

A FUZZY MULTIPLE CRITERIA DECISION MAKING MODEL FOR AIRLINE COMPETITIVENESS EVALUATION

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Abstract: This article presents a new fuzzy multiple criteria decision making model for the evaluation of airline competitiveness over a period. The evaluation problem is formulated as a fuzzy multiple criteria decision making problem and solved by our strength-weakness based approach. For finding out the strength and weakness of an airline over another airline, we present a preference function based on the extended fuzzy preference relation. The strength and weakness matrices are then calculated based on the preference function. We propose a method to aggregate the weights of criteria, strength matrix and weakness matrix into the strength indices and the weakness indices of airlines, by which each airline can identify its own strength and weakness. The strength and weakness indices can be further integrated into an overall performance indices, by which airlines can identify their competitiveness ranking.

Key Words: fuzzy multiple criteria decision making, airline competitiveness

1.INTRODUCTION

Airline competitiveness can be measure by a range of efficiency and effectiveness performance measures across a number of distinct dimensions that can reflect the capabilities and offerings of airlines in serving their customers. The performance evaluation of airlines can be measured in terms of some key competitiveness measures, such as cost (Oum and Yu, 1998), operational performance (Bureau of Industry Economics, (1994) and Schefczyk (1993)), cost and productivity (Encaoua (1991) and Windle (1991)), price and productivity (Good and Rhodes (1991)), price and service quality (Bureau of Transportation and Communications Economics, (1993)), productivity and efficiency (Good et al. (1993), Good et al. (1995), Oum and Yu (1995), Windle and Dresner (1995)), profitability (Bureau of Transportation and Communications Economics, (1993), Oum and Yu (1995), safety (Janic

(2000)), service quality (Chang and Yeh (2002), Young et al. (1994)), and service quality and productivity (Truitt and Haynes (1994)). However, these single measures alone do not reflect the overall airline competitiveness. In this paper, we assume the key performance measures used are cost (C_1), productivity (C_2), service quality (C_3), price (C_4), and management (C_5) (Chang and Yeh (2001)).

An airline competitiveness evaluation problem can be formulated as a multiple criteria decision making problem in which the alternatives are the airlines to be evaluated and the criteria are the performance measures of airlines under consideration. Assume there m airlines to be evaluated against n measures. The problem can be expressed in matrix format as follows:

$$D = \begin{matrix} & C_1 & C_2 & \cdots & C_n \\ \begin{matrix} A_1 \\ A_2 \\ \vdots \\ A_m \end{matrix} & \begin{bmatrix} x_{11} & x_{12} & \cdots & x_{1n} \\ x_{21} & x_{22} & \cdots & x_{2n} \\ \vdots & \vdots & \vdots & \vdots \\ x_{m1} & x_{m2} & \cdots & x_{mn} \end{bmatrix} \end{matrix}$$

and $W = [w_1 \ w_2 \ \cdots \ w_n]$

where A_1, A_2, \dots, A_m are the airlines to be evaluated, C_1, C_2, \dots, C_n are the performance measure against which the performance of airlines are measured, x_{ij} is the performance rating of i -th airline against j -th criterion, and w_j is the weight of j -th criterion.

In traditional MCDM, performance rating and weights are measured in crisp numbers (Dyer et al. (1992), Hwang and Yoon (1981) and Teghem et al. (1989)). To evaluate competitiveness of airlines in a specific year, traditional MCDM methods may suffice, since all performance ratings are crisp. However, if we want to evaluate the competitiveness of airlines over a period, say 5 years, traditional MCDM methods may be inadequate. We can not represent the performance of an airline under a specific measure by a crisp number, since the performance may vary within a range in 5 years. One way to represent a varying performance over a period is to represent the performance by a fuzzy number. Therefore, fuzzy multiple criteria decision making (FMCDM) is suitable for airline performance evaluation over a period. A FMCDM for m airlines and n criteria can be modeled as follows:

