any other controllable class (i.e., $\omega = S_c \xrightarrow{t_{\omega_1}} S_{\omega_1} \xrightarrow{t_{\omega_2}} \cdots \xrightarrow{t_{\omega_n}} S_{\rho_0} \xrightarrow{t_{\rho_1}} S_{\rho_1} \xrightarrow{t_{\rho_2}} \cdots \xrightarrow{t_{\rho_n}} S_{\rho_n}$, where $S_{\omega_i}$ is a non-controllable class $\forall i \in [1, n-1]$).

- Trace analysis enables the derivation of the range of feasible timings for $\omega$, which comprises i) the subset $\bar{S}_c$ of $S_c$ collecting all and only the states of $S_c$ that admit $\omega$ as a feasible run, and ii) a set of timing constraints for transitions that are newly enabled in classes visited by the run. Since values of non-controllable timers are autonomously selected by the IUT and may let it diverge from the selected test-case, the identified timing conditions for controllable timers comprise the necessary but not sufficient condition to execute the path $\omega$. Trace analysis also permits the derivation of the WCCT of $\omega$.

- The IUT is repeatedly started from a state in $\bar{S}_c$ and values of controllable timers are randomly sampled within the identified range. At each repetition, the IUT is stopped when time surpasses the WCET of $\omega$, beyond which either the IUT has covered the selected test-case or it has diverged.

### 5.3.2 Experimental results

The application of the proposed sensitization procedure is illustrated in relation to the execution of a test-case selected as a specific testing purpose [71]. The experimentation was carried out on the Basic Features Extraction CSCI of Fig. 1.8, whose dynamic architecture is specified by the pTPN model of Fig. 2.1. The test-case was identified on the SCG as a symbolic run of task $Tsk_4$ that may attain its WCCT of 58 ms. In particular, the selected test-case is the symbolic run $\rho$ illustrated in Fig. 2.5, which starts with the release of a
job of $Tsk_4$ (i.e., the firing of transition $t_{40}$ that enters state-class $S_{5005}$) and terminates with its completion (i.e., the firing of transition $t_{47}$): $\rho = S_{5005} \xrightarrow{t_{10}} S_{5795} \xrightarrow{t_{20}} S_{6092} \xrightarrow{t_{30}} S_{6591} \xrightarrow{t_{40}} S_{7198} \xrightarrow{t_{50}} S_{7741} \xrightarrow{t_{60}} S_{8120} \xrightarrow{t_{70}} S_{8406} \xrightarrow{t_{80}} S_{8711} \xrightarrow{t_{90}} S_{9030} \xrightarrow{t_{100}} S_{9333} \xrightarrow{t_{110}} S_{9921} \xrightarrow{t_{120}} S_{9687} \xrightarrow{t_{130}} S_{9873} \xrightarrow{t_{140}} S_{10121} \xrightarrow{t_{150}} S_{10396} \xrightarrow{t_{160}} S_{10670} \xrightarrow{t_{170}} S_{10969} \xrightarrow{t_{180}} S_{11322} \xrightarrow{t_{190}} S_{11729} \xrightarrow{t_{200}} S_{12164} \xrightarrow{t_{210}} S_{12607} \xrightarrow{t_{220}} S_{13028} \xrightarrow{t_{230}} S_{13454} \xrightarrow{t_{240}} S_{13907} \xrightarrow{t_{250}} S_{14344} \xrightarrow{t_{260}} S_{14739}$.

Following the sensitization strategy described in Sect. 5.3.1, the SCG was inspected in order to identify a path $\omega$ that starts from a controllable class and covers $\rho$ without visiting any other intermediate controllable class. This was obtained through the Model Checker of the Oris Tool [35], which provides all the symbolic paths in the SCG that are witnesses of a branching-time temporal logic formula, with state and action formulae expressing conditions on both visited markings and traversed transitions. According to this, the SCG was checked to identify any symbolic run that:

i) starts from a controllable class, identified by the marking $M_c$, which assigns a token to places $m_1$ and $m_2$ and no token to all the other places;

ii) reaches any state class that fires $t_{40}$ without visiting any intermediate controllable class;

iii) terminates with the firing of $t_{47}$ after 58 ms since the firing of $t_{40}$ without including any intermediate firing of $t_{47}$. A symbolic run $\omega$ that starts from the controllable class $S_{4959}$ and covers $\rho$ was thus selected among the witnesses provided by the Model Checker:

$$\omega = S_{4959} \xrightarrow{t_{50}} S_{5055} \xrightarrow{t_{51}} S_{5154} \xrightarrow{t_{52}} S_{5278} \xrightarrow{t_{53}} S_{5437} \xrightarrow{t_{54}} \rho$$

$$S_{4959} = (M_c, D_{4959}) \quad D_{4959} = \begin{cases} 26 \leq t_{10} \leq 33 \\ 26 \leq t_{20} \leq 33 \\ 26 \leq t_{30} \leq 33 \\ 26 \leq t_{40} \leq 33 \\ 0 \leq t_{50} \leq \infty \\ 0 \leq t_{10} - t_{20} \leq 0 \\ 0 \leq t_{10} - t_{30} \leq 0 \\ 0 \leq t_{10} - t_{40} \leq 0 \end{cases}$$

State class $S_{4959}$ collects states in which periodic tasks $Tsk_1$, $Tsk_2$, $Tsk_3$, and $Tsk_4$ are constrained to have the same release time within the interval
Test-case execution

[26, 33] ms, while no constraints exist on the release time of the sporadic task \( Tsk_5 \). The exact timing profile of \( \omega \) was derived through trace analysis and it restricts the time to fire of \( t_{50} \) in \( S_{4959} \) to be within 22 ms and 32 ms, which identifies the subset \( \bar{S}_{4959} \) of \( S_{4959} \) that admits \( \omega \) as a feasible run. According to this, the necessary condition to execute the test-case consists in releasing the sporadic task \( Tsk_5 \) within [22, 32] ms and starting the four periodic tasks \( Tsk_1, Tsk_2, Tsk_3, \) and \( Tsk_4 \) at the same time within [26, 33] ms. Since \( S_{4959} \) is a controllable class, \( Tsk_5 \) can be released just after the IUT is started, without waiting the minimum time of 22 ms: according to this, \( Tsk_5 \) is released within [0, 10] ms, and \( Tsk_1, Tsk_2, Tsk_3, \) and \( Tsk_4 \) are contemporary started within [4, 11] ms. The restart time of the IUT turns out to be equal to 69 ms, being the WCCT of \( \omega \) of 91 ms decremented by 22 ms.

The feasibility and effectiveness of the proposed approach to the execution of test-cases was evaluated with respect to randomized testing.

- **Randomized testing:** The IUT was run for 1 hour, which corresponds to 90000 releases of the shortest-period task \( Tsk_1 \). In a preliminary experiment, the sporadic task \( Tsk_5 \) was released according to a uniform distribution within \([120, N_{max}/10^6]\) ms, being \( N_{max} \) the maximum representable integer value. Coverage evaluation evidenced that the test-case \( \rho \) was never covered. Since \( \rho \) comprises the execution of a job of \( Tsk_5 \), a second experiment was performed by activating jobs of \( Tsk_5 \) according to a uniform distribution within \([120, 1000]\) ms. However, also in this case the test-case \( \rho \) was never covered.

- **Sensitized testing:** The IUT was repeatedly started every 69 ms, releasing \( Tsk_5 \) within [0, 10] ms and starting \( Tsk_1, Tsk_2, Tsk_3, \) and \( Tsk_4 \) at the same time within [4, 11] ms. One thousand executions were performed, which correspond to an overall Execution Time of a little more than 1 minute. During the test, \( \rho \) was executed 207 times, evidencing the effectiveness of the approach with respect to randomized testing.
5.4 Oracles verdict

Logs produced during the testing stage can be analyzed by different oracles evaluating the conformance between implementation and specification with different levels of abstraction, each implying a different run-time overhead for logging and a different off-line complexity for decision.

- The *end-to-end Oracle* verifies the satisfaction of end-to-end job deadlines. The oracle requires time-stamped logging of job releases and completions, and is implemented in a straightforward manner by comparing the time elapsed between release and completion of any job against the deadline of its task (without explicit reference to the structure of the pTPN model).

- The *sequencing Oracle* verifies that the qualitative ordering of events conforms with the specification model, i.e., that there exists at least one timing that makes the sequencing of the log feasible for the specification model. This requires logging of all the events corresponding to a transition in the pTPN model (i.e., job releases, completion of computation chunks, priority boost operations, semaphore wait operations, mailbox receipt operations). However, it does not require that logged events be associated with a time-stamp, thus avoiding the need for an invocation of the time measuring primitive of the operating system (*rt_get_time_ns()* in the case of RTAI).