$$D = \begin{matrix} & \tilde{A}_{11} & \tilde{A}_{12} & \cdots & \tilde{A}_{1n} \\ \begin{matrix} \tilde{A}_{21} \\ \vdots \\ \tilde{A}_{m1} \end{matrix} & \begin{bmatrix} \tilde{A}_{22} & \cdots & \tilde{A}_{2n} \\ \vdots & \vdots & \vdots \\ \tilde{A}_{m2} & \cdots & \tilde{A}_{mn} \end{bmatrix} \end{matrix}$$

and

$$W = \begin{bmatrix} \tilde{w}_1 & \tilde{w}_2 & \cdots & \tilde{w}_n \end{bmatrix}$$

where \tilde{A}_{ij} is the fuzzy number representing the performance of i -th airline under j -th criterion and \tilde{w}_j is the fuzzy number representing the weight of j th criterion.

In dealing with fuzzy numbers, ranking fuzzy number is one of the important issues. Many methods for fuzzy ranking have been proposed (Baas and Kwakernaak (1977), Bortolan and Degani (1985), Chang (1981), Chen (1985), Delgado (1988), Dubois and Prade (1983), Dyer et al. (1992), Lee (2001), Nakamura (1986), Teghem et al. (1989) and Yuan (1991)). They can be classified into two categories. The first category is based on defuzzification. Various methods of defuzzification have been proposed. In the first category, fuzzy numbers are defuzzified into crisp numbers or the so-called utilities in some literatures. The ranking are then done based on these crisp numbers. Though it is easy to compute, the main drawback of this type is that defuzzification tends to loss some information and thus is unable to grasp the sense of uncertainty. The other category is based on fuzzy preference relation. The advantage of this type is that uncertainties of fuzzy numbers are kept during ranking process. However, the fuzzy preference relations proposed thus far are too complex to compute. Yuan (1991) has proposed criteria for measuring ranking method. Lee (2001) has proposed a new fuzzy ranking method based on fuzzy preference relation satisfying all criteria proposed by Yuan. In Lee (2002), we extended the definition of fuzzy preference relation and propose an extended fuzzy preference relation which satisfies additivity and is easy to compute.

In this paper, we are going to propose a new FMCDM to evaluate the competitiveness of airlines over a period. To find out the strength and weakness of an airline over another airline, we present a preference function based on the extended fuzzy preference relation proposed in Lee (2002). The strength and weakness matrices are then calculated based on the preference function. We propose a method to aggregate the fuzzy weights of criteria, strength matrix and weakness matrix into the strength indices and the weakness indices of airlines, by which airlines can identify their strength and weakness. The strength and weakness indices can be further integrated into an the overall performance indices, by which airlines can identify their competitiveness ranking.

2.PRELIMINARIES

Definition 2.1 The α -cut of fuzzy set A , A^α is the crisp set $A^\alpha = \{x \mid \mu_A(x) \geq \alpha\}$. The support of A is the crisp $\text{Supp}(A) = \{x \mid \mu_A(x) > 0\}$. A is normal iff $\sup_{x \in U} \mu_A(x) = 1$, where U is the universal set.

Definition 2.2 A fuzzy subset A of a real number R is convex iff $\mu_A(\lambda x + (1-\lambda)y) \geq (\mu_A(x) \wedge \mu_A(y))$, $\forall x, y \in R, \forall \lambda \in [0, 1]$, where \wedge denotes the minimum operator.

Definition 2.3 A is a fuzzy numbers iff A is a normal and convex fuzzy subset of R .

Definition 2.4 A triangular fuzzy number A is a fuzzy number with piecewise linear

$$\text{membership function } \mu_A(x) \text{ defined by } \mu_A(x) = \begin{cases} \frac{x-a_1}{a_2-a_1}, & a_1 \leq x \leq a_2, \\ \frac{a_3-x}{a_3-a_2}, & a_2 \leq x \leq a_3, \\ 0, & \text{otherwise,} \end{cases} \text{ which can denoted as}$$

triplet (a_1, a_2, a_3) .