Decision of the oracle verdict requires state-space analysis, and basically consists in verifying whether the logged sequence is a *symbolic execution sequence* in the SCG of the pTPN model. If all reachable state classes have been computed, the problem of conformance reduces to verify whether the SCG contains a path that follows the sequence of logged events. If the SCG is not finite, or if it does not fit in the available memory, then conformance can be tested by reconstructing the fragment of the state-space composed by the classes visited by the logged sequence. To this end, the logged sequence is assumed to begin with the start-up of
the task-set. This identifies the initial marking, guarantees that all enabled transitions are newly enabled, and thus identifies a reachable state class that contains the initial state of the logged sequence. Since a state class is derived in time $O(N^2)$ with respect to the number $N$ of enabled transitions [122], [34], the entire fragment is computed in time $O(N^2 \cdot L)$, where $L$ is the length of the logged sequence.

- The time-sensitive Oracle verifies the timed trace inclusion relation of [71], i.e., it verifies that the logged sequence is a feasible execution for the specification. Verification requires that a time-stamped log is produced for each event of the implementation that corresponds to a transition in the pTPN model. Also in this case, to guarantee identification of the initial state, logging is assumed to start from an initial state with a known marking where all enabled transitions are newly enabled. This can be the initial state reached through a reset function that starts-up the task-set. More generally, the same condition can be attained through an ad-hoc function that starts-up the task-set from any intermediate controllable state where no computation is ongoing and all times to the next job release are known.

The decision algorithm does not require state-space analysis and basically relies on a simulation of the specification model: starting from the initial state $s_0 = \langle M_0, FI_0 \rangle$ accounting for conditions at which the system is started, the algorithm checks the feasibility of the first timed action $\langle a_1, \tau_1 \rangle$ and computes the subsequent state $s_1$; at the $n$-th step, the algorithm checks whether $t_n$ can be fired at time $\tau_n - \tau_{n-1}$ from state $s_{n-1}$ and computes the resulting state $s_n$. The Oracle emits a failure verdict as soon as any timed action $\langle a_n, \tau_n \rangle$ is not accepted by the simulator. A pass verdict is emitted when the run terminates. An inconclusive verdict is emitted when the trace diverges from the sequence of the test-case with an event that is accepted by the simulator.

The time-sensitive Oracle somehow performs the same function of the observers proposed in [71], [26]. In [71], an observer is an automaton.
employed online during the testing process to collect auxiliary information that is used for coverage evaluation. In [26], an observer is used to evaluate quantitative properties through state-space enumeration of the specification model augmented with additional places and transitions. Differently from both the concepts of observer, the time sensitive Oracle evaluates off-line the execution logs produced by an implementation. This is accomplished by verifying if the sequence of timed actions is a subset of the dynamic behavior that the semantics of the specification model may accept.

All the failures detected by the sequencing Oracle are also detected by the time-sensitive Oracle, while the vice-versa is of course not true. Besides, failure detection capability of the end-to-end Oracle are not comparable with those of the sequencing Oracle and the time-sensitive Oracle. In fact, an execution may break the expected sequencing and/or an internal time-frame and satisfy the deadline, and vice-versa. However, if state-space analysis of the specification model has verified the absence of symbolic runs that break any task deadline, then all the failures observed by the end-to-end Oracle are also observed by the sequencing Oracle (and thus also by the time-sensitive Oracle).

Any un-sequenced execution is detected by the sequencing Oracle (and thus also by the time-sensitive Oracle). Besides, any time frame violation is detected by the time-sensitive Oracle, but not by the sequencing Oracle unless timing causes the execution to diverge from the expected sequencing. Cycle stealing defects are recognized by the time-sensitive Oracle iff the quantity of stolen time exceeds the laxity between the actual Execution Time and its expected upper bound.

Coverage metrics can be obtained by mapping on the SCG the sequence of actions reproduced by the time-sensitive Oracle or by the sequence-sensitive Oracle. Regardless of the number of identified failures, a metric of coverage is needed to provide a measure of confidence in the absence of residual defects. The sequence of actions reproduced by the deadline-sensitive Oracle cannot be mapped on the SCG because the oracle does not observe all actions.
Chapter 6

Summary of the approach

For the convenience of the reader, this Chapter resumes the formal methodology for the development of real-time software components proposed in this dissertation. The approach casts the theory of pTPNs into an organic tailoring of design, coding, and testing activities within a V-Model software life cycle [42] and it is summarized by illustrating its application to the development of the IVSS presented in this work.