Definition 2.5 Let A and B be two fuzzy numbers. Let \circ be an operation on real numbers, such as $+, -, *, \wedge, \vee$, etc. By extension principle, the extended operation \circ on fuzzy numbers can be defined by $\mu_{A \circ B}(z) = \sup_{x,y:z=x \circ y} \{\mu_A(x) \wedge \mu_B(y)\}$. (1)

Definition 2.6 Let A be a fuzzy number. Then A_α^L and A_α^U are defined as

$$A_\alpha^L = \inf_{\mu_A(z) \geq \alpha} (z) \tag{2}$$

and

$$A_\alpha^U = \sup_{\mu_A(z) \geq \alpha} (z) \tag{3}$$

respectively.

Definition 2.7 A fuzzy preference relation R is a fuzzy subset of $R \times R$ with membership function $\mu_R(A, B)$ representing the degree of preference of fuzzy number A over fuzzy number B .

1. R is reciprocal iff $\mu_R(A, B) = 1 - \mu_R(B, A)$ for all fuzzy numbers A and B .
2. R is transitive iff $\mu_R(A, B) \geq (1/2)$ and $\mu_R(B, C) \geq (1/2) \Rightarrow \mu_R(A, C) \geq (1/2)$ for all fuzzy numbers A, B and C .
3. R is a fuzzy total ordering iff R is both reciprocal and transitive.

If fuzzy numbers are compared both based on fuzzy preference relations, then A is said to be greater than B iff $\mu_R(A, B) > (1/2)$.

Definition 2.8 An extended fuzzy preference relation R is an extended fuzzy subset of $R \times R$ with membership function $-\infty \leq \mu_R(A, B) \leq \infty$ representing the degree of preference of fuzzy number A over fuzzy number B .

1. R is reciprocal iff $\mu_R(A, B) = -\mu_R(B, A)$ for all fuzzy numbers A and B .

2. R is transitive iff $\mu_R(A, B) \geq 0$ and $\mu_R(B, C) \geq 0 \Rightarrow \mu_R(A, C) \geq 0$ for all fuzzy numbers A, B and C .
3. R is additive iff $\mu_R(A, C) = \mu_R(A, B) + \mu_R(B, C)$.
4. R is a fuzzy total ordering iff R is both reciprocal, transitive and additive.

If fuzzy numbers are compared based on extended fuzzy preference relations, then A is said to be greater than B iff $\mu_R(A, B) > 0$.

3. AN EXTENDED FUZZY PREFERENCE RELATION

Our extended fuzzy preference relation is defined as follows.

Definition 3.1 For any fuzzy number A and B , extended fuzzy preference relation $F(A, B)$ is defined by the membership function $\mu_F(A, B) = \int_0^1 ((A-B)_\alpha^L + (A-B)_\alpha^U) d\alpha$ (4)

Lemma 3.1 F is reciprocal, i.e., $\mu_F(B, A) = -\mu_F(A, B)$ (5)

Proof: since $(A-B)_\alpha^L + (A-B)_\alpha^U = A_\alpha^L - B_\alpha^U + A_\alpha^U - B_\alpha^L = -(B_\alpha^L - A_\alpha^U + B_\alpha^U - A_\alpha^L) = -((B-A)_\alpha^L + (B-A)_\alpha^U)$ (6)

we have $\mu_F(B, A) = -\mu_F(A, B)$. (7)

Lemma 3.2 F is additive, i.e., $\mu_F(A, B) + \mu_F(B, C) = \mu_F(A, C)$ (8)

Proof:

$$\begin{aligned} & \mu_F(A, B) + \mu_F(B, C) \\ &= \int_0^1 ((A-B)_\alpha^L + (A-B)_\alpha^U) d\alpha + \int_0^1 ((B-C)_\alpha^L + (B-C)_\alpha^U) d\alpha \\ &= \int_0^1 (A_\alpha^L - B_\alpha^U + A_\alpha^U - B_\alpha^L + B_\alpha^L - C_\alpha^U + B_\alpha^U - C_\alpha^L) d\alpha \\ &= \int_0^1 ((A-C)_\alpha^L + (A-C)_\alpha^U) d\alpha \end{aligned} \tag{9}$$