The case study described along this dissertation concerns an IVSS which employs a pan-tilt-zoom (PTZ) camera to perform real-time 3D tracking of multiple people moving over an extended area [29]. The activity SD1 identifies User Requirements of the vision system through the definition of parameters such as the frame rate (i.e., 25 frames per second), the image size (i.e., 160 x 120 pixels), the compression format (i.e., JPEG), the operating temperature (i.e., from 0°C to 40°C), the camera mass (i.e., up to 1.5 Kg). The activity SD2 specifies System Architecture through the UML-MARTE class diagram of Fig. 6.1, identifying a Control Unit, a PTZ Camera, and a Video Processing Unit. The Control Unit receives images acquired by the PTZ Camera, sends them to
the Video Processing Unit, and receives the elaborated images back. On the basis of these results, the Control Unit sets parameters of image processing algorithms (e.g., window size of non-linear filters) and parameters at which images are acquired (e.g., the levels of pan, tilt, and zoom), and sends them to the Video Processing Unit and to the PTZ Camera, respectively. The activity

SD3 details CSCIs and HCIs of each unit through the UML-MARTE class diagrams shown in Figs. 6.2 and 6.3. The Control Unit communicates with the PTZ Camera and with the Video Processing Unit through a serial bus; boards of both the Control Unit and the Video Processing Unit run RTAI operating system [95]. The Control Unit comprises a CSCI (i.e., System Management CSCI) and two HCIs (i.e., a board and a battery): the CSCI is mapped on an RTAI task-set and allocated to the board. The PTZ Camera consists of two HCIs (i.e., the Image Sensor Unit and the Mechanical PTZ Unit). The Video Processing Unit comprises three CSCIs (i.e., Images Acquisition CSCI, Basic Features Extraction CSCI, and Multiple Target Tracking CSCI) and four HCIs (i.e., three boards and a battery): each CSCI is mapped on a different RTAI task-set and allocated to a different board.

The approach proposed in this dissertation comes into play with the activities SD4-SW and SD5-SW through the definition of the dynamic architecture of the task-set allocated to each CSCI. Each task-set is initially specified through

![UML-MARTE class diagram](image)

**Figure 6.1. UML-MARTE class diagram of the System Architecture of an IVSS.** The *ProcessingResource* stereotype models an active, protected, executing-type resource that is allocated to the execution of schedulable resources. The *Device-Resource* stereotype specializes the concept of processing resource and typically represents an external device that may be manipulated or invoked by the platform and that may require specific services in the platform for its usage and/or management, but whose internal behavior is not a relevant part of the model under consideration. A *CommunicationMedia* represents the mean to transport information from one location to another.
Figure 6.2. UML-MARTE class diagram of the Control Unit and the PTZ Camera of the IVSS of Fig. 6.1. The rtUnit stereotype models a real-time application that owns one or more schedulable resources. A SchedulableResource is an active resource able to perform actions using the processing capacity brought from a processing resource by the scheduler that manages it. A Hw_Card symbolizes a printed circuit board, which typically comprises other sub-components like chips and electrical devices. The allocate stereotype identifies an allocation relation between elements of the application model, represented through the stereotype ApplicationAllocationEnd, and elements of the execution platform, modeled by the stereotype ExecutionPlatformAllocationEnd. A Hw_PowerSupply is a hardware component that supplies the hardware platform with power. The Hw_Bus stereotype represents a particular wired channel with specific functional properties.

the identification of minimum release inter-times, periods, and deadlines; then, it is refined through the definition task priorities and allowed time-frames of computation chunks. Task-sets are defined through the semi-formal specification of timelines, providing modeling convenience and facilitating industrial
acceptance; then, they are automatically translated into pTPN models through the Oris Tool [43], enabling schedulability analysis based on state space enumeration. Fig. 6.4 reports the timeline schema of the task-set allocated to the Basic Features Extraction CSCI of Fig. 6.3. The task-set is made by five
recurrent tasks synchronized by two binary semaphores and a mailbox:

- Task $Tsk_1$ performs noise reduction through a median filter. It is a periodic task with period and deadline of 40 time units. Each job of $Tsk_1$ consists of the unique chunk $C_{11}$ which is associated with entry-point $f_{11}$, requires resource cpu with priority level 1 (low priority numbers run first) for an Execution Time constrained within 1 and 2 time units, and receives a message from mailbox $mbx$ containing parameters for the noise reduction algorithm at the beginning of its execution.

- Task $Tsk_2$ manipulates parameters employed by the noise reduction algorithm. It is a periodic task with period and deadline of 40 time units. Each job of $Tsk_2$ consists of two chunks $C_{21}$ and $C_{22}$. Chunk $C_{21}$ is associated with entry-point $f_{21}$; it requires resource cpu with priority level 2 for an Execution Time constrained within 1 and 2 time units; at the end of its execution, it sends a message to mailbox $mbx$ containing parameters for the noise reduction algorithm. Chunk $C_{22}$ is associated with entry-point $f_{22}$ and requires resource cpu with priority level 2 for an Execution Time constrained within 1 and 2 time units.

- Task $Tsk_3$ performs edge detection through Sobel operator. It is a periodic task with period and deadline of 80 time units. Each job of $Tsk_3$ consists of three chunks $C_{31}$, $C_{32}$, and $C_{33}$. Chunk $C_{31}$ is associated with entry-point $f_{31}$, which acquires parameters for the edge detection algorithm from a memory space shared with tasks $Tsk_4$ and $Tsk_5$; it requires resource cpu with priority level 3 for an Execution Time constrained within 1 and 2 time units; it is synchronized on the binary semaphore $mux_1$ to access the memory space shared with tasks $Tsk_4$ and $Tsk_5$. Chunk $C_{32}$ is associated with entry-point $f_{32}$, which performs the edge detection algorithm, and requires resource cpu with priority level 3 for an Execution Time constrained within 5 and 10 time units. Chunk $C_{33}$ is associated with entry-point $f_{33}$, which writes results of the edge detection algorithm on a memory space shared with task $Tsk_4$; it requires resource cpu with priority level 3 for an Execution Time constrained within 1 and 2 time units.
units; it is synchronized on the binary semaphore \(mux_2\) to access the memory space shared with task \(Tsk_4\).

- Task \(Tsk_4\) performs corner detection through Moravec operator. It is a periodic task with period and deadline of 100 time units and it has the same structure as that of task \(Tsk_3\): chunk \(C_{41}\) acquires parameters for the edge detection algorithm from the memory space shared with tasks \(Tsk_3\) and \(Tsk_5\); chunk \(C_{42}\) performs the corner detection algorithm; chunk \(C_{43}\) writes results of the corner detection algorithm on the memory space shared with task \(Tsk_3\).

- Task \(Tsk_5\) manipulates parameters employed by edge and corner detection algorithms. It is a sporadic task with minimum interarrival time and deadline of 120 time units. Each job of \(Tsk_5\) consists of two chunks \(C_{51}\) and \(C_{52}\). Chunk \(C_{51}\) is associated with entry-point \(f_{51}\), which performs parameters manipulation, and requires resource cpu with priority level 5 for an Execution Time constrained within 1 and 2 time units. Chunk \(C_{52}\) is associated with entry-point \(f_{52}\), which writes parameters on the memory space shared with tasks \(Tsk_3\) and \(Tsk_4\); it requires resource cpu with priority level 5 for an Execution Time constrained within 1 and 2 time units; it is synchronized on the binary semaphore \(mux_1\) to access the memory space shared with tasks \(Tsk_3\) and \(Tsk_4\).

The timeline schema of Fig. 6.4 is automatically translated into the pTPN model of Fig. 6.5. Recurrent job releases are modeled by transitions with neither input places nor resource request, so as to fire repeatedly with intertimes falling within their respective firing intervals (e.g., transitions \(t_{10}\), \(t_{20}\), \(t_{30}\), \(t_{40}\), and \(t_{50}\) model recurrent job releases of tasks \(Tsk_1\), \(Tsk_2\), \(Tsk_3\), \(Tsk_4\), and \(Tsk_5\), respectively). Job chunks are modeled by transitions with static firing intervals corresponding to the min-max range of Execution Time, associated with resource requests and static priorities (e.g., transition \(t_{12}\) represents the completion of the unique chunk of each job of \(Tsk_1\)). Binary semaphores are modeled in a straightforward manner as places initially marked with 1 token (e.g., place \(mux_1\) models the binary semaphore that synchronizes the first
Figure 6.4. The timeline schema for the dynamic architecture of the Basic Features Extraction CSCI of Fig. 6.3, representing a task-set composed of five recurrent tasks synchronized by two binary semaphores and a mailbox.