Lemma 3.3 F is transitive, i.e., $\mu_F(A, B) \geq 0$ and $\mu_F(B, C) \geq 0 \Rightarrow \mu_F(A, C) \geq 0$ (10)

Proof: By lemma 3.2, we have $\mu_F(A, C) = \mu_F(A, B) + \mu_F(B, C)$. Since $\mu_F(A, B) \geq 0, \mu_F(B, C) \geq 0$, we have $\mu_F(A, C) \geq 0$

Lemma 3.4 Let $A = (a_1, a_2, a_3)$ and $B = (b_1, b_2, b_3)$ be two triangular fuzzy numbers. $\mu_F(A, B) \geq 0$ iff $a_1 + 2a_2 + a_3 - b_1 - 2b_2 - b_3 \geq 0$ (11)

Proof: $\mu_F(A, B) \geq 0$ iff

$$\mu_F(A, B) = \int_0^1 (A-B)_\alpha^L + (A-B)_\alpha^U d\alpha = \frac{a_1 + 2a_2 + a_3 - b_1 - 2b_2 - b_3}{2} \geq 0 \tag{12}$$

Definition 3.2 Let \geq be a binary relation on fuzzy numbers defined by $A \geq B$ iff $\mu_F(A, B) \geq 0$. (13)

Theorem 3.1 \geq is total ordering relation.

According to lemma 3.4, we have following lemma.

Lemma 3.5 Let $A = (a_1, a_2, a_3)$ and $B = (b_1, b_2, b_3)$ be two triangular fuzzy numbers. Then

$$A \geq B \text{ iff } a_1 + 2a_2 + a_3 - b_1 - 2b_2 - b_3 \geq 0. \tag{14}$$

Lemma 3.6 Let $A = (a_1, a_2, a_3, a_4, a_5, a_6)$ be a fuzzy number with parabolic membership

$$\text{function defined as } \mu_A(x) = \begin{cases} \frac{-a_2}{2a_1} + \sqrt{\frac{a_2^2}{2a_1} + \frac{(x-a_3)}{a_1}} & a_3 \leq x \leq a_1 + a_2 + a_3, \\ \frac{-a_5}{2a_4} - \sqrt{\frac{a_5^2}{2a_4} + \frac{(x-a_6)}{a_4}} & a_1 + a_2 + a_3 \leq x \leq a_6, \\ 0, & \text{otherwise,} \end{cases} \tag{15}$$

Let $B = (b_1, b_2, b_3, b_4, b_5, b_6)$ be another fuzzy number with parabolic membership function. Let

$$Q(A, B) = \frac{1}{3}(a_1 + a_4 - b_1 - b_4) + \frac{1}{2}(a_2 + a_5 - b_2 - b_5) + (a_3 + a_6 - b_3 - b_6) \tag{16}$$

Then $A \geq B$ iff $Q(A, B) \geq 0$.

In the case of ranking more than two fuzzy numbers, $A_1, A_2, A_3, \dots, A_n$. We may use the relation $F(A_i, A_j)$ for pairwise comparison and we need to calculate $(1/2)n(n-1)F$ values. To improve computational efficiency, we suggest comparing each fuzzy number $A_i, i = 1, 2, 3, \dots, n$, with the average fuzzy number $\bar{A} = \sum_{i=1}^n A_i / n$. Then rank A_i according to $\mu_F(A_i, \bar{A})$ which is followed from the additive property of F .

Theorem 3.2 It follows that the ranking method based on extended fuzzy preference relation F need $O(n)$ computations of F , which is more efficient than any known method.