chunk of $Tsk_3$, the first chunk of $Tsk_4$, and the second chunk of $Tsk_5$); their acquisition operations are modeled as immediate transitions, while their release operations are represented by the transitions that also model chunk completions (e.g., wait operations on semaphore $mux_1$ are modeled by transitions $t_{31}$, $t_{42}$, and $t_{53}$; signal operations are represented by transitions $t_{32}$, $t_{43}$, and $t_{54}$, which also account for the completion of the three synchronized chunks). Boost and deboost operations according to the priority ceiling emulation protocol are allocated to immediate transitions and to the transitions that also account for chunk completions, respectively (e.g., transition $t_{52}$ models priority boost of task $Tsk_5$, while transition $t_{54}$ represents the corresponding priority deboost and also accounts for the completion of the second chunk of task $Tsk_5$).
boxes are represented by empty places (e.g., place \( \text{mb}x \) models the mailbox shared between tasks \( Tsk_1 \) and \( Tsk_2 \)); message receipt operations are modeled by immediate transitions (e.g., transition \( t_{11} \) models the receipt of a message by the unique chunk of task \( Tsk_1 \)); message dispatch operations are modeled by the transitions that also account for chunk completions (e.g., transition \( t_{21} \) represents both the dispatch of a message to mailbox \( \text{mb}x \) performed by the first chunk of task \( Tsk_2 \) and the completion of that chunk).

![Figure 6.5. The pTPN model that corresponds to the timeline schema shown in Fig. 6.4.](image)

The pTPN model enables the verification of correctness requirements of the task-set through the enumeration of the SCG, the selection of symbolic runs attaining specific sequencing and timing conditions, and the tight evaluation of their range of timings. For the pTPN model of Fig. 6.5, the Oris Tool

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enumerates 51079 state classes and identifies 15295, 10967, 21170, 491703, and 156574 symbolic runs for tasks $T_{sk1}$, $T_{sk2}$, $T_{sk3}$, $T_{sk4}$, and $T_{sk5}$, respectively. The analysis of the SCG enables the identification of the WCCT of each task (12, 14, 30, 58, and 60 time units for $T_{sk1}$, $T_{sk2}$, $T_{sk3}$, $T_{sk4}$, and $T_{sk5}$, respectively) and the verification of deadlines (tasks $T_{sk1}$, $T_{sk2}$, $T_{sk3}$, $T_{sk4}$, and $T_{sk5}$ meet their respective deadlines with minimum laxity of 28, 26, 50, 22, and 60 time units, respectively). As an example, Fig. 6.6 reports the results of trace analysis on a symbolic run of $T_{sk4}$ that was selected through state-space analysis as a case in which $T_{sk4}$ may attain its WCCT of 58 time units. The schema displays the intervals during which each transition is progressing or suspended, highlighting the range of variability that results from mutual dependencies among transitions firing times.

The activity SD6-SW implements the dynamic architecture of each CSCI, providing code that assumes the following responsibilities: release task jobs according to their policies; invoke semaphore operations and connected priority handling operations; invoke mailbox operations; enforce sequenced invocation of entry-point methods. The implementation of the dynamic architecture of a CSCI is derived from the timeline specification of its task-set, either through disciplined manual programming or in automated manner through the Oris Tool [43]. As a salient trait, the code of the implementation has a readable structure, which follows natural and readable patterns of concurrent programming and which closely mirrors the structure of the corresponding pTPN model. Fig. 6.7 illustrates the correspondence of components of the timeline schema, the code, and the underlying pTPN model with reference to the implementation of task $T_{sk4}$ of Fig. 6.4 on RTAI 3.6 [95].

The code of the dynamic architecture can be complemented with busy-sleep functions, providing an implementation that conforms with expected timing requirements. This provides an Executable Architecture which enables the unit testing of low-level modules within their expected operation environment and supports incremental integration and testing of low-level modules.

The correspondence between the pTPN model of the dynamic architecture of a CSCI and its implementation enables a measurement-based approach to
Figure 6.6. A schema illustrating the range of feasible timings for the symbolic run $\rho = S_{5605} \xrightarrow{t_{10}} S_{5795} \xrightarrow{t_{20}} S_{6092} \xrightarrow{t_{30}} S_{6591} \xrightarrow{t_{21}} S_{7198} \xrightarrow{t_{11}} S_{7741} \xrightarrow{t_{12}} S_{8120} \xrightarrow{t_{22}} S_{8406} \xrightarrow{t_{31}} S_{8711} \xrightarrow{t_{41}} S_{9030} \xrightarrow{t_{32}} S_{9521} \xrightarrow{t_{43}} S_{9873} \xrightarrow{t_{44}} S_{10121} \xrightarrow{t_{42}} S_{10396} \xrightarrow{t_{43}} S_{10670} \xrightarrow{t_{44}} S_{10969} \xrightarrow{t_{45}} S_{11322} \xrightarrow{t_{46}} S_{11729} \xrightarrow{t_{11}} S_{12164}$ in the state-space of the pTPN model of Fig. 6.5. The run starts with the release of a job of $Tsk_4$ (i.e., the firing of transition $t_{10}$ that enters state-class $S_{5605}$, not shown in the schema) and terminates with its completion (i.e., the firing of transition $t_{47}$). Time advances along the horizontal axis. Transition firings are represented by arrows and they are positioned at their latest feasible time, while grey-filled rectangles indicate their allowed range of variation (e.g., transition $t_{12}$ fires twice along the sequence: the first time it can fire within time +10 and +12 and the second time it can fire within +46 and +52, and the two firings are displayed at time +12 and +52, respectively). Transitions enabling-periods are marked through rectangles that are either black or white whether the transition is progressing or suspended, respectively (e.g., transition $t_{22}$ fires twice along the sequence and both the times it is suspended until the firing of transition $t_{12}$ and it is then progressing until its own firing). Classes entered at transition firings are listed over the schema (e.g., the firing of transition $t_{10}$ enters state-class $S_{5795}$, which is left at the firing of transition $t_{20}$ to enter state-class $S_{6092}$).
Execution Time profiling, which reconstructs the Execution Time of chunk computations from a proper sequence of time-stamped logs. This is supported by the Oris Tool and applied to the unit-testing of low-level modules. With reference to the Basic Feature Extraction CSCI shown in Fig. 6.3, the histogram of Fig. 6.8 reports experimental results obtained for an input-data dependent implementation of the edge detection module, which corresponds to computation chunk $C_{21}$ of task $Tsk_{2}$ in the timeline model of Fig. 6.4. Observed Execution Times fall in the interval $[7.771, 8.620]$ ms with a peak on 7.955 ms.
accomplishing the time-frame requirement of [5, 10] ms. It is worth noting that Execution Times exhibit a quite wide spectrum with various peaks, due to a set of input-data dependent alternatives in the implementation of the module, and the distribution of peaks depends on the distribution of input-data. An input-data independent implementation of the edge detection module was developed and Execution Times observed on the same data-set are reported in the histogram of Fig. 6.9: they fall in the interval [7.279, 7.371] ms with a peak on 7.334 ms, showing a thinner spectrum and thus evidencing a substantial independence from input-data.

![Histogram of observed Execution Times for an input-data dependent implementation of the edge detection module of the Basic Features Extraction CSCI of Fig. 6.3.](image)

Figure 6.8. Histogram of observed Execution Times for an input-data dependent implementation of the edge detection module of the Basic Features Extraction CSCI of Fig. 6.3.

In the activity SD7-SW, the theory of pTPNs supports both unit and integration testing processes, contributing to test-case selection, test-case sensitization, oracle verdict and coverage evaluation. In fact, the state-space of pTPN models provides an abstraction that focuses on the aspects of concurrency and timing, supporting the selection of symbolic runs as the witnesses of a specific test purpose determined through a model checking technique [71]
Figure 6.9. Histogram of observed Execution Times for a input-data independent implementation of the edge detection module of the Basic Features Extraction CSCI of Fig. 6.3.

or as part of a test suite defined through various criteria that can be used to automate test-case selection and/or coverage analysis [72]. Moreover, the SCG also supports the definition of a sensitization procedure that optimizes the selection of timed inputs that let the system run along selected test-cases. The approach distinguishes between controllable and non-controllable timers of the model, identifies a path starting from a state class composed of controllable timers and covering the selected test-case, and derives values for controllable timers that comprise the necessary condition to execute the path. The method was applied to the development of the Basic Feature Extraction CSCI of Fig. 6.3. Experimental results concerning the sensitization of a symbolic run of task $Task_4$ that may attain its WCCT show the effectiveness of the approach with respect to randomized testing, where each timer is sampled within its nominal interval according to a uniform distribution.
This dissertation formalizes a comprehensive methodology for the development of real-time safety-critical software components, developing and integrating the theory of pTPNs into a tailoring of the V-Model software life cycle [42] that covers the activities of design, implementation and verification according to the principles of main regulatory standards applied to the construction of safety-critical software [60], [50]. To this end, the theory of state-space analysis [122], [34] is complemented with formal techniques and methods supporting automated derivation of pTPN models from a semi-formal specification, automated compilation of models into real-time code running under RTAI [95], measurement-based Execution Time evaluation, test-case selection and execution, and coverage evaluation. To effectively bring the theory to application, the overall toolchain is implemented within the Oris Tool [109] according to an MDD approach, and the proposed formal methodology is applied to the construction of real-time software components for an IVSS.