4. THE PROPOSED METHOD

Let \tilde{A}_{ij} be the performance of i -th airline under j -th criterion. To facilitate our method, we

define the preference function of fuzzy number \tilde{A}_{ij} over another number \tilde{A}_{kj} as follows:

$$P(\tilde{A}_{ij}, \tilde{A}_{kj}) = \begin{cases} \mu_F(\tilde{A}_{ij}, \tilde{A}_{kj}) & \text{if } \mu_F(\tilde{A}_{ij}, \tilde{A}_{kj}) \geq 0 \\ 0 & \text{otherwise} \end{cases}$$

Let J be the set of benefit criteria and J' be the set of cost criteria where

$$J = \{1 \leq j \leq n \text{ and } j \text{ belongs to benefit criteria}\},$$

$$J' = \{1 \leq j \leq n \text{ and } j \text{ belongs to cost criteria}\}, \text{ and } J \cup J' = \{1, \dots, n\}.$$

The strength matrix $S = (S_{ij})$ is given by letting

$$S_{ij} = \begin{cases} \sum_{k \neq i} P(\tilde{A}_{ij}, \tilde{A}_{kj}) & \text{if } j \in J \\ \sum_{k \neq i} P(\tilde{A}_{kj}, \tilde{A}_{ij}) & \text{if } j \in J' \end{cases} \quad (17)$$

Similarly, the weakness matrix $I = (I_{ij})$ is given by letting

$$I_{ij} = \begin{cases} \sum_{k \neq i} P(\tilde{A}_{kj}, \tilde{A}_{ij}) & \text{if } j \in J \\ \sum_{k \neq i} P(\tilde{A}_{ij}, \tilde{A}_{kj}) & \text{if } j \in J' \end{cases} \quad (18)$$

The fuzzy weighted strength matrix $\tilde{S} = (\tilde{S}_i)$ can be obtained by

$$\tilde{S}_i = \sum_j S_{ij} \tilde{W}_j \quad (19)$$

and the fuzzy weighted weakness matrix $\tilde{I} = (\tilde{I}_i)$ can be obtained by

$$\tilde{I}_i = \sum_j I_{ij} \tilde{W}_j \quad (20)$$

where $1 \leq i \leq m$. Now we are ready to present our method for FMCDM.

Step1: Define fuzzy weights $W = (\tilde{W}_j)$ of the performance measures by experts. Assume

the evaluation time interval is a period of T years. Let p_{ij}^t be the performance value

of i -th airlines under j -th criterion in year $1 \leq t \leq T$. Let triangular fuzzy number \tilde{A}_{ij}

be the fuzzy performance of i -th airline under j -th criterion and be denoted as

$(a_{ij1}, a_{ij2}, a_{ij3})$. Define fuzzy performance matrix $D = (\tilde{A}_{ij})$ of airline over a period by

letting

$$a_{ij1} = \min_{1 \leq t \leq T} p_{ij}^t, \quad (21)$$

$$a_{ij2} = \frac{\sum_{t=1}^T p_{ij}^t}{T}, \quad (22)$$

$$a_{ij3} = \max_{1 \leq t \leq T} p_{ij}^t. \quad (23)$$

Step 2: Calculate the strength matrix by (17).

Step 3: Calculate the weakness matrix by (18).

Step 4: Calculate the fuzzy weighted strength indices by (19).

Step 5: Calculate the fuzzy weighted weakness indices by (20).

Step 6: Derive the strength index S_i from the fuzzy weighted strength and the weakness indices by

$$S_i = \sum_{k \neq i} P(\tilde{S}_i, \tilde{S}_k) + \sum_{k \neq i} P(\tilde{I}_k, \tilde{I}_i). \quad (24)$$

Step 7: Derive the weakness index I_i from the fuzzy weighted strength and the weakness indices by

$$I_i = \sum_{k \neq i} P(\tilde{S}_k, \tilde{S}_i) + \sum_{k \neq i} P(\tilde{I}_i, \tilde{I}_k). \quad (25)$$

Step 8: Aggregate the strength and weakness indices into the overall performance indices by

$$t_i = \frac{S_i}{S_i + I_i}. \quad (26)$$

Step 9: Rank airlines by the overall performance index t_i for $1 \leq i \leq m$.