As a salient trait, the approach proposed in this dissertation has a smooth impact on the development process, as explicitly recommended by the RTCA/DO-178B standard [60], and it can be effectively applied in the industrial context. In fact, the main difficulty that the approach brings along is the need of a specification of the dynamic architecture through pTPNs. This is largely eased by the use of the semi-formal specification provided by timeline schemas, which better meet intuitions of the industrial practice, and by
their automated translation into pTPN models and real-time code. Without any additional effort on the part of the developer, the pTPN model provides a formal abstraction that supports verification of the dynamic architecture, Execution Time profiling of low-level modules, unit and integration testing.

Explosion of the timed state-space of the pTPN model may impair exhaustive verification of software design but it does not prevent the overall development approach: in fact, on the one hand, partial enumeration of the state-space enables the verification of a significant part of possible behaviors, reaching the level of rigor that can be attained through simulation; on the other hand, conformance of the implementation with respect to the specification is in any case achieved through testing, which is requested for certification purposes.

The code of the implementation follows in a straightforward manner the structure of the pTPN model and preserves its semantic properties. This enables the definition and the implementation of a measurement-based approach to the reconstruction of the Execution Time of entry-points from a proper sequence of time-stamped logs, by leveraging on the formal basis of pTPNs. As a characterizing trait, measurements are carried out by letting chunks run within the Executable Architecture of the task-set, thus accounting for pipeline damages consequent to the execution in preemptive interrupted mode. Since each component of the pTPN specification accepts a context-free translation, the code can be generated in automated manner by structural induction, thus providing a full fledged MDD. At the same time, and perhaps more importantly, the implementation code has a readable structure, which follows common patterns of concurrent programming, leaving the developer full insight and control over the final code and even allowing a disciplined code programming. This is a crucial point to support industrial acceptance and avoids legacy constraints on tools that support editing and translation of timeline schemas and pTPN models. A clean and readable structure of the code also prevents erroneous understanding of the semantics of pTPNs and timeline schemas, which in the industrial practice may be less understood and trusted than conventional programming languages and operating system primitives.
The methodology devised in this dissertation provides an adequate basis to extend the research in many possible directions regarding the various phases of software development process. In the design phase, the theory of pTPNs supports specification and symbolic state space analysis of real-time preemptive systems and enables qualitative verification of correctness requirements pertaining ordering and timings of events. The main criticism concerned with qualitative analysis techniques is the problem of state space explosion. Emerging techniques for Hierarchical Scheduling (HS) should provide support to mitigate the problem, by enabling the application of compositional analysis methods [37]. In particular, the theory of pTPNs seems to find an application in modeling and analysis of HS systems with a Time Division Multiplexing (TDM) global scheduler and Fixed Priority (FP) local schedulers. In fact, the temporal isolation among different applications permits to conveniently exploit the expressive power of pTPNs in the representation of preemptive behavior, allowing the specification of an HS system through a structured representation where each application and its interface towards the environment are accounted by a different pTPN model. This would largely reduce the complexity of the problem, facilitating the scalability of the approach and enabling exhaustive architectural verification of systems that could not be directly analyzed through a unique flat model.

Following the theory of stochastic state classes developed in [48], [45], the model of pTPNs could be extended by introducing a stochastic characterization of non-deterministic timers, which associates the time to fire of each transition with a probability density function. The SCG would then be expanded into a stochastic SCG where state density functions provide a measure of probability over the continuous set of states included in each class. The approach would complement the qualitative identification of feasible behaviors with a quantitative measure of their probability, enabling the verification of dependability requirements in dense-timed preemptive systems so as to meet Reliability, Availability, Maintainability and Safety (RAMS) objectives. This would also represent a suitable theoretical basis to improve testing activities through the optimization of both test-case selection and test-case sensitization.
In particular, quantitative analysis techniques should provide support for the identification of timed inputs that maximize the probability to let the system run along selected test-cases.

The development of multi-core systems might contribute to increase the value of the formal methodology proposed in this dissertation. In fact, the integration of multiple cores on the same processor for parallel computation is naturally encompassed in modeling and analysis of pTPNs, thus expanding the range of application of the proposed approach.


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