5. NUMERICAL EXAMPLE

Assume there are three airlines to be evaluated under 5 criteria over 5 years. Assume the performance ratings in 5 years are normalized within [0, 10] and then converted into fuzzy numbers by (21) (22), and (23) as shown in Table 1. Assume fuzzy weights of criteria are given by experts as shown in Table 1. The competitiveness ranking of airlines is resolved as follows:

Step 1: The fuzzy performance of airlines and the fuzzy weights of criteria are shown in Table 1.

Step 2: The strength matrix derived by (17) is shown in Table 2.

Step 3: The weakness matrix derived by (18) is shown in Table 3.

Step 4: The fuzzy weighted strength indices of airlines derived by (19) are shown in Table 4.

Step 5: The fuzzy weighted weakness indices of airlines derived by (20) are shown in Table 5.

Step 6: The strength indices of airlines derived by (24) are shown in Table 6.

Step 7: The weakness indices of airlines derived by (25) are shown in Table 7.

Step 8: The total performance indices aggregated by (26) are shown in Table 8.

Step 9: The rank of airlines by overall performance indices are shown in Table 9.

6. CONCLUSIONS

In this paper, we have presented a new FMCDM for airlines performance comparison. With

our method, two matrices are constructed. Namely, they are the strength matrix and weakness matrix from which the strength and weakness indices are derived. With strength and weakness indices, airlines can identify their strength and weakness under the performance measures taken into consideration. Airlines can identify their competitive positions by the overall performance indices obtained by aggregating the strength and weakness indices.

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Table 1. The fuzzy decision matrix and fuzzy weights

	C ₁	C ₂	C ₃	C ₄	C ₅
A ₁	(5.7,7.7,9.3)	(5,7,9)	(5.7,7.7,9)	(8.33, 9.67,10)	(3,5,7)
A ₂	(6.3,8.3,9.7)	(9,10,10)	(8.3,9.7,10)	(9,10,10)	(7,9,10)
A ₃	(6.3,8,9)	(7,9,10)	(7,9,10)	(7,9,10)	(6.3,8.3,9.7)
Weight	(0.7,0.9,1)	(0.9,1,1)	(0.77,0.93,1)	(0.9,1,1)	(0.43,0.63,0.83)

Table 2. The strength matrix

	C ₁	C ₂	C ₃	C ₄	C ₅
A ₁	0	0	0	1.335	0
A ₂	2.25	7.5	0.645	2.665	8.7
A ₃	0.45	3.5	2.45	0	5.95

Table 3. The weakness matrix

	C ₁	C ₂	C ₃	C ₄	C ₅
A ₁	1.8	9	7.55	0.655	13.45
A ₂	0	0	0	0	0
A ₃	0.9	2	1.35	3.335	1.2

Table 4. The fuzzy weighted strength indices of airlines

	fuzzy weighted strength index
A ₁	(1.2015, 1.335, 1.335)
A ₂	(14.96115, 18.27085, 20.281)
A ₃	(7.91, 9.932, 11.3385)

Table 5. The fuzzy weighted weakness indices of airlines

	fuzzy weighted weakness index
A ₁	(21.5555, 26.78, 30.1785)
A ₂	(0, 0, 0)
A ₃	(6.987, 8.1565, 8.581)

Table 6. The strength indices of airlines

	strength index
A ₁	50.7927
A ₂	210.125
A ₃	31.881

Table 7. The weakness indices of airlines

	weakness index
A ₁	171.8715
A ₂	31.881
A ₃	89.04635

Table 8. The total performance indices of airlines

	total performance index
A ₁	0.228113
A ₂	0.868264
A ₃	0.263638

Table 9. The rank of airlines based on overall performance indices

	rank
A ₁	3
A ₂	1
A ₃	2